

RESERVOIR STUDIES OF NEW MULTILATERAL WELL ARCHITECTURE

A Thesis

by

MANOJ SARFARE

Submitted to the Office of Graduate Studies of
Texas A&M University
in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

May 2004

Major Subject: Petroleum Engineering

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Approved as to style and content by:

Peter P. Valkó
(Chair of Committee)

J. Bryan Maggard
(Member)

Terry L. Kohutek
(Member)

Stephen A. Holditch
(Head of Department)

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Major Subject: Petroleum Engineering

ABSTRACT

Reservoir Studies of New Multilateral Well Architecture. (May 2004)

Manoj Sarfare, B.E., Maharashtra Institute of Technology, India

Chair of Advisory Committee: Dr. Peter P. Valkó

Hydrocarbon recovery from conventional reservoirs is decreasing and the need to produce oil cheaply from mature, marginal and unconventional reservoirs poses a big challenge to the industry today. Multilateral well technology can provide innovative solutions to these problems and prove to be the most likely tool to propel the industry in the next century. In this research we propose a new multilateral well architecture for more efficient and effective field drainage. We study the architecture from a reservoir engineering point of view and analyze the effect of various design parameters such as branch density and penetration extent of laterals on the performance of the proposed architecture for homogeneous reservoirs. We also analyze the performance in case of anisotropic reservoirs.

The numerical simulation results show that the multilateral wells usually help improve the overall cumulative production from a reservoir as compared to conventional wells. Also, they provide the added benefit of faster field drainage and present a more attractive return on investment. In this thesis we also present the results for a representative field case analysis. The rapidly changing Solution GOR contributed to making the oil viscous, which reduced the problem to optimize the mother bore location. In addition to these numerical studies we perform analytic studies to develop quick estimates of the theoretical limits of Productivity Index of the proposed architecture. We use known results from the literature to test their validity to estimate the upper and lower bounds on productivity. The results show that current tools to determine the lower limit is insufficient to predict performance.

DEDICATION

To my beloved mom, dad, and brother, who have always helped and supported me in all my endeavors.

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CHAPTER I

INTRODUCTION – RESERVOIR APPLICATIONS OF MULTILATERAL WELL TECHNOLOGY

1.1 Introduction

Since their introduction in the early part of the last decade, multilateral well systems and their applications have developed rapidly¹. They have been used in a myriad of operating conditions varying from mature fields to forming an integral part of completely new field development strategies. However under all the different operating arenas the aim is to produce hydrocarbons as quickly and efficiently as possible. In doing so the industry is faced by many challenges², some of which are:

1. complex geologic conditions such as compartmentalized or stacked reservoirs
2. difficult reservoir conditions such as viscous fluids or tight formations
3. hostile environments such as deep water or frontier development sites
4. efficient and effective reservoir management and development plans

Innovative solutions are necessary to tackle the problems and challenges facing the industry successfully. Multilateral well technology provides just such a solution. The technology has been successfully applied in all the above areas and shows a dramatic impact on the financial results of many, thus promising to be not just an evolutionary but also a revolutionary technology in the oil field.

1.2 Statement of Problem

Multilateral well has the potential for improvement in the productivity of a reservoir³⁻⁵. Over the last decade multilateral well technology¹ has been one of the most rapidly evolving and widely utilized production technology both for new as well as maturing reservoirs^{2, 6-7}. Reservoir applications of multilateral wells have been discussed and the need to identify and quantify the reservoir benefits of this technology has

This thesis follows the style of *SPE Reservoir Evaluation and Engineering*.

received attention. With applications anticipated from the deepwater to the arctic, from heavy oil to gas condensate reservoirs and from small isolated lens⁸ to giant field development – multilateral wells represent the leading edge in production technology.

Multilateral wells, used to develop fields in various locations³, are classified into different forms or levels namely on the basis of the junction structure⁸. Hundreds of highly specialized multilateral wells have been successfully drilled and completed. The forum for Technical Advancement of Multilaterals (TAML) was created and a multilateral classification matrix was developed to foster better understanding of multilateral applications, capabilities and equipment. With the increasing maturity of reservoirs and the need to produce oil cheaper and quicker, multilateral well technology provides the industry with another tool to lower the cost of reserve development¹. However this technology is still not widely accepted in the industry essentially due to the perceived high costs and the hesitation due to risks associated with implementing the technique.

In this thesis we propose an entirely new and advanced multilateral well architecture. It comprises a non-perforated horizontal mother bore with several laterals connected to it in the horizontal plane. The uniqueness of this architecture lies in the constructional and operational flexibility it affords for efficient reservoir drainage. We endeavor to further the present database of knowledge and understanding of multilateral wells with regards to reservoir engineering. To achieve this we study the parameters that affect the overall productivity of the new well architecture under various operational scenarios. While the final analysis with regards to feasibility of a technology depends greatly upon economic evaluation, it is beyond the scope of this study.

1.3 Multilateral Wells – An Overview

1.3.1 A Background of Multilateral Wells

It is acknowledged that the father of multilateral (ML) wells is Alexander Grigoryan⁹. In 1949, he developed an interest in the theoretical work of American scientist L. Yuren, who maintained that increased production could be achieved by increasing the diameter of the borehole in the productive zone of the formation.

Grigoryan took this theory a step further and proposed branching the borehole in the productive zone to increase surface exposure.

He put this theory into practice in the former U.S.S.R. field called Bashkiria (now known as Bashkortostan). His target in this field was an interval in the range of 10 to 60 m (33 to 197 ft) in thickness. He drilled to a depth of 575 m above the pay zone and then drilled nine branches from the open borehole. Compared with the other wells in the field this well was 1.5 times more expensive, but penetrated 5.5 times the pay thickness and produced 17 times more oil each day. This unprecedented success inspired the Soviets to drill an additional 110 ML wells.

1.3.2 Present State of Multilateral Wells

In spite of the success of the early ML wells, they have not yet evolved to the point of being the industry norm today. Like horizontal wells, ML well application is justified through their economic viability. Defined as a single well with one or more branches emanating from the main borehole, their aim is to improve production while saving time and money. The complexity of ML wells ranges from simple to extremely complex structures. According to the TAML classification ML wells are classified into 6 levels, shown in Figure 1.1, though they can be simply classified into two groups as:

- Wells that require pressure integrity at the junction
- Wells that do not require pressure integrity at the junction.

The characteristics of the various levels are¹⁰:

Level 1 - There is an openhole junction between the mainbore and the lateral.

Level 2 - The junction is constructed to be openhole extending from a cased and cemented mainbore.

Level 3 - This is a slight modification of the Level 2 junction in that the lateral borehole is drilled from a cased and cemented mainbore. However in addition a slotted liner or screen is placed in the lateral and tied back to the mainbore through a hanger device.

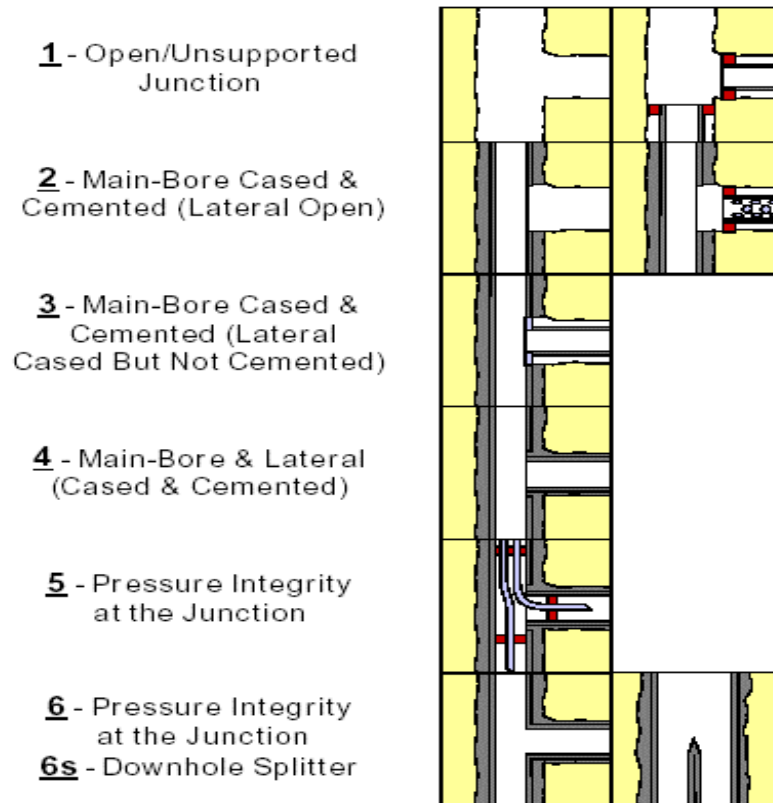


Figure 1.1 – TAML classification of ML wells¹⁰

Level 4 - The lateral borehole extends from a cased and cemented mainbore. The junction is constructed such that a lateral liner is cemented back to the mainbore.

Level 5 - This junction is described as a pressure seal across the junction established by the completion equipment. Packers and other seals may be used along with dual tubing strings to obtain a three-way pressure seal.

Level 6 - This junction provides for a pressure seal established by the casing itself. It is typically employed at the bottom of a casing string. After the casing and junction are cemented into place the laterals are drilled and tied back to the junction with some cemented lateral liner and hanger assembly.

ML wells with TAML junction levels 1 through 4 have been applied extensively in the new and maturing reservoirs of all sectors of the North Sea³. A Level 4 ML well has been successfully used in the Tern field in the North Sea. The Troll Olje field also in the North Sea is another example where ML technology was found more appropriate than conventional technologies¹¹. Multilaterals have provided a means to optimize slot usage, commercially develop lower-quality reserves in the Brent sequence and when applied with complementary technologies of underbalanced drilling and intelligent well completions help optimize field development

The economic benefits of ML wells compared to horizontal wells in water-drive reservoirs in varying permeability fields has been investigated and found to have a better net present value¹². A level 6 junction was used to simulate the performance of ML wells. Also when OOIP is lower the performance of a multilateral well is better than a horizontal well. The use of ML technology improved the recovery factor by water flooding in a mature oil field in Venezuela. The recovery factor, economic viability and lowest operational activity were achieved for a ML development scheme compared to the vertical well concept¹³. Level 4 ML technology in conjunction with intelligent systems helped improve the recovery at Wytch Farm, UK¹⁴. This scheme not only helped to recover the marginal reserves but also added new production at reduced risk. The Mukhaizna field, south Oman contains 14-16° API oil in unconsolidated sand¹⁵. The possibility of early water breakthrough posed further technical difficulties in producing the heavy crude. However the use of dual lateral wells helped make the project a very attractive investment opportunity.

Also studies have been performed to predict the performance of multilateral wells. Larsen¹⁶ computes the productivity indices or skin values for arbitrary well configurations in homogeneous reservoirs of constant thickness. Symmetry of the reservoirs is an important requirement in this computational technique. Other models to predict ML well performance assume the well to be divided into various segments and

computations are performed on each of these segments. Salas¹⁷ models the Well Index factor for ML wells by accounting for competition effects of inflow performance and interference effects of commingled production of branched wells. A transient model¹⁸ for ML wells is developed that can be applied in commingled reservoirs. The model accounts for crossflow between layers.

The ML wells applications mentioned above essentially address the various challenges facing the industry mentioned earlier. The history of the last decade of ML wells has helped establish the business driver for ML technology¹⁹. However inspite the successful application of ML technology in the oilfield the industry is hesitant to accept this technology in a big way. This inertia arises from the fact that the behavior of ML wells is not completely understood and the difficulty to evaluate the potential benefits of ML technology. The lack of willingness to adapt to it can be ascribed to the following reasons:

1. Reliability

Despite the high technical and economic success of ML wells they are still viewed to be associated with a great amount of risk. This perception exists though the industry wide statistics suggest otherwise.

2. Value

Even the operators most experienced with ML technology are sometimes hard pressed in identifying and quantifying the true value and return on investment of these wells. This is partly due to the inability to perform effective modeling and prediction of well performance and lateral contributions.

1.3.3 The Future

The future of ML wells is in harder-to-drill formations where the reservoirs require selective completions, selective isolations and stimulation operations. They could also be used in exploration wells, to mitigate geologic risks and navigate heterogeneous reservoirs¹. The future of the oil and gas business²⁰ lies in unconventional reservoirs like tight-gas sands, coalbed methane, heavy oil and gas shales. To be able to produce these

resources economically improved technology will be in greater demand. Many current technologies like hydraulic fracturing, steam injection will definitely be applicable along with improved reservoir characterization methods to reduce risk. But in addition to this the ability to produce the resources to the surface will need the development of multibranch well bores. Greater recoveries coupled with economic attractiveness will definitely help improve the confidence of operators in this nascent technology.

CHAPTER II

NEW MULTILATERAL WELL ARCHITECTURE

2.1 Description of the New Multi-lateral Well Architecture

Consider a reservoir or a part of it that has a rectangular cross-section along its depth. The new multilateral well architecture ²¹ consists of a horizontal well penetrating almost the entire length of the reservoir along with branches from the horizontal in the lateral direction. A vertical well is connected to one end, heel, of the horizontal well and it acts as the point of vertical lift. The other end of the horizontal is the toe so that the flow in the horizontal is from toe to heel. Hence there is only one vertical conduit acting as the production string. The main horizontal section (collector well or mother bore) is not perforated but contains several pre-prepared junctions. The diameter and completion type of the vertical and the main horizontal sections are such that they maximize the pipe flow capacity. The horizontal wellbore and the surrounding reservoir are completely isolated. Once cemented the vertical and horizontal sections are not readily accessible with well intervention tools. The junction equipment is placed during the drilling of the main horizontal well and it is cemented together with the main horizontal section. The pressure and structural integrity of these junctions is a critical requirement. However unlike traditional multilateral wells this integrity is not compromised by additional requirements such as potential capability of future well intervention, formation damage control during drilling or ability to accept tools in a later phase.

Once the main horizontal well bore is drilled the other laterals are drilled from one or more locations on the surface. The laterals are drilled in a direction perpendicular to the main horizontal well. The feeder lateral is connected to the main mother bore at the pre-prepared junction points. They are completed in a number of ways while focusing on maximizing the inflow potential without compromising it by additional requirements. For example relatively slim holes are acceptable as they are less capital intensive, not prepared to accept tools at a later stage and might be completed open-hole or frac-packed and hence disposable. Also the time schedule of feeder lateral drilling is very flexible and can change depending upon further information collected from the field and on market requirements.

The proposed architecture can be better understood from the Figure 2.1 given below. As shown in the figure, 25b is the main horizontal well with intersection points represented as 22 is placed in the casing. Well 226 is drilled with multiple feeder laterals

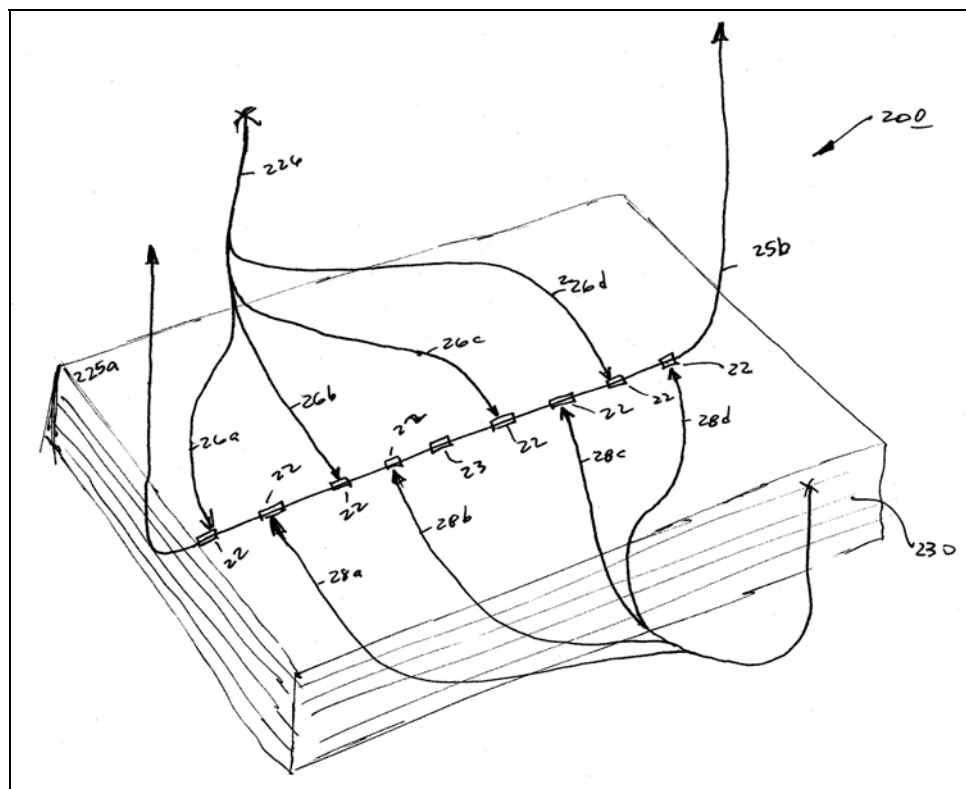


Figure 2.1- New multilateral well architecture

26a, b, c, d all connecting into the parent well. The casing of the feeder well intersects the casing of the parent well and is mechanically connected and sealed at the intersection points. Production flows from the toe of the feeder well into the mother bore to be lifted to the surface. A plug is used to prevent cross flow or pressure transition exposures at the junctions between the feeders (26) and the access well (22). In the well network so formed the feeders do not have to carry all the production of the field and so can be

smaller in diameter. The mother bore is a larger well bore so that it can handle the large flow rates.

The proposed architecture is radically new as the collector well is not used for lateral drilling or any well intervention in the laterals. Thus the continuity of production is not jeopardized on account of any event in the laterals. In fact there is a separation of two functions: one is to collect hydrocarbons from the reservoir as performed by the laterals and the other is to conduct the hydrocarbons to the point of vertical lift and ultimately to the surface.

2.2 Advantages of ML Wells

The various advantages of multilateral wells can be summarized as follows:

1. Reduction in well costs. This is due to the need to use fewer top-side and near surface equipment for a single multilateral well as compared to a group of conventional wells.
2. Mechanically sealed junctions with full casing integrity eliminate one of the main failure point as compared to other multilateral designs
3. Improves sweep efficiency by delaying gas or water breakthrough.
4. Facilitates better drainage of heterogeneous reservoir systems.
5. Enhances production for difficult fluids.
6. Reduction of environmental footprint.
7. Increases the reservoir exposure.
8. Better connects the natural reservoir permeability
9. Greater exposure accelerates the production rate.
10. Accelerated production also allows for early production of secondary or marginal reserves.
11. Reduced overall project costs improving the rate of return.

2.3 Multilateral Well Model

From a reservoir engineering point of view it is difficult to quantify various advantages of the proposed multilateral well architecture. However it is possible to investigate quantitatively ²¹ the productivity of the new well architecture through

numerical simulations. To simulate the proposed architecture the well bore structure is modeled as a main horizontal wellbore fed by many parallel laterals. This structure is shown in Figure 2.2. The reservoir essentially contains a vertical well bore that conducts the fluids to the surface. From this vertical, a main horizontal section called mother bore is drilled to penetrate the entire length of the reservoir in the direction of the largest horizontal dimension. Now feeder laterals are connected to the mother bore at the pre-prepared junction points. One lateral is drilled on either side of the mother bore so that they form a network of alternately placed laterals. The laterals are perpendicular to the mother bore and are in the direction of the smallest horizontal dimension.

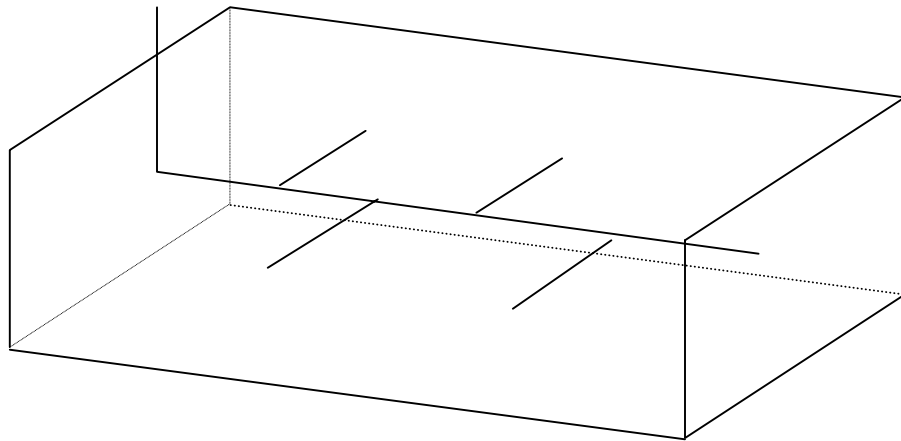


Figure 2.2 – Multilateral well model used for numerical simulations

As shown in the figure depending upon the branch density, we can have all the laterals drilled or any subset of it. In addition we can drill the laterals reaching the outer boundary of the drainage volume (100% penetration) or we can assume a smaller percentage of penetration. In the model the mother bore is not perforated and the feeder laterals are perforated (or completed open hole) providing communication with the reservoir. Formation damage in the vicinity of the laterals is neglected. This is because the feeder laterals are drilled and completed with the requirement of minimum formation damage made possible by lack of necessity to compromise for well integrity, larger hole

diameter, preparing for additional drilling activity, preparing for sophisticated completion equipment. Also frictional pressure losses in the main horizontal section are neglected due to its large diameter.

