STATISTICAL ESTIMATION OF WATER DISTRIBUTION SYSTEM PIPE

BREAK RISK

A Thesis

by

SHRIDHAR YAMIJALA

Submitted to the Office of Graduate Studies of
Texas A&M University
in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

August 2007

Major Subject: Civil Engineering

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Approved by:

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ABSTRACT

Statistical Estimation of Water Distribution System Pipe Break Risk. (August 2007)

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The deterioration of pipes in urban water distribution systems is of concern to water utilities throughout the world. This deterioration generally leads to pipe breaks and leaks, which may result in reduction in the water-carrying capacity of the pipes from tuberculation of interior walls of the pipe. Deterioration can also lead to contamination of water in the distribution systems. Water utilities which are already facing tight funding constraints incur large expenses in replacement and rehabilitation of water mains, and hence it becomes critical to evaluate the current and future condition of the system for making maintenance decisions. Quantitative estimates of the likelihood of pipe breaks on individual pipe segments can facilitate inspection and maintenance decisions. A number of statistical methods have been proposed for this estimation problem. This thesis focuses on comparing these statistical models on the basis of short time histories. The goals of this research are to estimate the likelihood of pipe breaks in the future and to determine the parameters that most affect the likelihood of pipe breaks. The various statistical models reviewed in this thesis are time linear and time exponential ordinary least squares regression models, proportional hazards models (PHM), and generalized linear models (GLM). The data set used for the analysis comes

from a major U.S. city, and the data includes approximately 85,000 pipe segments with nearly 2,500 breaks from 2000 through 2005. The covariates used in the analysis are pipe diameter, length, material, year of installation, operating pressure, rainfall, land use, soil type, soil corrosivity, soil moisture, and temperature. The Logistic Generalized Linear Model fits can be used by water utilities to choose inspection regimes based on a rigorous estimation of pipe breakage risk in their pipe network.

ACKNOWLEDGEMENTS

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1. INTRODUCTION

The progressive decay of the nation's infrastructure systems such as transportation, water supply, and sewer systems together with the burgeoning public awareness about this deterioration creates the need for more scientific studies to understand the failure patterns of infrastructure systems and propose methodologies to reduce the number of failures. All these systems constitute the infrastructure of urban centers, and water distribution systems play a critical role in the successful functioning of a city. Community public health standards and the drive for future growth and economic development are heavily dependent upon the condition of water mains and the services they provide.

The deterioration of pipes in urban water distribution systems presents a major challenge to water utilities throughout the world. Pipe deterioration can lead to pipe breaks and leaks, which may result in a reduction in the water carrying capacity of pipes and lead to substantial repair costs. Pipe breaks can also pose potential dangers by temporarily reducing fire fighting capabilities and contaminating water in distribution systems. These problems are responsible for increasing future repair and pumping costs, irregular services, potential for damage caused by breaks, for example flooding, traffic interruptions and functioning of other utilities, and problems of water quality due to manifestation of bacteria in the tubercles formed in the interiors of pipe walls (Andreou,

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This thesis follows the style of *Risk Analysis*.

1986). Solutions for the above problems include either replacing or rehabilitating (i.e. cleaning and lining) affected sections of pipes in the system.

The investment in maintaining and repairing pipes represents a major portion of the expenditure of water utilities. According to Kleiner and Rajani (2001), distribution networks often account for up to eighty percent of the total expenditure involved in water supply systems. Furthermore, Stratus Consulting (1998) indicated that approximately $325 billion is needed for replacement and rehabilitation of water distribution systems across the United States.

If abundant resources were available, it would not be a problem to renew and rehabilitate potable water distribution systems. However, the scarcity of resources necessitates the search for the most cost effective renewal or rehabilitation strategy. Before making decisions related to repair and rehabilitation for deteriorating pipelines, there is a need to develop an understanding about the failure mechanisms and factors contributing to pipe breaks. Pipe material, the environment in which the pipes are laid and the operating characteristics of the system combine to influence the likelihood of pipe breaks. Morris (1967) suggested a few possible causes of water main structural failures that include soil aggressiveness or corrosivity, soil stability, weather conditions, bedding conditions, construction quality and land development. Some other factors responsible for pipe failures include internal corrosion, pressure surges, and faulty anchorages at branches, bends and dead ends. Shamir and Howard (1979) extended the list to include manufacturing flaws, traffic loading, pressure and water hammer. Marks et al. (1987) raised the importance of joints leading to structural failure. The U.S. Army

Corps of Engineers (1980) found that prior leakage increased the moisture content of the surrounding soil and promoted corrosion when they conducted a study of the New York water supply system. Clark et al. (1988) analyzed break rates due to freezing ground conditions.

1.1. Causes and Effects of Pipe Failures

Some causes and effects of common pipe failures have been described by Mavin (1996). These include:

1) *Pipe manufacturing defects*: Inclusions, discontinuities or sporadic processing problems. Dimensional irregularities particularly in jointing areas.

2) *Storage and handling*: Stress deformation due to poor stacking or storage. Cuts or scratches on pipe walls or coatings. Impact cracks due to dropping or striking. UV degradation, over-weathering or contamination. Inadvertent mixing of pipe class or jointing material.

3) *During construction*: Poor laying, jointing or tapping techniques. Excessive overburden/soil slips causing distortion. Construction traffic. Groundwater flooding.

4) *Subsequent works*: Superimposed loadings, impacts or cover reduction. Side slips, service pulling or moling. Loss of support or bedding.

5) *Soil movement*: Subsidence due to mining, filled land etc. Differential consolidation or geological changes. Changes in water table or soil moisture content. Extremes of climate such as frost heave or clay shrinkage. Loss of

anchorage/support (horizontal or vertical). Shock waves such as seismic, blasting or vibration.

6) *Soil environment*: Poor original bedding/backfill. Point loads. Migration of bedding or sidefill material. External chemical attack from natural soil. Chemical attack due to spillages. Deterioration of the joint sealing ring(s).

7) *Impact damage*: Strike with bucket, pick or point (includes pulling). Point bearing in bedding or surround. Traffic loading causing fatigue or joint movement.

8) *Temperature changes*: Excess compression, end crushing. Pull out or separation of joint. Pipe blockages and splits.

9) *Internal pressure*: Excess testing pressure. Pressure surge, water separation, and vacuum collapse. Pipe tapping whilst under bending stress.

10) *Others*: Aggressive waters causing internal deterioration. Galvanic corrosion due to dissimilar metals.

Complications arise when one tries to analyze and predict the future behavior of individual pipes in a system. This is because there exists a high degree of variability in the failure patterns of different water distribution systems and also among the pipes of a given system. For making maintenance decisions, analysis at the individual pipe level is required subject to particular economic and reliability criteria. The information about structural integrity of water mains could be revealed by observing the physical condition of water mains onsite. However, such inspection would be beneficial only if there is presence of severe deterioration. In reality, the inspection of particular points along the

pipe length cannot really capture the localized nature of the various factors contributing to breaks, their interactions and the effects of aging of the system.

Most of the times, water utilities must make inspection and maintenance decisions about each pipe segment in their network on the basis of incomplete information about pipe status. Hence arises the need for analyzing historical records of pipe breaks and make use of the data concerning pipe characteristics and external environment conditions. The estimation of future break events for each individual pipe can serve many purposes. Taking into account the various replacement and rehabilitation strategies, the budgetary needs for future repairs can be determined. An economic assessment can be performed to determine optimum replacement time for affected mains. Depending on the position of certain pipes in the network and the potential damages associated with their failures, the estimates of reliability of individual pipe segments can be determined.

1.2. Physical Modeling of Pipe Breakages

The physical mechanisms that drive pipe breakage are complex. They are driven by three principal aspects: a) pipe structural properties, material type, pipe soil interaction, and quality of installation, b) internal loads due to operational pressure and external loads due to soil overburden, traffic loads, frost loads and third party interference, and c) material deterioration due largely to the external and internal chemical, biochemical and electro-chemical environment (Rajani and Kleiner, 2001). Figure 1 graphically illustrates the failure modes for buried pipes.

Physical modeling of individual pipes can provide strong inferences about pipe condition if sufficient data about the pipes is available. However, because pipes are buried, it is prohibitively difficult to gather the information needed for physical models of every pipe in a given water distribution system. According to Kleiner and Rajani (2001), physical models cannot be realistically applied to assess the structural resiliency of each individual pipe in most cases because accurate data are rarely available and are very costly to obtain. Physical models are most often used only for the largest pipes that are most critical to system integrity. Examples of these physical models are the frost load model developed by Rajani and Zhan (1996), pipe-soil interaction analysis (Rajani et al. 1996), residual structural resistance analysis (Kiefner and Vieth, 1989) and the corrosion status index of Kumar et al. (1984).

1.3.   Difference between Pipe Breaks and Leaks

There is a need to distinguish between breaks and leaks when it comes to modeling water distribution system reliability. The terms 'leak' and 'break' are used in different ways by water utility personnel. They do not have standard definitions. In general, a break in a main requires emergency repair whereas a leak does not. Also, evidence of a break is obvious unlike detection of a leak which requires special equipment. Table 1 gives the distinguishing characteristics between leaks and breaks.
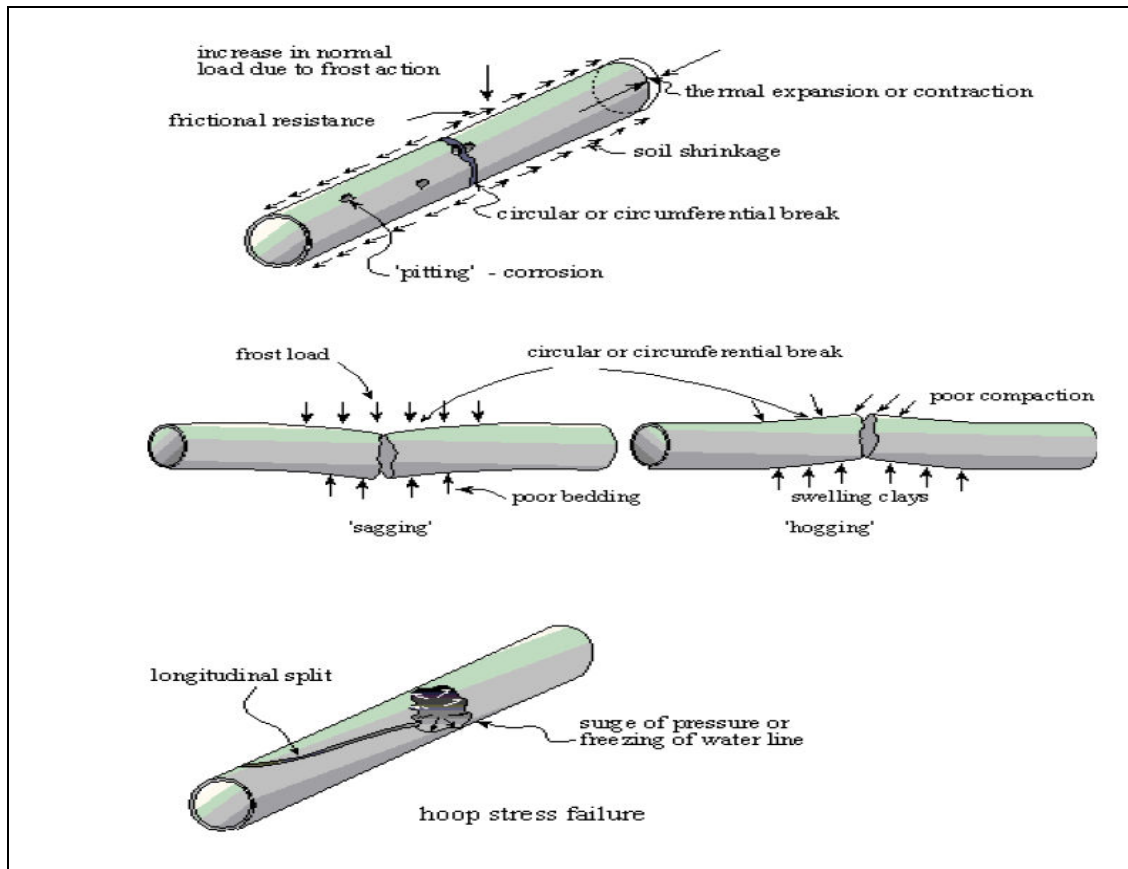
Figure 1. Failure modes for buried pipes: direct tension (top left), bending or flexural failure (middle), and hoop stress (bottom) (Taken from Rajani and Kleiner, 2001)

Table 1. General characteristics of leaks and breaks (Mays, L., 2000)

Sr. No.	Leak	Break
1.	Scheduled repairs are possible	Requires emergency repair
2.	Specific means of detection are necessary	Detection is obvious (e.g. surfacing water, low pressure)
3.	Repair does not usually interrupt service	Repair requires service shut down
4.	More frequently occurs at pipe joints and service lines	Often occurs along the pipe barrel

Breaks result in a clear disruption of service and require some kind of repair action whereas leaks are associated with the term 'unaccounted for water' and represent a different category of pipe failures, different from breaks. Usually, the largest portion of unaccounted for water is lost through main leaks. Yet, the popular belief is that leaks are associated with breaks, because they can weaken the bedding material beneath the pipes and create localized concentration of stresses. There also exists a difference between breaks in small (less than or equal to six inches) pipes and larger pipes. The breaks in smaller pipes are more frequent, mostly circumferential in nature, whereas those in larger pipes are longitudinal in nature. The breaks in larger pipes are more consequential when it comes to impacting the quality of service offered by the water utilities to its customers. They generally result in traffic disruptions, flooding on streets and in basements, interference with the operations of other utilities such as gas pipelines, sewers, cable lines, and interruptions in subway operations. It is considered economically more efficient to rehabilitate larger diameter pipelines than smaller ones.

1.4. Objectives of Research

While physical models are of limited usefulness in modeling entire water distribution networks, statistical models can be applied to water distribution pipes based on varying levels of input data. They can provide greater insight about failure patterns and quantify with more accuracy the existing trends in water main breaks. Many of the currently used rules of thumb developed for assessing the future performance of deteriorating pipes and making decisions with respect to replacement and or rehabilitation are based solely on pipe age and number of previous breaks. Examples of

these are the time-linear model (Kettler and Goulter, 1985), and the time-exponential model (Shamir and Howard, 1979). Hence more scientific study is required in order to examine whether such measures are justifiable.

The complex nature of pipe breaking mechanism and the highly variable rate of pipe breaks in existing pipe networks and water systems have led to the failure of many statistical studies and attempts to obtain predictive models for future breaks. They have been unsuccessful in capturing the detailed failure trends on individual pipes. They have also created uncertainty about the effects of pipe aging on the pipe breaks. Statistical analysis of breaks at the level of individual pipes can be beneficial in making inspection and maintenance decisions. A variety of statistical models have been proposed by a number of authors for this purpose, but the accuracy and usefulness of these models have not been systematically compared. This research aims to fill this gap by (1) comparing statistical models from the literature that are appropriate for modeling pipe break risk and (2) extending the methods used for this problem to include logistic generalized linear models, a flexible class of regression models for binary data. The models compared in this research are time linear and time exponential ordinary least squares regression models, generalized linear models (GLM) and logistic regression.

The focus of this research is on comparing the usefulness of different statistical models for estimating pipe break risk on the basis of break data from relatively short time periods (e.g., a few years of data). While it would be preferable to have many years of break data, many water supply utilities do not have systematic, pipe-specific break records that extend back beyond a 5-10 year time frame. The information about pipes

used in this research is pipe diameter, length, material, year of installation, pressure, land use, rainfall, soil type and temperature. These methods are demonstrated by applying them to the data provided by the water provider for a large city in Texas.

2. LITERATURE REVIEW

2.1. Introduction

Pipe breaks have been analyzed and statistically studied on several occasions. Such studies have revealed useful pattern in the behavior of deteriorating pipes, but have failed to answer the complex nature of the failure phenomenon at the individual pipe level, especially the effects of aging on the break rate, and the ability to provide reliable quantitative measures for determining the condition of individual water mains given their past break history and other pipe and environmental characteristics (Andreou, 1986). This tends to hide the high variability in failure patterns that exists among different pipes of a given system, because these studies try to identify trends in the overall system and not at the individual pipe level. Some of those past studies that were carried out have been described below.

2.2. Past Statistical Studies

O'Day et al. (1983) performed a detailed statistical analysis on main beak failures in the city of Philadelphia. Some of his important findings are as follows:

1) Break rates were increasing 1.8 percent per year since 1930.

2) The break rates in larger diameter mains (>= 16 inches) have remained relatively constant since 1910.

3) Water main break rates usually increase significantly in the winter months, but there has also been a sharp increase in breakage rate in non-winter months in the past 20 years, at an annual rate of 2.5 percent.

4) Small diameter mains are more susceptible to breaks than larger diameter mains.

5) As far as break type is concerned, about 71 percent of the breaks in 6 inch diameter pipes are circumferential in nature, dropping to 34 percent and 31 percent in 12 and 16 inch diameter pipelines, respectively. 18 percent of the breaks in 6 inch and 47 percent of the breaks in 10 inch pipes were longitudinal in nature.

6) The pipes installed during the period from 1940-1960 showed an unusually high breakage rate.

7) He found a strong correlation between break rate and residential development.

8) Internal corrosion of pipes turned out to be a significant contributor to reducing wall thickness as compared to external corrosion. This proved that internal corrosion not only forms tubercles inside the pipe that block the flow in the pipe, but also undermines the structural integrity of the pipe.

O'Day failed to consider important variables that could potentially lead to pipe breaks. These include pipe materials, operating pressure within the pipes, length of pipes, and type of soil around the pipes, and rainfall and temperature in the area.

The U.S. Army Corps of Engineers (1981) conducted a statistical analysis on main break patterns for the city of Buffalo, New York. Their study revealed a seasonal pattern in main breaks. Most of the breaks again were found in smaller diameter pipes. When compared with the findings of O'Day, the seasonal pattern in pipe breaks not only included winter months, but also included summer months of high demand. These breaks were attributed to the different operating practices in the two water systems. As

an example, the increase in the operating pressures in the Buffalo water system to meet the high demands during the summer period could be related to the increased stresses in pipes during the summer months. No satisfactory conclusion could be reached when an attempt was made by the U.S.A.C.E. to relate pipe breakage rate to the high annual average daily traffic volume.

Another study was performed by K. O'Day et al. (1980) for the New York district of the Corps of Engineers. The statistical analysis was of the water main breaks in the City of Manhattan, New York. They created a detailed computer database for the past 25 years that included the break records and information on pipe location, diameter, pipe length, date laid and number of hydrants. They applied a discriminant analysis to identify environmental and pipe characteristics that could contribute to breaks. In this they classified the pipes into two groups, those that broke and those that did not. They concluded that there was no consistent break pattern with increasing pipe age. Also, they could not conclusively prove that pipe material deteriorated as they got older. Like the findings from previous studies, they too found that smaller diameter pipes (<= 6 inches) experienced large number of breaks which were predominantly circumferential in nature. They also concluded that leaks could be the most important factor resulting in main breaks. This is because, depending on the soil condition, the bedding material could be washed away when leaks occur. The study teams pointed out that those areas with high breakage rates were associated with high levels of activities such as heavy traffic, major reconstruction, subways, and other underground utilities.

