

## Optimization of the Heating System Operation

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**Abstract:** A new regulation method of the heating system is presented, which is based on the variation of outdoor temperature, to improve the economical efficiency and the timing regulation of the heating system. A function is put forward between the energy loss of the heating system, the temperature difference of supply-return water and the outdoor temperature by making use of the second law of thermodynamics and analyzing the energy loss in the operating process. By means of mathematical deduction, a function is also given between the temperature difference of the supply-return water and the outdoor temperature. With the function, the economical temperature difference of the supply- return water and the correlated parameters can be determined on the basis of the variation of outdoor temperature, and in this way, the heating system can be optimized.

**Key words:** variation of outdoor temperature , temperature difference of supply-return water, energy loss, optimized parameters

### 1. INTRODUCTION

The operational regulation of the heating system mainly includes the following methods: quality regulation, quantity regulation, intermittent regulation and quality regulation combined with altering flowrate by phases. With these methods, the economy of the heating system operation can be improved to different degrees, but due to the fact that the operational regulation of the heating system is not in step with outdoor temperature, a large quantity of energy is wasted all the same. So based on the variation of outdoor temperature, a new regulation method of the heating system is presented in the paper. The function between the optimized operating

parameters of the system and the outdoor temperature is deduced by making use of the second law of thermodynamics and the correlative theory of *heat transfer* and *hydrodynamics*. With the function, the optimization of the operating parameters of the heating system can be realized according to the variation of outdoor temperature so as to achieve the economical operation.

### 2. OPTIMIZED FUNCTION AMONG THE OPERATING PARAMETERS OF THE HEATING SYSTEM

The operational regulation of the heating system based on the variation of the outdoor temperature is an operational regulation method in which the outdoor temperature is regarded as the input variable and the parameters such as the temperature difference of the supply- return water and the flowrate as the target variables. In order to deduce the function between the input variable and the target variable, the exergy loss of the system can serve as the intermediate target variable, and the function between the exergy loss of the system, the temperature difference of supply-return water and the outdoor temperature is firstly gained. Then, by mathematical deduction, the function between the input variable and the target variable is produced.

#### 2.1 The Function between the Average Temperature of Supply-return Water and the Outdoor Temperature

To make the analysis of the question easy, the heat system is simplified as follows:

Suppose the outdoor temperature is indicated as  $t_w$  , the reduced area of the exterior-protected

construction is  $F_1$  (the heat consumption of the cold air by intruding and infiltrating are both regarded as the heat consumption of the exterior-protected construction), the heat transfer coefficient of the exterior-protected construction is  $K_1$  and the indoor temperature is  $t_n$ , the total heat consumption of the system can be expressed as the function of the outdoor temperature.

$$Q = K_1 \cdot F_1 \cdot \Delta t_1 = K_1 \cdot F_1 \cdot (t_n - t_w) \quad (1)$$

Suppose the heat transfer coefficient of the radiator is  $K_2$  and the average temperature of the supply- return water in the radiator is  $t_p$ ,  $K_2$  can be denoted by the function of the heat transfer temperature difference.

$$K_2 = \alpha \cdot \Delta t_2^\beta = \alpha \cdot (t_p - t_n)^\beta \quad (2)$$

In addition, the heat waste of the pipe system is ignored and the total heat is assumed to give out to the heating room through the radiator entirely.

Suppose the total heat transfer area of the radiator is  $F_2$ , then the total heat transfer to the heating room can also be expressed as:

$$Q = K_2 \cdot F_2 \cdot \Delta t_2 = \alpha \cdot (t_p - t_n)^\beta \cdot F_2 \cdot (t_p - t_n) \quad (3)$$

To the system in use,  $F_1$ 、 $F_2$ 、 $K_1$ 、 $t_n$ 、 $\alpha$ 、 $\beta$  can all be regarded as constant. So according to equation (1) and equation (3),  $t_p$  can be expressed as follows:

$$t_p = \left( \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{\alpha \cdot F_2} \right)^{\frac{1}{1+\beta}} + t_n \quad (4)$$

## 2.2 The Relation between the Exergy Loss and the Temperature Difference of the Supply-return Water

Based on the simplification and suppositions of heating system, the following two parts can show the

exergy loss of the system: one is the exergy loss caused by the heat release of the radiator; the other is the exergy loss caused by the fluid resistance of the system. The two exergy losses both have direct relation to the temperature difference of the supply-return water. The bigger the temperature difference, the smaller the water flowrate and the fluid resistance, thus the smaller of the exergy loss caused by the resistance energy loss, but the bigger the exergy loss caused by the heat release of the radiator. On the contrary, if the temperature difference is smaller, the exergy loss caused by the fluid resistance will increase and the exergy loss caused by the heat release of the radiator will decrease. Therefore, in theory, there must be an optimal temperature difference to make the sum of two exergy losses least.