2.4 Methodology and Procedure

The first task in evaluating the performance of the suggested well architecture would be to identify the types of reservoir applications for which the technology may be used. From this point of view various parameters affecting the performance of multilateral wells must be identified and analyzed. In this work we focus on the reservoir engineering aspects, investigating such issues as the effect of branch density (number of laterals) and the penetration of laterals (with respect to the lateral dimensions of the reservoir). The main issue is the overall productivity of the well architecture as a complex drainage tool.

The primary tool to do such investigations is reservoir simulation. However it is also important to put the results into perspective, partly by comparing them to more conventional drainage systems and partly by establishing theoretical limits. Such a methodology ensures that no false anticipations are generated and a realistic evaluation can be performed.

The obvious reservoir engineering approach to do this job is to establish a “base case” and perform parametric studies. We perform simulations using Eclipse – one of the most widely used reservoir simulators in the industry. The multilateral well model discussed above forms the basis of these parametric studies. The lateral configurations are changed as per the investigative needs.

Firstly the performance is investigated in a homogeneous reservoir model. In this model, we build rectangular reservoir with the architecture proposed above. In all the models we can have up to 60 laterals producing into the mother bore. Branch density and penetration of laterals are the two basic parameters that most affect overall productivity. Assume that a multilateral well must be designed to drain the net pay for a given reservoir. The very first question that arises is: what should be the number of feeder laterals drilled? The next issue is: how far should these laterals penetrate into the bulk of the reservoir. While this decision will depend upon the cost of drilling and completion,

various additional factors such as hydrocarbons in place, reservoir structure, driving mechanism and others will influence the final answer. Hence our strategy is to evaluate the simplest assumptions through this preliminary analysis and consider the additional details with particular reservoirs. Along with the homogeneous case we try to incorporate heterogeneity in the model by using anisotropic reservoirs.

Secondly, representative cases will be set up for field data. Reservoir and fluid data are used to prepare models wherein a part of the actual field is represented as the rectangular reservoir we use in the preliminary analysis. The performance of the multilateral well architecture will be compared with that of conventional vertical wells.

2.5 Technical Indicator

Cumulative production is one of the most important quantities considered while making a decision about the feasibility of any field development theme. In addition to cumulative production (in a certain amount of time) one should consider the actual distribution of production in time. However both cumulative production and its distribution in time both have only a limited information value, if we cannot compare it to some ideal drainage structure or an existing well architecture.

The reservoir engineering concept of Productivity Index ²² (PI) is a quantity which helps to put the various results into perspective. While traditionally this concept is used mostly for a single well, its generalization is a valuable tool to evaluate complex well architectures. Also it can be un-dimensionalized in a format that is representative not only for a given reservoir-fluid system, but for a whole family of them.

Productivity index essentially describes a linear relationship between the production rate and the driving force. For practical and theoretical purposes we select the driving force as the drawdown pressure. The drawdown pressure is defined as the average pressure in the reservoir minus the average pressure along the sink surface (i.e. the wellbore pressure). The Productivity Index, denoted by J is given by,

$$J = \frac{q}{p_{res} - p_{wf}} \dots\dots\dots (2.1)$$

where p_{res} is the average volumetric pressure in the reservoir and p_{wf} is the wellbore flowing pressure.

The value calculated from equation 1 in general is not constant in the transient flow regime as J decreases with time. In the stabilized flow regime the PI is constant. There are three main stabilized flow regimes:

Steady-state

The boundary at the top and bottom are no flow. A constant pressure is assumed at the outer boundary of the reservoir in the lateral directions. In addition, p_{wf} or the production rate is kept constant. The steady-state is characterized by a non-changing pressure distribution in the reservoir.

Pseudo-steady state

Again the boundary condition at the top and bottom are no flow. At the outer boundary of the reservoir in the lateral directions we assume the same conditions: no flow across the boundaries. Such an idealization is often called a volumetric reservoir. In addition we keep constant total production rate. The pseudo-steady state represents the long-time limiting behavior of the reservoir and is characterized by a constant change in pressure with time everywhere in the reservoir. This implies that the shape of pressure distribution in the reservoir is preserved during production though the reservoir is being depleted at a uniform depletion rate. However such a regime cannot be maintained forever, because the reservoir is depleted at a constant rate and hence the wellbore pressure is also decreasing with a constant rate and will ultimately reach a physical limit of zero pressure.

Boundary-dominated state

Once more the top and bottom boundaries are at no flow condition. At the outer boundary of the reservoir in the lateral directions we assume no flow condition with a constant wellbore pressure. The boundary-dominated state is the long-time limiting behavior of the system and is characterized by a completely different pressure distribution than the pseudo-steady state pressure distribution. Under boundary-dominated flow the rate of depletion depends both upon the location as well as the time, but the rate of change of depletion rate is a function of location only. At any particular

instant the depletion rate is such a function of location that the further the location from the nearest wellbore larger is the depletion rate at that location. Such a flow regime exhibits a continuously decreasing production rate and a similarly decreasing drawdown.

Though Productivity Index is a valuable technical indicator only factors like oil in place and profit analysis will essentially determine the optimum Productivity Index to be used. In practice, however it is observed that the increase in Productivity Index requires investment but the relation between PI and cost increase is very stochastic in nature.

CHAPTER III

ESTIMATION OF THEORETICAL UPPER AND LOWER LIMITS

3.1 Motivation

The need to provide a theoretical framework for the simulation results obtained in the later part of the research is a major driving force in performing the analytical work presented in this chapter. A firm theoretical basis is necessary to put numerical results into perspective and be confident of the results obtained in a new study. The architecture studied in this thesis is unique and hitherto uninvestigated in the literature. Also the currently available models to evaluate the productivity of a single ML well comprises variables and effects that are not applicable in the cases we analyze and hence are not suited to predict the performance accurately. Some of these variables are those of friction effect in the flowline and crossflow between layers.

As mentioned earlier the PI is a very effective tool in analyzing well performance and comparing different reservoir flow systems. Hence the objective of the material presented in this chapter is to develop back of the envelope methods to obtain theoretical limits of productivity index attainable by the advanced well architecture design.

3.2 Methodology

We aim to obtain a theoretical upper and lower limit for the productivity of the proposed well architecture for some particular cases and to do so we use results available in the literature to model the fluid flow in a ML well.

The concept of infinite fracture conductivity²³ is used to establish the maximum PI obtainable by the ML well architecture. The flow into the laterals penetrating the smaller horizontal dimension of a reservoir is linear. This is similar to the linear flow into an infinite conductivity fracture, which extends from the well bore to the lateral reservoir boundaries in the vertical plane. An infinite conductivity fracture is characterized by negligible pressure drop in the flow direction and hence represents the greatest throughput of fluids as per the definition of PI. The flow is both linear as well as perpendicular to the fracture and the laterals. In order to model the ML well as an infinite conductivity fracture we assume infinite lateral branch density in the horizontal plane.

Since we neglect the frictional pressure drop in the laterals the fluids will be conveyed to the mother bore instantly without any need to expend fluid energy to overcome resistance to flow and thus maximize the productivity. We then turn the reservoir with infinite laterals in the horizontal plane on one of its sides so that the laterals are in a vertical plane. The maximum or the upper limit of productivity for the infinite laterals is obtained when the pressure drop in the laterals is negligible and hence they can then be modeled as an infinite conductivity fracture. We first present a rigorous derivation of the maximum dimensionless PI (J_d) for an infinite conductivity fracture as presented by Wattenbarger²³ *et al.* This result ($J_{d\max}$) is then used to obtain the maximum PI for a reservoir geometry used extensively in this research.

Again to estimate the theoretical lower limit of PI we use the known analytical result²⁴, which predicts the PI for a reservoir of arbitrary drainage area and shape and given as,

$$J = \frac{kh}{141.2B\mu} \frac{1}{\left(\frac{1}{2} \ln\left(\frac{4A}{\gamma C_A r_w^2}\right) + s\right)} \dots\dots\dots (3.1)$$

where,

k = Permeability, md

h = Reservoir depth, ft

B = Oil formation volume factor

μ = Viscosity, cp

A = Drainage Area, ft²

γ = Euler's Constant

C_A = Dietz shape factor

r_w = Well bore radius, ft

s = skin factor

The above equation is essentially derived for a vertical well operating at pseudo-steady state. As in the case of determining the upper limit, we rotate the reservoir on one of its sides so that all the laterals are in the vertical plane. With such a rearrangement we

can consider each lateral as a unique identity separated from the neighboring laterals in the reservoir by an imaginary no flow boundary. Then each block containing one lateral in the vertical plane surrounded by no flow boundaries on all sides can be assumed to represent a partially penetrating vertical well. Such a rearrangement is shown in Figure 3.1 for a ML well containing 2 laterals in the horizontal plane. Any partially penetrating well imparts a skin also known as the pseudo-skin factor. Cinco-Ley²⁵ *et al.* has published data for the skin effects of partially penetrating wells. The PI for a block containing a partially penetrating vertical well can be determined using the known values of Dietz' shape factor and pseudo-skin as given by Cinco-Ley. We expect, from basic reservoir engineering principles, that the sum of PI's for each of the block should be equal to the theoretical value of the least PI attainable by using the ML well architecture. However modeling the worst case behavior by introducing a no flow boundary between the laterals is not very intuitive and obvious.

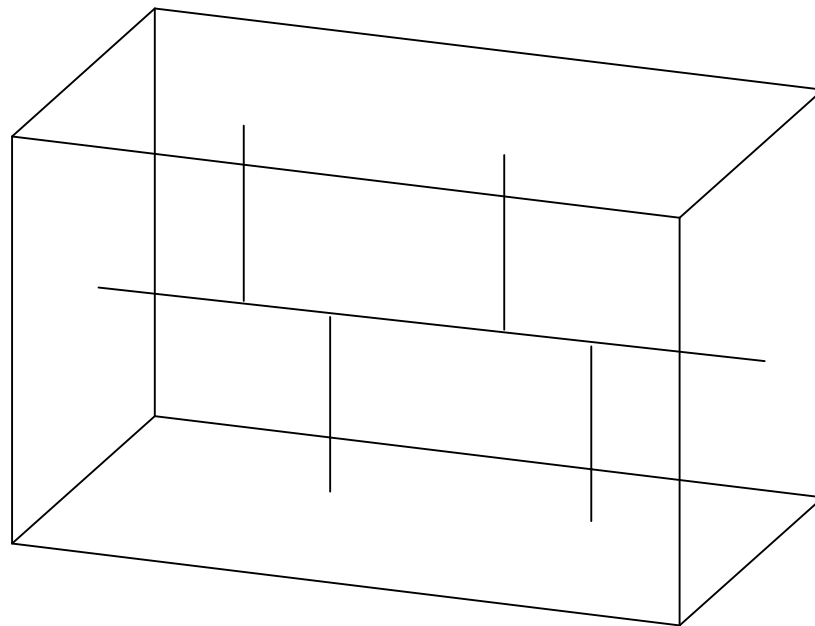


Figure 3.1 – Rearranged form of a horizontal well architecture

3.3 Upper Limit / Maximum Achievable PI

3.3.1 Infinite Conductivity Fracture PI

The PI attainable for an infinite conductivity fracture has been obtained by Watterbarger *et al.* In this section we present a rigorous derivation of the result for pseudo-steady state behavior. As mentioned earlier the flow into an infinite conductivity fracture is linear. Hence to model this physics of the phenomenon we use the linear diffusivity equation and obtain its solution for pseudo-steady state which requires a no flow outer boundary and constant rate inner boundary condition. The linear diffusivity equation has been presented in fluid flow texts. Consider a hydraulically fractured well in a rectangular geometry as shown in Figure 3.2. We use the equation as given below in field units. A rigorous derivation of the result obtained in the literature has been provided in the appendix.

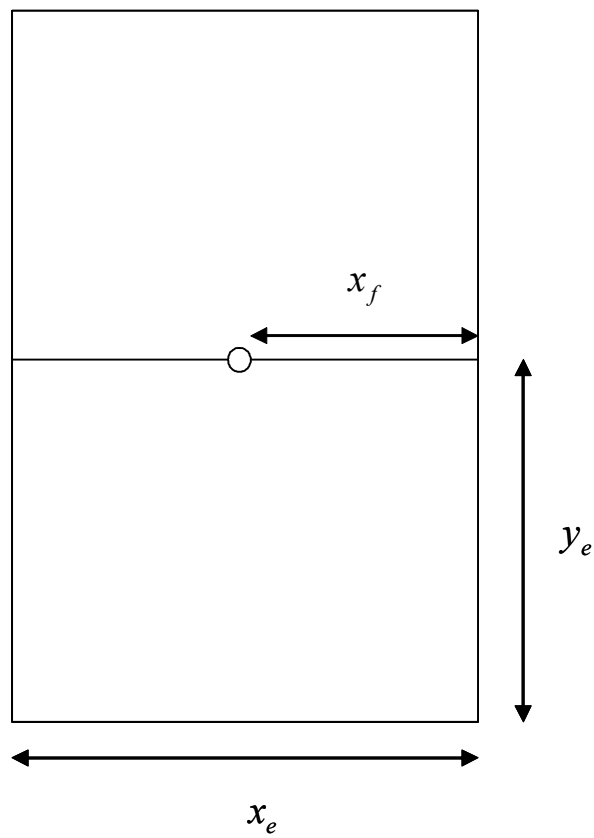


Figure 3.2 – Infinite conductivity fracture in a rectangular geometry

The maximum PI attainable for the case of an infinite fracture is

$$J_{CR} = \frac{kh}{141.2 B\mu \left[\frac{\pi}{6} \left(\frac{y_e}{x_f} \right) \right]} \dots\dots\dots (3.2)$$

3.3.2 Application to ML Well Architecture

As mentioned earlier we rotate the reservoir on one of its sides so that the lateral structure can be modeled as an infinite conductivity fracture. This rearrangement of the horizontal laterals so that they lie in the vertical plane is shown in Figure 3.3. The correspondence between the dimensions of the original structure and the rearranged structure can be seen in figure and is given below,

$$x_h = x_f \dots\dots\dots (3.3)$$

$$y_h = h \dots\dots\dots (3.4)$$

$$h_h = y_e \dots\dots\dots (3.5)$$

In eqn. 3.2 the term x_f , is the fracture half length. The fracture wings extend from the well bore to the lateral boundaries in the x-direction, and so x_f is equal to half the length of the reservoir in the x-direction. Similarly the term y_e is equal to half the length of the reservoir in the y-direction. This is seen in Figure 3.3. Hence, in order to

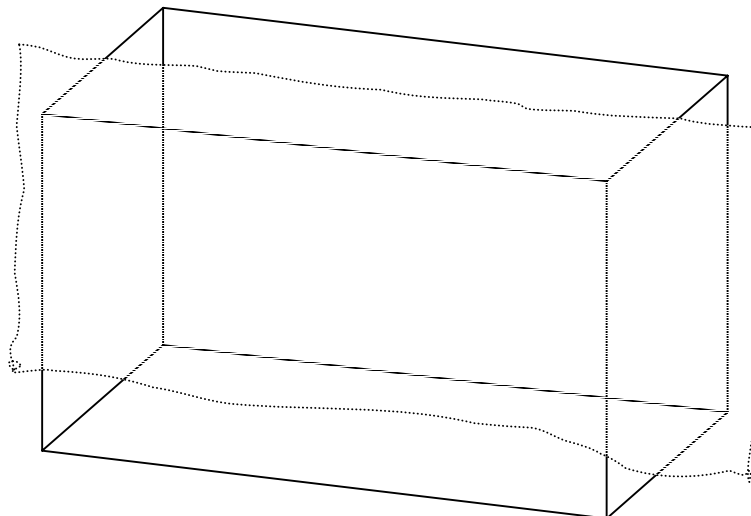


Figure 3.3 – Infinite laterals forming an infinite conductivity fracture in the vertical plane

determine the maximum PI for the ML well architecture the ratio $\left(\frac{y_e}{x_f}\right)$ in the infinite conductivity fracture solution can be replaced by the ratio of the lengths of the original reservoir in the y and x – directions as $\left(\frac{y_h}{x_h}\right)$. Hence the maximum PI for the case shown in Figure 3.3 is given by the following equation,

$$J = \frac{kh}{141.2 B\mu} \left[\left(\frac{x_f}{y_e} \right) \frac{6}{\pi} \right] \dots\dots\dots (3.6)$$

The data used to evaluate the above expression are,

$$k = 0.1 \text{ mD}$$

$$h = 2000 \text{ ft}$$

$$x_e = 4000 \text{ ft}$$

$$y_e = 110 \text{ ft}$$

$$B = 1.012 \text{ rb/stb}$$

$$\mu = 1.0 \text{ cp}$$

$$J = \frac{0.1 \times 2000}{141.2 \times 1.012 \times 1.0} \left[\left(\frac{4000}{110} \right) \frac{6}{\pi} \right] \dots\dots\dots (3.7)$$

$$J \approx 97 \text{ stbd/psia} \dots\dots\dots (3.8)$$

Hence the maximum PI of the ML well architecture is 97 stbd/psia.

3.4 Lower Limit for PI

3.4.1 Outline

We believe that a restriction in the form of a no flow boundary between neighboring laterals will be a good way to estimate the lower limit of productivity that can be delivered by the ML well architecture. Consider the Figure 3.1 shown earlier. In the rearranged vertical form the no flow boundary allows each lateral to be considered as a partially penetrating vertical well. The productivity of each well or block can be predicted by using a known analytical result from the literature as given by equation 3.1. This result accounts for the irregular shape of the reservoir, the well location and the skin

due to a partially penetrating well. Reservoir engineering logic suggests that the sum of the productivity of all the blocks should be equal to the productivity of the ML well architecture. In fact the estimate by the analytical result should slightly under predict the ML well productivity as the laterals will normally drain the reservoir more uniformly than the set of partially penetrating vertical wells. However from the results shown in the next section we see that the present analytical tool is inadequate to predict the performance of ML wells as they more often than not tend to over-predict the PI in most cases analyzed.

Ideally the analytical result should be compared with the numerical solution of productivity for the reservoir geometry used. The reservoir considered is $4000 \times 2000 \times 110$ feet in the x, y and z directions respectively. Rearrangement of the reservoir causes re-orientation of the dimensions in the y and z directions with the dimensions in the 3 coordinate directions now being $4000 \times 110 \times 2000$ feet. Data for pseudo-skin and Dietz shape factor are not available for this geometry and hence we adopt a two step approach to investigate the ability of the current analytic tool to predict performance.

3.4.2 Step 1 - Numerical Analysis of Actual ML Well with Single Block Productivity

The first step is essentially a validation of the reservoir engineering principle that

the sum of PI's for all blocks must be nearly equal to the PI of a ML well architecture. Herein we numerically simulate the performance of an 8 lateral and a 15 lateral structure in the original geometry. We then compare this performance with that of a single block which would be a subset of the rearranged ML well architecture. The geometry of the single block, the x-dimension, depends upon the number of laterals in the original ML well architecture. All the blocks have the same geometry, so the number of blocks is equal to the number of laterals considered. The results confirm that a single block of appropriate dimensions could be used to accurately predict the productivity of a large ML well.

The results for an 8 lateral structure are shown below. For a single block of appropriate dimensions ($500 \times 110 \times 2000$) the pseudo-steady state PI is 0.21. Hence for 8 vertical well this sums to 1.68 (Table 3.1). The productivity of an 8 lateral structure with dimensions $4000 \times 110 \times 2000$ is observed to be 1.69 as shown in Table 3.2. Similarly the performance of a 15 lateral structure and the corresponding single block structure are compared in Tables 3.3 and 3.4.