The general findings from the statistical studies conducted on most of the cities (New York City, U.S. Army Corps of Engineers (1980); Cincinnati, Ohio, Clark et al. (1982); Binghamton, NY, Walski et al. (1982); Philadelphia, O'Day (1983); Buffalo, NY, U.S. Army Corps of Engineers (1981)) concluded that high breakage rates occur in the winter months. Frost penetration resulting in external forces on pipes and thermal contraction are considered to be the major causes of this pattern. These forces depend upon factors such as depth of cover of the pipe, soil type, and joint and pipe material (Andreou, 1986). As far as pipe age is concerned, the Manhattan study showed that the mains were not wearing out with age. The study conducted by O'Day showed that there was a weak correlation between break rate and age of mains when he observed 6 inch diameter mains. Another of his observations was that on an average there was higher number of breaks for older mains when he aggregated all the pipe segments together. The U.S.A.C.E. study does not give any information to relate pipe breakage rate to its age.

2.3. Predictive Statistical Models for Pipe Break Failures

The need to obtain quantitative estimates of the likelihood of pipe breaks on individual pipes for making repair versus replacement decisions for deteriorating water pipes led to the derivation of predictive models for pipe break failures. Three basic categories of such models are

1) Aggregate type models, where the expected number of breaks is a function of time t, since a reference time period and a set of constant model parameters.

2) Regression type models, where the expected number of breaks, or the expected time to the next break, are predicted as a function of independent variables reflecting environmental conditions and pipe characteristics.

3) Probabilistic or choice models, where discriminant analysis is applied on the data, and failure time models, where a survivor function is estimated for each individual pipe, which provides the probability that a pipe will survive without breaks beyond time 't', as a function again of a number of independent covariates related to environmental conditions and other pipe characteristics (Andreou, 1986).

2.3.1. *Aggregate Type Models*

Shamir and Howard (1979) developed two equations (one linear and one exponential) to describe break rate as a function of time:

$$N(t) = N(t_0)e^{A(t-t_0)}$$

(1)

$$N(t) = N(t_0) + A(t - t_0)$$

(2)

where N is the expected number of breaks in year t per unit length, t_0 is the base year time, A is the growth rate coefficient. These models are applied to pipes with similar internal and external characteristics. Shamir and Howard (1979) proposed values for A in the range of 0.01-0.15. Clark (1982) proposed a value of 0.086 and Walski et al. (1982) reported values of 0.021 and 0.014 for pit cast iron and sandspun cast iron pipes respectively, when they employed a similar modeling approach on other datasets.

The Shamir and Howard models are one of the first attempts to statistically analyze break records and use the results for making maintenance decisions. Their advantage lies in the fact that they are simple to use. However, they have a few drawbacks which include a) they do not consider other factors such as environmental characteristics, operating pressures, and previous break history of individual pipe segments, and b) their studies do not provide any information about the goodness of fit tests and the statistical significance of the coefficients of their models.

They thus fail to develop insights about the mechanisms causing breaks and the major factors contributing to pipe breaks. The goodness of fit statistics such as Akaike Information Criterion (AIC), deviance, and log-likelihood determine how good the model is. Thus due to the absence of these statistics, it is difficult to say how good their model is.

Since their focus is not at the individual pipe level, the application of these models for making repair versus replacement decisions could lead to suboptimal replacement strategies (Andreou, 1986). However these models do require smaller amounts of data as compared with other regression models. There is also a likelihood of these models predicting well at the smaller diameter ($<=$ 6 inches) pipe level, where breaks are more frequent.

2.3.2. *Introduction to multiple regression type models*

Clark et al. (1982) developed this type of model. The following two equations were proposed:

First Event Equation:

$$NY = 4.13 + 0.338D - 0.022P - 0.265I - 0.0983RES - 0.003LH + 13.28T \qquad (3)$$

where NY = number of years from installation to first repair

D = diameter of pipe in inches

P = absolute pressure within a pipe in pounds per square inch

I = percent of pipe overlain by industrial development in a census tract

RES = percent of pipe overlain by residential development in a census tract

LH = length of pipe in highly corrosive soil

T = pipe type (1 = metallic, 0 = reinforced concrete)

Accumulated Event Equation:

$$REP = (0.1721)(e^{0.7197})^{T}(e^{0.0044})^{PRD}(e^{0.0865})^{A}(e^{0.0121})^{DEV}(SL)^{0.014}(SH)^{0.069} \qquad (4)$$

where REP = number of repairs

T = pipe type

PRD = pressure differential, in pounds per square inch

A = age of pipe from first break

DEV = percentage of land under pipe which is developed

SL = surface area of pipe in low corrosive soil

SH = surface area of pipe in highly corrosive soil

The R^2 values obtained by Clark et al. for the above two equations were 0.23 and 0.47, respectively. This shows that the models do not fit the data satisfactorily well. Also it is not known how statistically significant the estimated coefficients are. The original

study gave the partial correlations of the independent variables with the response variable. This gives an idea about which variables have a stronger impact on the regression equation, but it is very difficult to evaluate the statistical significance of each variable in the equation. This could make the R^2 value artificially high. Thus this type of model can provide more insights into failure of water mains compared to those proposed by Shamir and Howard (1979). However, availability of appropriate data could be a problem.

The models suggested in the literature vary in complexity from simple linear regression models (e.g., Kettler and Goulter, 1985) to proportional hazards models (e.g., Cox, 1972) and generalized linear models (e.g., Andreou, 1986). These models are separated into four distinct classes of models – time linear regression models, time exponential regression models, proportional hazards models, and generalized linear models. Past uses of each of these are reviewed below.

a) *Time linear model*

Linear regression models assume that the variable of interest, y, is a linear function of a set of explanatory variables x_i as given by equation (5)

$$y = \beta_0 + \sum_i \beta_i x_i + \varepsilon \qquad (5)$$

Where β_0 and β_i are unknown constants to be estimated and ε is an error term. The errors are assumed to be normally distributed with a mean of zero and unknown variance, and they are assumed to be independent (Montgomery and Peck, 1992). Note that this implies that the errors are homoscedastic; the magnitude of the error does not

depend on the magnitude of the response variable y. There exists a probability distribution for y at each possible value for x. The mean of this distribution is

$$E(y \mid x) = \beta_0 + \beta_1 x \tag{6}$$

and the variance is given by equation (7) as

$$V(y \mid x) = V(\beta_0 + \beta_1 x + \varepsilon) = \sigma^2 \tag{7}$$

This shows that the mean of y is a linear function of x, but the variance of y does not depend on the value of x.

There are several limitations of the linear regression model. The distribution of y conditional on the observed data x has to be Normal. Due to the integral nature of count data, this assumption becomes invalid. The magnitude of the errors in the linear regression model is implicitly assumed to be independent of the magnitude of y, even though count data typically demonstrate heteroscedasticity. The independent variables are assumed to be independent of each other and can therefore only result in linear impacts on the response variable.

The use of a linear relationship between the number of pipe breaks on a segment of pipe per kilometer per year and the diameter of the pipe was suggested by Kettler and Goulter (1985). They used pipe breakage data from the cities of Philadelphia and New York in the United States, and Winnipeg and St. Catharines in Canada. Table 2 gives a summary of the results obtained by them.

Table 2. Number of failures per kilometer per year for various pipe sizes and types in 4 cities (Kettler and Goulter, 1985)

		Failures per kilometer per year for:			
City		New York (Manhattan)	Philadelphia	St. Catharines	Winnipeg (District)
Pipe diameter (mm)	Type of pipe examined	Cast iron	Cast iron	63% cast iron	Cast iron
100		-	0.26	0.49	1.05
150		0.34	0.32	0.30	1.06
200		-	0.07	0.16	0.76
250		-	0.13	-	0.39
300		0.11	0.05	-	0.07
400		-	0.07	-	-
Time frame		5 years 1959, 1964, 1969, 1974, 1975	17 years 1964-1980	6 years 1977-1982	6 years 1975-1980

For each of the cities it can be seen that there is a decreasing trend in failure rate with increase in diameter of the pipe. They obtained an 'r' value (sample correlation coefficient) of -0.963 for the 6 year averaged Winnipeg data. Thus the decreasing tendency is strongly linear (i.e. strong negative correlation). Another observation from their analysis was that the increase in breakage rate of cast iron pipes with age was mostly due to circular cracks. In cast iron pipes, the increase in breakage rate was largely related to corrosion whereas the circular breakage rate decreased with age. This type of model is simple and straightforward. The authors never reported an attempt to validate their model by applying it to a holdout sample.

Kettler and Goulter (1985) related pipe breakage linearly to its age. Their model is of the form as given in equation (8).

$$N = k_0 A \tag{8}$$

where N is number of breaks on a given pipe segment per year, k_0 is the unknown regression parameter, and A is the age of the pipe at first break. They obtained the data based on a relatively constant sample of pipes installed within a 10-year period in Winnipeg, Manitoba. For asbestos cement and cast iron pipes, they obtained a moderate correlation of 0.563 and 0.103 respectively between annual breakage rate and pipe age.

McMullen (1982) applied a linear regression model to the water distribution system of Des Moines, Iowa. His linear model was of the form shown in equation (9).

$$Age = 0.028 * SR - 6.33 * pH - 0.049 * r_d \qquad (9)$$

where Age is the age of the pipe at the first break (years), SR is the saturated soil resistivity (Ω cm), pH is the soil pH, r_d is the redox potential in millivolts. He obtained a moderate coefficient of determination of 0.375. His team concluded that corrosion was a dominant factor in pipe breakage since they observed that 94 percent of pipe failures occurred in soils with saturated resistivities of less than 2000 Ω cm. This model predicts only the time to first break of a pipe and hence cannot be used as a full-fledged pipe break prediction model (Kleiner and Rajani, 2001).

Jacobs and Karney (1994) applied a linear regression model to 390 km of 6 inch cast iron water mains with about 3550 breakage events recorded in Winnipeg. The water mains were divided into three age groups namely 0-18, 19-30, and > 30 years to obtain relatively homogeneous groups of water mains. They used the equation of the form as given in equation (10).

$$P = a_0 + a_1 Length + a_2 Age \qquad (10)$$

where P is the reciprocal of the probability of a day with no breaks; a_0, a_1, a_2 are the regression coefficients. They first applied this equation to all the recorded breaks and obtained coefficients of determination ranging from R^2 of 0.704 to 0.937 for the three age groups. This meant that the pipe breaks were uniformly distributed along the pipe. The predictive power of the regression model slightly improved after introduction of pipe age for relatively new pipes, and significantly for old pipes.

b) *Time exponential model*

Non-linear regression extends linear regression to a much larger and more general class of functions. In its most basic form, a non-linear model is given by equation (11) as

$$y = f(\vec{x}; \vec{\beta}) + \varepsilon \tag{11}$$

where y is the dependent variable, the function $f(\vec{x}; \vec{\beta})$ is non-linear with respect to the unknown parameters β_0, β_1,...., and ε is the residual error. This type of model is often transformed to yield a model that is linear in the regression parameters, and then the transformed model is fit as a linear regression model. The assumptions underlying linear regression then apply to the transformed model. The biggest advantage with non-linear models is that it can fit a broad range of functions. For example, the strengthening of concrete as it cures is a non-linear process. Research has shown that initially the strength increases quickly and then levels off over time.

Shamir and Howard (1979) used non-linear regression analysis to relate a pipe's breakage to the exponent of its age. Their model is given by equation (12) as

$$N(t) = N(t_0)e^{A(t+g)} \tag{12}$$

where $N(t)$ is the number of breaks per unit length per year, $N(t_0)$ is the number of breaks per unit length at the year of installation of the pipe, t is the time between the present time and the time of a given break in the past in years, g is the age of the pipe at time t, and A is a breakage rate coefficient in yr^{-1} that is fit based on the data.

Shamir and Howard (1979) did not provide any details on the location of the study, the quality and quantity of available data or the method of analysis. However, they did recommend that the regression analysis be applied to groups of pipes that were homogeneous with respect to the parameters influencing their breaks. They subsequently used this model to analyze the cost of pipe replacement in terms of the present value of both break repair and capital investment.

Walski and Pellicia (1982) extended the time exponential model of Shamir and Howard (1979) to incorporate two additional parameters in the analysis based on observations made by the US Army Corps of Engineers in Binghamton, NY. Their model was of the form as shown in equation (13).

$$N(t) = C_1 C_2 N(t_0)e^{A(t+g)} \tag{13}$$

where C_1 is the ratio between [break frequency for (pit/sandspun) cast iron with (no/one or more) previous breaks] and [overall break frequency for (pit/sandspun) cast iron]; C_2 is the ratio between [break frequency for pit cast pipes 500 mm diameter] and [overall break frequency for pit cast pipes]. C_1 accounts for known previous breaks in the pipe,

based on an observation that once a pipe broke, it is more likely to break again. C_2 accounts for observed differences in breakage rates in larger diameter pit cast iron pipes.

Clark et al. (1982) enhanced the Shamir and Howard (1979) model further to transform into a two-phase model. They used the following equation

$$NY = x_1 + x_2 D + x_3 P + x_4 I + x_5 RES + x_6 LH + x_7 T \tag{14}$$

where NY is the number of years from installation to first repair; x_i are the regression parameters; D is the diameter of pipe; P is the absolute pressure within a pipe; I is the percentage of pipe underlain by industrial development; RES = percentage of pipe underlain by residential development; LH is the length of pipe in highly corrosive soil; T is the pipe type (1 = metallic, 0 = reinforced concrete). They observed a pause between the year of installation of the pipe and the first break and hence proposed the above model to predict the time elapsed to first break. They also proposed an exponential equation of the form shown below to predict the number of subsequent breaks.

$$REP = y_1 e^{y_2 t} e^{y_3^T} e^{y_4 PRD} e^{y_5 DEV} SL^{y_6} SH^{y_7} \tag{15}$$

where REP is the number of repairs; PRD is the pressure differential; t is the age of pipe from first break; DEV is the percentage of pipe length in moderately corrosive soil; SL is the surface area of pipe in low corrosivity soil; SH is the surface area of pipe in highly corrosive soil; y_i are the regression parameters.

c) *Proportional hazards model*

The Cox proportional hazards model was first proposed by Cox (1972) as a statistical model for how long different events last. It is widely used in a number of fields such as estimating the effectiveness of cancer treatments (e.g., Schoenfeld, 1982) and AIDS clinical trials (e.g., Kim and Gruttola, 1999) in the medical field. It is a fairly general regression model with less restrictive assumptions concerning the nature or shape of the underlying survival distribution than some other models. This general failure prediction model takes the form

$$h(t, Z) = h_0(t)e^{bZ} \tag{16}$$

where t is the time of occurrence of the event of interest, $h(t, Z)$ is the hazard function (i.e. the probability of the event occurring by time t + Δt given that it has not occurred prior to time t), $h_0(t)$ is an arbitrary baseline hazard function, Z is a vector of covariates acting multiplicatively on the hazard function, and b is the vector of coefficients to be estimated by regression from available data. In applying this model to pipe break prediction, the baseline hazard function can be interpreted as a time dependent aging component, and the covariates can represent environmental and operational stress factors that act on the pipe to increase or reduce its failure hazard.

Some of the reasons provided by Cox and Oakes (1984) for considering the hazard function are as follows:

a) It is possible to generate physical insights about the failure mechanism by considering the immediate risk of an individual known to have survived at age 't'.

b) Once the functional form of the hazard rate is obtained, it is possible to make comparisons about whether an exponential distribution would adequately describe the phenomenon.

When modeling pipe breaks, the effect of explanatory variables on the failure time is of interest. Examples of such explanatory variable are:

a) Previous break and maintenance history.

b) Inherent properties of individual pipes, material, internal pressure, size.

c) External variables describing environmental characteristics like soil properties and land activities in the neighborhood of the pipes.

A limitation of the Cox proportional hazards model for predicting pipe breakage risk is that without pipe break data over a long time horizon, it is difficult to get good breakage risk estimates. If a pipe break data set includes information about breaks only in the recent past, many intermediate breaks between the time at which the pipe was installed and the time at which the detailed data becomes available would be missing. The data would then be heavily "left censored." This would lead to difficulties in obtaining strong inferences about pipe breaks with a proportional hazards model because so much of the early-life information is not included. Because the data set in this research covers only a 6-year portion of the life of the water system (over 100 years), a common situation for water utilities, the proportional hazards model was not used in this analysis.

Andreou (1986) applied the proportional hazards model to the Cincinnati water distribution system. He mainly concentrated on deriving models that described the time

from first break to a later break event, such as the second break, the third break or entry into a stage in which many breaks occur within a short time window. He also modeled the time from the second to third break. He obtained different results for the model of inter-break time period. He concluded that the proportional hazards model can work successfully in predicting breaks at the slow breaking stage. However, his work focused on breaks early in the life-cycle of a water distribution system when the data is not heavily left-censored.

d) *Generalized linear models*

Generalized linear models (GLMs) generalize linear regression to allow for non-normal, count data. They link the mean response of a specified condition distribution to a predictor function. They are based on an assumed probability distribution function (pdf) for discrete (count) data and a link function that connects the parameters of this pdf to the available covariates (e.g., Cameron and Trivedi 1998, Agresti 2002).

A Poisson GLM is a model commonly used for regression analysis of count data such as failures in an infrastructure system. Let $\vec{x}_i^{'} = [x_{1i},...,x_{ni}]$ be the vector of n covariates for system segment i (i = 1,…, m) and the number of failures on segment i be given by y_i. In the case of this research the system is a water distribution system and the segments are individual pipe segments. A regression model based on the Poisson distribution for the counts conditional on the observed values of the covariates specifies that the conditional mean of the counts is given by a continuous function $\mu(\vec{\beta}, \vec{x}_i)$ of the

covariate values as given by equation (17), where $\vec{\beta}$ is the n x 1 vector of regression parameters.

$$E\left[y_i \mid \vec{x}_i\right] = \mu\left(\vec{\beta}, \vec{x}_i\right) \tag{17}$$

Conditional on $\vec{x}_i'$, the probability density function assumed for y_i in a Poisson regression model is given, for positive integers y_i, by:

$$f\left(y_i \mid \vec{x}_i\right) = \frac{e^{-\mu_i}\mu_i^{y_i}}{y_i!} \tag{18}$$

The log link function has been used in this research to specify the conditional mean, i.e., it is assumed that $E[y_i \mid \vec{x}_i] = \exp(\vec{x}_i'\vec{\beta})$. Guikema and Davidson (2006) and Guikema et al. (2006) provided examples of using a Poisson GLM to estimate the risk of failures in an infrastructure network. They developed Poisson GLMs to predict the numbers of power outages in different segments of an electric power distribution system on the basis of explanatory variables that included information about the system, local geography, and hazards (e.g., hurricanes) that impacted the system.