### 2.2.1 The Relation between the Exergy Loss Caused by the Heat Release of the Radiator and Temperature Difference of the Supply-return Water

Suppose the supply-return water temperature is  $\Delta t$ , the flowrate can be expressed as follows:

$$\dot{m} = \frac{Q}{c \cdot \Delta t} = \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{c \cdot \Delta t} \quad (5)$$

The supply-water temperature and the return-water temperature of the heating system can be respectively denoted as follows:

$$t_g = t_p + \Delta t / 2 \quad (6)$$

$$t_h = t_p - \Delta t / 2 \quad (7)$$

The exergy loss caused by the heat transfer  $\Delta E_t$  is the product of the surrounding temperature  $T_w$  and the system entropy generation  $\Delta S_t$ .

$$\Delta E_t = T_w \cdot \Delta S_t = (273 + t_w) \cdot \Delta S_t \quad (8)$$

Moreover,  $\Delta S_t$  is the sum of the indoor air entropy increment  $\Delta S_1$  and the heat medium entropy increment  $\Delta S_2$ .

$$\Delta S_t = \Delta S_1 + \Delta S_2 \quad (9)$$

$$\Delta S_1 = \frac{Q}{T_n} = K_1 \cdot F_1 \cdot (t_n - t_w) / (273 + t_n) \quad (10)$$

$$\begin{aligned} \Delta S_2 &= \int_{T_g}^{T_h} \frac{m \cdot c \cdot dT}{T} = \frac{Q}{\Delta t} \ln\left(\frac{T_h}{T_g}\right) \\ &= \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{\Delta t} \ln\left(\frac{273 + t_p - \Delta t/2}{273 + t_p + \Delta t/2}\right) \end{aligned} \quad (11)$$

In this way, the function between the exergy loss caused by the heat release of the radiator and the temperature difference of the supply-return water is presented as follows:

$$\begin{aligned} \Delta E_t &= (273 + t_w) \cdot K_1 \cdot F_1 \cdot (t_n - t_w) \cdot \\ &\left[ \frac{1}{(273 + t_n)} + \frac{1}{\Delta t} \ln\left(\frac{273 + t_p - \Delta t/2}{273 + t_p + \Delta t/2}\right) \right] \end{aligned} \quad (12)$$

### 2.2.2 The function between the Exergy Loss Caused by the Fluid Resistance and the Supply-return Water Temperature Difference

When the system is operating in gear, the flow pattern of the fluid in the pipe is in the resistance square section and the resistance  $\Delta p$  is in the direct proportion to the square of the flowrate of the heating system. In order to simplify the calculation, the resistance of the heat medium in the radiator is ignored because its value is very small compared to the total resistance of the system. Suppose  $S_g$  as the total impedance of the pipeline of supplying heat medium and  $\rho_g$  as the fluid density in the pipe, the resistance of the pipeline can be expressed as follows:

$$\Delta p_g = S_g \cdot \bar{V}_g^2 = \frac{S_g}{\rho_g^2} \cdot m^2 \quad (13)$$

And the entropy increment caused by the fluid resistance in the supply-pipe is gained as follows:

$$\Delta S_{pg} = \frac{g \cdot m \cdot \Delta p_g}{10000 \cdot T_g} = \frac{g \cdot S_g \cdot m}{10000 \cdot (273 + t_g) \cdot \rho_g^2} \quad (14)$$

Similarly, the entropy increment caused by the fluid resistance in the return-pipe is gained as follows:

$$\Delta S_{ph} = \frac{g \cdot m \cdot \Delta p_h}{10000 \cdot T_h} = \frac{g \cdot S_h \cdot m}{10000 \cdot (273 + t_h) \cdot \rho_h^2} \quad (15)$$

Therefore, the total entropy increment caused by the fluid resistance of the heat medium can be expressed as:

$$\begin{aligned} \Delta S_p &= \Delta S_{pg} + \Delta S_{ph} \\ &= \frac{g \cdot S_g \cdot m}{10000 \cdot (273 + t_g) \cdot \rho_g^2} + \frac{g \cdot S_h \cdot m}{10000 \cdot (273 + t_h) \cdot \rho_h^2} \end{aligned} \quad (16)$$