Table 3.1 – Single block productivity for an 8 lateral structure subset

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|--------|-------|-------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | - |
| 1 | 0.0 | 100 | 100 | 3,994 | 3,796 | 0.50 |
| 3 | 0.0 | 100 | 300 | 3,983 | 3,758 | 0.45 |
| 5 | 0.0 | 100 | 500 | 3,971 | 3,734 | 0.42 |
| 10 | 0.0 | 100 | 1,000 | 3,943 | 3,683 | 0.39 |
| 15 | 0.0 | 100 | 1,500 | 3,914 | 3,635 | 0.36 |
| 20 | 0.1 | 100 | 2,000 | 3,885 | 3,589 | 0.34 |
| 35 | 0.1 | 100 | 3,500 | 3,799 | 3,464 | 0.30 |
| 50 | 0.1 | 100 | 5,000 | 3,713 | 3,349 | 0.27 |
| 75 | 0.2 | 100 | 7,500 | 3,569 | 3,173 | 0.25 |
| 100 | 0.3 | 100 | 10,000 | 3,426 | 3,009 | 0.24 |
| 125 | 0.3 | 100 | 12,500 | 3,282 | 2,852 | 0.23 |
| 150 | 0.4 | 100 | 15,000 | 3,138 | 2,699 | 0.23 |
| 175 | 0.5 | 100 | 17,500 | 2,994 | 2,549 | 0.22 |
| 200 | 0.5 | 100 | 20,000 | 2,850 | 2,402 | 0.22 |
| 225 | 0.6 | 100 | 22,500 | 2,706 | 2,255 | 0.22 |
| 250 | 0.7 | 100 | 25,000 | 2,562 | 2,110 | 0.22 |
| 275 | 0.8 | 100 | 27,500 | 2,418 | 1,964 | 0.22 |
| 300 | 0.8 | 100 | 30,000 | 2,274 | 1,819 | 0.22 |
| 325 | 0.9 | 100 | 32,500 | 2,130 | 1,675 | 0.22 |
| 350 | 1.0 | 100 | 35,000 | 1,985 | 1,530 | 0.22 |
| 375 | 1.0 | 100 | 37,500 | 1,841 | 1,385 | 0.22 |
| 400 | 1.1 | 100 | 40,000 | 1,697 | 1,241 | 0.22 |
| 425 | 1.2 | 100 | 42,500 | 1,552 | 1,096 | 0.22 |
| 450 | 1.2 | 100 | 45,000 | 1,408 | 951 | 0.22 |
| 475 | 1.3 | 100 | 47,500 | 1,263 | 806 | 0.22 |
| 500 | 1.4 | 100 | 50,000 | 1,118 | 662 | 0.22 |
| 525 | 1.4 | 100 | 52,500 | 974 | 517 | 0.22 |
| 550 | 1.5 | 67 | 54,178 | 876 | 500 | 0.18 |
| 575 | 1.6 | 46 | 55,334 | 809 | 500 | 0.15 |
| 600 | 1.6 | 34 | 56,186 | 760 | 500 | 0.13 |

For a single block $PI = 0.21$

Hence for 8 vertical wells the $PI = 0.21 \times 8 = 1.68$

Table 3.2-Productivity of an 8 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|-------|-------|-----------|
| days | years | stb/day | Stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | - |
| 1 | 0.0 | 400 | 400 | 3,997 | 3,874 | 3.26 |
| 3 | 0.0 | 400 | 1,200 | 3,991 | 3,856 | 2.96 |
| 5 | 0.0 | 400 | 2,000 | 3,986 | 3,845 | 2.84 |
| 10 | 0.0 | 400 | 4,000 | 3,971 | 3,821 | 2.66 |
| 15 | 0.0 | 400 | 6,000 | 3,957 | 3,798 | 2.52 |
| 20 | 0.1 | 400 | 8,000 | 3,943 | 3,777 | 2.41 |
| 35 | 0.1 | 400 | 14,000 | 3,900 | 3,717 | 2.19 |
| 50 | 0.1 | 400 | 20,000 | 3,856 | 3,662 | 2.05 |
| 75 | 0.2 | 400 | 30,000 | 3,785 | 3,576 | 1.92 |
| 100 | 0.3 | 400 | 40,000 | 3,713 | 3,495 | 1.84 |
| 125 | 0.3 | 400 | 50,000 | 3,641 | 3,417 | 1.79 |
| 150 | 0.4 | 400 | 60,000 | 3,569 | 3,342 | 1.76 |
| 175 | 0.5 | 400 | 70,000 | 3,497 | 3,267 | 1.74 |
| 200 | 0.5 | 400 | 80,000 | 3,426 | 3,194 | 1.72 |
| 225 | 0.6 | 400 | 90,000 | 3,354 | 3,120 | 1.72 |
| 250 | 0.7 | 400 | 100,000 | 3,282 | 3,048 | 1.71 |
| 275 | 0.8 | 400 | 110,000 | 3,210 | 2,975 | 1.71 |
| 300 | 0.8 | 400 | 120,000 | 3,138 | 2,903 | 1.70 |
| 325 | 0.9 | 400 | 130,000 | 3,066 | 2,831 | 1.70 |
| 350 | 1.0 | 400 | 140,000 | 2,994 | 2,759 | 1.70 |
| 375 | 1.0 | 400 | 150,000 | 2,922 | 2,687 | 1.70 |
| 400 | 1.1 | 400 | 160,000 | 2,850 | 2,615 | 1.70 |
| 425 | 1.2 | 400 | 170,000 | 2,778 | 2,542 | 1.70 |
| 450 | 1.2 | 400 | 180,000 | 2,706 | 2,470 | 1.70 |
| 475 | 1.3 | 400 | 190,000 | 2,634 | 2,398 | 1.70 |
| 500 | 1.4 | 400 | 200,000 | 2,562 | 2,326 | 1.70 |
| 525 | 1.4 | 400 | 210,000 | 2,490 | 2,254 | 1.70 |
| 550 | 1.5 | 400 | 220,000 | 2,418 | 2,182 | 1.70 |
| 575 | 1.6 | 400 | 230,000 | 2,346 | 2,110 | 1.69 |
| 600 | 1.6 | 400 | 240,000 | 2,274 | 2,038 | 1.69 |

The PI of the 8 lateral structure compares very well with the 8 block PI's

Table 3.3 – Single block productivity of a 15 lateral subset

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|--------|-------|-------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | |
| 1 | 0.0 | 50 | 50 | 3,995 | 3,876 | 0.42 |
| 3 | 0.0 | 50 | 150 | 3,984 | 3,850 | 0.37 |
| 5 | 0.0 | 50 | 250 | 3,973 | 3,829 | 0.35 |
| 10 | 0.0 | 50 | 500 | 3,946 | 3,782 | 0.30 |
| 15 | 0.0 | 50 | 750 | 3,919 | 3,737 | 0.27 |
| 20 | 0.1 | 50 | 1,000 | 3,892 | 3,694 | 0.25 |
| 35 | 0.1 | 50 | 1,750 | 3,812 | 3,578 | 0.21 |
| 50 | 0.1 | 50 | 2,500 | 3,731 | 3,471 | 0.19 |
| 75 | 0.2 | 50 | 3,750 | 3,596 | 3,309 | 0.17 |
| 100 | 0.3 | 50 | 5,000 | 3,462 | 3,157 | 0.16 |
| 125 | 0.3 | 50 | 6,250 | 3,327 | 3,011 | 0.16 |
| 150 | 0.4 | 50 | 7,500 | 3,192 | 2,870 | 0.16 |
| 175 | 0.5 | 50 | 8,750 | 3,057 | 2,730 | 0.15 |
| 200 | 0.5 | 50 | 10,000 | 2,922 | 2,593 | 0.15 |
| 225 | 0.6 | 50 | 11,250 | 2,787 | 2,456 | 0.15 |
| 250 | 0.7 | 50 | 12,500 | 2,652 | 2,320 | 0.15 |
| 275 | 0.8 | 50 | 13,750 | 2,517 | 2,184 | 0.15 |
| 300 | 0.8 | 50 | 15,000 | 2,382 | 2,048 | 0.15 |
| 325 | 0.9 | 50 | 16,250 | 2,247 | 1,913 | 0.15 |
| 350 | 1.0 | 50 | 17,500 | 2,112 | 1,777 | 0.15 |
| 375 | 1.0 | 50 | 18,750 | 1,976 | 1,642 | 0.15 |
| 400 | 1.1 | 50 | 20,000 | 1,841 | 1,506 | 0.15 |
| 425 | 1.2 | 50 | 21,250 | 1,706 | 1,371 | 0.15 |
| 450 | 1.2 | 50 | 22,500 | 1,570 | 1,235 | 0.15 |
| 475 | 1.3 | 50 | 23,750 | 1,435 | 1,100 | 0.15 |
| 500 | 1.4 | 50 | 25,000 | 1,299 | 964 | 0.15 |
| 525 | 1.4 | 50 | 26,250 | 1,164 | 828 | 0.15 |
| 550 | 1.5 | 50 | 27,500 | 1,028 | 693 | 0.15 |
| 575 | 1.6 | 50 | 28,750 | 892 | 557 | 0.15 |
| 600 | 1.6 | 36 | 29,649 | 795 | 500 | 0.12 |

Hence the productivity of 15 blocks = $0.15 \times 15 = 2.25$

Table 3.4 – Productivity of a 15 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|--------|-------|-------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | |
| 1 | 0.0 | 200 | 200 | 3,999 | 3,963 | 5.63 |
| 3 | 0.0 | 200 | 600 | 3,996 | 3,957 | 5.17 |
| 5 | 0.0 | 200 | 1,000 | 3,993 | 3,952 | 4.88 |
| 10 | 0.0 | 200 | 2,000 | 3,986 | 3,940 | 4.38 |
| 15 | 0.0 | 200 | 3,000 | 3,978 | 3,929 | 4.02 |
| 20 | 0.1 | 200 | 4,000 | 3,971 | 3,918 | 3.75 |
| 35 | 0.1 | 200 | 7,000 | 3,950 | 3,889 | 3.27 |
| 50 | 0.1 | 200 | 10,000 | 3,928 | 3,861 | 2.98 |
| 75 | 0.2 | 200 | 15,000 | 3,892 | 3,819 | 2.73 |
| 100 | 0.3 | 200 | 20,000 | 3,856 | 3,779 | 2.58 |
| 125 | 0.3 | 200 | 25,000 | 3,821 | 3,741 | 2.50 |
| 150 | 0.4 | 200 | 30,000 | 3,785 | 3,703 | 2.45 |
| 175 | 0.5 | 200 | 35,000 | 3,749 | 3,666 | 2.42 |
| 200 | 0.5 | 200 | 40,000 | 3,713 | 3,630 | 2.40 |
| 225 | 0.6 | 200 | 45,000 | 3,677 | 3,593 | 2.39 |
| 250 | 0.7 | 200 | 50,000 | 3,641 | 3,557 | 2.38 |
| 275 | 0.8 | 200 | 55,000 | 3,605 | 3,521 | 2.37 |
| 300 | 0.8 | 200 | 60,000 | 3,569 | 3,485 | 2.37 |
| 325 | 0.9 | 200 | 65,000 | 3,533 | 3,449 | 2.37 |
| 350 | 1.0 | 200 | 70,000 | 3,497 | 3,413 | 2.37 |
| 375 | 1.0 | 200 | 75,000 | 3,461 | 3,377 | 2.36 |
| 400 | 1.1 | 200 | 80,000 | 3,425 | 3,341 | 2.36 |
| 425 | 1.2 | 200 | 85,000 | 3,390 | 3,305 | 2.36 |
| 450 | 1.2 | 200 | 90,000 | 3,354 | 3,269 | 2.36 |
| 475 | 1.3 | 200 | 95,000 | 3,318 | 3,233 | 2.36 |

Again from the above simulation results we see that the productivity of 15 identical blocks will slightly under predict the productivity of a ML well with 15 laterals Fig 3.4 shows a comparison of these simulation results and reinforce the belief that single block PI can be used to accurately predict the PI of the ML well architecture.

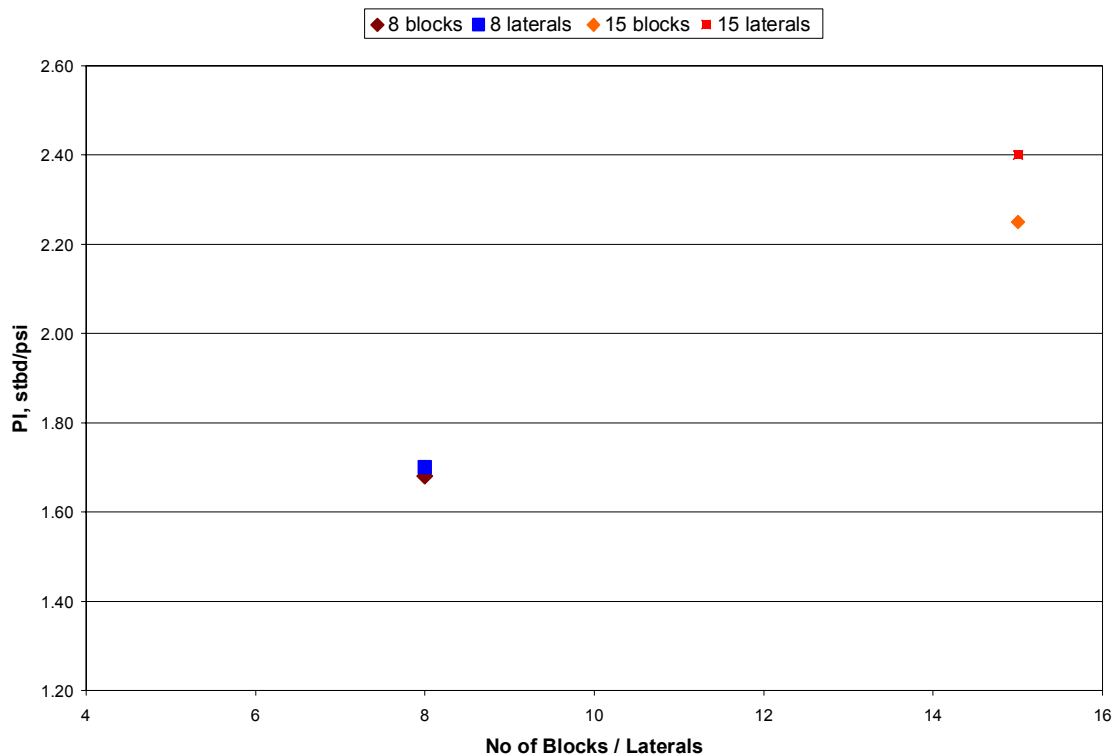


Figure 3.4 – Comparison of single block performance with the corresponding ML well structure

3.4.3 Step 2 – Analysis of Analytic and Numeric Solution for Well-Defined Geometry

In the second step the idea is to use the pseudo-skin and shape factor data published in the literature to evaluate the PI of a single block and compare it to the numerical solution of similar geometry containing a partially penetrating well. By doing so we can observe the results and comment whether the current tools are good enough to accurately predict the performance of a block which in turn predicts ML well performance. Dietz shape factor²⁴ is available for an aspect ratio of 1:5 with the well in the center. This geometry shown in Figure 3.5 comes closest to the single block geometry of an 8 lateral structure subset and hence we choose this ratio for our computations. The dimensions used in the x and y directions are 500 × 100 feet with varying depths. We also perform the comparison of analytic and numeric solutions for the isotropic and anisotropic case. The anisotropy exists in the horizontal plane in the rearranged structure,

in other words for the anisotropic case $k_x = k_z \neq k_y$. In all the cases analyzed we consider a vertical well with 50% penetration in the z-direction.

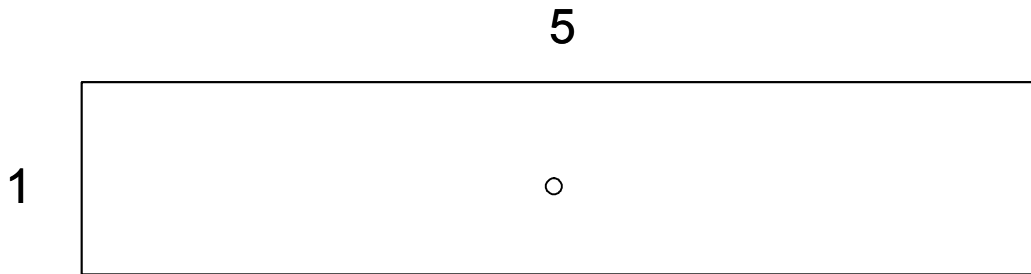
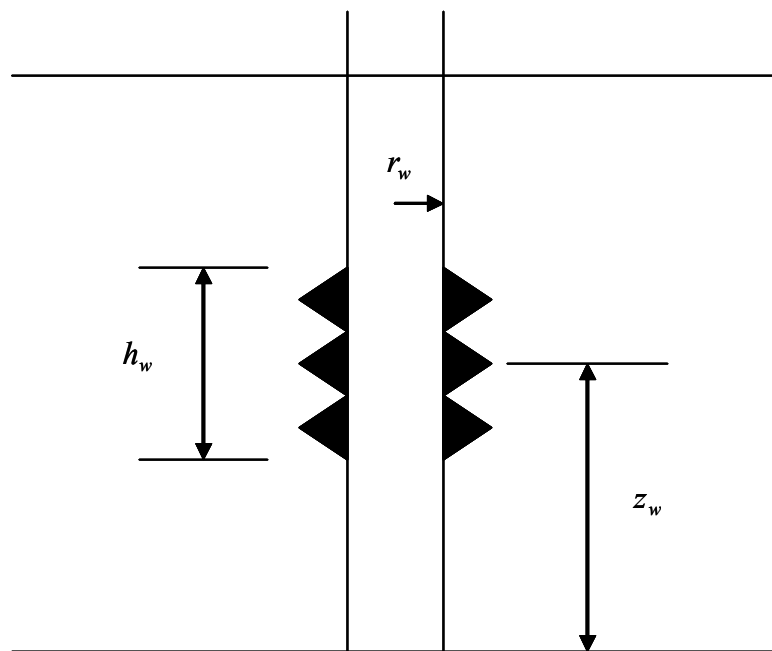


Figure 3.5– Simplest single block structure with a 5:1 ratio between its sides

Cinco-Ley *et. al.* have presented pseudo-skin data for partially penetrating wells for certain dimensionless variables such as $h_D = h/r_w$; z_w/h ; h_w/h and h/r_w . The data is available for values of h_D equal to 100 and 1000. Hence we define cases such the dimensionless thickness h_D is equal to either of these values. Figure 3.6 shows a partially penetrating well and significance of the values. Hence z_w/h is the elevation ratio while h_w/h is the completion ratio. In all the cases analyzed here we assume 50% penetration in the upper half of the reservoir. Hence the elevation ratio and the completion ratio is 0.75 and 0.5 in all the cases studied. The value of the dimensionless thickness depends upon the choice of the well bore radius. In order to match the available solutions from Cinco-Ley we use the following sets of values for reservoir depth and well bore radius as given in Table 3.5. The table also gives the corresponding value of pseudo-skin.



h_w = Completion Thickness

z_w = Elevation

Figure 3.6– Partially penetrating vertical well

Table 3.5 – Dimensionless height for Cinco pseudo-skin data

| Depth, ft | Well bore Radius, ft | h_D | Skin, S |
|-----------|----------------------|-------|---------|
| 50 | 0.5 | 100 | 3.067 |
| 500 | 0.5 | 1000 | 5.467 |
| 1000 | 1 | 1000 | 5.467 |
| 1500 | 1.5 | 1000 | 5.467 |

Consider the first case when the depth is equal to 50 ft. The dimensions of the block are $500 \times 100 \times 50$ in the three co-ordinate directions. As in all the other cases the drainage area to be used for the analytic solution is 500×100 . For this drainage area with the well in the center the Dietz shape factor is 2.36. For a given depth corresponding values of well bore radius and skin are used. The equation used is,

$$J = \frac{kh}{141.2B\mu} \frac{1}{\left(\frac{1}{2} \ln \left(\frac{4A}{\gamma C_A r_w^2} \right) + s \right)} \dots\dots\dots (3.1)$$

Depending upon the permeability distribution in the reservoir the value of k will change for a isotropic and anisotropic reservoir. For the rearranged structure the permeability anisotropy exists in the x-y plane i.e. in the horizontal plane. For the purpose of this calculation we have used $k = \sqrt{k_x k_y}$ in anisotropic cases. For the isotropic case we assume the permeability to be equal to 1 in all directions.

Hence for a given reservoir configuration we have solutions for the isotropic as well as the anisotropic case. A comparison of the analytic and numeric results is shown in Table 3.6 for the isotropic case and Table 3.7 for the anisotropic case. These results are then plotted to in Figure 3.7 and Figure 3.8 to show the deviation in the results with increasing depths.