GLMs assume that the explanatory variables are independent, but they do not assume that the errors are normally distributed or homoscedastic. Rather, they allow for non-normal errors and heteroscedasticity. However, in a Poisson GLM it is assumed that the conditional mean and conditional variance, given by ω_i, of the count data are equal as given by:

$$\mu_i = \omega_i = \exp(\vec{x}_i'\vec{\beta}) \tag{19}$$

This can cause difficulties in some data sets where the variance of the counts exceeds the mean of the counts (see Cameron and Trivedi 1998 and Guikema et al. 2006).

Andreou et al. (1987b) applied an exponential regression model for estimating pipe break rate λ, as a function of several covariates (pipe conditions and environmental characteristics). The third and sixth break stages were considered for estimating break rates of pipes that had reached those milestones. The probability of having y failures during a time period t was given by

$$P(y) = \frac{(\lambda t)e^{-\lambda t}}{y!}$$

(20)

where $y = 0, 1, 2,....$; λ is the yearly break rate and is given by equation (21) as

$$\lambda = \exp(bz) + e$$

(21)

where z is the vector of independent variables; b is the vector of estimated coefficients; e is the model error term. The assumptions of the model were: a) constant break rate for the period under consideration, b) independent break events for each individual pipe, and c) the covariates have a multiplicative effect on the break rate (Andreou et al, 1987). After the third break stage, the coefficient of determination R^2 was 0.34 and after the sixth break stage it was 0.46. Thus the model could be considered satisfactory after the sixth break stage.

e) *Logistic generalized linear model*

The Logistic Generalized Linear Model or Logistic regression is another type of GLM. This model predicts the probability of a discrete outcome, such as group membership, from a set of explanatory variables that may be discrete, continuous, and dichotomous or a combination of any of these. In general the dependent or response

variable is dichotomous, i.e. either 'presence or absence' or 'success or failure'. The literature review that has been done so far shows that the Logistic GLM has not been used to predict water distribution pipe break risk, yet it is an attractive model for this problem. In many cases a water utility cares more about whether or not there will be at least one break on a pipe in a given time period rather than on the precise number of breaks. The presence of one break is often enough to trigger the need for costly repair measures.

The dependent variable is a 0-1 variable that takes on the value of 1 for a given pipe segment in a given time period if there is at least one break on that pipe segment during that period. The independent variables do not have to be normally distributed, linearly related or of equal variance within each group. The dependent variable can take the value 1 with a probability of success P or the value 0 with a probability of failure (1-P). Such a variable is a binary variable and the logistic regression is then called binary logistic regression. Logistic regression can also be multinomial in cases when the dependent variable has more than two values and in such cases it is called multinomial logistic regression. This research deals only with binary logistic regression. In logistic regression, the relationship between the dependent and independent variable is not linear. A logistic regression function that is the logit transformation of P is used as in equation (22).

$$P = \frac{e^{(\alpha + \beta_1 x_1 + \beta_2 x_2 + ... + \beta_i x_i)}}{1 + e^{(\alpha + \beta_1 x_1 + \beta_2 x_2 + ... + \beta_i x_i)}} \tag{22}$$

where α is the constant regression parameter, β_i are the regression coefficients for the explanatory variables, and x_i are independent variables.

An alternative form of this model called the logit model wherein the link is a logit link unlike the Poisson GLM where the link is a log link as shown in equation (23).

$$\text{logit}[P(x)] = \log\left[\frac{P(x)}{1-P(x)}\right] = \alpha + \beta_1(X_1) + \beta_2(X_2) + \beta_3(X_3) + \dots + \beta_n(X_n) \tag{23}$$

3.   DATA DESCRIPTION

The water utility that provided the data used in this thesis is located in Texas and serves several hundred thousand customers. Almost 400,000 acre feet of water are conveyed per year through more than 4000 miles of pipes in the utility's distribution system. The average age of pipes in the system is approximately 22 years. The pipes are buried in predominantly expansive clay soils, which shrink and swell due to changes in soil moisture over the course of a year. The area served by the utility has a pronounced dry season in summer. Pipes laid in clay soil in such situations develop tensile stresses when they try to resist deformation imposed by soil shrinkage, as moisture is depleted. If there is an increase in vertical load or frictional angle, then the frictional resistance increases.

Frost load or swelling and shrinkage of expansive soils can increase vertical load (e.g. Kleiner and Rajani, 2000). Clay soils are also corrosive to buried pipes (Rajani and Zhan, 1996). Baracos et al. (1955) observed that water main breaks in Winnipeg occurred primarily between September and January and peaked when dry soil conditions existed after a hot summer or just prior to spring thaw. Morris (1967) and Clark (1971) found that volumetric swelling and shrinkage of clays contribute to high breakage rates. According to Hudak et al. (1998), water main breaks in Texas peaked in expansive soils during extreme dry periods. Based on these previous observations, the data was divided into two six month periods – November through April and May through October.

The data consisting of number of pipe breaks, the pipe diameter, pipe materials, length of pipe, the year of installation of each pipe, time since last break on each pipe,

and operating pressure within each pipe were available as attributes of the pipe network in a GIS. Among these variables, pipe materials are recorded as a set of categorical variables, each with a value of 0 or 1.

USGS data about land use and land cover in the utility's service area were obtained from WebGIS (webgis 2006). The land use and land cover data are GIS shapefiles having attributes explained in the form of codes, each code representing a particular type of land cover. The percentage length of each pipe falling in each land use type and soil type were calculated by extracting data from the GIS shapefile and then analyzing them in Microsoft Excel. These percentages were then used as input parameters. Appendix B describes the GIS processing in more detail.

The climatic data of temperature and rainfall were obtained from National Oceanographic and Atmospheric Administration's National Climatic Data Center (NCDC 2006). Both temperature and rainfall values were averaged over each six month periods.

Based on the latitude and longitude of the area in which the distribution system is located, the soil moisture data were obtained from the Land Surface Hydrology Research Group of the University of Washington (http://www.hydro.washington.edu). The website developed by this group presents a near real time daily analysis of hydrologic conditions throughout the continental United States. Their objective is to monitor the departures from normal conditions (anomalies) that may help characterize evolving drought and/or flood risks. The maximum and (maximum – minimum) soil moisture values were calculated from the available data for two six month periods each year. The

(maximum-minimum) soil moisture covariate was included because it accounts for the variability in soil moisture.

Soil corrosivity data were obtained from the Soil Survey Geographic (SSURGO) Database. The data depicts soils that are highly corrosive, moderately corrosive or mildly corrosive to steel and concrete. From this, the percentage length of each pipe falling in a particular soil corrosivity class was calculated in Microsoft Excel. The soils were divided into six types on the basis of their respective corrosivities when into contact with steel and concrete pipes. They were high steel soil, medium steel soil, low steel soil, high concrete soil, medium concrete soil and low concrete soil. High correlation was found between the soil corrosivity covariates. Principal components analysis (PCA) was therefore done to reduce the six soil corrosivity covariates to three transformed covariates which accounted for nearly hundred percent of the variability among the soil corrosivity covariate values. The following section explains the concept of PCA in more detail.

3.1. Principal components analysis

When analyzing data, one often encounters situations where there are large numbers of variables in the database. In such situations there is often a high degree of correlation between a subset of these variables. Including such variables in the analysis may affect the accuracy and reliability of the prediction model being used for analysis. If two or more covariates are correlated, there may be multiple solutions to the MLE method, an optimization problem. The estimates will then be unstable. Some of the

remedial measures to counter high correlation are to drop one or more variables causing high correlations or use methods like Principal Components Analysis.

The dimensionality of a model is the number of independent or predictor variables used by the model. A critical step in data analysis is thus to reduce the dimensionality without sacrificing the accuracy of the model. The aim of dimensionality reduction is to make the analysis and interpretation easier and at the same time preserving most of the information contained in the data. This can be achieved by a technique called Principal Components Analysis (PCA). The technique originally devised by Pearson (1901) and later developed by Hotelling (1933) is 100 years old. The properties of PCA and the interpretation of its components have been investigated extensively by various researchers. PCA has been applied in many diverse fields such as ecology, economics, psychology, meteorology, oceanography, and zoology (Cangelosi and Goriely, 2007).

In statistical terms, PCA is a linear transformation of a set of p correlated variables into a set of p pair-wise uncorrelated variables called principal components. The resulting components are arranged in such a way that the first component explains the largest portion of the total variance in the data and the subsequent components follow in decreasing order of variance explained.

PCA can also be thought of as a multivariate analysis technique, which produces a series of axes in the multidimensional data space projecting the existing data points onto these new axes. The first new axis lies along the direction that explains the largest amount of variance in the data. The second axis lies along the direction that explains the

greatest amount of variance in the remaining data and at the same time is uncorrelated

with (orthogonal to) the first axis and so on (Scott and Clarke, 2000). PCA is eigenvalue

decomposition. Mathematically, PCA can be explained as follows:

$$X^T X = VD^2 V^T$$
$$Z_j = XV_j \tag{24}$$
$$\mathrm{var}(Z_1) > \mathrm{var}(Z_2) > ..... > \mathrm{var}(Z_n)$$

where X is an $n \times m$ data matrix with n being the number of observations and m being

the number of covariates or independent variables; V is an eigen vector also called

loadings or rotation; D is the vector of eigen values; Z_j is a principal component, j.

3.2. A Sample of the Dataset

In order to give the reader an idea about the dataset, Table 3 shows the first 10

observations with a few covariates as a sample from the original dataset. The complexity

of the dataset can be understood by going through this table.

Table 3. A sample of the dataset used in the analysis

PID	NBRKS	DIA	AC	CI	CSC	DI	PVC	STL	L	INSTYR	TIME	PRE	LU1	LU2	LU3	LU4	LU5	LU6
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	1	6	1	0	0	0	0	0	548	1979	3	72	90.15	0	0	0	0	0
46	1	6	1	0	0	0	0	0	548	1979	2	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
46	0	6	1	0	0	0	0	0	548	1979	0	72	90.15	0	0	0	0	0
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	1	6	1	0	0	0	0	0	537	1984	5	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
51	0	6	1	0	0	0	0	0	537	1984	0	72	84.17	0	0	0	0	15.83
60	0	8	1	0	0	0	0	0	1122	1983	0	70	0	0	0	0	0	70.59
60	0	8	1	0	0	0	0	0	1122	1983	0	70	0	0	0	0	0	70.59
60	0	8	1	0	0	0	0	0	1122	1983	0	70	0	0	0	0	0	70.59
60	0	8	1	0	0	0	0	0	1122	1983	0	70	0	0	0	0	0	70.59
60	0	8	1	0	0	0	0	0	1122	1983	0	70	0	0	0	0	0	70.59
60	0	8	1	0	0	0	0	0	1122	1983	0	70	0	0	0	0	0	70.59

Table 4 summarizes each variable used in the analysis in terms of its mean and standard deviation and the units.

Table 4. Summary of input data. NA symbolizes that there are no units

VARIABLE	DESCRIPTION	UNITS	MEAN	STANDARD DEVIATION
NBRKS	Number of breaks		0.12	0.34
DIA	Diameter	inches	7.67	3.48
AC	Asbestos cement	NA	0.44	0.49
CI	Cast iron	NA	0.34	0.47
CSC	Concrete steel cage	NA	0.01	0.10
DI	Ductile iron	NA	0.19	0.39
PVC	Polyvinyl chloride	NA	0.02	0.14
STL	Steel	NA	0.003	0.05
L	Length	feet	721.37	548.26
INSTYR	Year of installation	NA	1973.33	18.42
TIME	Time since last break	Years	0.39	1.22
PRE	Pressure	Pounds per square inch	72.31	10.77
LU1	Residential land cover	percentage	68.41	44.36
LU2	Commercial services land cover	percentage	6.08	21.95
LU3	Industrial land cover	percentage	0.28	4.79
LU4	Transportation & communications land cover	percentage	2.50	14.38
LU5	Built up land	percentage	4.16	18.33
LU6	Agricultural land	percentage	8.35	26.74
LU7	Rangeland	percentage	3.25	16.51
LU8	Forest land	percentage	4.24	19.62
LU9	Reservoirs	percentage	0.04	1.62
LU10	Bare exposed rock	percentage	0.22	4.17
LU11	Transitional areas land cover	percentage	2.46	14.70
ST1	0-15 percent clay	percentage	2.62	13.96
ST2	15-35 percent clay	percentage	1.73	12.04
ST3	35-55 percent clay	percentage	30.30	43.47
ST4	55-65 percent clay	percentage	65.15	45.51
ST5	65-80 percent clay	percentage	0.20	4.05
TEMP	Temperature	Degrees Fahrenheit	69.47	10.43
RAIN	Rainfall	Hundredth of inches	1685.33	929.92
SMAX	Maximum soil moisture	millimeters	246.85	23.01
MX.MN	(max-min) soil moisture	millimeters	60.82	17.71
PC1	Principal Component 1	NA	-0.76	0.63
PC2	Principal Component 2	NA	-0.19	4.79
PC3	Principal Component 3	NA	0.01	0.54

The table shows that the pipes in this system are predominantly made up of asbestos cement (44 percent), cast iron (34 percent), and ductile iron (19 percent of the total number of pipes). Nearly 70 percent of the pipe (by length) is located in residential areas, and 65 percent of the pipe (by length) is in soil with a clay content of at least 55 percent. Rainfall in the area averaged approximately 17 inches per six month period. The descriptive statistics suggest that pipe breaks due to differential movement due to shrinking and swelling of clay soils may be a significant issue in this area.

Figure 2 shows a graphical representation of a few variables in the form of histograms. These variables were chosen to see how number of breaks is related with the pipe characteristics of diameter and length, the operating pressure within the pipe and the time dependent covariates such as time since last break and year of installation. These histograms suggest that none of these variables have any unusual values that could skew the results. Figure 3 shows scatter plots of number of pipe breaks against selected covariates. It can be seen that in general the number of breaks increases with increase in year of installation of the pipes, and there are more breaks for smaller diameter pipes.
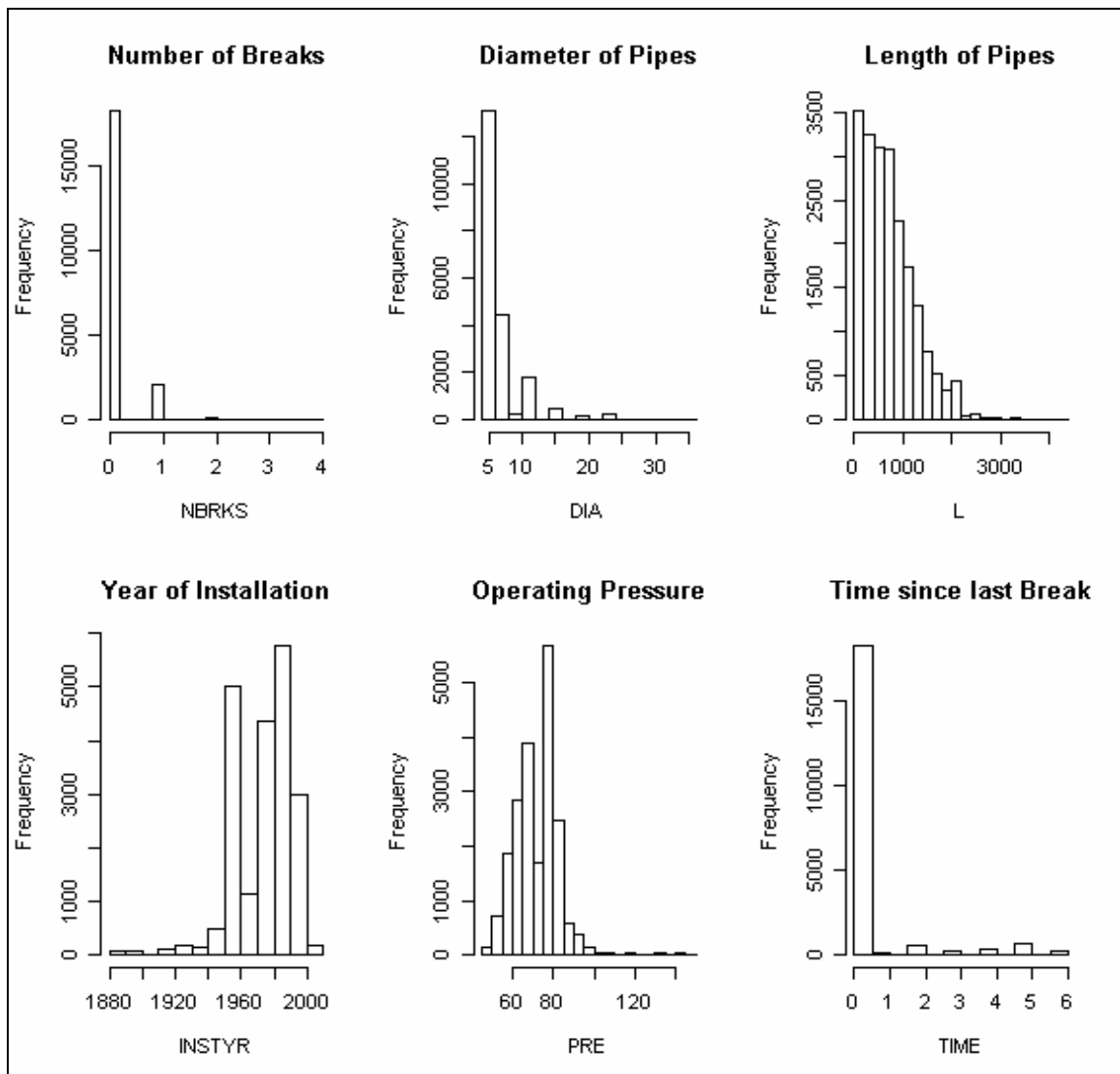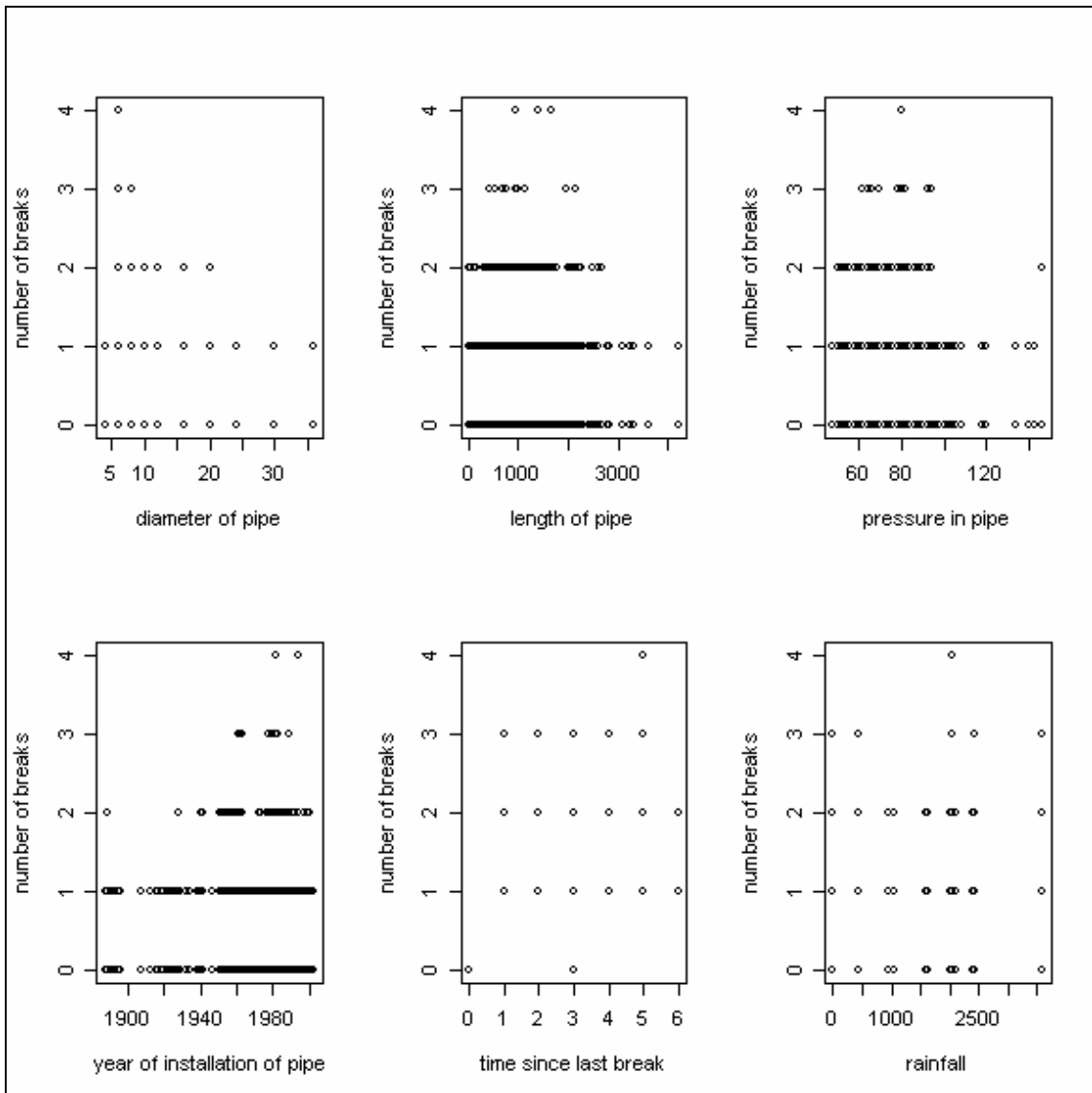
Figure 2. Histograms of some variables