Thus, the exergy loss caused by the fluid resistance is:

$$\begin{aligned} \Delta E_p &= T_w \cdot \Delta S_p = (273 + t_w) \cdot \Delta S_p \\ &= \left[ \frac{g \cdot S_g \cdot m}{10000 \cdot (273 + t_g) \cdot \rho_g^2} \right. \\ &\left. + \frac{g \cdot S_h \cdot m}{10000 \cdot (273 + t_h) \cdot \rho_h^2} \right] \cdot (273 + t_w) \end{aligned} \quad (17)$$

Then, the function between the exergy loss caused by the fluid resistance and the supply-return water temperature difference can be expressed as:

$$\begin{aligned} \Delta E_p &= \left[ \frac{g \cdot S_g \cdot [K_1 \cdot F_1 \cdot (t_n - t_w)]^3}{10000 \cdot (273 + t_p + \Delta t/2) \cdot \rho_g^2 \cdot (c \cdot \Delta t)^3} \right. \\ &\left. + \frac{g \cdot S_h \cdot [K_1 \cdot F_1 \cdot (t_n - t_w)]^3}{10000 \cdot (273 + t_p - \Delta t/2) \cdot \rho_h^2 \cdot (c \cdot \Delta t)^3} \right] \cdot (273 + t_w) \end{aligned} \quad (18)$$

### 2.2.3 The Function between the Total Exergy Loss of the System and the Temperature Difference of the Supply-return Water

After the analysis above, the function can be obtained between the total exergy loss of the system and the temperature difference of the supply-return water:

$$\begin{aligned} \Delta E = \Delta E_t + \Delta E_p = & (273+t_w) \cdot K_1 \cdot F_1 \cdot (t_n - t_w) \\ & \cdot \left[ \frac{1}{(273+t_n) + \frac{1}{\Delta t} \ln \left( \frac{273 + \left( \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{\alpha \cdot F_2} \right)^{\frac{1}{1+\beta}} + t_n - \Delta t/2}{273 + \left( \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{\alpha \cdot F_2} \right)^{\frac{1}{1+\beta}} + t_n + \Delta t/2} \right)} \right] \\ & + \left[ \frac{g \cdot S_g \cdot [K_1 \cdot F_1 \cdot (t_n - t_w)]^3}{10000 \cdot \left( 273 + \left( \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{\alpha \cdot F_2} \right)^{\frac{1}{1+\beta}} + t_n + \Delta t/2 \right) \cdot \rho_g^2 \cdot (c \cdot \Delta t)^3} \right. \\ & \left. + \frac{g \cdot S_h \cdot [K_1 \cdot F_1 \cdot (t_n - t_w)]^3}{10000 \cdot \left( 273 + \left( \frac{K_1 \cdot F_1 \cdot (t_n - t_w)}{\alpha \cdot F_2} \right)^{\frac{1}{1+\beta}} + t_n - \Delta t/2 \right) \cdot \rho_h^2 \cdot (c \cdot \Delta t)^3} \right] \cdot (273+t_w) \end{aligned} \quad (19)$$

### 2.2.4 The Functional Relation between the Optimized Value of the Supply-return Water Temperature Difference and the Outdoor Temperature

In condition that  $F_1, F_2, t_n, K_1, S_g, S_h, \alpha$  and  $\beta$  are all given, the function between the total exergy loss of the heat system  $\Delta E$ , the temperature difference of the supply-return water  $\Delta t$  and the outdoor temperature  $t_w$  can be presented as follows:

$$\Delta E = f(\Delta t, t_w) \quad (20)$$

Based on the extremum theory of the advanced algebra and after the mathematics treatment to equation (20), the functional relation can be obtained between the temperature difference of supply-return water  $\Delta t$  and the outdoor temperature  $t_w$  under the minimum value of the total exergy loss of the system. The solving procedure is as follows:

Partial derivative is solved of the equation (20)

and at the same time  $\frac{\partial(\Delta E)}{\partial(\Delta t)} = 0$  is requested.