Table 3.6 – Comparison of PI's for isotropic case

| Reservoir Dimension | $J_{Analytical}$ Stbd/psia | $J_{Numerical}$ Stbd/psia |
|---------------------|-------------------------------|------------------------------|
| 500 × 100 × 50 | 0.038 | 0.032 |
| 500 × 100 × 500 | 0.306 | 0.2 |
| 500 × 100 × 1000 | 0.644 | 0.296 |
| 500 × 100 × 1500 | 1.004 | 0.307 |

Table 3.7 – Comparison of PI's for anisotropic case

| Reservoir Dimension | $J_{Analytical}$ Stbd/psia | $J_{Numerical}$ Stbd/psia |
|---------------------|-------------------------------|------------------------------|
| 500 × 100 × 50 | 0.011 | 0.015 |
| 500 × 100 × 500 | 0.093 | 0.107 |
| 500 × 100 × 1000 | 0.199 | 0.183 |
| 500 × 100 × 1500 | 0.311 | 0.219 |

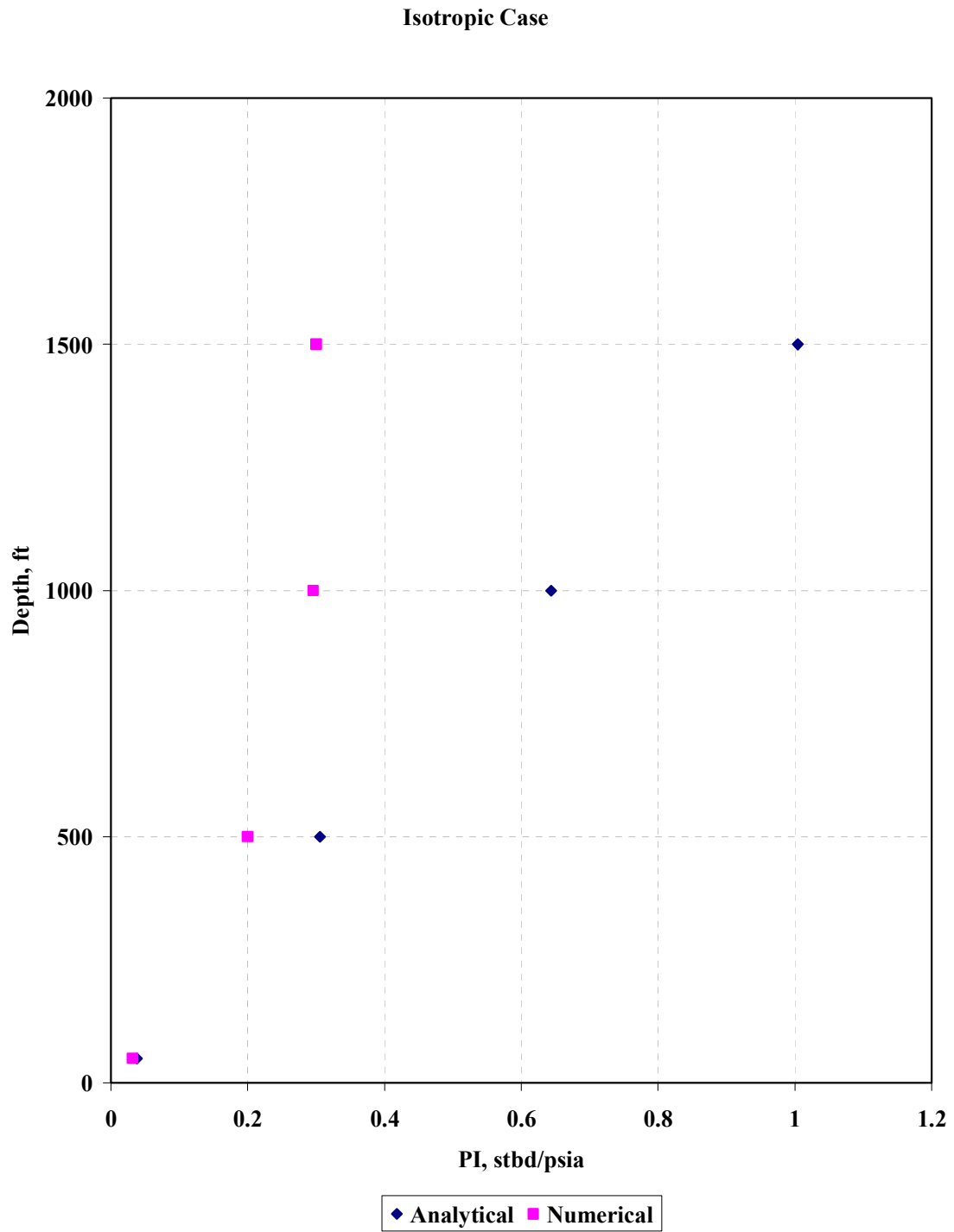


Figure 3.7 – Comparison of results for isotropic case

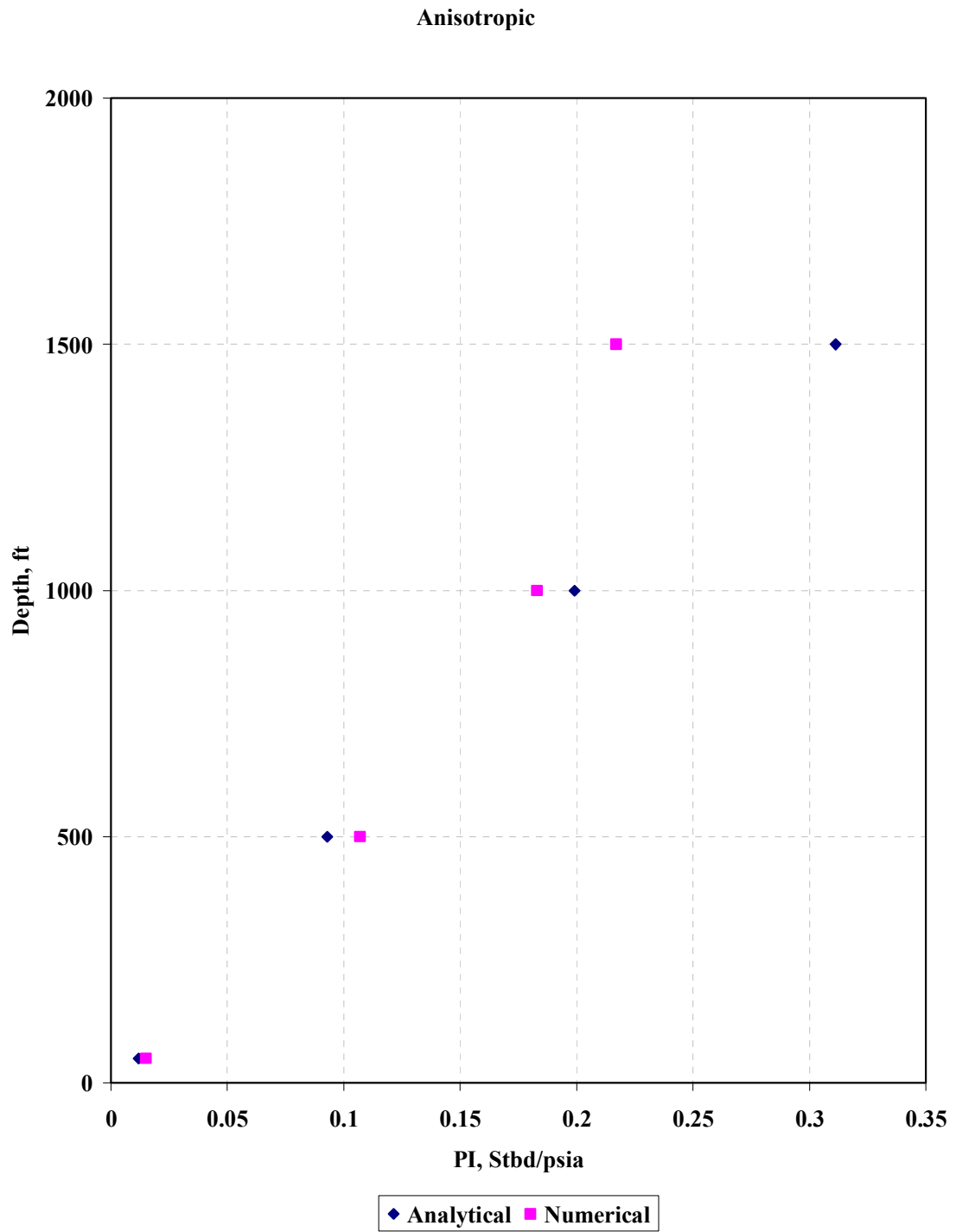


Figure 3.8 – Comparison of results for anisotropic case

3.4.4 Discussion of Results

From the results we can clearly see that the present analytical tool is not very effective in accurately predicting the productivity of a block containing a partially penetrating well. The analytical solution compares reasonable well with the numerical results at low depths. But at greater depths the analytical and numerical solutions diverge for both the isotropic and anisotropic case.

CHAPTER IV

PRELIMINARY ANALYSIS OF PROPOSED ARCHITECTURE FOR SYNTHETIC CASES

4.1 Parameters to be Analyzed

In this chapter we simulate synthetic cases to study the effect of various parameters on the performance of ML wells. A base case is set up containing a ML well architecture described earlier. Single phase flow of dry oil, which contains no dissolved gases, is considered in this parametric analysis. The parameters we wish to investigate are essentially related to the design of the architecture and primary reservoir properties that affect the flow of the fluids in the reservoir.

Branch Density & Extent of Penetration – The cost of a ML well will depend greatly upon the number of laterals to be drilled and extent of their penetration into the bulk of the reservoir. Drilling any more laterals than absolutely necessary puts greater burden on the cash flow. On the other hand fewer laterals might not utilize the full benefits of the larger reservoir exposure offered by ML wells. It is expected that initially adding a lateral to the structure will continuously add production but after a certain extent the addition of each extra lateral will not significantly add to the total production. In such a case the excess laterals become redundant. Also it might be beneficial to drill the laterals only to a certain extent into the reservoir rather than all the way to the lateral boundary. We wish to address such issues through this analysis. The aim in designing the architecture is to drill an optimum number of laterals with an optimum penetration extent so that the benefit to cost ratio of the well, which is nothing but the stock tank barrels of oil produced per dollar spent, is maximized. Hence we choose branch density and penetration extent as the investigative parameters at the outset.

Permeability Variations – The flow into the laterals will be normally linear and perpendicular. The laterals are considered to be only in the horizontal direction and hence the permeability in the z direction plays an important role in the inflow to the laterals. We compare the effect of permeability variation for a given lateral structure.

4.2 Reservoir Geometry and Properties

A homogeneous rectangular reservoir is simulated. The dimensions of the reservoir in the 3 co-ordinate directions are $2000 \times 4000 \times 110$ respectively. The mother bore is placed at the middle of the reservoir in the z-direction. While the laterals form an alternating mesh of perforated slim holes connected to the mother bore. The base case analyzed is anisotropic, so that the permeability in the horizontal and vertical direction is not the same. A $21 \times 62 \times 11$ grid is used. The other important input properties are shown in the Table 4.1 below.

Table 4.1 – Base case reservoir properties

| | |
|--|-------------------------------------|
| Grid Size | $21 \times 62 \times 11$ |
| Reservoir Size | $2000 \times 4000 \times 110$ |
| Permeability (mD) $k_x = k_y$ k_z | Anisotropic 1.00 0.10 |
| Porosity | 0.3 |

4.3 Simulation Cases

To analyze density effects of laterals we simulate a 60, 30, 15 and a 4 – lateral structure for complete penetration from the mother bore to the lateral boundary. This is followed by simulation for the lateral partial penetration assuming they penetrate out to

an extent of 45% and 75% of lateral dimension. Finally to observe permeability effects we simulate the base case assuming isotropic permeability in the reservoir.

4.4 Simulation Results

4.4.1 Branch Density and Partial Penetration Effects

A summary of some key results for branch density effects is given in Table 4.2. From the table we see that the cumulative production for a structure with 60 laterals is 0.5520 MMSTB, while the cumulative production from a 4 - lateral structure is 0.5505 MMSTB. The difference of about 1500 STB indicates that the same reservoir can be depleted to nearly the same extent by using much fewer laterals. In other words after a certain number increasing the number of laterals does not increase the cumulative production by a large amount. The only noticeable difference between using a very high number of laterals as compared to using an optimum is in the time required to attain a certain amount of cumulative production. For example the time to obtain 550,000 STB of cumulative production from a 60 and a 4 lateral structure would be 287 days and 1000 days respectively.

In all the runs mentioned above the bottom hole flowing pressure was allowed to fall to 14.7 psia. These cases were simulated again, but this time the bottom hole flowing pressure is set to not decrease below 1000 psia. The corresponding results are tabulated in Table 2 - B. Again the difference in cumulative for 60 and 4 laterals is very small and the basic difference is in the time distribution of the production. The results of the simulation for the effect of density are shown in Tables 4.3 – 4.6. Figure 4.1 shows a variation in bottomhole pressure with the number of laterals.

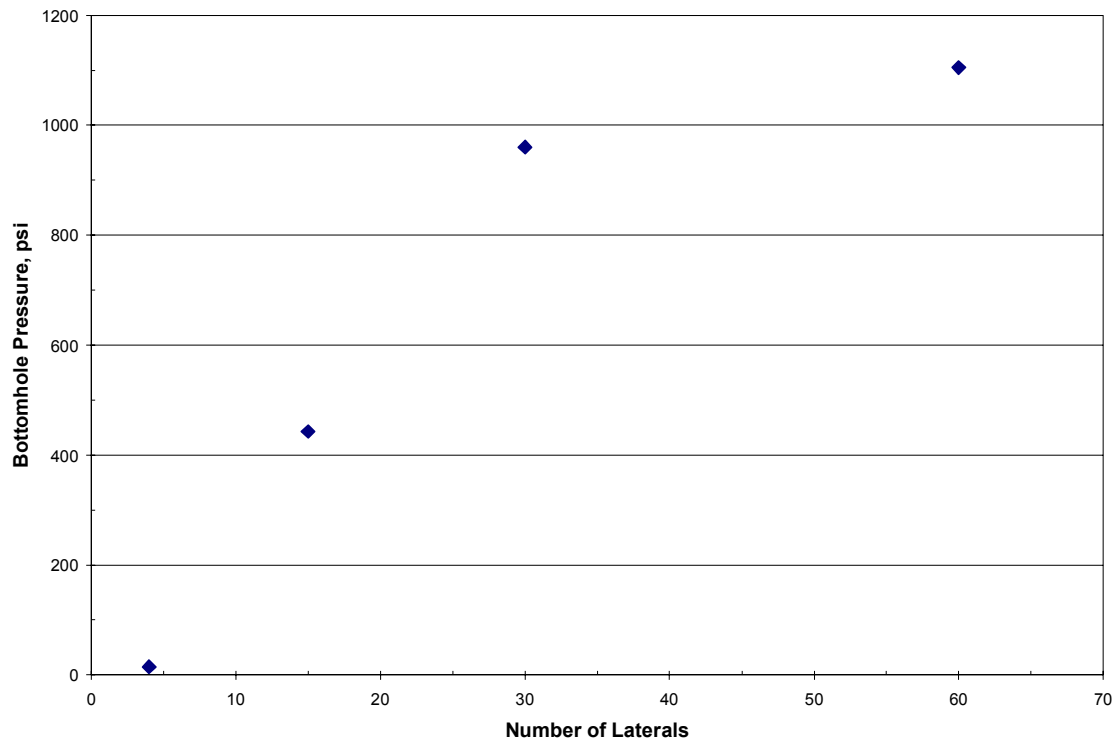


Figure 4.1 – A much lower bottomhole pressure is needed when using fewer laterals, increasing the possibility of borehole collapse, sand production, water coning.

Table 4.2 - Summary of simulation results

| Well Structure | Cum Prod. | Field Pressure | BHP |
|--------------------------------------|-----------|----------------|-------|
| (No. of Laterals) | stb | psia | psia |
| [A] Base Case Runs | | | |
| 60 | 552,030 | 18 | 0 |
| 30 | 552,048 | 18 | 14.7 |
| 15 | 552,041 | 18 | 14.7 |
| 4 | 550,539 | 29 | 14.7 |
| [B] Base Case Runs (BHP = 1000 PSIA) | | | |
| 60 | 416,055 | 1,003 | 0 |
| 30 | 416,049 | 1,003 | 0 |
| 4 | 414,971 | 1,011 | 1,000 |

Table 4.3 – Productivity of a 60 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|--------|-------|---------|----------|--------|--------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0.0 | 0.0 | 0.0 | 0.0 | 4000.0 | 4000.0 | - |
| 1.0 | 0.0 | 3818.2 | 3818.2 | 3972.5 | 3838.6 | 28.5 |
| 3.0 | 0.0 | 3818.2 | 11454.5 | 3917.8 | 3774.7 | 26.7 |
| 5.0 | 0.0 | 3818.2 | 19090.9 | 3863.0 | 3718.9 | 26.5 |
| 10.0 | 0.0 | 3818.2 | 38181.8 | 3726.1 | 3581.7 | 26.4 |
| 15.0 | 0.0 | 3818.2 | 57272.7 | 3589.1 | 3444.6 | 26.4 |
| 20.0 | 0.1 | 3818.2 | 76363.6 | 3452.0 | 3307.4 | 26.4 |
| 35.0 | 0.1 | 3818.2 | 133636.3 | 3040.4 | 2895.7 | 26.4 |
| 50.0 | 0.1 | 3818.2 | 190909.0 | 2628.3 | 2483.4 | 26.3 |
| 75.0 | 0.2 | 3818.2 | 286363.5 | 1940.4 | 1795.2 | 26.3 |
| 100.0 | 0.3 | 3818.2 | 381818.0 | 1251.1 | 1105.6 | 26.2 |
| 150.0 | 0.4 | 3086.5 | 536140.8 | 133.4 | 14.7 | - |
| 200.0 | 0.5 | 287.5 | 550515.1 | 29.1 | 14.7 | - |
| 300.0 | 0.8 | 14.4 | 551952.1 | 18.6 | 14.7 | - |
| 400.0 | 1.1 | 0.7 | 552024.4 | 18.1 | 14.7 | - |
| 500.0 | 1.4 | 0.1 | 552029.8 | 18.1 | 14.7 | - |
| 600.0 | 1.6 | 0.0 | 552030.1 | 18.1 | 14.7 | - |
| 700.0 | 1.9 | 0.0 | 552030.1 | 18.1 | 0.0 | - |
| 800.0 | 2.2 | 0.0 | 552030.1 | 18.1 | 0.0 | - |
| 900.0 | 2.5 | 0.0 | 552030.1 | 18.1 | 0.0 | - |
| 1000.0 | 2.7 | 0.0 | 552030.1 | 18.1 | 0.0 | - |

Table 4.4 – Productivity of a 30 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|---------|---------|-----------|
| days | years | stb/day | stb | psia | Psia | stbd/psia |
| 0 | 0.0 | 0.0 | 0 | 4,000.0 | 4,000.0 | - |
| 1 | 0.0 | 3,818.2 | 3,818 | 3,972.6 | 3,706.7 | 14.4 |
| 3 | 0.0 | 3,818.2 | 11,455 | 3,917.9 | 3,634.5 | 13.5 |
| 5 | 0.0 | 3,818.2 | 19,091 | 3,863.1 | 3,576.9 | 13.3 |
| 10 | 0.0 | 3,818.2 | 38,182 | 3,726.2 | 3,438.7 | 13.3 |
| 15 | 0.0 | 3,818.2 | 57,273 | 3,589.2 | 3,301.0 | 13.3 |
| 20 | 0.1 | 3,818.2 | 76,364 | 3,452.1 | 3,163.6 | 13.2 |
| 35 | 0.1 | 3,818.2 | 133,636 | 3,040.5 | 2,751.4 | 13.2 |
| 50 | 0.1 | 3,818.2 | 190,909 | 2,628.4 | 2,338.8 | 13.2 |
| 75 | 0.2 | 3,818.2 | 286,364 | 1,940.5 | 1,650.2 | 13.2 |
| 100 | 0.3 | 3,818.2 | 381,818 | 1,251.2 | 960.3 | 13.1 |
| 150 | 0.4 | 2,817.5 | 522,695 | 231.1 | 14.7 | - |
| 200 | 0.5 | 484.3 | 546,911 | 55.4 | 14.7 | - |
| 300 | 0.8 | 46.4 | 551,549 | 21.7 | 14.7 | - |
| 400 | 1.1 | 4.5 | 551,996 | 18.5 | 14.7 | - |
| 500 | 1.4 | 0.5 | 552,042 | 18.1 | 14.7 | - |
| 600 | 1.6 | 0.0 | 552,047 | 18.1 | 14.7 | - |
| 700 | 1.9 | 0.0 | 552,048 | 18.1 | 14.7 | - |
| 800 | 2.2 | 0.0 | 552,048 | 18.1 | 14.7 | - |
| 900 | 2.5 | 0.0 | 552,048 | 18.1 | 14.7 | - |
| 1000 | 2.7 | 0.0 | 552,048 | 18.1 | 14.7 | - |

Table 4.5 - Productivity of a 15 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|---------|---------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0.0 | 0 | 4,000.0 | 4,000.0 | - |
| 1 | 0.0 | 3,818.2 | 3,818 | 3,972.9 | 3,295.8 | 5.6 |
| 3 | 0.0 | 3,818.2 | 11,455 | 3,918.2 | 3,166.5 | 5.1 |
| 5 | 0.0 | 3,818.2 | 19,091 | 3,863.4 | 3,092.1 | 5.0 |
| 10 | 0.0 | 3,818.2 | 38,182 | 3,726.5 | 2,942.4 | 4.9 |
| 15 | 0.0 | 3,818.2 | 57,273 | 3,589.5 | 2,799.8 | 4.8 |
| 20 | 0.1 | 3,818.2 | 76,364 | 3,452.4 | 2,659.5 | 4.8 |
| 35 | 0.1 | 3,818.2 | 133,636 | 3,040.9 | 2,242.6 | 4.8 |
| 50 | 0.1 | 3,818.2 | 190,909 | 2,628.8 | 1,826.9 | 4.8 |
| 75 | 0.2 | 3,818.2 | 286,364 | 1,940.8 | 1,135.2 | 4.7 |
| 100 | 0.3 | 3,818.2 | 381,818 | 1,251.4 | 443.0 | 4.7 |
| 150 | 0.4 | 2,141.5 | 488,894 | 476.3 | 14.7 | - |
| 200 | 0.5 | 788.0 | 528,292 | 190.5 | 14.7 | - |
| 300 | 0.8 | 181.7 | 546,464 | 58.6 | 14.7 | - |
| 400 | 1.1 | 42.5 | 550,715 | 27.7 | 14.7 | - |
| 500 | 1.4 | 10.1 | 551,722 | 20.4 | 14.7 | - |
| 600 | 1.6 | 2.4 | 551,964 | 18.7 | 14.7 | - |
| 700 | 1.9 | 0.6 | 552,022 | 18.2 | 14.7 | - |
| 800 | 2.2 | 0.1 | 552,036 | 18.1 | 14.7 | - |
| 900 | 2.5 | 0.0 | 552,040 | 18.1 | 14.7 | - |
| 1000 | 2.7 | 0.0 | 552,041 | 18.1 | 14.7 | - |