Figure 3. Scatter plot of number of pipe breaks against diameter of pipes, length of pipes, pressure in pipes, year of installation of pipes, time since last break on the pipes, and rainfall.

4. MODEL DESCRIPTION

4.1. Time linear model

The original time linear model proposed by Kettler and Goulter (1985) has been modified from its basic form by extending it to include pipe diameter, pipe segment length, pipe material, the year of installation of the pipe, the operating pressure of the pipe, the land use above the pipe, the type of soil around the pipe, and the temperature, rainfall, maximum and (maximum − minimum) soil moisture in the vicinity of the pipe, soil corrosivity within each six-month period, and three principal components PC1, PC2, and PC3 with loadings or eigenvalues as shown in Appendix A. The modified model formulation is given by equation (25)

$$
\begin{aligned}
N = {} & \beta_0(D) + \beta_1(AC) + \beta_2(CI) + \beta_3(CSC) + \beta_4(DI) + \beta_5(PVC) + \beta_6(LEN) \\
& + \beta_7(INSTYR) + \beta_8(PRE) + \sum_{j=9}^{19} \beta_j(LUj) + \sum_{k=20}^{24} \beta_k(STk) + \beta_{25}(TEMP) + \beta_{26}(RAIN) \qquad (25) \\
& + \beta_{27}(SMAX) + \beta_{28}(MX.MN) + \beta_{29}(PC1) + \beta_{30}(PC2) + \beta_{31}(PC3)
\end{aligned}
$$

where N is the number of breaks per pipe in each six month period, D is the diameter of the pipe segment in inches, AC is asbestos cement, CI is cast iron, CSC is concrete steel cage, DI is ductile iron, PVC is polyvinyl chloride, L is the length of pipe in feet, Y is the year of installation of the pipe, P is the operating pressure of the pipe in pounds per square inch, LU is the land use above the pipe, ST is the type of soil around the pipe, TEMP is the average monthly temperature over each six month period, and RAIN is the total rainfall measured in hundredths of an inch at the local airport in each six month period. The pipe type, land use, soil type, and soil moisture variables were discussed in

Section 3. PC1, PC2, and PC3 are the three principal components obtained after doing a Principal Components Analysis (PCA) on the six soil corrosivity covariates.

4.2. Time exponential model

The time exponential model was first proposed by Shamir and Howard (1979). Their model was of the form as shown in equation (12). They related pipe breakage only to pipe age. The model proposed in this research has been modified to include time since last break on the pipe and year of installation of the pipe. Thus, in a way it not only includes pipe age, but also considers the number of years since last break. In general, it is observed that immediately after a pipe breaks, the breakage rate increases and then goes on decreasing as the time since last break increases. But once it has reached old age the breakage rate increases again. In other words, the pipe breakage rate follows a 'bath tub' curve. The covariates considered in the model in this research are more likely to model pipe breaks. The model is of the form as shown in equation (26).

$$y = \beta_0 * \exp(\beta_1(TIME) + \beta_2(INSTYR)) \tag{26}$$

where β_0 is the coefficient of regression, β_1 is the coefficient of time since last break, β_2 is the coefficient of year of installation.

4.3. Poisson generalized linear model

The Poisson GLM used in this analysis is of the form shown in equations (27), (28) and (29) as

$$P(Y = y \mid \vec{x}) = e^{-\mu} \frac{\mu^y}{y!} \tag{27}$$

where

$$\mu = E(Y \mid \vec{x}) \tag{28}$$

and

$$\log(\mu) = \beta_0(D) + \beta_1(AC) + \beta_2(CI) + \beta_3(CSC) + \beta_4(DI) + \beta_5(PVC) + \beta_6(LEN)$$
$$+ \beta_7(INSTYR) + \beta_8(PRE) + \sum_{j=9}^{19} \beta_j(LUj) + \sum_{k=20}^{24} \beta_k(STk) + \beta_{25}(TEMP) + \beta_{26}(RAIN) \tag{29}$$
$$+ \beta_{27}(SMAX) + \beta_{28}(MX.MN) + \beta_{29}(PC1) + \beta_{30}(PC2) + \beta_{31}(PC3)$$

where Y is the number of breaks to be predicted given the explanatory variables as explained before and β_i are the regression parameters to be estimated.

4.4. Logistic generalized linear model

The Logistic Generalized Linear Model has not been used before in modeling water distribution system reliability. And hence its usage to determine if a break will occur on a particular pipe or not becomes important. The Logistic GLM proposed in this research is of the form shown in equation (30).

$$\text{logit}[P(x)] = \log\left[\frac{P(x)}{1-P(x)}\right] = \alpha + \beta_0(D) + \beta_1(AC) + \beta_2(CI) + \beta_3(CSC) + \beta_4(DI) + \beta_5(PVC) + \beta_6(LEN)$$
$$+ \beta_7(INSTYR) + \beta_8(PRE) + \sum_{j=9}^{19} \beta_j(LUj) + \sum_{k=20}^{24} \beta_k(STk) + \beta_{25}(PC1) + \beta_{26}(PC2) + \beta_{27}(PC3) \tag{30}$$

where $P(x)$ is the probability of having a break, $1-P(x)$ is the probability of not having a break, α is the intercept, β_i are the regression parameters to be estimated, and the corresponding explanatory variables are the same as explained in Section 3.

4.5. Methodology

The models used to fit the data in this research were all regression type models. Hence there is a need to outline a general process of fitting regression type models. However, it should be noted that all the steps outlined below were not carried out. The steps that were not carried out have been mentioned at the respective step level. The following steps are commonly implemented in the regression process:

1) The data is first obtained as required. This sometimes takes longer than the actual model fitting process. The preprocessing for most of the data for this research was done in ArcGIS. This is explained in detail in Appendix B.

2) Then begins the process of checking for obvious data errors. Some means of doing this are using histograms and two dimensional plots of variables in the data against the dependent variable. An important part of data analysis is to check for outliers or influential points which tend to skew the fit results. For example, one method for checking for outliers is to use Cook's distance, D. This measures the influence of the ith data point on all the other data points. The formula for calculating Cook's distance (Belsley et al. 1980) is

$$D_i = (\hat{\beta}_i - \hat{\beta})^T X^T X (\hat{\beta}_i - \hat{\beta}) / ps^2 = (\frac{1}{p})r_i'^2 \{\frac{h_i}{1-h_i}\} \tag{31}$$

where $\hat{\beta}_i$ is the least squares estimate of the ith value of any parameter estimate β; X^T is the transpose of an $n \times p$ matrix of explanatory variables X; p is the number of parameters in the model; s^2 is the residual mean square estimate of the

population variance σ^2; r_i' is the vector of standardized residuals, and h_i is a measure of leverage.

3) A preliminary exploration is then carried out using scatter plots or data mining.

4) A correlation test is run to determine the correlation between the inputs in order to satisfy the assumption of regression models that the independent variables are uncorrelated. This can be done in R using the command cor(data).

5) Then the data is standardized using the formula:

$$\frac{x_i - \mu}{\sigma_i^2} \tag{32}$$

Standardization of a particular covariate changes the variability in that covariate and makes its mean 0 and variance 1. The data for this research were not standardized. However, the range of values for all the covariates was checked and none of them had any unusual values that could affect the model. Hence, using non-standardized variables in the models did not turn out to be a problem in this research. For future research however, it would be beneficial to use standardized variables for modeling due to the reason mentioned above.

6) High correlations between any of the variables are taken care of using Principal Components Analysis (PCA).

7) If Bayesian approach is being employed, then priors have to be developed. Since this research was done using the Frequentist approach, there was no need to develop priors.

8) Models are then fit to the data in an iterative process.

9) The goodness of fit of the different models is checked. Some goodness of fit statistics that can be used includes:

a) Log- Likelihood (LL):

$$LL = \sum_{i=1}^{m} \ln[f(Y_i \mid \beta, X_i)] \tag{33}$$

where Y_i is the actual value of the dependent variable, X_i is the independent variable, and β is the coefficient of the independent variable. Higher likelihood represents a better match between the actual value Y_i and the predicted value $\hat{Y}_i$ of the dependent variable. Thus a high log-likelihood means that the model matches the data well.

b) Akaike Information Criterion (AIC) (Akaike, 1974):

$$AIC = 2k - 2LL \tag{34}$$

where k is the number of parameters in the model. AIC takes into account the number of parameters. A lower AIC represents a model that matches the data well.

c) Deviance (D):

$$D = -2(LL - LL^*) \tag{35}$$

where LL^* is the LL for a model with one parameter per observation. Deviance measures how close to a "perfect" model (i.e. a model for which the predicted value is equal to the observed value) a particular model is. A model with lower deviance matches the data well.

d) Generalized Cross Validation (GCV):

$$GCV = \frac{1}{(1-\frac{K}{m})^2} \frac{1}{m} \sum_{i=1}^{m} (Y_i - \hat{Y}_i)^2 \qquad (36)$$

where K is the number of parameters, and m is the number of observations in the data. GCV is a measure of the match between Y_i and $\hat{Y}_i$ without using likelihood. A good model is one which has a lower GCV.

10) If the above process results in poor fits, then it makes sense to gather more or better or different data.

11) To check the predictive accuracy of the models, hold out samples can be used. If the accuracy is still poor, then it is advisable to gather better data or try using different models.

12) The final step in the regression process is to use the model for

a) Prediction – The final model can be used for estimating future events of concern.

b) Inference – From the prediction results, conclusions can be drawn regarding how good the model is in predicting new observations and whether it could be used for modeling other systems. MSE or GCV could be used for this purpose.

The analysis in this research was carried out in three stages.

The time linear, time exponential, and the Poisson GLM models were applied to the entire dataset.

A holdout sample analysis was carried out. This was done for the Time Linear, Time Exponential, and Poisson GLM models.

A random holdout sample analysis was carried out. This was performed on all the models. To check the predictive accuracy of the time linear, time exponential, Poisson GLM, and the Logistic GLM models, Mean Square Error (MSE) was used as the measure.

5. RESULTS

In this research three different methods were employed to fit the models to the data. In the first method, the models were fit to the entire dataset. In the second method, a holdout sample analysis was done, and in the third method a random holdout sample analysis was done as mentioned in Section 4.5. A detailed explanation is provided in the results of each model. The results of all the model fits are as follows.

5.1. Time linear model

The time linear model was fit in R using the command "lm". It was applied to the reduced dataset consisting of those pipes that had experienced a break during the data recording period, and the goal then was to estimate the number of breaks on each pipe segment in each six month period. This was done to avoid a zero-inflation problem (e.g., an excess of zeros above what the models could reasonably predict) that would have resulted if all pipes were included in the analysis. A step-wise regression process was employed based on p-values.

Table 5 below summarizes the parameter fit results for ten different time linear models together with the overall model fit results. The time linear model used in this research did not have an intercept term. Because past researchers who have used the time linear model chose not to include the intercept term, the intercept term was excluded from the model. However, in the future it would be a good thing to examine how the model fits the data by including the intercept term. Of the 10 models shown in Table 5, model 10 is an attractive model because (1) it contains only variables that are

statistically significant and (2) it has the highest F value (195.4) while simultaneously having the lowest number of parameters. However, its R-squared value is 0.117. This is too low to call the model a good model.

The best fit regression equation (model 10) is given by equation (37) below where the parameter definitions are the same as in the description of the data above.

$$y = -(0.0027)*(DIA) - (0.44)*(AC) - (0.45)*(CI) - (0.43)*(CSC) - (0.46)*(DI)$$
$$-(0.45)*(PVC) + (2.6 \times 10^{-5})*(L) - (0.00027)*(LU6) - (0.00032)*(LU8) \qquad (37)$$
$$-(0.00035)*(LU11) + (0.0018)*(TEMP) + (3.7*10^{-5})*(RAIN) + (0.0015)*(SMAX)$$

The highest p-values for the parameters included in equation (37) were 0.03 for transitional areas land cover (the LU11 variable), and 0.01 for agricultural land (the variable LU6). All other parameters were significant at levels below 0.01.

The results in Table 5 suggest that the time linear model can account for some of the uncertainty in the data. However, the accuracy of the predictions must also be examined. As discussed above, a linear regression model would not be expected to fit the data particularly well given that the data consists of counts of events for which the assumptions of linear regression do not hold. Figure 4 gives a plot of the predicted values versus the actual counts for the time linear model. It can be seen that there is no specific trend in the plot. In general, the time linear model predicts zero counts better than the non zero counts of breaks. However, it does predict a negative value for a few breaks.

Table 5. Parameter significance results for time linear model

Model	1	2	3	4	5	6	7	8	9	10
Diameter	**	**	**	**	***	***	**	***	***	***
Asbestos cement	N	N	N	N	***	***	***	***	***	***
Cast iron	N	N	N	N	***	***	***	***	***	***
Concrete steel cage	N	N	N	N	***	***	***	***	***	***
Ductile iron	N	N	N	N	***	***	***	***	***	***
Polyvinyl chloride	N	N	N	N	***	***	***	***	***	***
Length	***	***	***	***	***	***	***	***	***	***
Year of installation	N									
Pressure	N	N	N	N	N	N				
Land use1	N	N	N	N	N	N				
Land use2	N	N	N	N						
Land use3	N									
Land use4	N	N	N	*	.	.	N	N		
Land use5	N	N	N							
Land use6	N	N	N	***	**	**	**	**	**	**
Land use7	N	N	N	*	.	N	N			
Land use8	N	N	N	**	**	**	**	**	**	**
Land use9	N	N	N							
Land use10	N	N	N	N						
Land use11	N	N	N	**	**	*	*	*	*	*
Soil type1	N	N	N	N						
Soil type2	N	N	N	N	N					
Soil type3	N	N	N	N	N					
Soil type4	N	N	N	N	N	N				
Soil type5	N	N	N	N	N					
Temperature	*	*	*	*	*	*	*	***	***	***
Rainfall	***	***	***	***	***	***	***	***	***	***
Maximum soil moisture	***	***	***	***	***	***	***	***	***	***
(max-min) soil moisture	N	N	N	N	N	N	N			
Principal component 1	N	N								
Principal component 2	N	N	*	*	*	*	*	*	*	
Principal component 3	N	N								
Multiple R-Squared	0.118	0.118	0.118	0.118	0.118	0.118	0.118	0.118	0.117	0.117
F-statistic	83.36	88.74	94.86	101.9	114.5	130.9	152.5	171.4	182.7	195.4
DF	20511	20513	20515	20517	20520	20523	20526	20528	20529	20530

'***' signifies that the parameter is significant at p-values between 0 and 0.001, '**' signifies that the parameter is significant at p-values between 0.001 and 0.01, '*' signifies that the parameter is significant at p-values between 0.01 and 0.05, '.' Signifies that the parameter is significant at p-values between 0.05 and 0.1, 'N' signifies that the variable was included in the model but was not significant, and a blank cell signifies that the parameter was not used in the model.
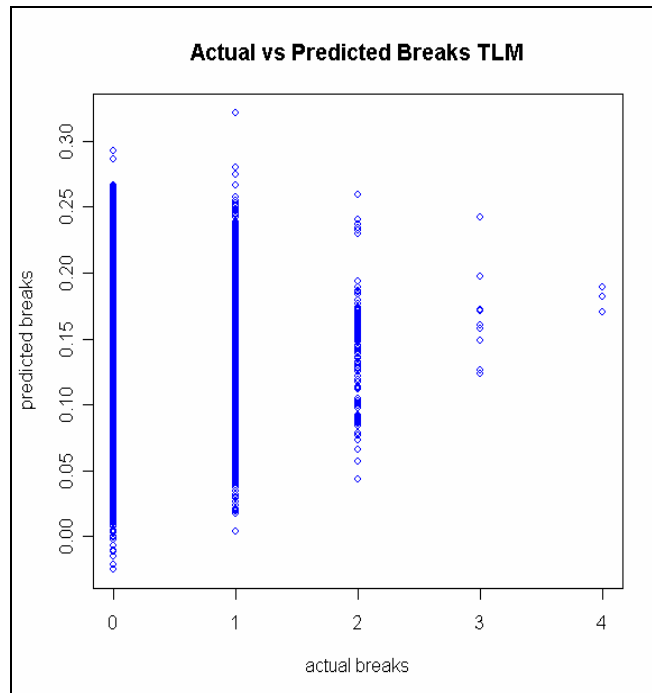
Figure 4. Time linear model predictions
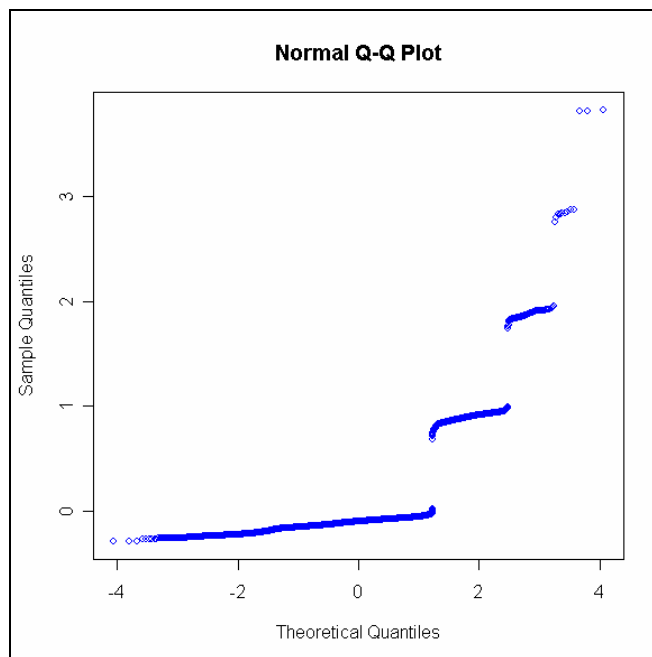
Figure 5. Q-Q plot for residuals of TLM

Figure 5 is the Q-Q plot of the residuals for the final time linear model. It can be seen that the residuals are clearly not normally distributed. Thus the assumption of linear regression models that the residuals are normally distributed is violated.