$$\frac{\partial(\Delta E)}{\partial(\Delta t)} = 0 \quad (21)$$

Where,

$$\frac{\partial(\Delta E)}{\partial(\Delta t)} = \frac{\partial(\Delta E_t)}{\partial(\Delta t)} + \frac{\partial(\Delta E_p)}{\partial(\Delta t)} \quad (22)$$

$$\frac{\partial(\Delta E_t)}{\partial(\Delta t)} = (273+t_w) K_1 F_1 \Delta t^{-2} \left[ - \frac{273+t_p}{(273+t_p+\Delta t/2)(273+t_p-\Delta t/2)} - \ln \frac{273+t_p-\Delta t/2}{273+t_p+\Delta t/2} \right] \quad (23)$$

$$\frac{\partial(\Delta E_p)}{\partial(\Delta t)} = (273+t_w) \left\{ \frac{g S_g [K_1 F_1 (t_n - t_w)]^3 - [3(273+t_p) + 2\Delta t]}{10^4 \rho_g^2 c^3 (273+t_p + \Delta t/2)^2 \Delta t^4} + \frac{g S_h [K_1 F_1 (t_n - t_w)]^3 - [3(273+t_p) - 2\Delta t]}{10^4 \rho_h^2 c^3 (273+t_p - \Delta t/2)^2 \Delta t^4} \right\} \quad (24)$$

Added the equation (23) and (24), the value equal to zero, so the function is like this:

$$\begin{aligned} F(\Delta t, t_w) = & (273+t_w) K_1 F_1 \Delta t^{-2} \left[ \frac{273+t_p}{(273+t_p+\Delta t/2)(273+t_p-\Delta t/2)} - \ln \frac{273+t_p-\Delta t/2}{273+t_p+\Delta t/2} \right] \\ & + (273+t_w) \left\{ \frac{g S_g [K_1 F_1 (t_n - t_w)]^3 - [3(273+t_p) + 2\Delta t]}{10^4 \rho_g^2 c^3 (273+t_p + \Delta t/2)^2 \Delta t^4} + \frac{g S_h [K_1 F_1 (t_n - t_w)]^3 - [3(273+t_p) - 2\Delta t]}{10^4 \rho_h^2 c^3 (273+t_p - \Delta t/2)^2 \Delta t^4} \right\} = 0 \end{aligned} \quad (25)$$

The equation (25) can explain the functional relation between the optimized value of the supply-return water temperature difference  $\Delta t$  and the outdoor temperature  $t_w$  when the total exergy loss of the system is a minimum value. The curve corresponding to the function can be got with Matlab, by which the optimized temperature difference  $\Delta t$  is presented under a random  $t_w$ . In this way, a series of the parameter values of the heating system correlative to  $\Delta t$  can be obtained, such as circulation flowrate and the temperature of the supply-return water and so on. According to these parameters, the work condition can be regulated and the heating system can be operated economically.

### 3. CONCLUSION

A new regulation method of the heating system is presented, which is based on the variation of outdoor temperature, to improve the economical efficiency and the timing regulating of the heating system. A function is put forward between the exergy loss of the heating system, the temperature difference of supply-return water and outdoor temperature by making use of the second law of thermodynamics and

analyzing the exergy loss in the operating process. By means of mathematical deduction, a function is also given between the temperature difference of the supply-return water and the outdoor temperature. With the function, the economical temperature difference of the supply-return water and the correlated parameters can be determined on the basis of the variation of outdoor temperature, and in this way, the heating system can be optimized.

#### Symbol:

$T_p (t_p)$  :the average temperature of supply-return water, K ( °C);

$T_w (t_w)$  : the outdoor temperature, K ( °C);

$T_n (t_n)$  : the indoor temperature, K ( °C);

$T_g (t_g)$  : temperature of the supply-water, K ( °C);

$T_h (t_h)$  : temperature of the return-water, K ( °C);

$\Delta t$  : temperature difference of the supply-return water, °C;

$\Delta t_1$  : temperature difference of indoor and outdoor, °C;

$\Delta t_2$  : temperature difference of the heat transfer of the radiator, °C;

$\alpha$  、  $\beta$  : The constant fixed on the radiator.

$\bar{V}$  :the volume flowrate of the heat medium,  $m^3/s$  ;

$\bar{m}$  :the mass flowrate of the heat medium,  $kg/s$  ;

$\rho$  : water density under the average temperature of supply-return water,  $kg/m^3$ ;

$\rho_h$  :The water density under the return-water temperature,  $kg/m^3$ ;

$S_h$  : The total impedance of the pipe line of returning heat medium;

$\Delta p$  : The fluid resistance of the heat system, Pa ;

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