Table 4.6 - Productivity of a 4 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|---------|---------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0.0 | 0 | 4,000.0 | 4,000.0 | - |
| 1 | 0.0 | 3,818.2 | 3,818 | 3,973.5 | 2,341.4 | 2.3 |
| 3 | 0.0 | 3,818.2 | 11,455 | 3,918.9 | 1,993.4 | 2.0 |
| 5 | 0.0 | 3,818.2 | 19,091 | 3,864.2 | 1,817.9 | 1.9 |
| 10 | 0.0 | 3,818.2 | 38,182 | 3,727.3 | 1,528.4 | 1.7 |
| 15 | 0.0 | 3,818.2 | 57,273 | 3,590.4 | 1,285.4 | 1.7 |
| 20 | 0.1 | 3,818.2 | 76,364 | 3,453.3 | 1,064.4 | 1.6 |
| 35 | 0.1 | 3,818.2 | 133,636 | 3,041.5 | 477.6 | 1.5 |
| 50 | 0.1 | 3,701.5 | 189,159 | 2,641.8 | 14.7 | - |
| 75 | 0.2 | 2,701.4 | 256,694 | 2,154.9 | 14.7 | - |
| 100 | 0.3 | 2,072.3 | 308,502 | 1,781.0 | 14.7 | - |
| 150 | 0.4 | 1,385.1 | 377,756 | 1,280.7 | 14.7 | - |
| 200 | 0.5 | 965.2 | 426,017 | 931.6 | 14.7 | - |
| 300 | 0.8 | 539.3 | 479,945 | 541.1 | 14.7 | - |
| 400 | 1.1 | 306.9 | 510,631 | 318.6 | 14.7 | - |
| 500 | 1.4 | 175.9 | 528,219 | 191.1 | 14.7 | - |
| 600 | 1.6 | 101.1 | 538,329 | 117.7 | 14.7 | - |
| 700 | 1.9 | 58.2 | 544,147 | 75.4 | 14.7 | - |
| 800 | 2.2 | 33.5 | 547,498 | 51.1 | 14.7 | - |
| 900 | 2.5 | 19.3 | 549,427 | 37.1 | 14.7 | - |
| 1000 | 2.7 | 11.1 | 550,539 | 29.1 | 14.7 | - |

Further results for partial penetration of laterals are shown in Tables 4.7 – 4.9. Here we compare partial penetration effects using 2 to 30 - laterals. A comparison of results shows that using 4 laterals produces just as well as 30 - laterals. However a comparison of production from 4 and 2 - laterals indicates a significant difference in cumulative production. This is observed even when the 4 - lateral structure penetrated to only 45% while the 2 lateral structure penetrated to about 73%. Also the time taken to produce the same amount of reservoir fluids is much less for the 4 – laterals case with 45% penetration thus increasing the economy of operation.

Table 4.7- Productivity of a 30 lateral structure with 45% penetration

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|-------|-------|---------|---------|-------|-------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0.0 | 0 | 4,000 | 4,000 | - |
| 1 | 0.0 | 3,818.2 | 3,818 | 3,972 | 3,302 | 5.7 |
| 4 | 0.0 | 3,818.2 | 15,273 | 3,890 | 3,106 | 4.9 |
| 13 | 0.0 | 3,818.2 | 49,636 | 3,643 | 2,724 | 4.2 |
| 25 | 0.1 | 3,818.2 | 95,455 | 3,314 | 2,302 | 3.8 |
| 50 | 0.1 | 3,818.2 | 190,909 | 2,627 | 1,546 | 3.5 |
| 75 | 0.2 | 3,430.8 | 276,680 | 2,009 | 1,000 | 3.4 |
| 100 | 0.3 | 2,003.1 | 326,756 | 1,647 | 1,000 | 3.1 |
| 200 | 0.5 | 340.8 | 399,892 | 1,119 | 1,000 | 2.9 |
| 300 | 0.8 | 61.7 | 412,979 | 1,024 | 1,000 | 2.5 |
| 305 | 0.8 | 55.7 | 413,257 | 1,022 | 1,000 | 2.5 |
| 310 | 0.8 | 50.3 | 413,509 | 1,020 | 1,000 | 2.5 |
| 315 | 0.9 | 45.5 | 413,736 | 1,018 | 1,000 | 2.4 |
| 320 | 0.9 | 41.1 | 413,942 | 1,017 | 1,000 | 2.4 |
| 325 | 0.9 | 37.1 | 414,128 | 1,016 | 1,000 | 2.3 |
| 337.5 | 0.9 | 29.4 | 414,496 | 1,013 | 1,000 | 2.2 |
| 350 | 1.0 | 23.2 | 414,785 | 1,011 | 1,000 | 2.1 |
| 400 | 1.1 | 9.9 | 415,410 | 1,006 | 1,000 | 1.5 |
| 500 | 1.4 | 1.8 | 415,786 | 1,004 | 1,000 | - |
| 600 | 1.6 | 0.3 | 415,853 | 1,003 | 1,000 | - |
| 700 | 1.9 | 0.1 | 415,865 | 1,003 | 1,000 | - |
| 800 | 2.2 | 0.0 | 415,867 | 1,003 | 1,000 | - |
| 900 | 2.5 | 0.0 | 415,867 | 1,003 | 1,000 | - |
| 1000 | 2.7 | 0.0 | 415,867 | 1,003 | 1,000 | - |

Table 4.8 – Productivity of a 4 lateral structure with 45% penetration in the reservoir

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|-------|------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4000 | - |
| 1 | 0.0 | 2,305 | 2,305 | 3,984 | 1000 | 0.77 |
| 3 | 0.0 | 1,953 | 6,211 | 3,956 | 1000 | 0.66 |
| 5 | 0.0 | 1,843 | 9,898 | 3,929 | 1000 | 0.63 |
| 10 | 0.0 | 1,716 | 18,478 | 3,868 | 1000 | 0.60 |
| 15 | 0.0 | 1,635 | 26,655 | 3,809 | 1000 | 0.58 |
| 50 | 0.1 | 1,353 | 76,606 | 3,450 | 1000 | 0.55 |
| 100 | 0.3 | 1,100 | 134,554 | 3,034 | 1000 | 0.54 |
| 200 | 0.5 | 746 | 221,247 | 2,409 | 1000 | 0.53 |
| 300 | 0.8 | 512 | 280,501 | 1,982 | 1000 | 0.52 |
| 400 | 1.1 | 354 | 321,376 | 1,687 | 1000 | 0.52 |
| 500 | 1.4 | 246 | 349,749 | 1,482 | 1000 | 0.51 |
| 600 | 1.6 | 172 | 369,529 | 1,339 | 1000 | 0.51 |
| 625 | 1.7 | 157 | 373,462 | 1,311 | 1000 | 0.51 |
| 650 | 1.8 | 144 | 377,059 | 1,284 | 1000 | 0.51 |
| 675 | 1.8 | 132 | 380,349 | 1,261 | 1000 | 0.50 |
| 700 | 1.9 | 120 | 383,359 | 1,239 | 1000 | 0.50 |
| 725 | 2.0 | 110 | 386,112 | 1,219 | 1000 | 0.50 |
| 750 | 2.1 | 101 | 388,631 | 1,201 | 1000 | - |
| 775 | 2.1 | 92 | 390,938 | 1,184 | 1000 | - |
| 800 | 2.2 | 84 | 393,047 | 1,169 | 1000 | - |
| 900 | 2.5 | 59 | 399,847 | 1,120 | 1000 | - |
| 1000 | 2.7 | 42 | 404,629 | 1,085 | 1000 | - |

Table 4.9 – Productivity of a 2 lateral structure with 73 % penetration

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|-------|------|-----------|
| Days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4000 | - |
| 1 | 0.0 | 1,765 | 1,765 | 3,988 | 1000 | 0.59 |
| 3 | 0.0 | 1,385 | 4,535 | 3,968 | 1000 | 0.47 |
| 5 | 0.0 | 1,253 | 7,040 | 3,950 | 1000 | 0.42 |
| 10 | 0.0 | 1,100 | 12,540 | 3,910 | 1000 | 0.38 |
| 50 | 0.1 | 772 | 46,477 | 3,667 | 1000 | 0.29 |
| 75 | 0.2 | 699 | 63,950 | 3,541 | 1000 | 0.28 |
| 100 | 0.3 | 647 | 80,119 | 3,425 | 1000 | 0.27 |
| 200 | 0.5 | 516 | 136,038 | 3,023 | 1000 | 0.26 |
| 300 | 0.8 | 428 | 181,985 | 2,692 | 1000 | 0.25 |
| 400 | 1.1 | 358 | 220,296 | 2,416 | 1000 | 0.25 |
| 500 | 1.4 | 299 | 252,319 | 2,185 | 1000 | 0.25 |
| 600 | 1.6 | 250 | 279,096 | 1,992 | 1000 | 0.25 |
| 700 | 1.9 | 209 | 301,490 | 1,831 | 1000 | 0.25 |
| 800 | 2.2 | 175 | 320,217 | 1,695 | 1000 | - |
| 900 | 2.5 | 146 | 335,878 | 1,582 | 1000 | - |
| 925 | 2.5 | 140 | 339,375 | 1,557 | 1000 | - |
| 950 | 2.6 | 134 | 342,720 | 1,533 | 1000 | - |
| 975 | 2.7 | 128 | 345,918 | 1,510 | 1000 | - |
| 1000 | 2.7 | 122 | 348,976 | 1,487 | 1000 | - |

4.4.2 Permeability

Permeability is perhaps the most important reservoir property that has a significant effect on the performance of multilateral wells. This is amply noticeable from the simulation results for isotropic and anisotropic reservoirs. The value of permeability used for isotropic reservoirs is 1 md while for the anisotropic reservoir a k_v/k_h ratio of 0.1 is used with a horizontal permeability of 1 md.

For both isotropic and anisotropic reservoirs the results show that as we decrease the branch density by half the PI also decreases by more than half. For example from the table we see that for an isotropic reservoir with a 60 – lateral structure the PI is 74 STBD/psia, while for a 30 – lateral structure the PI is 33 STBD/psia. This indicates a reduction of more than 50% in the PI. This trend is also observed when we reduce the branch density even further. Similar variation of results is also observed for an anisotropic reservoir though a much lower PI is achieved for a vertical to horizontal permeability ratio of 0.1.

The cumulative production from an isotropic reservoir is comparable for a structure with 60 – laterals and with 4 – laterals. However for the k_v/k_h ratio of 0.1 the cumulative production from a 4 – lateral structure is only 0.3085 MMSTB while it is 0.3818 MMSTB for a 15 – lateral structure. This shows that for a large permeability variation in the two directions the capacity to produce the fluids is lower and more time will be required to produce the same amount. The results are shown in Tables 4.10 – 4.15. Comparison of the PI for the two cases is shown in Figure 4.2

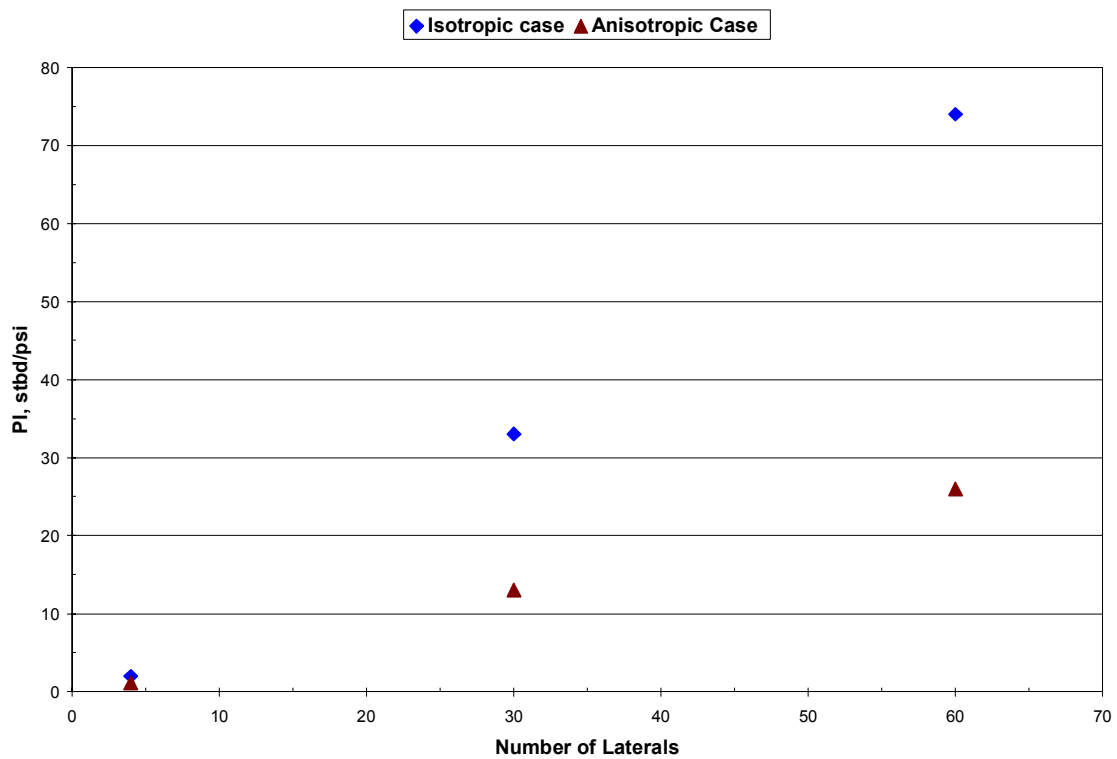


Figure 4.2 – Productivity of the ML well architecture decreases significantly (by 50%) as we go from an isotropic reservoir to an anisotropic reservoir

Table 4.10 – Isotropic reservoir productivity with a 60 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|-------|-------|-----------|
| Days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | - |
| 1 | 0.0 | 3,818 | 3,818 | 3,973 | 3,922 | 76.1 |
| 3 | 0.0 | 3,818 | 11,455 | 3,918 | 3,867 | 74.9 |
| 5 | 0.0 | 3,818 | 19,091 | 3,863 | 3,812 | 74.7 |
| 10 | 0.0 | 3,818 | 38,182 | 3,726 | 3,675 | 74.6 |
| 15 | 0.0 | 3,818 | 57,273 | 3,589 | 3,538 | 74.6 |
| 20 | 0.1 | 3,818 | 76,364 | 3,452 | 3,401 | 74.5 |
| 50 | 0.1 | 3,818 | 190,909 | 2,628 | 2,576 | 74.4 |
| 100 | 0.3 | 3,818 | 381,818 | 1,250 | 1,198 | 74.1 |
| 125 | 0.3 | 1,273 | 413,653 | 1,019 | 1,000 | 65.4 |
| 150 | 0.4 | 83 | 415,724 | 1,004 | 1,000 | 18.6 |
| 175 | 0.5 | 6 | 415,862 | 1,003 | 1,000 | 1.6 |
| 200 | 0.5 | 0 | 415,871 | 1,003 | 1,000 | 0.1 |
| 225 | 0.6 | 0 | 415,871 | 1,003 | 1,000 | 0.0 |
| 250 | 0.7 | 0 | 415,871 | 1,003 | 1,000 | 0.0 |
| 275 | 0.8 | 0 | 415,871 | 1,003 | 1,000 | - |
| 300 | 0.8 | 0 | 415,871 | 1,003 | 1,000 | - |
| 400 | 1.1 | 0 | 415,871 | 1,003 | 0 | - |
| 500 | 1.4 | 0 | 415,871 | 1,003 | 0 | - |
| 600 | 1.6 | 0 | 415,871 | 1,003 | 0 | - |
| 700 | 1.9 | 0 | 415,871 | 1,003 | 0 | - |
| 800 | 2.2 | 0 | 415,871 | 1,003 | 0 | - |
| 900 | 2.5 | 0 | 415,871 | 1,003 | 0 | - |
| 1000 | 2.7 | 0 | 415,871 | 1,003 | 0 | - |

Table 4.11 – Isotropic reservoir productivity with a 30 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|-------|-------|-----------|
| Days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | - |
| 1 | 0.0 | 3,818 | 3,818 | 3,973 | 3,867 | 36.0 |
| 3 | 0.0 | 3,818 | 11,455 | 3,918 | 3,807 | 34.4 |
| 5 | 0.0 | 3,818 | 19,091 | 3,863 | 3,751 | 34.0 |
| 10 | 0.0 | 3,818 | 38,182 | 3,726 | 3,613 | 33.8 |
| 15 | 0.0 | 3,818 | 57,273 | 3,589 | 3,476 | 33.7 |
| 20 | 0.1 | 3,818 | 76,364 | 3,452 | 3,338 | 33.6 |
| 35 | 0.1 | 3,818 | 133,636 | 3,040 | 2,926 | 33.6 |
| 50 | 0.1 | 3,818 | 190,909 | 2,628 | 2,514 | 33.5 |
| 75 | 0.2 | 3,818 | 286,364 | 1,939 | 1,825 | 33.5 |
| 100 | 0.3 | 3,818 | 381,818 | 1,250 | 1,135 | 33.4 |
| 125 | 0.3 | 1,171 | 411,100 | 1,038 | 1,000 | 30.9 |
| 150 | 0.4 | 163 | 415,181 | 1,008 | 1,000 | 19.4 |
| 175 | 0.5 | 24 | 415,769 | 1,004 | 1,000 | 5.7 |
| 200 | 0.5 | 4 | 415,858 | 1,003 | 1,000 | 1.0 |
| 300 | 0.8 | 0 | 415,871 | 1,003 | 1,000 | 0.0 |
| 400 | 1.1 | 0 | 415,871 | 1,003 | 1,000 | 0.0 |
| 500 | 1.4 | 0 | 415,871 | 1,003 | 0 | - |
| 600 | 1.6 | 0 | 415,871 | 1,003 | 0 | - |
| 700 | 1.9 | 0 | 415,871 | 1,003 | 0 | - |
| 800 | 2.2 | 0 | 415,871 | 1,003 | 0 | - |
| 900 | 2.5 | 0 | 415,871 | 1,003 | 0 | - |
| 1000 | 2.7 | 0 | 415,871 | 1,003 | 0 | - |

Table 4.12 – Isotropic reservoir productivity with a 4 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|-------|-------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000 | 4,000 | - |
| 1 | 0.0 | 3,818 | 3,818 | 3,973 | 3,055 | 4.16 |
| 3 | 0.0 | 3,818 | 11,455 | 3,918 | 2,756 | 3.29 |
| 5 | 0.0 | 3,818 | 19,091 | 3,863 | 2,558 | 2.93 |
| 10 | 0.0 | 3,818 | 38,182 | 3,726 | 2,233 | 2.56 |
| 15 | 0.0 | 3,818 | 57,273 | 3,589 | 1,981 | 2.37 |
| 20 | 0.1 | 3,818 | 76,364 | 3,452 | 1,768 | 2.27 |
| 35 | 0.1 | 3,818 | 133,636 | 3,040 | 1,245 | 2.13 |
| 50 | 0.1 | 3,358 | 184,013 | 2,677 | 1,000 | 2.00 |
| 75 | 0.2 | 2,317 | 241,934 | 2,260 | 1,000 | 1.84 |
| 100 | 0.3 | 1,680 | 283,929 | 1,957 | 1,000 | 1.76 |
| 125 | 0.3 | 1,241 | 314,952 | 1,733 | 1,000 | 1.69 |
| 150 | 0.4 | 927 | 338,128 | 1,566 | 1,000 | 1.64 |
| 175 | 0.5 | 699 | 355,606 | 1,439 | 1,000 | 1.59 |
| 200 | 0.5 | 531 | 368,891 | 1,343 | 1,000 | 1.55 |
| 300 | 0.8 | 190 | 397,722 | 1,135 | 1,000 | 1.41 |
| 400 | 1.1 | 74 | 408,512 | 1,057 | 1,000 | 1.29 |
| 500 | 1.4 | 30 | 412,815 | 1,026 | 1,000 | 1.16 |
| 600 | 1.6 | 13 | 414,631 | 1,013 | 1,000 | 1.02 |
| 700 | 1.9 | 5 | 415,377 | 1,007 | 1,000 | 0.73 |
| 800 | 2.2 | 2 | 415,681 | 1,005 | 1,000 | 0.43 |
| 900 | 2.5 | 1 | 415,804 | 1,004 | 1,000 | 0.21 |
| 1000 | 2.7 | 0 | 415,855 | 1,004 | 1,000 | 0.10 |