Figure 6 shows a plot of the Cook's distance for each observation in the data against the respective pipe segment. In general an observation is considered an outlier if the value of Cook's distance is greater than 1. Since there were no observations with $D > 1$, Figure 6 suggests that there are no outlier problems.
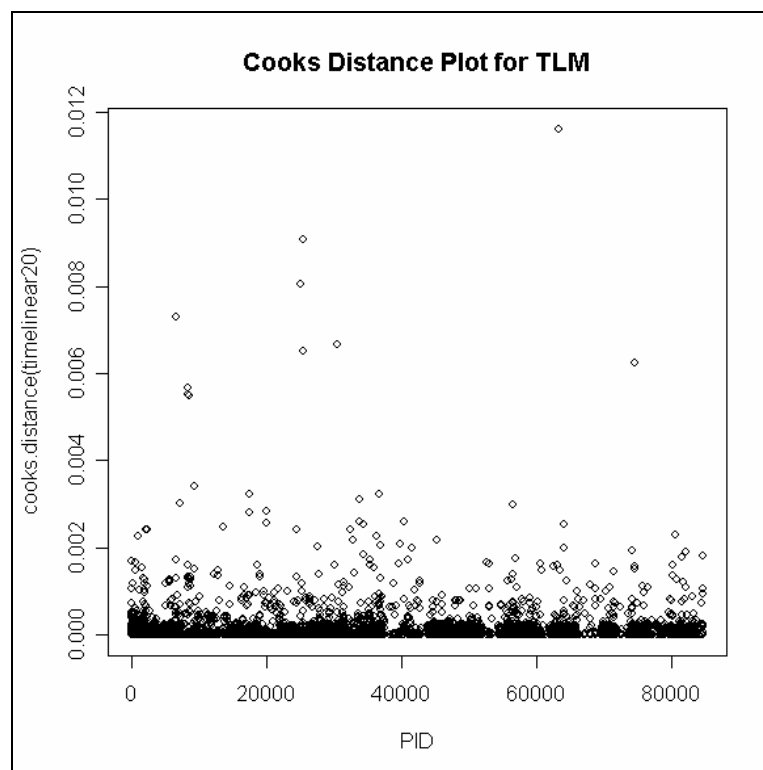
Figure 6. Cook's distance for time linear model

5.1.1. Hypothesis testing using likelihood ratio statistic

When considering the choice of a model for some data, the range of possibilities has to be defined. Hypothesis testing was performed on all the regression step models given the condition that all these models were nested models. The null hypothesis was that the deviance of each successive model was equivalent to that of the previous model. The command in R for doing this goodness of fit test by examining the size of the residual deviance compared to its degrees of freedom is

1–pchisq((dev(model2)–dev(model1)),(df.residual(model2)–df.residual(model1)))

where *dev* represents the residual deviance and *df.residual* represents the degrees of freedom for the residual deviance. The significance level for these tests was set to 0.05. Thus if the hypothesis test gives a p-value greater than 0.05, it means that the null hypothesis cannot be rejected. The results of these hypothesis tests are summarized in Table 6. This table shows that each successive model is equivalent to the previous model in terms of its deviance.

Table 6. Hypothesis tests for time linear model

MODEL	NULL HYPOTHESIS	p-value
1		
	H0: deviance(2) equivalent to deviance(1)	0.964
2		
	H0: deviance(3) equivalent to deviance(2)	0.924
3		
	H0: deviance(4) equivalent to deviance(3)	0.890
4		
	H0: deviance(5) equivalent to deviance(4)	0.896
5		
	H0: deviance(6) equivalent to deviance(5)	0.872
6		
	H0: deviance(7) equivalent to deviance(6)	0.885
7		
	H0: deviance(8) equivalent to deviance(7)	0.811
8		
	H0: deviance(9) equivalent to deviance(8)	0.759
9		
	H0: deviance(10) equivalent to deviance(9)	0.763
10		

5.1.2. *Relative effects of variables*

The covariates in the final time linear model have been listed in equation (37). When the covariates are uncorrelated as is the case in equation (37), then the β_i's could be used as indicators of contribution to the prediction of y (Bring, 1996). For a variable such as diameter, the marginal rate of change in y with respect to a change in x_j can be written as

$$\gamma_j = \frac{\partial E[Y]}{\partial X_j} = \frac{\partial(\sum \beta_j X_j)}{\partial X_j} = \beta_j \tag{38}$$

The units and variability of each covariate X_j are different. Hence the meaning of a unit change is different. To take into account this variability, the product of β_j and σ_j is considered.

$$\gamma_{\sigma j} = \beta_j \sigma_j \tag{39}$$

The parameters γ_j and $\gamma_{\sigma j}$ give an indication of the impacts of each covariate on the expected number of breaks and their relative importance (Cameron and Trivedi, 1998). Figure 7 displays a bar chart indicating the magnitude of the estimates of each covariate and the magnitude of the product of the estimate and the standard deviation for each covariate. Steel was chosen as the base material and then the fitting was done. It can be seen that the pipe materials have similar negative effects on the expected number of breaks, whereas the rest of the covariates despite being statistically significant have very little impact on the expected number of breaks.
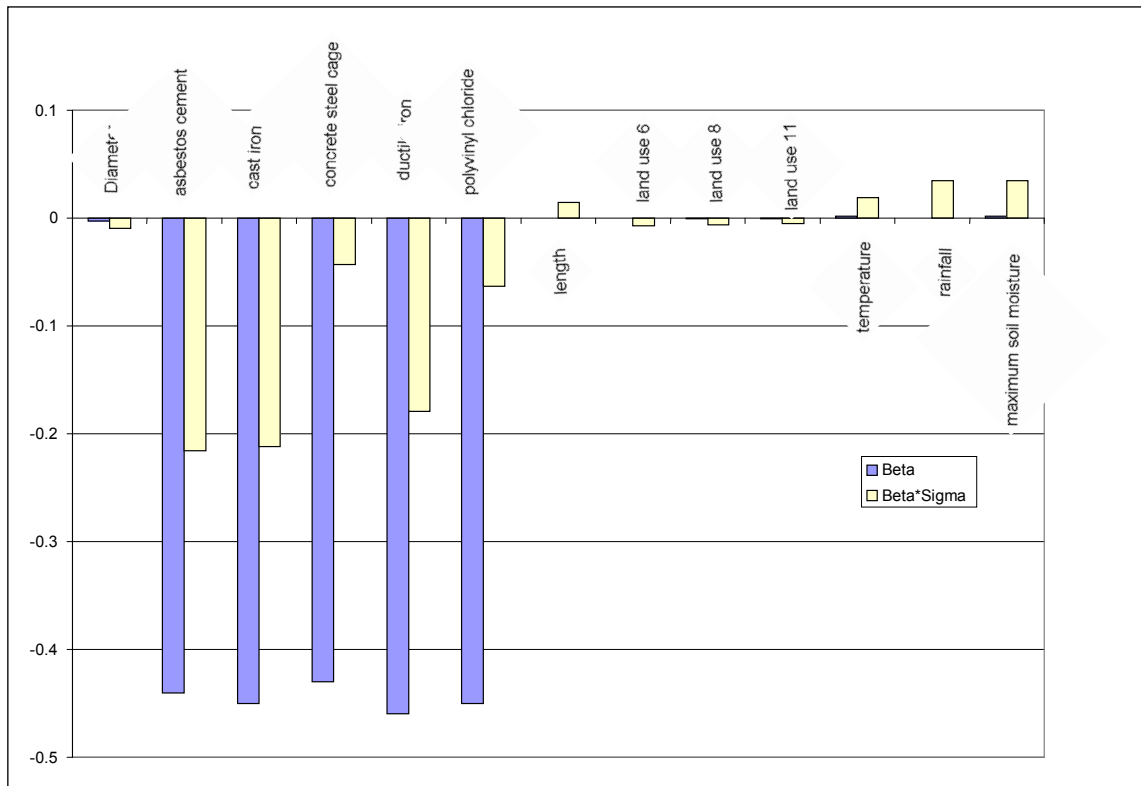
Figure 7. Relative effects of covariates in the time linear model

5.1.3. *Holdout sample analysis results*

The entire data consisting of 20,544 observations were divided into two sets. The first dataset was from the year 2000 to 2004 and was named "Train". The second dataset was for 2005 and was named "Test". The final time linear model obtained from fitting the entire dataset was then applied to the "Train" dataset and the results from this fit were used to calculate the number of breaks for the "Test" dataset. These calculated breaks were compared with the actual number of breaks in the "Test" dataset. Figure 8 shows a plot of the predicted breaks against the actual number of breaks. It can be seen again as in the full analysis, the model predicts the zero counts well as compared to the

non zero counts. The MSE for the zero counts is 0.014 and for non-zero counts it is 1.12.

This is summarized in the table on page 74.
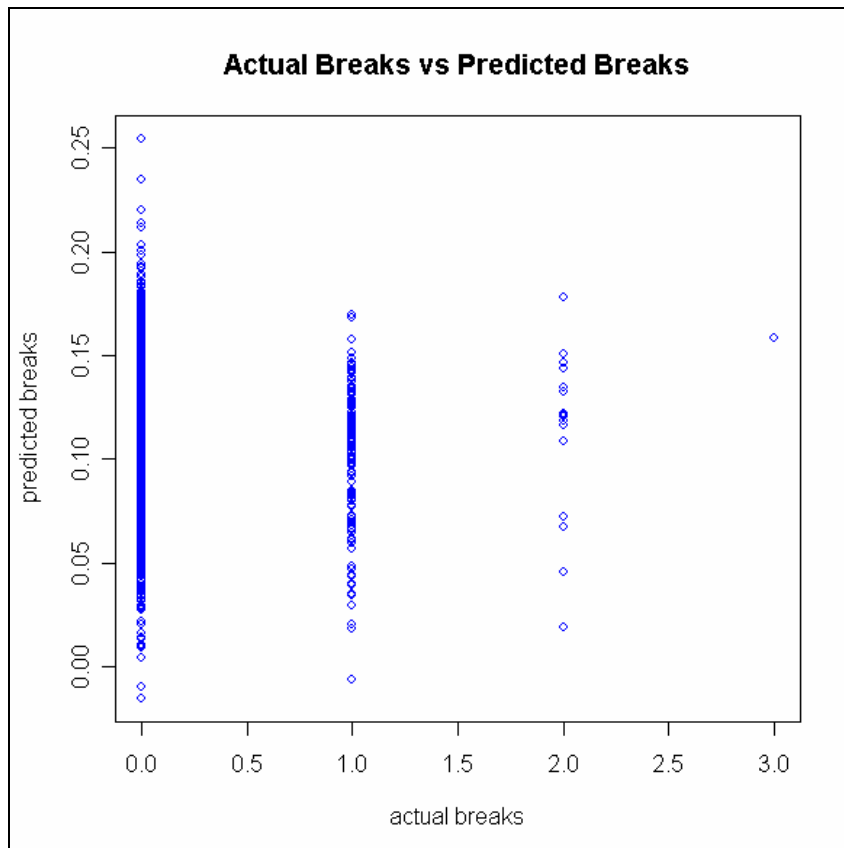
Figure 8. Holdout sample results for time linear model

5.1.4. *Random holdout sample analysis*

In this procedure, the complete data consisting of 20,544 observations was divided randomly into five pairs, each pair consisting of a "Fit" dataset and a "Validate" dataset. This was done by executing a MATLAB script. The script dropped 10% from the full dataset randomly to give five different holdout samples. "Fit" was fit with the statistical models described above and the results obtained were then used to calculate the number of breaks in "Validate". These calculated breaks were then compared with the actual number of breaks in "Validate". Figure 9 shows a plot of actual versus predicted number of breaks for all the random holdout samples. The plots show that the model behaves well when predicting zero breaks as compared to non-zero breaks. This also reflects in the MSE values for random holdout sample analysis. They were 0.015, 0.014, 0.015, 0.015, and 0.015 for the zero counts for the five random holdouts. Whereas, for the non-zero counts they were 0.96, 0.93, 0.85, 0.87, and 1. These are summarized in the table on page 75.

Figure 9. Random holdout sample analysis of time linear model

5.2. Time exponential model

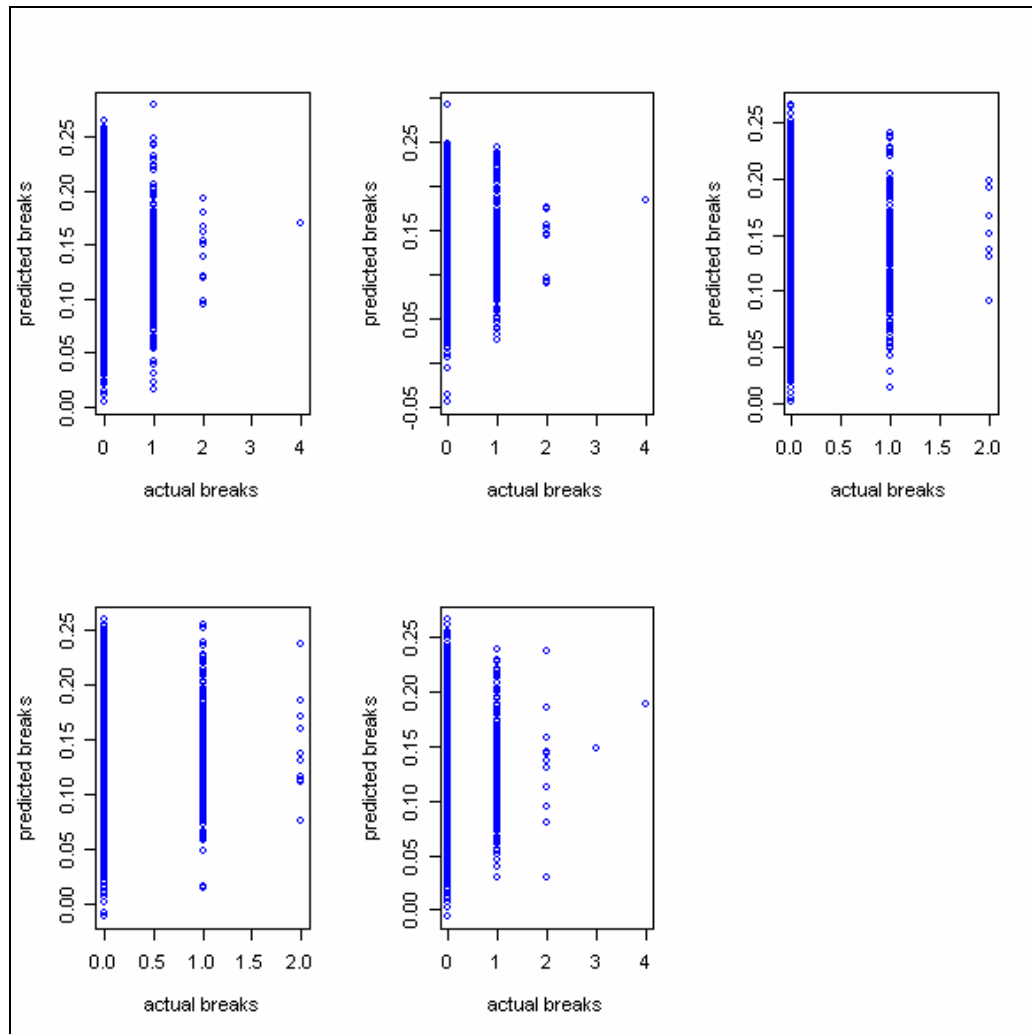Because the time exponential model is a non-linear model, it was fit in R using the 'nls' command. Only two variables were used in this model, namely, year of installation of each pipe and time since last break on each pipe. Fitting a non linear regression model requires starting values of the model parameters. Good starting values

are those that are close to the true parameter values that minimize convergence difficulties (Montgomery and Peck, 1992). A poor choice could result in convergence to a local minimum of the function, and a suboptimal solution may be obtained. To obtain good starting values for the model parameters, the solver add-in in Excel was first used to find the set of parameter values that minimized the Sum of Squared Error (SSE). These were then used as the starting values for the fitting done in R.

The fit results show that the number of breaks per time period for each pipe increases with an increase in the time since the last break on the respective pipe. Time since last break is statistically significant at a lower p-value than year of installation. An examination of the predictive accuracy of the model through Figure 10 shows that the model does better than the time linear model.