Table 4.13 – Anisotropic reservoir productivity with a 60 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|---------|---------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000.0 | 4,000.0 | - |
| 1 | 0.0 | 3,818 | 3,818 | 3,972.5 | 3,838.6 | 28.51 |
| 3 | 0.0 | 3,818 | 11,455 | 3,917.8 | 3,774.7 | 26.69 |
| 5 | 0.0 | 3,818 | 19,091 | 3,863.0 | 3,718.9 | 26.50 |
| 10 | 0.0 | 3,818 | 38,182 | 3,726.1 | 3,581.7 | 26.44 |
| 15 | 0.0 | 3,818 | 57,273 | 3,589.1 | 3,444.6 | 26.42 |
| 20 | 0.1 | 3,818 | 76,364 | 3,452.0 | 3,307.4 | 26.41 |
| 35 | 0.1 | 3,818 | 133,636 | 3,040.4 | 2,895.7 | 26.38 |
| 50 | 0.1 | 3,818 | 190,909 | 2,628.3 | 2,483.4 | 26.35 |
| 75 | 0.2 | 3,818 | 286,364 | 1,940.4 | 1,795.2 | 26.29 |
| 100 | 0.3 | 3,818 | 381,818 | 1,251.1 | 1,105.6 | 26.24 |
| 150 | 0.4 | 3,086 | 536,141 | 133.4 | 14.7 | 26.00 |
| 200 | 0.5 | 287 | 550,515 | 29.1 | 14.7 | 20.00 |
| 300 | 0.8 | 14 | 551,952 | 18.6 | 14.7 | 3.64 |
| 400 | 1.1 | 1 | 552,024 | 18.1 | 14.7 | - |
| 500 | 1.4 | 0 | 552,030 | 18.1 | 14.7 | - |
| 600 | 1.6 | 0 | 552,030 | 18.1 | 14.7 | - |
| 700 | 1.9 | 0 | 552,030 | 18.1 | 0.0 | - |
| 800 | 2.2 | 0 | 552,030 | 18.1 | 0.0 | - |
| 900 | 2.5 | 0 | 552,030 | 18.1 | 0.0 | - |
| 1000 | 2.7 | 0 | 552,030 | 18.1 | 0.0 | - |

Table 4.14 - Anisotropic reservoir productivity with a 30 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|---------|---------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000.0 | 4,000.0 | - |
| 1 | 0.0 | 3,818 | 3,818 | 3,972.6 | 3,706.7 | 14.4 |
| 3 | 0.0 | 3,818 | 11,455 | 3,917.9 | 3,634.5 | 13.5 |
| 5 | 0.0 | 3,818 | 19,091 | 3,863.1 | 3,576.9 | 13.3 |
| 10 | 0.0 | 3,818 | 38,182 | 3,726.2 | 3,438.7 | 13.3 |
| 15 | 0.0 | 3,818 | 57,273 | 3,589.2 | 3,301.0 | 13.3 |
| 20 | 0.1 | 3,818 | 76,364 | 3,452.1 | 3,163.6 | 13.2 |
| 35 | 0.1 | 3,818 | 133,636 | 3,040.5 | 2,751.4 | 13.2 |
| 50 | 0.1 | 3,818 | 190,909 | 2,628.4 | 2,338.8 | 13.2 |
| 75 | 0.2 | 3,818 | 286,364 | 1,940.5 | 1,650.2 | 13.2 |
| 100 | 0.3 | 3,818 | 381,818 | 1,251.2 | 960.3 | 13.1 |
| 150 | 0.4 | 2,818 | 522,695 | 231.1 | 14.7 | 13.0 |
| 200 | 0.5 | 484 | 546,911 | 55.4 | 14.7 | 11.9 |
| 300 | 0.8 | 46 | 551,549 | 21.7 | 14.7 | 6.6 |
| 400 | 1.1 | 4 | 551,996 | 18.5 | 14.7 | 1.2 |
| 500 | 1.4 | 0 | 552,042 | 18.1 | 14.7 | 0.1 |
| 600 | 1.6 | 0 | 552,047 | 18.1 | 14.7 | 0.0 |
| 700 | 1.9 | 0 | 552,048 | 18.1 | 14.7 | 0.0 |
| 800 | 2.2 | 0 | 552,048 | 18.1 | 14.7 | 0.0 |
| 900 | 2.5 | 0 | 552,048 | 18.1 | 14.7 | 0.0 |
| 1000 | 2.7 | 0 | 552,048 | 18.1 | 14.7 | 0.0 |

Table 4.15 – Anisotropic reservoir productivity with a 4 lateral structure

| Time | Years | Wopr | Fopt | Fpr | Wbhp | J |
|------|-------|---------|---------|---------|---------|-----------|
| days | years | stb/day | stb | psia | psia | stbd/psia |
| 0 | 0.0 | 0 | 0 | 4,000.0 | 4,000.0 | - |
| 1 | 0.0 | 3,818 | 3,818 | 3,973.5 | 2,341.4 | 2.34 |
| 3 | 0.0 | 3,818 | 11,455 | 3,918.9 | 1,993.4 | 1.98 |
| 5 | 0.0 | 3,818 | 19,091 | 3,864.2 | 1,817.9 | 1.87 |
| 10 | 0.0 | 3,818 | 38,182 | 3,727.3 | 1,528.4 | 1.74 |
| 15 | 0.0 | 3,818 | 57,273 | 3,590.4 | 1,285.4 | 1.66 |
| 20 | 0.1 | 3,818 | 76,364 | 3,453.3 | 1,064.4 | 1.60 |
| 35 | 0.1 | 3,818 | 133,636 | 3,041.5 | 477.6 | 1.49 |
| 50 | 0.1 | 3,701 | 189,159 | 2,641.8 | 14.7 | 1.41 |
| 75 | 0.2 | 2,701 | 256,694 | 2,154.9 | 14.7 | 1.26 |
| 100 | 0.3 | 2,072 | 308,502 | 1,781.0 | 14.7 | 1.17 |
| 150 | 0.4 | 1,385 | 377,756 | 1,280.7 | 14.7 | 1.09 |
| 200 | 0.5 | 965 | 426,017 | 931.6 | 14.7 | 1.05 |
| 300 | 0.8 | 539 | 479,945 | 541.1 | 14.7 | 1.02 |
| 400 | 1.1 | 307 | 510,631 | 318.6 | 14.7 | 1.01 |
| 500 | 1.4 | 176 | 528,219 | 191.1 | 14.7 | 1.00 |
| 600 | 1.6 | 101 | 538,329 | 117.7 | 14.7 | 0.98 |
| 700 | 1.9 | 58 | 544,147 | 75.4 | 14.7 | 0.96 |
| 800 | 2.2 | 34 | 547,498 | 51.1 | 14.7 | 0.92 |
| 900 | 2.5 | 19 | 549,427 | 37.1 | 14.7 | 0.86 |
| 1000 | 2.7 | 11 | 550,539 | 29.1 | 14.7 | 0.77 |

4.4.3 Grid Refinement

The most common technique to establish the numerical accuracy of simulation results is to perform grid refinement. The base case comprises a grid of $21 \times 62 \times 11$. We have refined the grid by a factor of 2 both in each of the directions X and Z, individually as well as simultaneously, so that the biggest case simulated is $81 \times 62 \times 41$. The results shown in Table 4.16 are obtained for the case of 60 and 30 laterals only. Also only the anisotropic reservoir case is refined to determine the accuracy. The following table summarizes the results of grid refinement. A comparison of the PI for the base case and the refined cases indicates a good validation of the results obtained from the base case simulations. As mentioned earlier these results are obtained for an anisotropic reservoir with permeability in the three directions given as (1.0, 1.0, 0.1) md.

Table 4.16 – Results showing numerical consistency with grid refinement

| Grid Structure | Number of Laterals | Productivity Index, J |
|---------------------------|---------------------------|------------------------------|
| A. Base Case | | |
| $21 \times 62 \times 11$ | 60 | 26.2447 |
| | 30 | 13.1281 |
| B. Grid Refinement | | |
| Z - Direction: | | |
| $21 \times 62 \times 21$ | 60 | 23.9285 |
| | 30 | 11.936 |
| X - Direction: | | |
| $41 \times 62 \times 11$ | 60 | 23.5568 |
| | 30 | 11.7413 |
| X & Z - Direction: | | |
| $41 \times 62 \times 21$ | 60 | 23.6054 |
| | 30 | 11.7428 |
| $81 \times 62 \times 41$ | 60 | 23.429 |
| | 30 | 11.6357 |

CHAPTER V

FIELD CASE SIMULATION AND ANALYSIS

5.1 Data for El Furrial Field

El Furrial is an onshore field, located in the North of Monagas basin in Eastern Venezuela. It is conformed of three major reservoirs, Naricual Superior, Naricual Inferior and Cretaceous-01, all of them totaling approximately 6 billion barrels of oil in place. The lowest one, **Cretaceous-01 Reservoir** area is approximately 18 Km². Well Ful-04 discovered this reservoir in 1987 with an initial production of 4,000 BOPD 26°API oil with a ½” production choke. Figure 5.1 shows the location of the field.

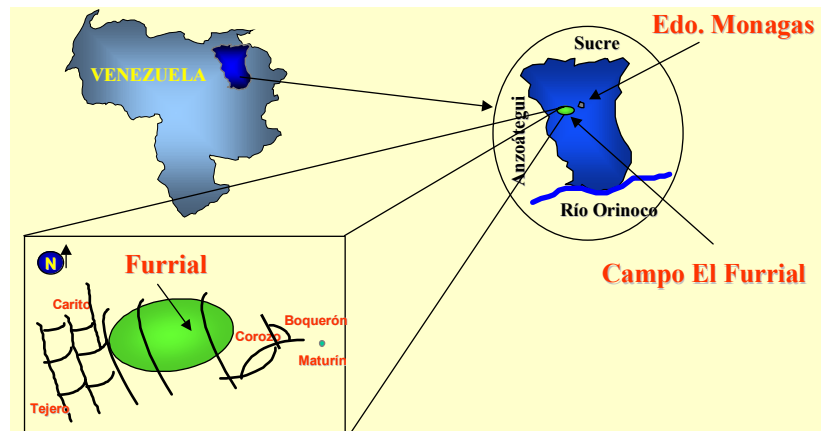


Figure 5.1 – El Furrial field location

Structural model (Figure 5.2) reveals fault-driven asymmetric anticline, NE-SW oriented. Structure is affected by several axial transversal faults. Fault throws are not greater than 500 ft. Also, NE-SW preferentially oriented normal faults were identified.

NO

SE

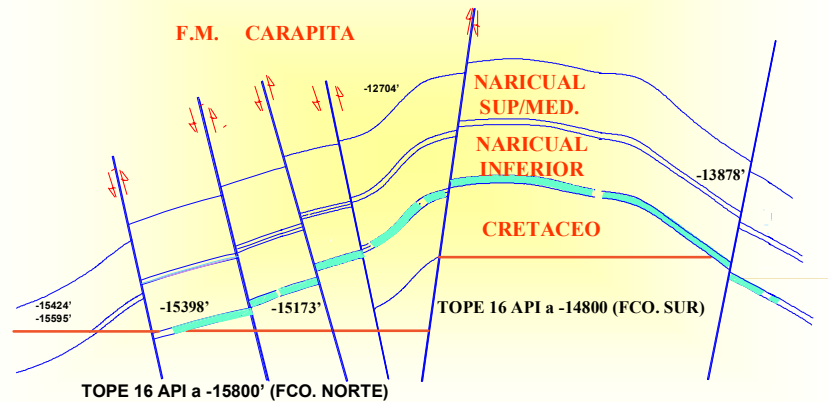


Figure 5.2 – Structural model of El Furrial

Fluid column characterization showed depth variations on thermodynamic and chemical properties, associated to gravity drainage process of the heavy components of the crude, which originated heavy crude formation and tar mat.

The main reservoir characteristics are summarized in Table 5.1

Table 5.1 – Reservoir characteristics of El Furrial

| Porosity | Net ht (ft) | S_w | A | B_o (rb/stb) | μ_o (cp) | k (md) | pi(psia) |
|----------|----------------|--------|--------------------|-------------------|--------------|--------|----------|
| 9-15% | 200-800 | 19-24% | 18 km ² | 1.5 | 0.5-0.6 | 10-80 | 11,200 |

5.2 Representative Unit

To simulate the field we will consider a representation of the Cretaceous Reservoir that is simplified in many senses, but still contains the main formation characteristics and basic fluid properties. Our goal is to make the reservoir model as simple as possible, but capture all the major factors responsible for the performance differences between traditional and the suggested advanced well architecture. In the representative unit we assume $x_e = 20,000$ ft; $y_e = 10,000$ ft and $h = 750$ ft.

The permeability field is anisotropic. The two horizontal permeabilities are:

$$k_x = 86.6 \text{ md}$$

$$k_y = 28.7 \text{ md}$$

and the vertical permeability is

$$k_z = 2.6 \text{ md}$$

Note the large permeability contrast between horizontal and vertical.

The porosity is 0.12, providing the oil in place. The PVT properties of the fluids are given in Table 5.2

Table 5.2 – El Furrial fluid PVT properties

| P | R_s | B_o | μ |
|------|---------|--------|-------|
| Psia | mcf/stb | rb/stb | Cp |
| 500 | 0.054 | 1.045 | 7666 |
| 714 | 0.055 | 1.047 | 7366 |
| 1428 | 0.125 | 1.080 | 1251 |
| 2142 | 0.215 | 1.124 | 212 |
| 2857 | 0.335 | 1.185 | 36 |
| 3571 | 0.502 | 1.273 | 6 |
| 4285 | 0.753 | 1.409 | 1.04 |
| 4642 | 0.933 | 1.508 | 0.43 |
| 5000 | 1.172 | 1.640 | 0.17 |

Table 5.3 shows the variation of solution gas oil ratio with depth. It can be seen

from the data that gas volume decreases by a couple of order magnitudes within a few 1000 ft. Due to this rapid change the oil viscosity increases rapidly with depth.

Table 5.3 – Solution GOR vs. depth

| Depth, ft | R_s (mcf/stb) |
|-----------|-----------------|
| 12000 | 1.145 |
| 14350 | 0.874 |
| 14646 | 0.747 |
| 14700 | 0.619 |
| 14800 | 0.538 |
| 14880 | 0.330 |
| 14960 | 0.244 |
| 15000 | 0.055 |
| 16500 | 0.055 |

Thus from the PVT and Solution GOR data we can see that there exist a very high contrast in mobility in the reservoir. Figure 5.3 and 5.4 shows the change in Solution GOR and Viscosity with pressure. The bar charts show the sharp change in properties with decrease in pressure. The variation of solution GOR and viscosity with depth in the reservoir is shown in Figures 5.5 and Figure 5.6 respectively.