Figure 11 shows a QQ pot for the time exponential model. It is evident that the residuals are not distributed normally.
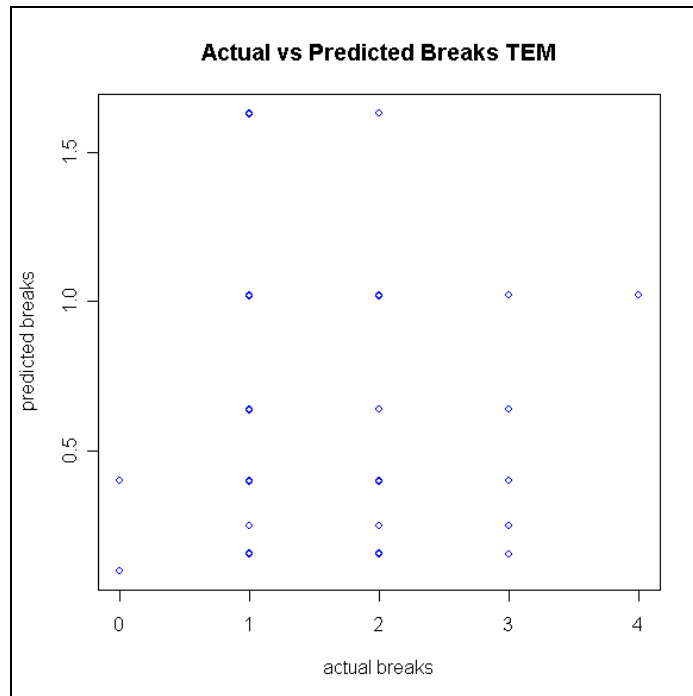
Figure 10. Time exponential model predictions
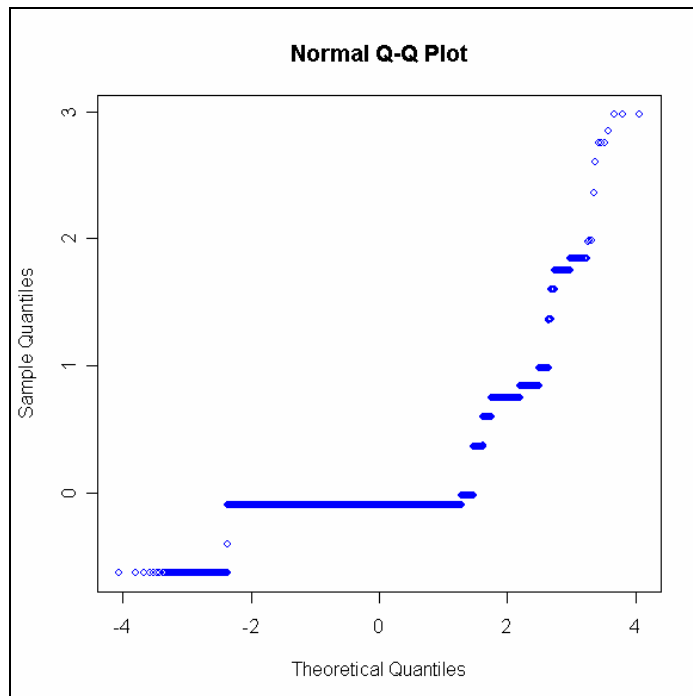
Figure 11. QQ plot for time exponential model

5.2.1. Holdout sample analysis results

Holdout sample analysis was performed in a similar fashion as in the time linear model. Figure 12 shows a plot of the predicted breaks for the holdout sample. It can be seen that the model predicts zero counts of breaks very well compared to the non-zero counts. The Mean Square Error values computed for the zero counts and for the non-zero counts of breaks for this model are 0.03 and 0.78 respectively. These are summarized in the table on page 74.
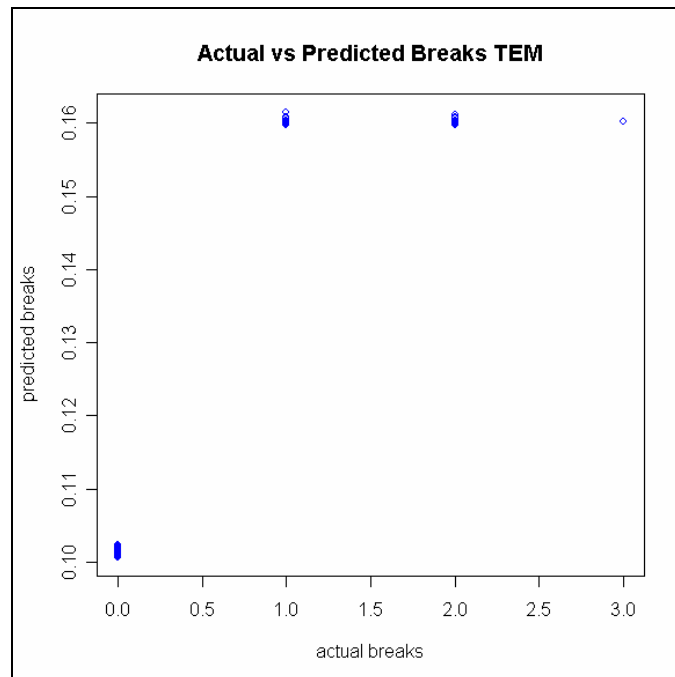
Figure 12. Holdout sample analysis for time exponential model

5.2.2. *Random holdout sample analysis*

This analysis was performed exactly as done in the random holdout sample analysis of time linear model. The same random holdouts were used. Figure 13 exhibits predicted versus actual number of breaks for each pipe of the five "validate" samples.
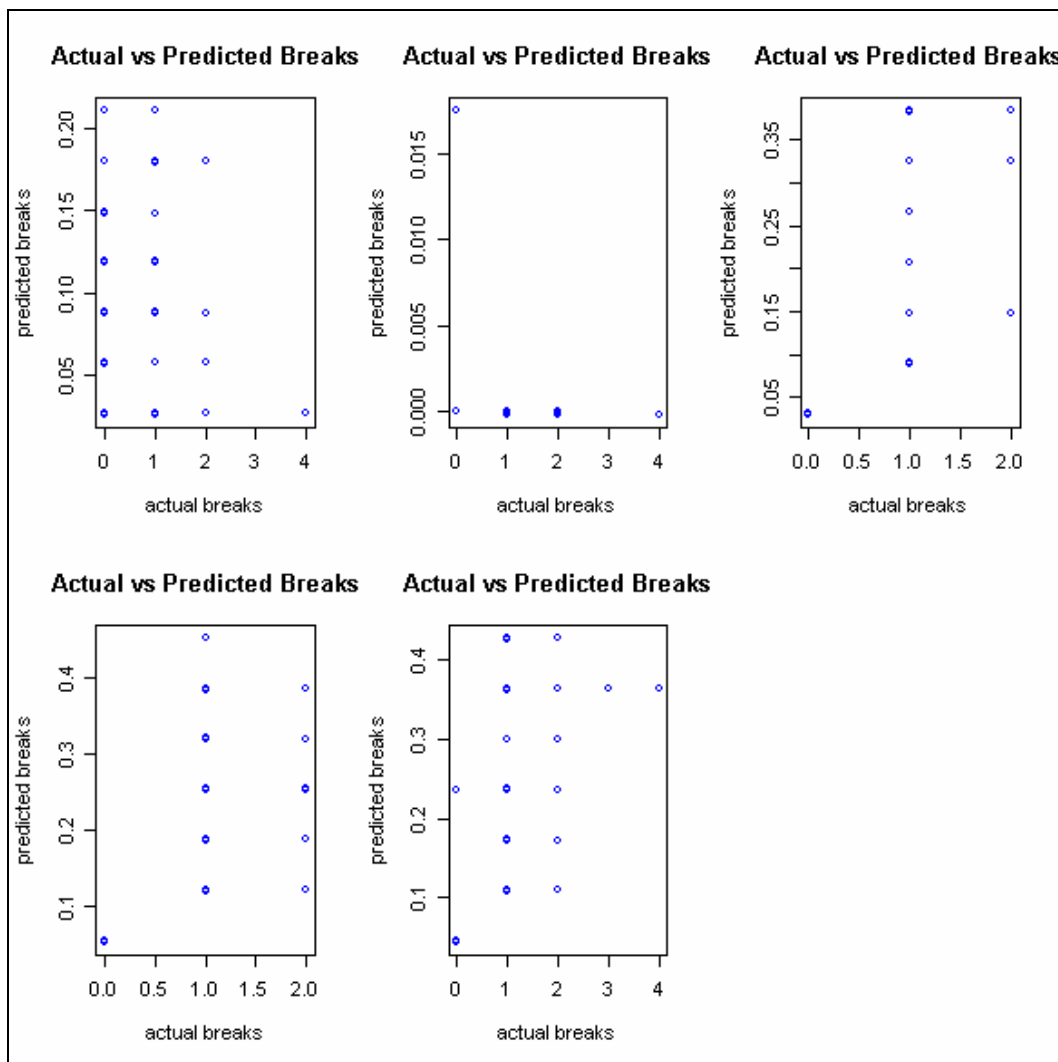
Figure 13. Random holdout sample analysis for time exponential model

It can be seen that the model predicts zero counts of breaks better than the non-zero counts. The MSE values for the five random holdouts were 0.003, 0, 0.0009, 0.003, 0.002 for zero counts of breaks and 1.146, 1.195, 0.664, 0.625, and 0.763 for non-zero counts respectively. These Mean Square Error values are summarized in the table on page 75.

5.3. Poisson generalized linear model

The table on page 68 gives the parameter significance results for ten different Poisson GLMs together with the overall model fit results. One measure of the amount of overdispersion in a data set is the deviance divided by the degrees of freedom, a quantity known as the Pearson statistic. If this quantity is greater than 1, the data is overdispersed relative to the Poisson model (Cameron and Trivedi 1998). For all of the models given in Table 8, the Pearson statistic is less than 1, suggesting that overdispersion is not a significant problem in this data set. The Poisson GLM is an appropriate model for this data set.

There are a number of ways to assess the relative goodness of fit of different Poisson GLMs. One of these is by comparing models based on the Akaike Information Criterion (AIC) score of each model as explained in Section 4.5. Minimizing the AIC yields a model that maximizes the log-likelihood with the minimum number of parameters. Model 10 has all significant variables, and its AIC is reasonably close to that of model 9 (model with the least AIC score). Model 10 is thus the preferred model.

5.3.1. *Hypothesis Testing*

A second approach for comparing Poisson GLMs is based on a likelihood ratio test. The difference in deviance between two nested models (i.e., two models for which the explanatory variables in one are a subset of the variables in the other) has approximately a Chi-squared distribution with degrees of freedom equal to the difference in degrees of freedom between the two models (see Cameron and Trivedi 1998). Hypothesis tests were carried out to compare each successive model with the previous model. The null hypothesis was that the new model and the previous old model have deviances that are equivalent. With this criterion, it can be concluded that model 10 in Table 8 provides a better fit than models 1-9 in Table 8 at a level of at least 0.05. This is summarized in Table 7.

Among the models presented in Table 8, model 10 is thus the preferred model. It cannot be shown to be inferior to the other models on the basis of a likelihood ratio test, and it is the only model that includes all statistically significant variables. For Poisson GLM model 10, the Transitional Areas land cover (Landuse 11) variable has the highest p-value (0.036) followed by the Forest land cover (Landuse 8) variable (a p-value of 0.008) and Agricultural land cover (Landuse 6) variable (a p-value of 0.002). The other covariates are significant at the 0.001 significance level.

The best fit regression equation for model 10 is given by equation (40) below where the parameter definitions are the same as in the description of the data above.

$$
\begin{aligned}
\log \mu = &-6.84 - (0.023)*(DIA) + (0.12)*(AC) + (2.2 \times 10^{-4})*(L) - (2.6 \times 10^{-3})(LU6) \\
&- (3.2 \times 10^{-3})*(LU8) - (3.3 \times 10^{-3})*(LU11) + (0.0166)*(TEMP) + (2.65 \times 10^{-4})*(RAIN) \\
&+ (0.012)*(SMAX)
\end{aligned}
\tag{40}
$$

Table 7. Hypothesis tests for Poisson generalized linear model

MODEL	NULL HYPOTHESIS	p-value
1		
	H0: deviance(2) equivalent to deviance(1)	0.92
2		
	H0: deviance(3) equivalent to deviance(2)	0.841
3		
	H0: deviance(4) equivalent to deviance(3)	0.764
4		
	H0: deviance(5) equivalent to deviance(4)	0.708
5		
	H0: deviance(6) equivalent to deviance(5)	0.689
6		
	H0: deviance(7) equivalent to deviance(6)	0.603
7		
	H0: deviance(8) equivalent to deviance(7)	0.258
8		
	H0: deviance(9) equivalent to deviance(8)	0.186
9		
	H0: deviance(10) equivalent to deviance(9)	0.093
10		

Table 8. Parameter significance results for Poisson generalized linear model

Model	1	2	3	4	5	6	7	8	9	10
Intercept	N	N	N	N	N	N	N	***	***	***
Diameter	**	**	**	**	**	**	**	**	**	***
Asbestos cement	N	**	**	**	**	**	**	**	**	**
Cast iron	N	N	.	.	.	N	N	N	N	
Concrete steel cage	N	N	N	N	N					
Ductile iron	N									
Polyvinyl chloride	N									
Length	***	***	***	***	***	***	***	***	***	***
Year of installation	N	N								
Pressure	N	N	N	N	N	N	N	N		
Land use1	N	N	N	N	N	N	N			
Land use2	N	N	N	N	N	N				
Land use3	N									
Land use4	N	N	N	N	.	.	N	N	N	
Land use5	N	N	N	N						
Land use6	N	N	N	N	**	**	**	**	**	**
Land use7	N	N	N	N	.	.	N	N		
Land use8	N	.	.	.	**	**	**	**	*	**
Land use9	N	N	N	N						
Land use10	N	N	N	N	N					
Land use11	N	.	.	.	**	**	*	*	*	*
Soil type1	N	N	N	N	N	N	N	N		
Soil type2	N	N	N	N	N	N	N	N		
Soil type3	N	N	N	N	N	N	N	N		
Soil type4	N	N	N	N	N	N	N	N		
Soil type5	N	N	N	N	N	N	N			
Temperature	**	**	**	**	**	**	***	***	***	***
Rainfall	***	***	***	***	***	***	***	***	***	***
Maximum soil moisture	***	***	***	***	***	***	***	***	***	***
(max-min) soil moisture	N	N	N	N	N	N				
Principal component 1	N	N	N							
Principal component 2	N	N	N	.	.	.	.	.	.	
Principal component 3	N	N	N							
Residual Deviance	10343	10343	10344	10344	10344	10345	10347	10348	10353	10360
AIC	14961	14958	14954	14950	14946	14943	14941	14938	14931	14932
DF	20511	20513	20515	20517	20519	20521	20523	20525	20531	20534

'***' signifies that the parameter is significant at p-values between 0 and 0.001, '**' signifies that the parameter is significant at p-values between 0.001 and 0.01, '*' signifies that the parameter is significant at p-values between 0.01 and 0.05, '.' Signifies that the parameter is significant at p-values between 0.05 and 0.1, 'N' signifies that the variable was included in the model but was not significant, and a blank cell signifies that the parameter was not used in the model.

Figure 14 shows a plot between actual breaks and predicted breaks for the Poisson GLM. It is visually evident from Figure 10 and Figure 14 that the model does not predict the zero and non-zero breaks as well as the time exponential model. Also looking at Figure 4 and Figure 14, the Poisson GLM and the time linear model predict the non-zero breaks in a similar fashion, but the time linear model predicts negative values of the zero counts of breaks as opposed to the Poisson GLM.
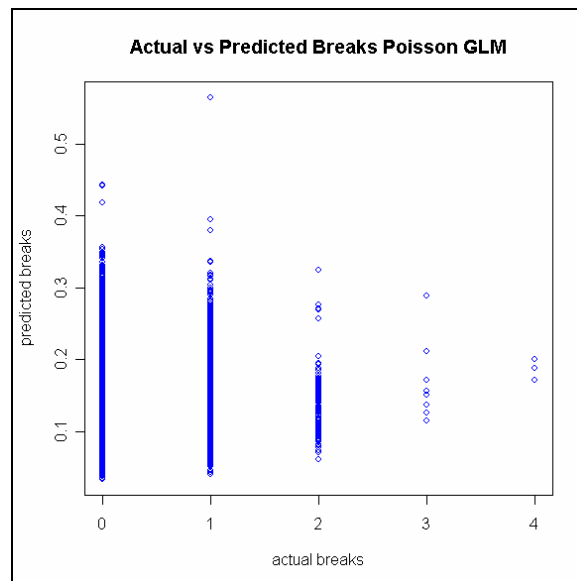

Figure 14. Poisson generalized linear model predictions

5.3.2. *Relative Effects of Variables*

For any variable such as diameter for example, the relative rate of change in y with respect to a change in x_j can be written as

$$\delta_j = (\frac{1}{\mu(y)})\frac{\partial\mu(y)}{\partial x_j} = \beta_j \tag{41}$$

For categorical variables such as AC, CI, CSC, DI, and PVC that takes on values of 0 and 1, the interpretation of the derivative may be different, but the same formula is used (Cameron and Trivedi, 1998). The units and variability of each covariate x_j are different. Hence the meaning of a unit change is different (Liu et al., 2005). To take into account this variability, the product of β_j and σ_j is considered.

$$\delta_{\sigma_j} = \beta_j \sigma_j \qquad\qquad (42)$$

The parameters δ_j and δ_{σ_j} give an indication of the impacts of each covariate on the expected number of breaks and their relative importance (Cameron and Trivedi, 1998).

Figure 15 displays a bar chart indicating the magnitude of the estimates of each covariate and the magnitude of the product of the estimate and the standard deviation for each covariate. It can be seen that the pipe material Asbestos Cement has the largest positive impact followed by temperature and maximum soil moisture on the predicted number of breaks, whereas diameter has the most negative impact on the predicted number of breaks. Based on these observations, it can be said that Asbestos Cement is not a good material for manufacturing pipes for water distribution systems, as it has a high incidence of breakage rate. Temperature, rainfall and soil moisture have high variability. Thus their values can vary from one extreme to the other. This is likely to affect pipe breaks due to the fact that the area where this water utility is located has predominantly clay soils which shrink and swell. On the other hand, with decrease in diameter of pipes, the breakage rate increases.
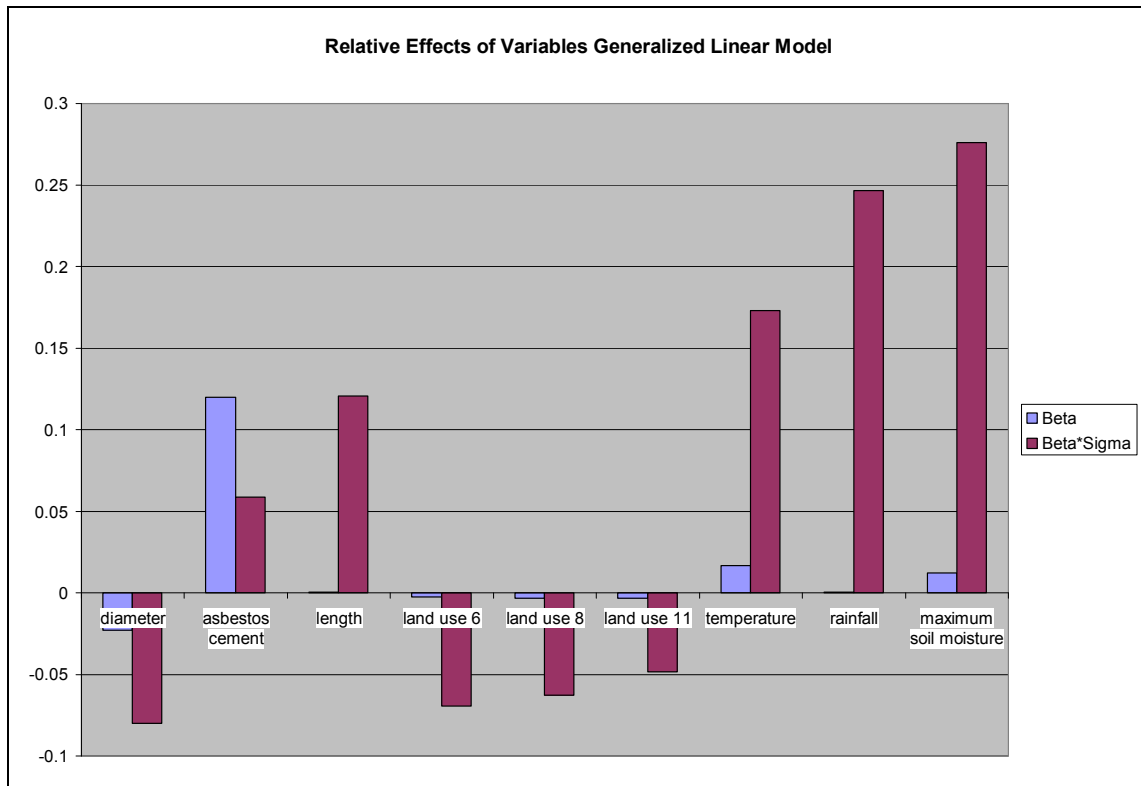
Figure 15. Relative effects of variables for Poisson GLM

5.3.3. *Holdout sample analysis*

The procedure followed in the holdout sample analysis was similar to the ones adopted in time linear and time exponential models. Figure 16 shows a plot of the predicted breaks against the actual numbers of breaks for the holdout sample. The plot shows that the model predicts zero counts of breaks very well compared to the non-zero counts. The Mean Square Error values for this analysis were 0.02 and 1.1 for zero counts and non-zero counts of breaks respectively. This is summarized in Table 10.
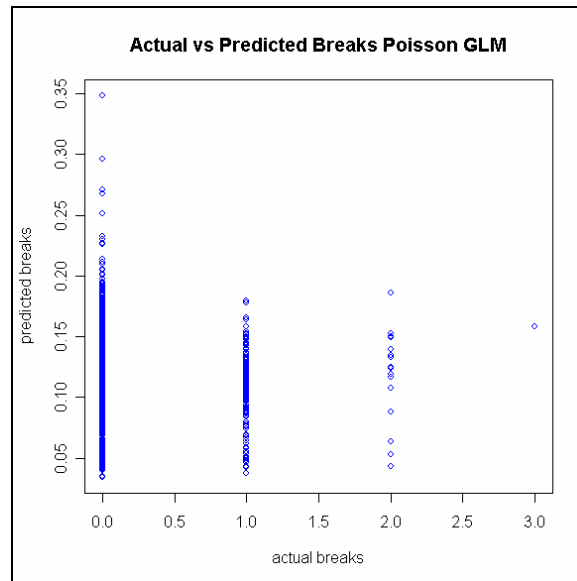
Figure 16. Holdout sample analysis plot

5.3.4. *Random holdout sample analysis*

The same procedure of random holdout sample analysis that was performed on the time linear model was repeated here. Figure 17 exhibits predicted versus actual number of breaks for each pipe of the five "validate" samples. The plots show that as a predictive model, the Poisson GLM predicts zero counts of breaks significantly better than non zero breaks. The Mean Square Error values for zero counts and for non-zero counts were 0.016, 0.015, 0.015, 0.016, 0.015 and 0.965, 0.87, 0.90, 1.04, and 1 respectively. The Mean Square Error values have been summarized in Table 11.
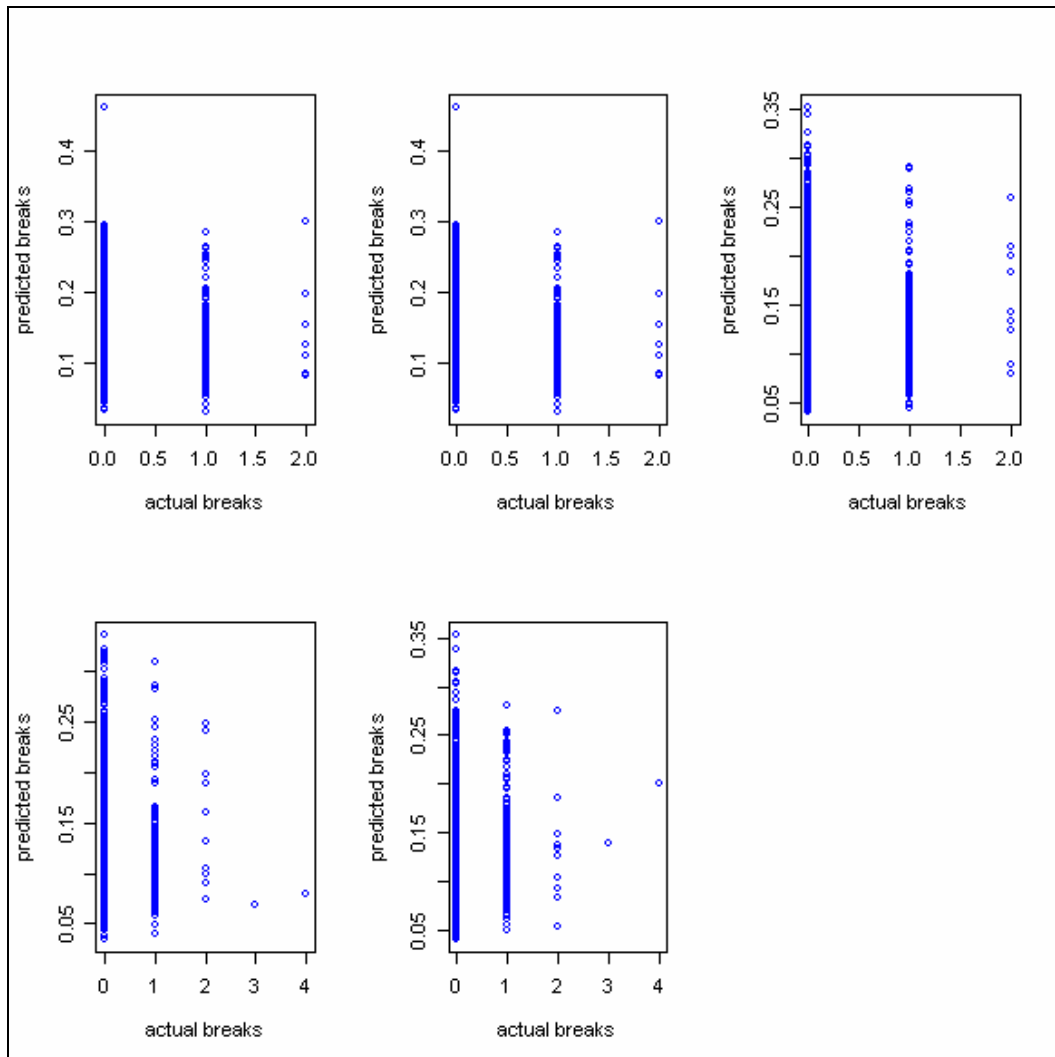
Figure 17. Random holdout sample analysis of Poisson GLM

Table 9 summarizes the goodness of fit statistics for the time linear, time exponential, and Poisson GLM models. Table 10 and 11 summarize the Mean Square Errors (MSE) and the ratio of Root Mean Square Error (RMSE) to the average number of breaks in the system for the TLM, TEM, and Poisson GLM models respectively for holdout sample analysis and random holdout sample analysis. As far as Deviance and AIC are concerned, the model with the least values of these statistics is considered a

good model. On the other hand, the model with the highest log-likelihood is considered a good model. Table 9 suggests that the time exponential model is the best among the three models.

Table 9. Goodness of fit statistics for all models

Model	Deviance	Log-Likelihood	Degrees of Freedom	AIC
TLM	2405.45	-7118.96	20530	14267.91
TEM	1141.57	-537.09	20541	1066.18
Poisson GLM	10360	-7456.03	20534	14932

The Mean Square Errors for all three models were computed separately for zero count and non zero count breaks. This was done because the data consists of nearly 90 percent pipe segments with zero breaks. Table 10 shows that all three models predict zero counts reasonably well and are nearly equivalent. With respect to non-zero counts, the TEM does the best.

Table 10. Mean square error for holdout sample analysis of all models

Model	Mean Square Error		RMSE/Average no. of breaks	
	For Zeros	For Non-zeros	For Zeros	For Non-zeros
TLM	0.014	1.12	0.986	8.82
TEM	0.03	0.78	1.443	7.36
Poisson GLM	0.02	1.1	1.178	8.74

Table 11 displays the minimum, mean and maximum of Mean Square Errors as well as the ratio of Root Mean Square Error to the average number of breaks for all the three models. This ratio explains the relation between the root mean square error and the

average number of breaks. Ideally this ratio should be close to zero. For example, in case of the time exponential model, the root mean square error is 1.44 times the average number of breaks for zeros and 7.36 times the average number of breaks for non-zeros. Unlike the holdout sample analysis, the TEM is the best model for predicting zero counts as well as non-zero counts of breaks.

In general, all the models that were applied in this research are not good predictors of non-zero counts of breaks. A possible reason for this could be due to the fact that the data is heavily zero inflated. Usually, when there a lot of zeros in the response variable, it is advisable to try zero inflated models. The most common zero inflated models are the Zero Inflated Poisson (ZIP) and the Zero Inflated Negative Binomial (ZINB) models. To deal with the inability of the three models to predict non-zeros well, it was decided to try the Logistic GLM. Instead of predicting actual counts of breaks, this model predicts the probability of having breaks on any particular pipe.

Table 11. Mean square error for random holdout sample analysis of all models

Mean Square Error		Model		
		TLM	TEM	Poisson GLM
For Zeros	Min	0.0148	1.67×10^{-7}	0.015
	Mean	0.0152	0.0017	0.0155
	Max	0.0154	0.003	0.016
For Non Zeros	Min	0.847	0.625	0.87
	Mean	0.924	0.878	0.955
	max	1	1.195	1.04
Root Mean Square Error/Average number of breaks				
For Zeros		1.02	0.34	1.02
For Non-zeros		8.01	7.8	8.14

5.4. Logistic generalized linear model

The logistic regression model was fit in R using the command "glm." However, an expanded data was used relative to the one used to test the time linear model, time exponential model, and Poisson GLM. Unlike these three models that do not model an excess of zero counts well, the logistic model is designed specifically to deal with 0-1 data where there are a large percentage of zeros. This allowed the usage of the full data set of 83,300 pipe segments rather than only those pipes that experienced at least one break during the recording period. Fur the purposes of demonstrating the logistic model the data was not separated into distinct time periods. That is, there was one entry in the data set per pipe. If there was at least one break over the entire collection period (2000-2005) the 0-1 response variable was set to 1. Because the timing of breaks was not accounted for, the rainfall or temperature variables were not used in the model. In its current form, this model would then predict the probability of a break on a given pipe segment over a six year period on the basis of time-invariant explanatory variables. The best fit model results show that the following variables are statistically significant at a 0.05 level:

- pipe diameter,
- the asbestos cement, cast iron, and concrete steel cage pipe material variables,
- pipe length,
- the residential, commercial services, industrial, transportation and communications, built up land, agricultural land, rangeland, reservoirs and transitional land covers,

- soil types variables for the 0-15 percent clay, 35-55 percent clay categories, and principal component 1.

The ductile iron variable, the year of installation, pressure, the forest land cover (LU8), the land cover of bare exposed rock (land use 10), soils with clay percentages between 15-35, 55-65, and 65-80 were removed from the model since they did not turn out to be significant in the models tried before obtaining the final model. The parameter significance results along with the overall model fit results are listed in Table 12. Equation (43) shows the final model with the parameter estimates.

$$
\begin{aligned}
\operatorname{logit}[P(x)] = \log\left[\frac{P(x)}{1-P(x)}\right] =\ & -5.82 - (0.12)*(DIA) + (1.21)*(AC) + (1.48)*(CI) + (1.84)*(CSC) \\
& + (1.6\times10^{-3})*(L) + (0.02)*(LU1) + (0.02)*(LU2) + (0.02)*(LU3) + (0.02)*(LU4) + 0.02*(LU5) \\
& + (0.01)*(LU6) + (0.02)*(LU7) + (0.02)*(LU9) + (0.02)*(LU11) - (0.01)*(ST1) - 0.005*(ST3) \\
& - (0.02)*(PC1)
\end{aligned}
\tag{43}
$$

The deviance for this model was 20,559 for 83,282 degrees of freedom and the AIC was 20,595 for the same number of degrees of freedom. The low deviance/degrees of freedom ratio combined with the AIC value substantially below the degrees of freedom suggest that this model fits the data reasonably well. Also, a hypothesis test done to compare the deviances of the final model to that of the null model gives a p-value of 1. The high p-value shows that the final model is a good model for this dataset.

The parameter values suggest that larger pipes are less likely to experience breaks. The fact that all of the regression parameters for the included pipe materials are positive, suggests that these material types are more likely to experience breaks than PVC pipe, the omitted material type. Furthermore, concrete steel cage (CSC) and cast iron (CI) pipes are likely to have the highest breakage risk from among all pipe types, all

other variables being equal. Conclusions such as this can help guide pipe inspection decisions. More specific guidance can come from examining the predicted probabilities of breaks for each pipe and coupling this with an estimate of the severity of not catching a break on a given pipe.

5.4.1. *Random holdout sample analysis*

The large dataset consisting of 83,300 pipe segments was divided into five different pairs, each pair consisting of a "fit" dataset that was fit with the Logistic GLM and a "validate" dataset which was used to validate the model i.e. the dataset for which predictions were done using the model. The Mean Square Errors for all five samples were calculated separately for zeros and ones, and the mean of all these MSEs turned out to be 0.25. The ratio of Root Mean Square Error to the average number of breaks was found to be 4.17.

Table 12. Parameter significance results for logistic generalized linear model

Model	1	2	3	4	5	6	7	8	9	10
Intercept	N	N	N	.	.	.	.	***	***	***
Diameter	***	***	***	***	***	***	***	***	***	***
Asbestos cement	N	***	***	***	***	***	***	***	***	***
Cast iron	N	***	***	***	***	***	***	***	***	***
Concrete steel cage	N	***	***	***	***	***	***	***	***	***
Ductile iron	N	.	.	.	.	.				
Steel	N	*	*	*	*	*	N	N	N	
Length	***	***	***	***	***	***	***	***	***	***
Year of installation	N	N								
Pressure	N	N								
Land use1	.	.	.	.	.	.	.	***	***	***
Land use2	.	.	.	.	.	.	.	***	***	***
Land use3	.	.	.	.	.	.	.	***		***
Land use4	.	.	.	.	.	.	.	***	***	***
Land use5	.	.	.	.	.	.	.	***	***	***
Land use6	.	.	.	.	.	.	.	***	***	***
Land use7	.	.	.	.	.	.	.	***	***	***
Land use8	.	.	.	.	.	.	.			
Land use9	.	.	.	.	.	.	.	*	***	*
Land use10	.	.	.	.	.	.	.	N		
Land use11	.	.	.	.	.	.	.	***	***	***
Soil type1	N	N	N	***	***	***	***	***	***	***
Soil type2	N	N	N							
Soil type3	N	N	N	***	***	***	***	***	***	***
Soil type4	N	N	N							
Soil type5	N	N	N	N						
Principal component 1	N	**	**	**	**	**	**	**	**	**
Principal component 2	N	N	N	N	N					
Principal component 3	N									
Residual Deviance	20541	20544	20544	20545	20546	20549	20552	20555	20557	20559
AIC	20601	20600	20596	20593	20592	20593	20594	20595	20595	20595
DF	83270	83272	83274	83276	83277	83278	83279	83280	83281	83282

'***' signifies that the parameter is significant at p-values between 0 and 0.001, '**' signifies that the parameter is significant at p-values between 0.001 and 0.01, '*' signifies that the parameter is significant at p-values between 0.01 and 0.05, '.' Signifies that the parameter is significant at p-values between 0.05 and 0.1, 'N' signifies that the variable was included in the model but was not significant, and a blank cell signifies that the parameter was not used in the model.