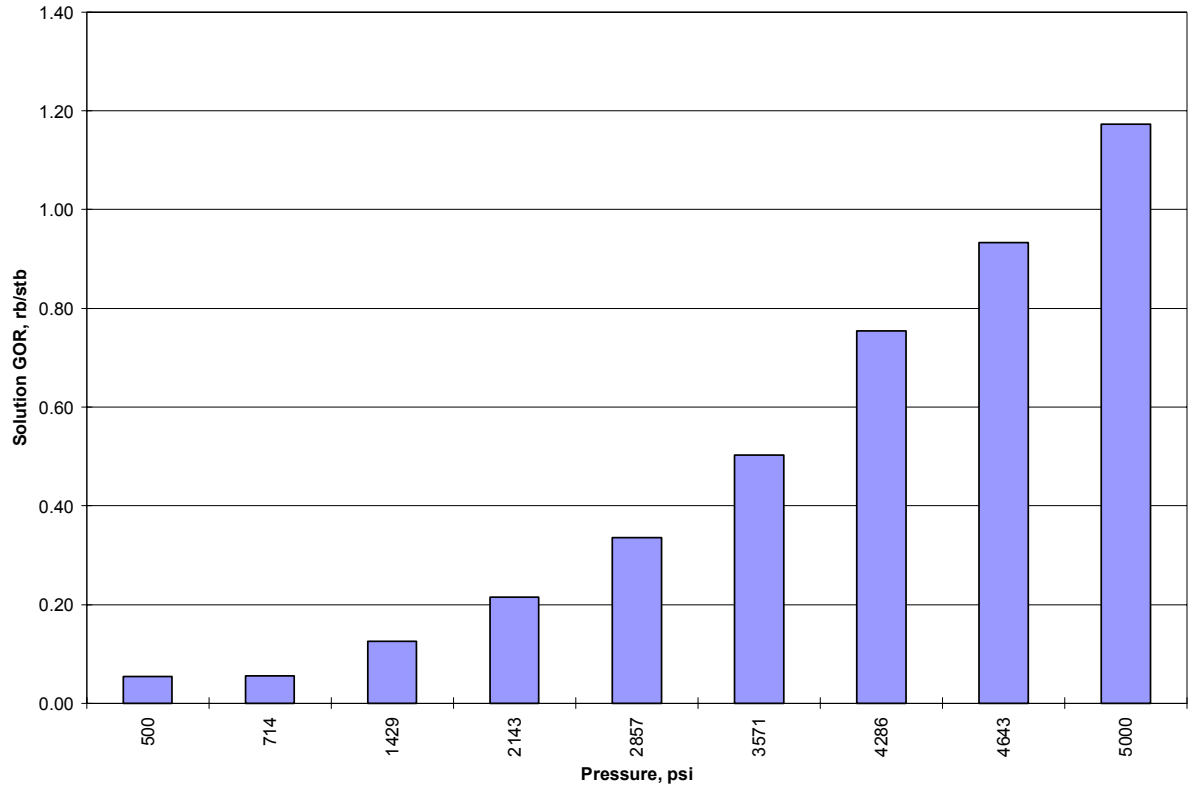


Figure 5.3– Variation of solution GOR with pressure

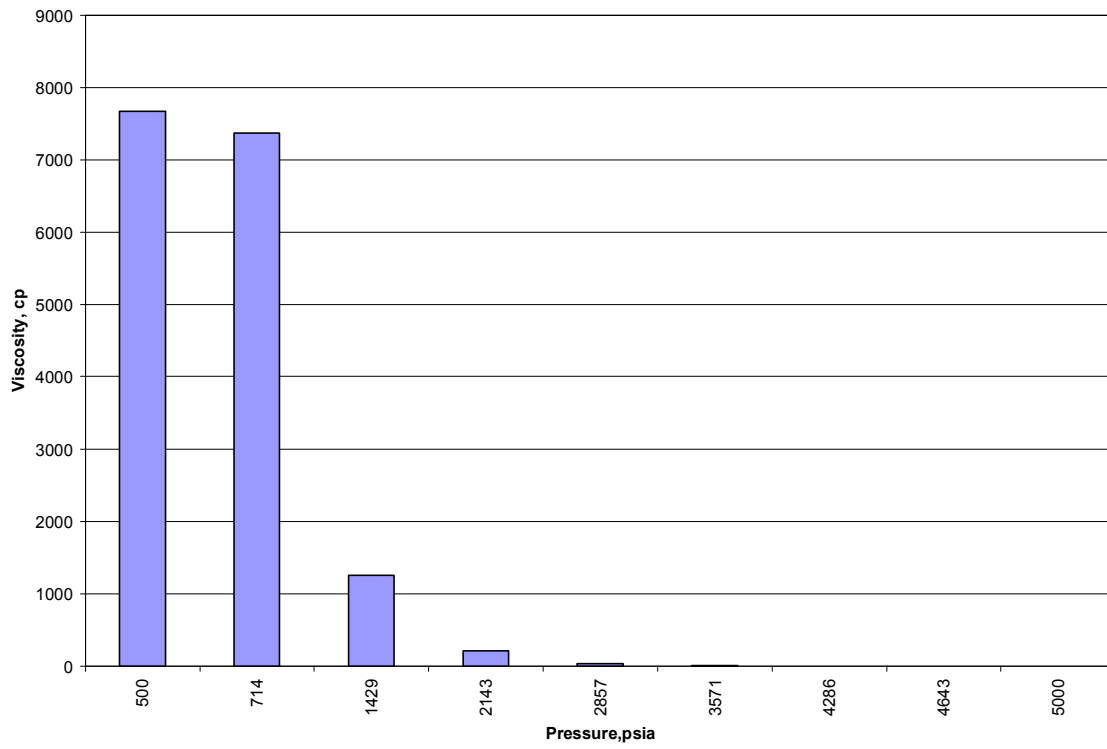


Figure 5.4– Variation of viscosity with pressure

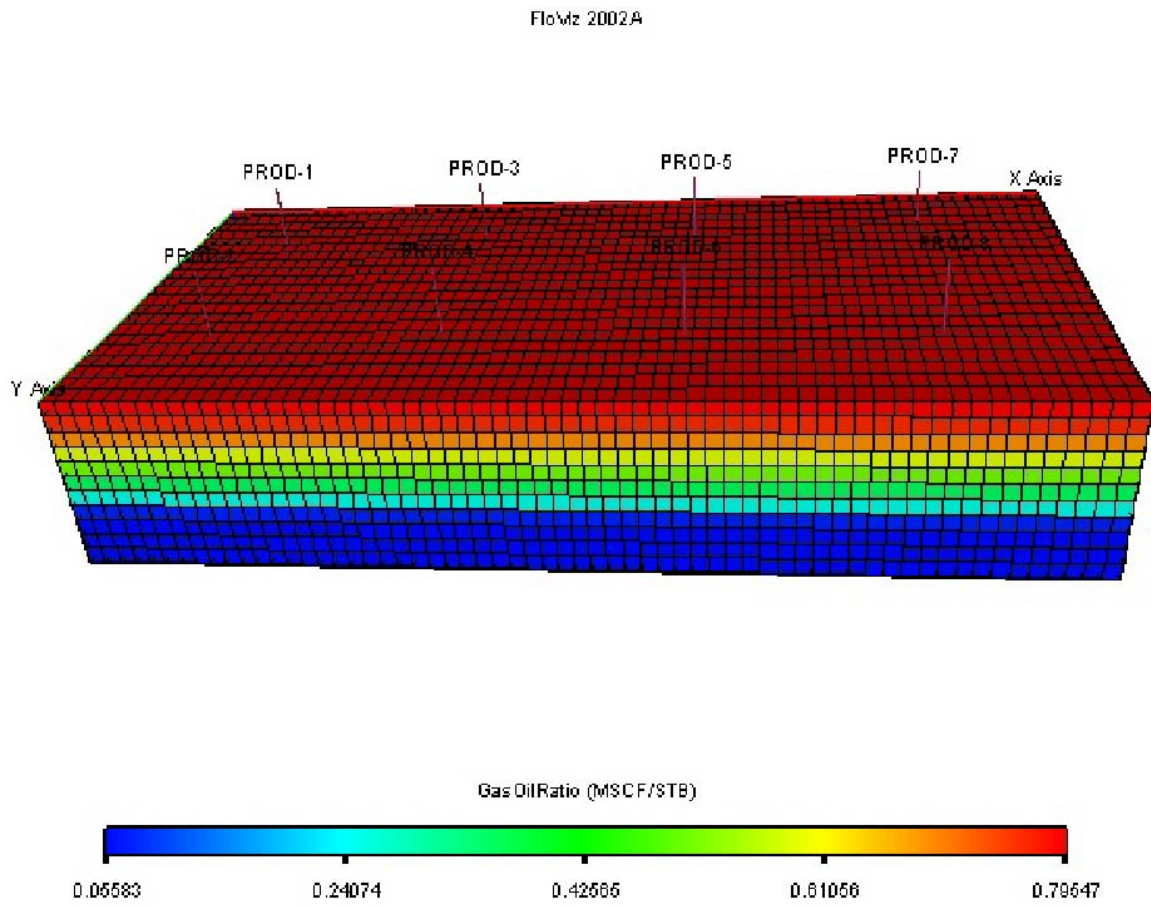


Figure 5.5– Variation of solution GOR with depth

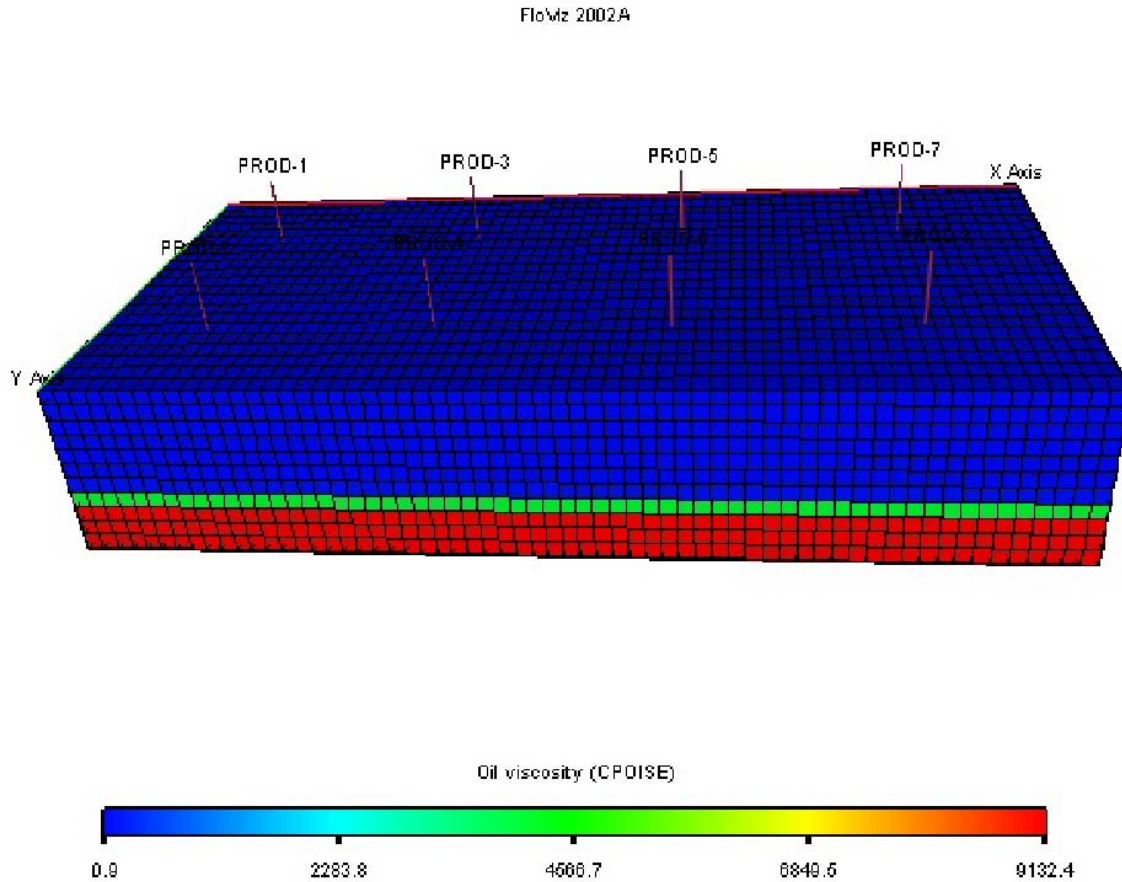


Figure 5.6 – Variation of viscosity with depth

5.3 Base Case

The basis for all comparisons is the drainage strategy of vertical wells drilled on a 1 square mile spacing basis. Hence the base case contains 8 fully penetrating vertical wells, each with equal drainage areas.

5.4 ML Well Architecture and Simulation Cases

As in all the previous ML well cases studied here too we consider the horizontal mother bore with laterals connected to drain the reservoir. However the main problem here is that of determining the location of the mother bore on account of the rapid change in properties of the fluids with depth. Hence the issue is that of optimizing the mother

bore lateral in addition to determining the optimum lateral density and penetration ratio. We assume that the laterals are 100% penetrating when they extend from the mother bore to the lateral boundary. Penetration ratio (the extent of penetration) is an important design parameter to be neglected. Taking into account all of these variable the following cases have been simulated. The cases designed are described as the location of the horizontal mother bore, number of laterals and finally the penetration ratio.

Case A – Mother bore: 375 ft from top; 15 horizontal legs; Penetration: 100 %

Case B – Mother bore: 239 ft from top; 15 horizontal legs; Penetration: 100 %

Case C – Mother bore: 239 ft from top; 15 horizontal legs; Penetration: 67 %

Case D – Mother bore: 239 ft from top; 8 horizontal legs; Penetration: 100 %

Case E – Mother bore: 239 ft from top; 8 horizontal legs; penetration: 100 %

Figure 5.7 shows a general representation of the cases simulated

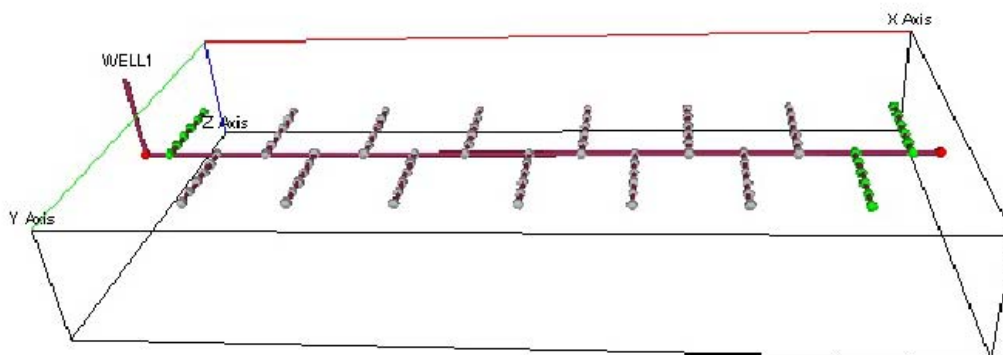


Figure 5.7 – General ML well architecture used for simulation

5.5 Simulation Results

The results of the simulation are presented in this section in Tables 5.4-5.9. The time over which the simulation is run is three years. An example input data file for the advanced well architecture case has been attached in the APPENDIX B for reference. For the economic evaluation of the technology the cumulative production is an important parameter.

Table 5.4 – Base case results (8 vertical wells)

| Base Case: 8 Vertical wells | | | | | | | |
|------------------------------------|-----------|-------|--------|--------|------------|--------|--------|
| Time | Field Pr. | W1 | W1 cum | W1 bhp | ΔP | Np Cum | Gp Cum |
| Days | psia | stbd | MMstb | psia | psi | MMstb | Bscf |
| 0 | 11,204 | 0 | 0.00 | 11,077 | 128 | 0.0 | 0.0 |
| 30 | 11,179 | 4,500 | 0.14 | 10,491 | 688 | 1.1 | 0.8 |
| 60 | 11,154 | 4,500 | 0.27 | 10,438 | 717 | 2.2 | 1.6 |
| 90 | 11,129 | 4,500 | 0.41 | 10,390 | 739 | 3.2 | 2.3 |
| 120 | 11,104 | 4,500 | 0.54 | 10,346 | 758 | 4.3 | 3.1 |
| 150 | 11,079 | 4,500 | 0.68 | 10,303 | 777 | 5.4 | 3.9 |
| 180 | 11,054 | 4,500 | 0.81 | 10,260 | 794 | 6.5 | 4.6 |
| 210 | 11,032 | 3,900 | 0.93 | 10,312 | 720 | 7.4 | 5.3 |
| 240 | 11,011 | 3,900 | 1.04 | 10,279 | 732 | 8.4 | 6.0 |
| 270 | 10,989 | 3,900 | 1.16 | 10,244 | 744 | 9.3 | 6.7 |
| 300 | 10,967 | 3,900 | 1.28 | 10,210 | 757 | 10.2 | 7.3 |
| 330 | 10,945 | 3,900 | 1.40 | 10,175 | 771 | 11.2 | 8.0 |
| 360 | 10,923 | 3,900 | 1.51 | 10,140 | 784 | 12.1 | 8.7 |
| 390 | 10,904 | 3,500 | 1.62 | 10,168 | 736 | 12.9 | 9.3 |
| 420 | 10,884 | 3,500 | 1.72 | 10,139 | 745 | 13.8 | 9.9 |
| 450 | 10,865 | 3,500 | 1.83 | 10,109 | 756 | 14.6 | 10.5 |
| 480 | 10,845 | 3,500 | 1.93 | 10,078 | 767 | 15.5 | 11.1 |
| 510 | 10,826 | 3,500 | 2.04 | 10,047 | 778 | 16.3 | 11.7 |
| 540 | 10,806 | 3,500 | 2.14 | 10,017 | 789 | 17.1 | 12.3 |
| 570 | 10,789 | 3,100 | 2.24 | 10,049 | 739 | 17.9 | 12.8 |
| 600 | 10,771 | 3,100 | 2.33 | 10,024 | 747 | 18.6 | 13.3 |
| 630 | 10,754 | 3,100 | 2.42 | 9,998 | 755 | 19.4 | 13.9 |
| 660 | 10,736 | 3,100 | 2.51 | 9,972 | 765 | 20.1 | 14.4 |
| 690 | 10,719 | 3,100 | 2.61 | 9,945 | 774 | 20.9 | 14.9 |
| 720 | 10,702 | 3,100 | 2.70 | 9,919 | 783 | 21.6 | 15.4 |
| 750 | 10,686 | 2,800 | 2.78 | 9,940 | 746 | 22.3 | 15.9 |
| 780 | 10,670 | 2,800 | 2.87 | 9,917 | 753 | 22.9 | 16.4 |
| 810 | 10,654 | 2,800 | 2.95 | 9,894 | 760 | 23.6 | 16.9 |
| 840 | 10,639 | 2,800 | 3.04 | 9,870 | 768 | 24.3 | 17.4 |
| 870 | 10,623 | 2,800 | 3.12 | 9,847 | 776 | 25.0 | 17.8 |
| 900 | 10,607 | 2,800 | 3.20 | 9,823 | 784 | 25.6 | 18.3 |
| 930 | 10,592 | 2,600 | 3.28 | 9,831 | 761 | 26.3 | 18.8 |
| 960 | 10,578 | 2,600 | 3.36 | 9,810 | 767 | 26.9 | 19.2 |
| 990 | 10,563 | 2,600 | 3.44 | 9,789 | 774 | 27.5 | 19.7 |
| 1020 | 10,549 | 2,600 | 3.52 | 9,767 | 781 | 28.1 | 20.1 |
| 1050 | 10,534 | 2,600 | 3.59 | 9,746 | 788 | 28.8 | 20.6 |
| 1080 | 10,519 | 2,600 | 3.67 | 9,724 | 795 | 29.4 | 21.0 |

Table 5.5 – Case A results

| Case A - Motherbore 375 ft from top;15 horizontal laterals;100% | | | | | | | |
|--|-----------|--------|-------|--------|------------|--------|--------|
| Time | Field Pr. | W | W cum | W BHP | ΔP | Np Cum | Gp Cum |
| Days | psia | Stbd | MMstb | psia | psi | MMstb | Bscf |
| 0 | 11,204 | 0 | 0.0 | 11,200 | 4.5 | 0.0 | 0.0 |
| 30 | 11,185 | 33,000 | 1.0 | 10,411 | 773.8 | 1.0 | 0.4 |
| 60 | 11,165 | 33,000 | 2.0 | 10,386 | 779.5 | 2.0 | 0.7 |
| 90 | 11,146 | 33,000 | 3.0 | 10,363 | 782.2 | 3.0 | 1.1 |
| 120 | 11,126 | 33,000 | 4.0 | 10,342 | 784.0 | 4.0 | 1.4 |
| 150 | 11,106 | 33,000 | 5.0 | 10,321 | 785.4 | 5.0 | 1.8 |
| 180 | 11,087 | 33,000 | 5.9 | 10,300 | 786.6 | 5.9 | 2.2 |
| 210 | 11,067 | 33,000 | 6.9 | 10,279 | 787.8 | 6.9 | 2.5 |
| 240 | 11,047 | 33,000 | 7.9 | 10,258 | 789.1 | 7.9 | 2.9 |
| 270 | 11,027 | 33,000 | 8.9 | 10,237 | 790.7 | 8.9 | 3.3 |
| 300 | 11,008 | 33,000 | 9.9 | 10,215 | 792.5 | 9.9 | 3.6 |
| 330 | 10,988 | 33,000 | 10.9 | 10,193 | 794.5 | 10.9 | 4.0 |
| 360 | 10,968 | 33,000 | 11.9 | 10,171 | 796.9 | 11.9 | 4.4 |
| 390 | 10,949 | 32,000 | 12.8 | 10,168 | 781.0 | 12.8 | 4.7 |
| 420 | 10,930 | 32,000 | 13.8 | 10,146 | 783.3 | 13.8 | 5.1 |
| 450 | 10,910 | 32,000 | 14.8 | 10,124 | 786.2 | 14.8 | 5.5 |
| 480 | 10,891 | 32,000 | 15.7 | 10,101 | 789.4 | 15.7 | 5.9 |
| 510 | 10,872 | 32,000 | 16.7 | 10,079 | 793.0 | 16.7 | 6.2 |
| 540 | 10,852 | 32,000 | 17.6 | 10,055 | 796.8 | 17.6 | 6.6 |
| 570 | 10,834 | 30,000 | 18.5 | 10,067 | 766.8 | 18.5 | 7.0 |
| 600 | 10,816 | 30,000 | 19.4 | 10,046 | 769.6 | 19.4 | 7.3 |
| 630 | 10,797 | 30,000 | 20.3 | 10,024 | 773.2 | 20.3 | 7.7 |
| 660 | 10,779 | 30,000 | 21.2 | 10,002 | 777.3 | 21.2 | 8.0 |
| 690 | 10,761 | 30,000 | 22.1 | 9,979 | 781.7 | 22.1 | 8.4 |
| 720 | 10,743 | 30,000 | 23.0 | 9,956 | 786.3 | 23.0 | 8.8 |
| 750 | 10,725 | 29,000 | 23.9 | 9,950 | 775.1 | 23.9 | 9.1 |
| 780 | 10,707 | 29,000 | 24.8 | 9,928 | 779.3 | 24.8 | 9.5 |
| 810 | 10,689 | 29,000 | 25.7 | 9,905 | 784.0 | 25.7 | 9.8 |
| 840 | 10,672 | 29,000 | 26.5 | 9,883 | 788.9 | 26.5 | 10.2 |
| 870 | 10,654 | 29,000 | 27.4 | 9,860 | 794.0 | 27.4 | 10.5 |
| 900 | 10,636 | 29,000 | 28.3 | 9,837 | 799.4 | 28.3 | 10.9 |
| 930 | 10,620 | 27,000 | 29.1 | 9,845 | 774.5 | 29.1 | 11.2 |
| 960 | 10,603 | 27,000 | 29.9 | 9,825 | 778.3 | 29.9 | 11.5 |
| 990 | 10,586 | 27,000 | 30.7 | 9,803 | 782.8 | 30.7 | 11.9 |
| 1020 | 10,570 | 27,000 | 31.5 | 9,782 | 787.7 | 31.5 | 12.2 |
| 1050 | 10,553 | 27,000 | 32.3 | 9,760 | 792.8 | 32.3 | 12.5 |
| 1080 | 10,536 | 27,000 | 33.1 | 9,738 | 798.0 | 33.1 | 12.9 |

Table 5.6 – Case B results

| Case B - Mother bore 239 ft from top; 15 horizontal laterals;100% | | | | | | | |
|--|-----------|--------|-------|--------|------------|--------|--------|
| Time | Field Pr. | W | W cum | W BHP | ΔP | Np Cum | Gp Cum |
| Days | psia | Stbd | MMstb | psia | psia | MMstb | Bscf |
| 0 | 11,204 | 0 | 0.00 | 11,149 | 55 | 0.00 | 0.00 |
| 30 | 11,163 | 63,000 | 1.89 | 10,802 | 360 | 1.89 | 1.11 |
| 60 | 11,121 | 63,000 | 3.78 | 10,729 | 392 | 3.78 | 2.23 |
| 90 | 11,080 | 63,000 | 5.67 | 10,659 | 421 | 5.67 | 3.35 |
| 120 | 11,038 | 63,000 | 7.56 | 10,590 | 448 | 7.56 | 4.47 |
| 150 | 10,996 | 63,000 | 9.45 | 10,523 | 474 | 9.45 | 5.60 |
| 180 | 10,955 | 63,000 | 11.34 | 10,456 | 499 | 11.30 | 6.73 |
| 210 | 10,915 | 60,000 | 13.14 | 10,414 | 501 | 13.10 | 7.80 |
| 240 | 10,875 | 60,000 | 14.94 | 10,352 | 523 | 14.90 | 8.88 |
| 270 | 10,835 | 60,000 | 16.74 | 10,290 | 545 | 16.70 | 9.96 |
| 300 | 10,795 | 60,000 | 18.54 | 10,227 | 568 | 18.50 | 11.00 |
| 330 | 10,755 | 60,000 | 20.34 | 10,165 | 590 | 20.30 | 12.10 |
| 360 | 10,715 | 60,000 | 22.14 | 10,103 | 612 | 22.10 | 13.20 |
| 390 | 10,677 | 57,000 | 23.85 | 10,065 | 612 | 23.90 | 14.20 |
| 420 | 10,639 | 57,000 | 25.56 | 10,006 | 632 | 25.60 | 15.30 |
| 450 | 10,600 | 57,000 | 27.27 | 9,948 | 653 | 27.30 | 16.30 |
| 480 | 10,562 | 57,000 | 28.98 | 9,889 | 673 | 29.00 | 17.30 |
| 510 | 10,524 | 57,000 | 30.69 | 9,830 | 694 | 30.70 | 18.40 |
| 540 | 10,485 | 57,000 | 32.40 | 9,771 | 714 | 32.40 | 19.40 |
| 570 | 10,448 | 55,000 | 34.05 | 9,728 | 721 | 34.10 | 20.40 |
| 600 | 10,411 | 55,000 | 35.70 | 9,671 | 740 | 35.70 | 21.40 |
| 630 | 10,374 | 55,000 | 37.35 | 9,614 | 759 | 37.40 | 22.40 |
| 660 | 10,337 | 55,000 | 39.00 | 9,558 | 779 | 39.00 | 23.40 |
| 690 | 10,299 | 55,000 | 40.65 | 9,501 | 798 | 40.70 | 24.40 |
| 720 | 10,262 | 55,000 | 42.30 | 9,444 | 818 | 42.30 | 25.40 |
| 750 | 10,236 | 38,000 | 43.44 | 9,508 | 728 | 43.40 | 26.10 |
| 780 | 10,210 | 38,000 | 44.58 | 9,472 | 738 | 44.60 | 26.80 |
| 810 | 10,184 | 38,000 | 45.72 | 9,435 | 749 | 45.70 | 27.50 |
| 840 | 10,158 | 38,000 | 46.86 | 9,398 | 760 | 46.90 | 28.20 |
| 870 | 10,132 | 38,000 | 48.00 | 9,360 | 772 | 48.00 | 28.90 |
| 900 | 10,106 | 38,000 | 49.14 | 9,322 | 784 | 49.10 | 29.60 |
| 930 | 10,085 | 30,000 | 50.04 | 9,334 | 752 | 50.00 | 30.20 |
| 960 | 10,065 | 30,000 | 50.94 | 9,306 | 759 | 50.90 | 30.70 |
| 990 | 10,044 | 30,000 | 51.84 | 9,277 | 768 | 51.80 | 31.30 |
| 1020 | 10,024 | 30,000 | 52.74 | 9,248 | 776 | 52.70 | 31.80 |
| 1050 | 10,003 | 30,000 | 53.64 | 9,218 | 785 | 53.60 | 32.40 |
| 1080 | 9,983 | 30,000 | 54.54 | 9,189 | 794 | 54.50 | 32.90 |