5.5. Comparison of Poisson GLM and Logistic GLM

From the predicted breaks obtained by applying the Poisson GLM to the smaller dataset of 20,796 observations, the probability of having one or more breaks for the zero counts of breaks and the non-zero counts of breaks were obtained using equation (20). Histograms of these predicted probabilities are shown in Figure 18. To compare the Poisson GLM and the Logistic GLM, the Logistic GLM was applied to the smaller dataset. From the predicted probabilities that were calculated, histograms were plotted separately for the 0 variable and the 1 variable for probability of having one or more than one break. These are shown in Figure 19. In each of these figures, the histogram on the left of the figure is for the zero counts and the one on the right is for the non-zero counts. It can be clearly seen from the two figures that the Poisson GLM and Logistic GLM are equivalent in predicting the zero counts and the non-zero counts for the same set of pipes.
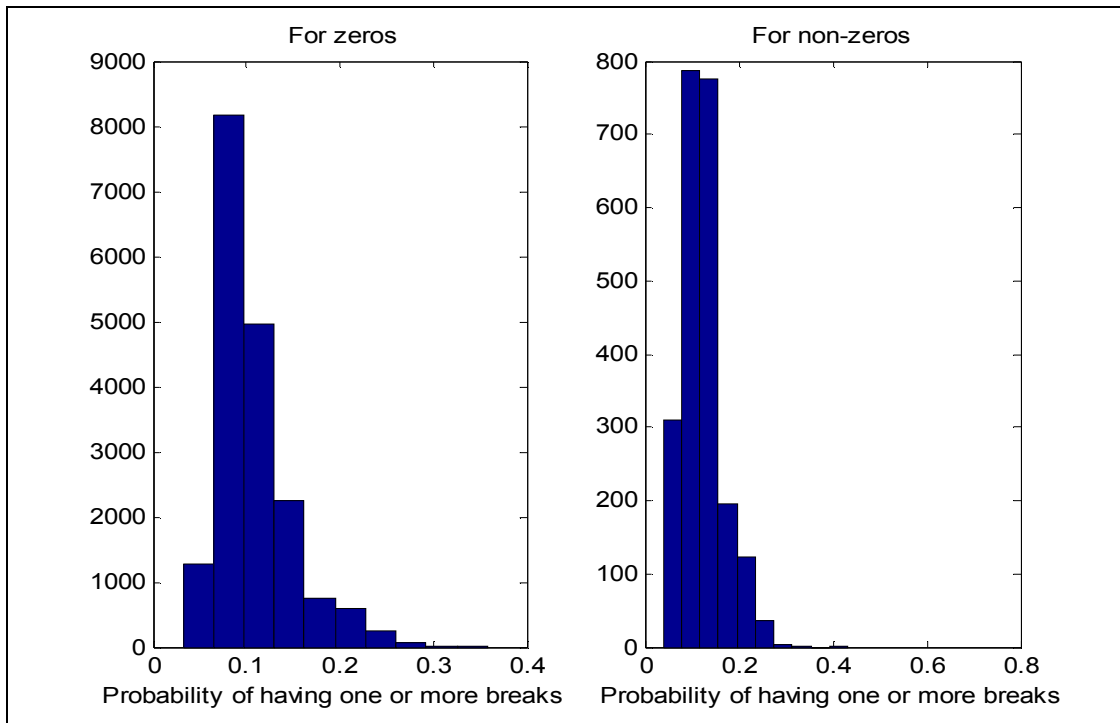
Figure 18. Probability of having one or more breaks for Poisson generalized linear model
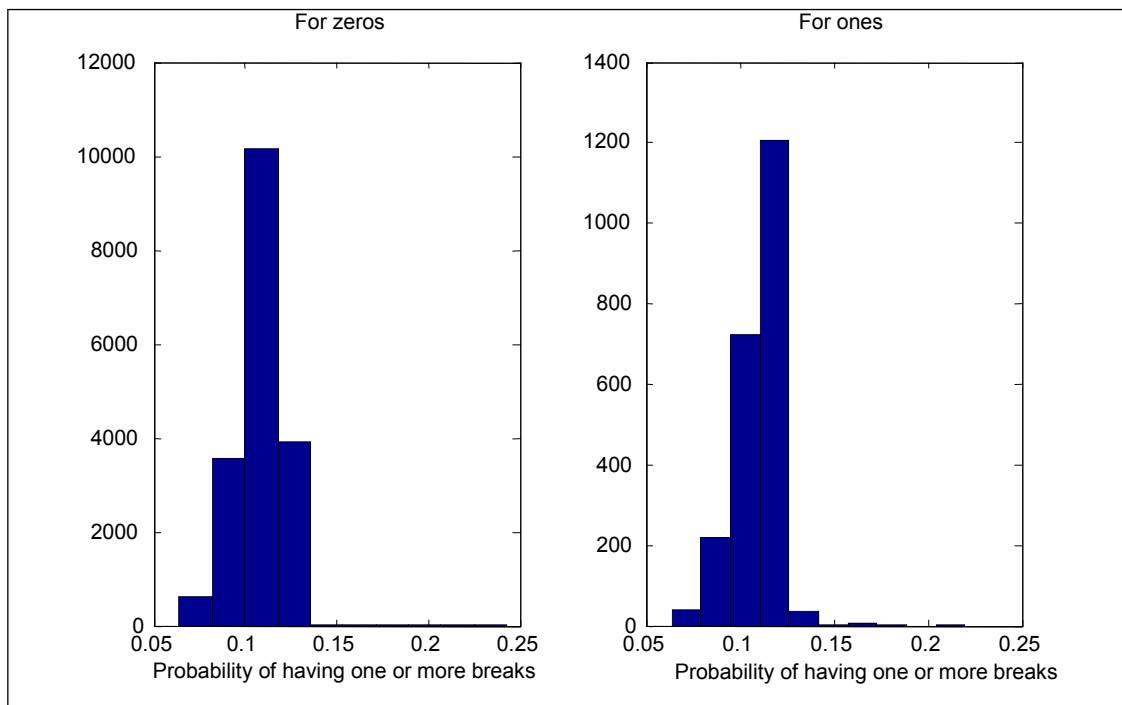
Figure 19. Probability of having no breaks or more than one break for logistic generalized linear model

5.6. Summary

In this research, four different models namely, the time linear model, the time exponential model, the Poisson Generalized Linear Model, and the Logistic Generalized Linear Model were used. The smaller dataset consisting of 20,796 observations were fit with the time linear, time exponential, and the Poisson GLM, whereas the larger dataset consisting of 83,300 observations were fit with the Logistic GLM.

The results from fitting the time linear model to the data show that the model is not a good model for modeling water distribution system reliability. The R-squared value for this model is very low i.e. 0.117. This clearly shows that the relationship between the predicted breaks and the actual breaks is not linear. The time exponential model behaves better than the time linear model in fitting this data. The fit results indicate that the number of breaks per time period for each pipe increases with an increase in the time since the last break on the respective pipe. For the Poisson GLM the Pearson statistic is less than 1 indicating that there is no overdispersion in the data. The model appears to be modeling the number of breaks pretty similar to the time linear model.

A comparison of the goodness of fit between the time linear, time exponential and Poisson GLM models shows that the AIC, deviance and the log-likelihood for the time exponential model are the best according to the criteria mentioned in Section 4.5. As far as predictive ability is concerned, again the time exponential model does well in modeling the zero counts as well as the non-zero counts of breaks.

For the logistic GLM, the low deviance/degrees of freedom ratio combined with the AIC value substantially below the degrees of freedom suggest that this model fits the data reasonably well. Also, a hypothesis testing done to compare the deviances of the final model to that of the null model gives a p-value of 1. The high p-value shows that the final model obtained after going through the stepwise regression procedure is a good model for this dataset. A random holdout sample analysis carried out to check the predictive accuracy of the model in estimating the probability of future breaks gives an MSE of 0.25. The logistic GLM is a regression model that has been specifically designed to handle excess amount of zeros in the data and it does this job successfully in this research by giving a low MSE value for no break pipes.

A Logistic GLM was also fit to the smaller dataset. The overall fit results give an AIC value of 14,097 and a deviance of 14,061. The log-likelihood for this model is -7,030.34. Comparing these values to those of the time linear, time exponential and the Poisson GLM (Table 9), it can be observed that the Logistic GLM has lower AIC and higher log-likelihood than the time linear and the Poisson GLM, but it has higher AIC, deviance and lower log-likelihood than the time exponential model. The logistic GLM and the Poisson GLM predict the zero counts of breaks equivalently but the logistic GLM does well in predicting the non-zero counts of breaks.

6. DISCUSSION

The present state of deterioration in water distribution systems gives rise to questions regarding optimal repair, replacement and rehabilitation strategies that need to be implemented. The heavy presence of zero counts of breaks in the water distribution system data used in this research indicates that the system has been well maintained and is pretty robust. However, the results from this research show that the water utility cannot relax on this issue. The water utility managers still have to be on their toes to ensure that in the future their distribution system remains robust.

6.1.   Applications of the logistic GLM

One could envision water utilities assigning ranks to all the pipes in their distribution systems based on probabilities predicted by using models like the Logistic GLM. Then a plot such as the one shown in Figure 20 could be made. In this plot, the X-axis represents the ranking of pipes based on predicted probabilities obtained by applying the above model and the Y-axis represents the fraction of pipes at or above the rank that had a break. Since zeros and ones were being predicted, there were bound to be a lot of pipes with the same predicted probabilities. Thus these pipes were assigned the same ranks. After manually counting the number of pipes it can be deduced that if the first 30 ranked pipes are observed, only about 100 pipes need to be inspected. The probability of finding a break per pipe would be nearly 35%. However, if the utility decides to inspect 100 pipes at random from the 83,300 pipes, then the probability of finding a break per pipe would be about 5%. By conducting this random inspection, the

utilities would be wasting their precious time, manpower and monetary resources. A water utility would thus concentrate their resources on inspecting those first 30 ranked pipes. Thus a plot such as Figure 20 could be really beneficial to water utilities trying to conserve their precious time and monetary resources.
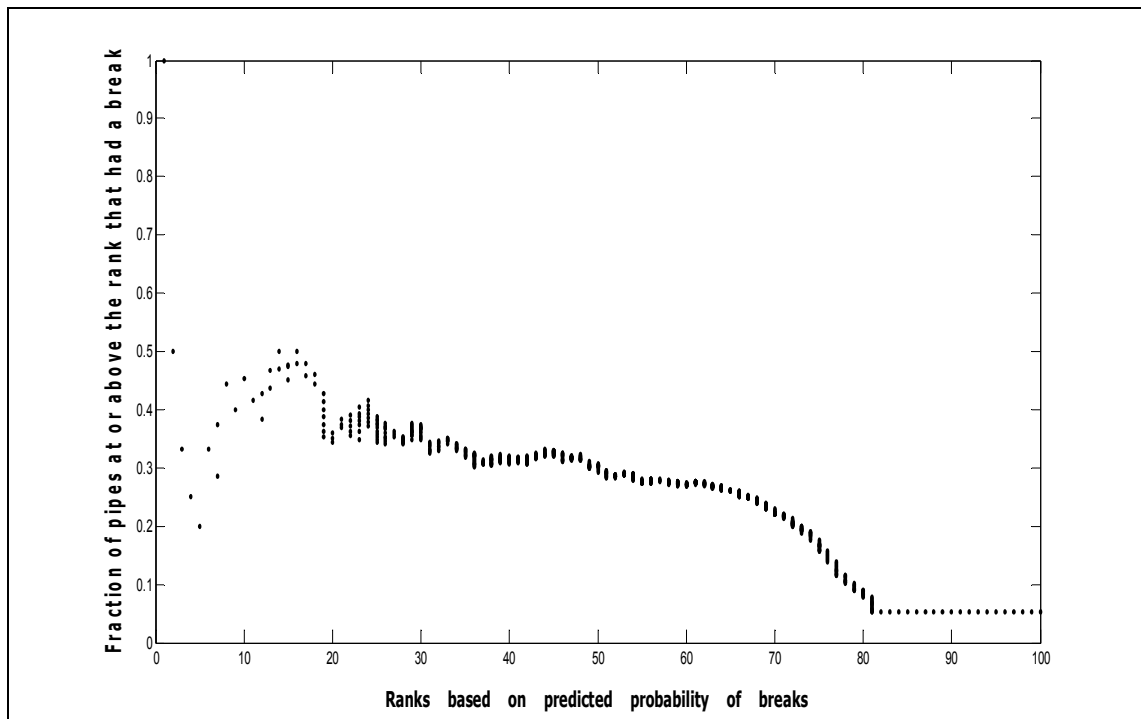
Figure 20. Plot of ranking of pipes against fraction of pipes at or above the rank that had a break

6.2. Applications to other systems

The results from these models could be used for modeling reliability of other water distribution systems too. However, care will have to be taken in applying these models to other water distribution systems, especially those in other regions where the local ground conditions and meteorological conditions could differ substantially from

that in the area where this water utility is located. Similar models could be fit using data from a different region if such data becomes available. Extension of the proposed models to analyze failure records on sewers, oil and gas pipelines, depending on the availability of data, could generate useful insights about the behavior of such systems.

6.3. Limitations in analysis

This research has been successful in modeling water distribution system reliability. However, there are a few limitations that need to be addressed to make the modeling more robust.

The biggest limitation is the size of the data. The data used is heavily left censored. This limits the use of models such as Proportional Hazards model and Accelerated Lifetime model which are particularly designed for modeling failure of individual or group elements in a system. Even for the models used in this research data worth 10 to 15 years at least would have comparatively provided a lot of insight into the system.

Additional covariates could have made the models more accurate. In the models, external corrosion was considered. Internal corrosion due to presence of different compounds in water also plays a significant role in deteriorating pipelines in water distribution systems. However, the difficulty of obtaining this data and lack of time forced the use of external corrosion only. The pH of soil in which the pipes are buried, the redox potential and saturated soil resistivity are important parameters that could give an idea about the chemical properties of soil. Traffic loading, data on construction

activities in the area and number of repairs carried out up to the time under consideration are other factors that could have provided more insight into the system.

Finally, the use of other models such as negative binomial GLM, negative binomial GAM and Multivariate Additive Regression Splines (MARS) probably could have more accurately modeled the system. However, lack of time prevented the application of these models.

6.4. Suggestions for future research

It is evident from the dataset there are about 90% zero counts of breaks. As mentioned in Section 5, zero inflated models are specifically designed to model zero values in the dependent variable. A future endeavor in this research could be to try applying the Zero inflated Poisson (ZIP) model to the dataset of 20,796 observations.

The results from this research could be further used in calculating maintenance costs (including repair and replacement costs). From these parameters optimal replacement time of pipes could be calculated. Also decisions on whether to repair or replace an affected pipeline can be taken by using the results obtained. For example, Hong et al. (2006) developed and demonstrated an approach for the prioritization of replacement or rehabilitation activities associated with buried pipe networks. Their approach was based on the minimization of the expected annual average cost associated with the planning period of pipelines. Kleiner et al. (1998) used the time exponential model of Shamir and Howard (1979) to develop a cost model to calculate the present value of breakage repairs for the years elapsed from the present to the year of

rehabilitation using the cost of single breakage repair. The models used in this research could be used to develop such cost models.

Kleiner et al. (1998) used the equation developed by Sharp and Walski (1988) to model the effect that aging has on the carrying capacity of pipes in the distribution network. They determined this capacity separately for pipelines before rehabilitation and after rehabilitation. Thus the predicted probabilities of failure could be combined with a numerical hydraulic model of the water distribution system to examine the consequences of a break in terms of flow and pressure reductions in areas at various distances from the break. Sometimes water utilities have to make decisions on whether to repair or replace an affected pipeline. The results from statistical models such as those used in this research could be extremely useful in developing models to facilitate such decisions.

7. CONCLUSION

In this research, the time linear, time exponential and Poisson GLM models were reviewed based on pipe break data from 2000-2005 from a water utility company serving a large city in Texas. The tests of these models suggest that the time exponential model and the Poisson GLM are reasonably accurate predictive models for pipe breakage risk, especially zero counts of breaks. The time linear model gives a very low R-squared value and it predicts negative values for the zero counts of breaks. Hence it is not a good model for this dataset. A comparison of the three models based on AIC, deviance and log-likelihood shows that the time exponential model turns out to be the best model.

A model may be very good statistically, but applying it for predicting future events is important from public safety and policy making point of view. The holdout sample analysis and the random holdout sample analysis were used to test the predictive accuracy of these models. The parameter of MSE was used to compare the predictive ability of these models. Based on this, the time exponential model behaves better than the time linear model and the Poisson GLM. Based on the results obtained from the time linear model and the Poisson generalized linear model, the diameter of pipes, the material asbestos cement, land cover variables of forest landuse, agricultural landuse and transitional land use, and meteorological variables like temperature, rainfall and soil moisture appear to be contributing the most to causing the breaks in the system. From the results obtained after fitting the time exponential model to the data, the number of breaks appears to be increasing with increase in time since last break.

The logistic GLM was applied to the larger dataset consisting of 83,300 observations. The ratio of deviance to degrees of freedom was small and the AIC value was also considerably small. This shows that the model fit the data reasonably well. The logistic GLM was also applied to the smaller dataset of 20,796 observations and compared with the other three models. The results show that the AIC, deviance and log-likelihood of this model were better compared to the time linear model and the Poisson GLM. However, they were not so good compared to those of the time exponential model. A comparison between the Poisson GLM and the logistic GLM based on MSE shows that the two models are equivalent in predicting the zero counts of breaks but the logistic GLM does well in predicting the non-zero counts of breaks.

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APPENDIX A

LOADINGS FOR PRINCIPALCOMPONENTS

PC1	PC2	PC3	PC4	PC5	PC6
0.0079	0.9999	0.0078	0.0008	0	0
0.0005	0.0078	-0.9999	0.0108	0	0
0	0.0008	-0.0108	-0.9999	0	0
0	0	0	0	0	1
0	0	0	0	1	0
-1	0.0079	-0.0004	0	0	0

APPENDIX B

WORK DONE IN ArcGIS

The data for many of the covariates was provided in the form of layers. These layers were part of shape files which spatially describe features such as points, lines and polygons. Each of these features has attributes associated with them. A shape file can have one or more layers forming a Geographic Information System (GIS). A GIS is a system for capturing, storing, analyzing and managing data and related attributes that are spatially referenced to the geographic location under consideration.

Using ArcMap (a part of ArcGIS), a platform for visualizing spatial data and performing spatial analysis, the pipe network for this water utility was related to each and every covariate used in the statistical analysis. The number of breaks on each pipe segment being the dependent variable in this analysis, the first step was to relate the break data to each pipe segment. A major hurdle in this process was the fact that some of the breaks were slightly skewed from the pipes i.e. not lying exactly on the pipes, probably because of measurement errors. This was taken care of by making buffers, 160 feet wide, around each pipe while spatially joining the breaks to the pipes using the spatial join command in ArcMap. The covariates of pipe diameter, pipe length, pipe materials, the year of installation of each pipe, and the time since last break on each pipe were then extracted from the attributes of the pipe network layer.

The covariates of pressure, land use, soil type, and soil corrosivity were obtained by doing GIS analysis as given below.

Pressure

The water distribution system under study is divided into 12 pressure zones and the data was in the form of layers for each of these pressure zones. The pipes intersected by each pressure zone were selected using the "Select by Location" tab in ArcMap and new layers were made out of them. These new layers were then related spatially to the pressure zones using the "Joins and Relates" tab and this way the pressure in each pipe was obtained.

Land use

New layers were made using ArcMap in each of the eleven land covers obtained from WebGIS. The pipe network was then clipped based on the above layers using the "Clip" tool from the ArcToolbox. Then by using XtoolsPro (an extension for ArcGIS), the lengths of each of the pipes in these clips were recalculated using the "Calculate Area, Perimeter, Length, Area and Hectares" tab in "table Operations". These lengths were then converted to percentages of the overall pipe segment length.

Soil type

The soils were first grouped into five categories based on their clay content: 0-15 percent clay, 15-35 percent clay, 35-55 percent clay, 55-65 percent clay and 65-80 percent clay. Using ArcMap, layers were created for each category. Clips of the pipe network were made using each of the category layers. The GIS toolbox XtoolsPro was used to recalculate the length of each pipe within each soil group after clipping. These lengths were then converted to percentages of the overall pipe segment length.

Soil Corrosivity

The soil corrosivity data obtained from SSURGO was overlaid on the pipe network and clipping was done similarly to the one done in extracting soil type data. The length of each pipe in each of the six soil corrosivities were then recalculated using XtoolsPro. From this the percentage length of each pipe in each of the soil corrosivities were calculated and these were then used in the statistical analysis.

VITA

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