Table 5.7 – Case C results

| Case C - Mother Bore 239 ft from top; 15 horizontal laterals; 67% Penetration | | | | | | | |
|--|-----------|--------|-------|--------|------------|--------|--------|
| Time | Field Pr. | W | W cum | W BHP | ΔP | Np Cum | Gp Cum |
| Days | psia | Stbd | stb | psia | psia | MMstb | Bscf |
| 0 | 11,205 | 0 | 0.00 | 11,149 | 55 | 0.00 | 0.00 |
| 30 | 11,163 | 63,000 | 1.89 | 10,645 | 518 | 1.89 | 1.12 |
| 60 | 11,121 | 63,000 | 3.78 | 10,553 | 568 | 3.78 | 2.24 |
| 90 | 11,080 | 63,000 | 5.67 | 10,472 | 607 | 5.67 | 3.36 |
| 120 | 11,038 | 63,000 | 7.56 | 10,398 | 640 | 7.56 | 4.50 |
| 150 | 10,996 | 63,000 | 9.45 | 10,327 | 669 | 9.45 | 5.63 |
| 180 | 10,954 | 63,000 | 11.34 | 10,258 | 696 | 11.30 | 6.77 |
| 210 | 10,915 | 59,000 | 13.11 | 10,231 | 684 | 13.10 | 7.84 |
| 240 | 10,876 | 59,000 | 14.88 | 10,171 | 705 | 14.90 | 8.92 |
| 270 | 10,836 | 59,000 | 16.65 | 10,110 | 726 | 16.70 | 9.99 |
| 300 | 10,797 | 59,000 | 18.42 | 10,049 | 747 | 18.40 | 11.10 |
| 330 | 10,757 | 59,000 | 20.19 | 9,989 | 768 | 20.20 | 12.20 |
| 360 | 10,717 | 59,000 | 21.96 | 9,928 | 790 | 22.00 | 13.20 |
| 390 | 10,685 | 49,000 | 23.43 | 9,962 | 723 | 23.40 | 14.10 |
| 420 | 10,652 | 49,000 | 24.90 | 9,917 | 735 | 24.90 | 15.00 |
| 450 | 10,619 | 49,000 | 26.37 | 9,869 | 749 | 26.40 | 16.00 |
| 480 | 10,586 | 49,000 | 27.84 | 9,821 | 764 | 27.80 | 16.90 |
| 510 | 10,552 | 49,000 | 29.31 | 9,772 | 780 | 29.30 | 17.80 |
| 540 | 10,519 | 49,000 | 30.78 | 9,722 | 797 | 30.80 | 18.70 |
| 570 | 10,492 | 40,000 | 31.98 | 9,752 | 740 | 32.00 | 19.40 |
| 600 | 10,465 | 40,000 | 33.18 | 9,717 | 748 | 33.20 | 20.20 |
| 630 | 10,438 | 40,000 | 34.38 | 9,679 | 759 | 34.40 | 20.90 |
| 660 | 10,411 | 40,000 | 35.58 | 9,640 | 770 | 35.60 | 21.70 |
| 690 | 10,383 | 40,000 | 36.78 | 9,601 | 783 | 36.80 | 22.40 |
| 720 | 10,356 | 40,000 | 37.98 | 9,561 | 795 | 38.00 | 23.10 |
| 750 | 10,334 | 32,000 | 38.94 | 9,587 | 747 | 38.90 | 23.70 |
| 780 | 10,313 | 32,000 | 39.90 | 9,560 | 753 | 39.90 | 24.30 |
| 810 | 10,291 | 32,000 | 40.86 | 9,530 | 760 | 40.90 | 24.90 |
| 840 | 10,269 | 32,000 | 41.82 | 9,500 | 769 | 41.80 | 25.50 |
| 870 | 10,247 | 32,000 | 42.78 | 9,469 | 778 | 42.80 | 26.10 |
| 900 | 10,225 | 32,000 | 43.74 | 9,437 | 788 | 43.70 | 26.70 |
| 930 | 10,206 | 27,000 | 44.55 | 9,445 | 761 | 44.60 | 27.20 |
| 960 | 10,188 | 27,000 | 45.36 | 9,421 | 766 | 45.40 | 27.80 |
| 990 | 10,169 | 27,000 | 46.17 | 9,396 | 773 | 46.20 | 28.30 |
| 1020 | 10,151 | 27,000 | 46.98 | 9,371 | 780 | 47.00 | 28.80 |
| 1050 | 10,132 | 27,000 | 47.79 | 9,345 | 787 | 47.80 | 29.30 |
| 1080 | 10,114 | 27,000 | 48.60 | 9,318 | 795 | 48.60 | 29.80 |

Table 5.8 – Case D results

| Case D - Mother bore 239 ft from top; 8 horizontal laterals; 100% penetration | | | | | | | |
|--|-----------|--------|-------|--------|------------|--------|--------|
| Time | Field Pr. | W | W cum | W BHP | ΔP | Np Cum | Gp Cum |
| Days | psia | Stbd | MMstb | psia | Psia | MMstb | Bscf |
| 0 | 11,204 | 0 | 0.00 | 11,149 | 55 | 0.00 | 0.00 |
| 30 | 11,163 | 62,000 | 1.86 | 10,505 | 659 | 1.86 | 1.10 |
| 60 | 11,122 | 62,000 | 3.72 | 10,433 | 690 | 3.72 | 2.20 |
| 90 | 11,082 | 62,000 | 5.58 | 10,365 | 717 | 5.58 | 3.31 |
| 120 | 11,040 | 62,000 | 7.44 | 10,299 | 742 | 7.44 | 4.43 |
| 150 | 10,999 | 62,000 | 9.30 | 10,233 | 766 | 9.30 | 5.55 |
| 180 | 10,958 | 62,000 | 11.16 | 10,169 | 789 | 11.20 | 6.67 |
| 210 | 10,922 | 54,000 | 12.78 | 10,221 | 701 | 12.80 | 7.65 |
| 240 | 10,886 | 54,000 | 14.40 | 10,167 | 719 | 14.40 | 8.63 |
| 270 | 10,850 | 54,000 | 16.02 | 10,113 | 737 | 16.00 | 9.62 |
| 300 | 10,814 | 54,000 | 17.64 | 10,058 | 756 | 17.60 | 10.60 |
| 330 | 10,778 | 54,000 | 19.26 | 10,003 | 775 | 19.30 | 11.60 |
| 360 | 10,742 | 54,000 | 20.88 | 9,947 | 794 | 20.90 | 12.60 |
| 390 | 10,711 | 46,000 | 22.26 | 9,999 | 712 | 22.30 | 13.40 |
| 420 | 10,680 | 46,000 | 23.64 | 9,954 | 726 | 23.60 | 14.30 |
| 450 | 10,649 | 46,000 | 25.02 | 9,907 | 741 | 25.00 | 15.10 |
| 480 | 10,618 | 46,000 | 26.40 | 9,861 | 757 | 26.40 | 16.00 |
| 510 | 10,587 | 46,000 | 27.78 | 9,814 | 773 | 27.80 | 16.80 |
| 540 | 10,556 | 46,000 | 29.16 | 9,767 | 788 | 29.20 | 17.70 |
| 570 | 10,529 | 40,000 | 30.36 | 9,794 | 735 | 30.40 | 18.40 |
| 600 | 10,501 | 40,000 | 31.56 | 9,755 | 747 | 31.60 | 19.20 |
| 630 | 10,474 | 40,000 | 32.76 | 9,715 | 760 | 32.80 | 19.90 |
| 660 | 10,447 | 40,000 | 33.96 | 9,674 | 773 | 34.00 | 20.70 |
| 690 | 10,420 | 40,000 | 35.16 | 9,634 | 786 | 35.20 | 21.40 |
| 720 | 10,393 | 40,000 | 36.36 | 9,593 | 800 | 36.40 | 22.20 |
| 750 | 10,370 | 33,000 | 37.35 | 9,632 | 738 | 37.40 | 22.80 |
| 780 | 10,348 | 33,000 | 38.34 | 9,600 | 747 | 38.30 | 23.40 |
| 810 | 10,325 | 33,000 | 39.33 | 9,568 | 757 | 39.30 | 24.00 |
| 840 | 10,303 | 33,000 | 40.32 | 9,535 | 768 | 40.30 | 24.60 |
| 870 | 10,280 | 33,000 | 41.31 | 9,502 | 778 | 41.30 | 25.30 |
| 900 | 10,257 | 33,000 | 42.30 | 9,469 | 789 | 42.30 | 25.90 |
| 930 | 10,238 | 28,000 | 43.14 | 9,488 | 750 | 43.10 | 26.40 |
| 960 | 10,219 | 28,000 | 43.98 | 9,461 | 758 | 44.00 | 26.90 |
| 990 | 10,200 | 28,000 | 44.82 | 9,434 | 766 | 44.80 | 27.50 |
| 1020 | 10,180 | 28,000 | 45.66 | 9,406 | 774 | 45.70 | 28.00 |
| 1050 | 10,161 | 28,000 | 46.50 | 9,379 | 783 | 46.50 | 28.50 |
| 1080 | 10,142 | 28,000 | 47.34 | 9,351 | 791 | 47.30 | 29.00 |

Table 5.9 – Case E results

| Case E - Mother bore 239 ft from top; 8 horizontal laterals; 67% penetration | | | | | | | |
|---|-----------|--------|-------|--------|------------|--------|--------|
| Time | Field Pr. | W | W cum | W BHP | ΔP | Np Cum | Gp Cum |
| Days | psia | stbd | stb | psia | Psia | stb | Mscf |
| 0 | 11,204 | 0 | 0.00 | 11,149 | 55 | 0.00 | 0.00 |
| 30 | 11,172 | 49,000 | 1.47 | 10,507 | 665 | 1.47 | 0.87 |
| 60 | 11,140 | 49,000 | 2.94 | 10,439 | 700 | 2.94 | 1.75 |
| 90 | 11,107 | 49,000 | 4.41 | 10,380 | 727 | 4.41 | 2.63 |
| 120 | 11,075 | 49,000 | 5.88 | 10,325 | 749 | 5.88 | 3.52 |
| 150 | 11,042 | 49,000 | 7.35 | 10,273 | 769 | 7.35 | 4.41 |
| 180 | 11,010 | 49,000 | 8.82 | 10,222 | 787 | 8.82 | 5.30 |
| 210 | 10,981 | 43,000 | 10.11 | 10,263 | 718 | 10.10 | 6.09 |
| 240 | 10,952 | 43,000 | 11.40 | 10,223 | 729 | 11.40 | 6.88 |
| 270 | 10,923 | 43,000 | 12.69 | 10,181 | 742 | 12.70 | 7.68 |
| 300 | 10,895 | 43,000 | 13.98 | 10,139 | 755 | 14.00 | 8.47 |
| 330 | 10,866 | 43,000 | 15.27 | 10,097 | 769 | 15.30 | 9.27 |
| 360 | 10,837 | 43,000 | 16.56 | 10,054 | 783 | 16.60 | 10.08 |
| 390 | 10,811 | 38,000 | 17.70 | 10,082 | 729 | 17.70 | 10.79 |
| 420 | 10,786 | 38,000 | 18.84 | 10,047 | 738 | 18.80 | 11.50 |
| 450 | 10,760 | 38,000 | 19.98 | 10,011 | 749 | 20.00 | 12.21 |
| 480 | 10,734 | 38,000 | 21.12 | 9,974 | 761 | 21.10 | 12.92 |
| 510 | 10,709 | 38,000 | 22.26 | 9,936 | 772 | 22.30 | 13.64 |
| 540 | 10,683 | 38,000 | 23.40 | 9,898 | 785 | 23.40 | 14.35 |
| 570 | 10,660 | 34,000 | 24.42 | 9,915 | 745 | 24.40 | 15.00 |
| 600 | 10,637 | 34,000 | 25.44 | 9,884 | 753 | 25.40 | 15.64 |
| 630 | 10,614 | 34,000 | 26.46 | 9,851 | 763 | 26.50 | 16.28 |
| 660 | 10,591 | 34,000 | 27.48 | 9,817 | 773 | 27.50 | 16.93 |
| 690 | 10,568 | 34,000 | 28.50 | 9,784 | 784 | 28.50 | 17.57 |
| 720 | 10,545 | 34,000 | 29.52 | 9,750 | 795 | 29.50 | 18.22 |
| 750 | 10,525 | 29,000 | 30.39 | 9,781 | 744 | 30.40 | 18.77 |
| 780 | 10,505 | 29,000 | 31.26 | 9,755 | 750 | 31.30 | 19.33 |
| 810 | 10,485 | 29,000 | 32.13 | 9,728 | 757 | 32.10 | 19.88 |
| 840 | 10,465 | 29,000 | 33.00 | 9,700 | 765 | 33.00 | 20.43 |
| 870 | 10,446 | 29,000 | 33.87 | 9,672 | 774 | 33.90 | 20.99 |
| 900 | 10,426 | 29,000 | 34.74 | 9,643 | 783 | 34.70 | 21.54 |
| 930 | 10,408 | 26,000 | 35.52 | 9,652 | 756 | 35.50 | 22.04 |
| 960 | 10,390 | 26,000 | 36.30 | 9,628 | 762 | 36.30 | 22.54 |
| 990 | 10,372 | 26,000 | 37.08 | 9,604 | 769 | 37.10 | 23.04 |
| 1020 | 10,355 | 26,000 | 37.86 | 9,579 | 776 | 37.90 | 23.54 |
| 1050 | 10,337 | 26,000 | 38.64 | 9,553 | 784 | 38.60 | 24.04 |
| 1080 | 10,319 | 26,000 | 39.42 | 9,527 | 791 | 39.40 | 24.53 |

CHAPTER VI

CONCLUSIONS AND RECOMMENDATIONS

6.1 Conclusions

A new multilateral well architecture is proposed and investigated in this thesis. Its performance is compared against conventional vertical wells in most cases, as this was the original development plan used in the field. Initially parametric studies were performed to evaluate and understand performance by using simple models. These models were then applied to representative field cases and the numerical results analyzed. Also simple methods to estimate productivity are used and tested for their applicability. The following conclusions can be drawn from the study:

1. Simulations show that for the reservoir studied there exist an optimum number of laterals that can be used to drain the reservoir efficiently. Increasing the laterals after a certain number does not produce any significant difference in the cumulative production from the reservoir. For most of the cases studied 4 laterals were usually sufficient to drain the reservoir efficiently in a given period of time.
2. Parametric studies were performed by varying the lateral penetration. Initially 100% lateral penetration was assumed. However comparable production was obtained even when the penetration was lowered to 50%.
3. A comparison of results shows that to maintain a given production rate at lower branch densities much lower flowing bottom hole pressures are needed. The resulting large pressure drawdowns could cause sand production, early water or gas breakthrough or collapse of the slender laterals since they are completed open hole. To avoid such catastrophes it would be a better idea to use more laterals with lower penetration extents. This would present the added advantage of marginal reserve development while lowering drilling cost per field compared to conventional wells.

4. The numerical validation of parametric studies has been performed through a grid refinement study. The results obtained are within permissible error limits.
5. Permeability is a very important variable affecting the performance of the ML well architecture. For a given branch density the PI in the case of an isotropic permeability distribution is almost always twice the PI for anisotropic permeability variation in the reservoir. The reduced flow in the vertical direction (direction of assumed anisotropy) is the most obvious reason for this reduced productivity. However it is anticipated that better performance in anisotropic reservoirs can be achieved by using deviated laterals. Hence deviated laterals form the next direction of studies.
6. The field case studied showed that the reservoir fluid properties play a very important role in fixing the ML well architecture. The nature of the fluids is such that gas production causes the oil viscosity to rise quickly in the upper part. Hence the most desirable location of the horizontal mother bore was in the upper region of the reservoir. This essentially is indicative of the fact that a standard architecture is not necessarily effective in all cases.
7. A simple method to evaluate the maximum PI achievable using the ML well architecture is developed. Laterals have been modeled using the infinite conductivity fracture concept to arrive at this estimate which also depends upon the reservoir geometry.
8. The present analytical tool available to determine a lower limit for PI is unable to predict the performance within acceptable limits of error. The estimate is highly dependent upon the geometry and specifically the depth of the reservoir. At lower depths usually deviation between predicted and calculated values is not very large. However at large values of depth the departure between the two values is large and the calculated PI seems to attain a certain maximum value. Such

behavior is not captured by the analytical tool which does not quite account for the depth in the dimensionless PI.

6.2 Recommendations for Future Studies

The following recommendations can be made on the basis of the results and conclusions:

1. The proposed architecture is a very effective tool to better produce oil and gas. The cases analyzed were mostly homogeneous in nature.
2. The benefits of reduced cost per barrel of oil produced, greater reserve production and improved environmental footprint make it a lucrative technology which should be tested more in developing fields.
3. For heterogeneous cases a slightly modified architecture should be considered for better performance.
4. Better performance prediction tools are necessary to fully appreciate the benefits of this technology.

NOMENCLATURE

- A = Drainage area (ft²)
 B = Oil formation volume factor (rb/stb)
 C_A = Dietz shape factor
 c_t = Compressibility factor (1/psia)
 h = Reservoir depth (ft)
 h_h = Reservoir height for horizontal lateral case (ft)
 h_w = Completion thickness (ft)
 J = Productivity Index (stbd/psia)
 J_D = Dimensionless productivity index
 $J_{D_{max}}$ = Maximum dimensionless productivity index
 k = Permeability, (mD)
 k_x = Permeability in the x-direction (mD)
 k_y = Permeability in the y-direction (mD)
 k_z = Permeability in the z-direction (mD)
 p = Pressure (psia)
 p_D = Dimensionless pressure
 p_{res} = Average reservoir pressure (psia)
 \bar{p}_D = Volumetric average reservoir pressure (psia)
 p_{wf} = Well bore flowing pressure (psia)
 q = Flow rate (stb/d)
 r = Radius (ft)
 R_s = Solution GOR (rb/stb)
 r_w = Well bore radius (ft)
 s = Skin factor
 t = Time (day)
 t_D = Dimensionless time

t_{Dx_f} = Dimensionless time with respect to x_f

t_{Dy_e} = Dimensionless time with respect to y_e

V = Reservoir pore volume (ft³)

x_e = Length of rectangular reservoir in x-direction (ft)

x_f = Fracture half length (ft)

x_h = Reservoir x-dimension for horizontal lateral case (ft)

y = Length in y-direction (ft)

y_D = Dimensionless length in y-direction

y_e = Length of rectangular reservoir in y-direction (ft)

y_h = Reservoir y-dimension for horizontal lateral case (ft)

z_w = Elevation (ft)

Greek Letters

ϕ = Porosity

γ = Euler's constant, 1.78

μ = Viscosity, cp

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APPENDIX A

Development of the infinite conductivity PI for the a vertical well

$$\frac{\partial^2 p}{\partial y^2} = \frac{\phi\mu c_t}{0.00633k} \frac{\partial p}{\partial t} \dots\dots\dots (A.1)$$

The initial and boundary conditions are given by,

Initial Condition: (Uniform Pressure Distribution)

$$p(r, t < 0) = p_i \dots\dots\dots (A.2)$$

Inner Boundary Condition: (Constant well rate)

$$q = \text{constant} = 0.00633 \frac{kA}{B\mu} \frac{\partial p}{\partial y} \dots\dots\dots (A.3)$$

$$\left(\frac{\partial p}{\partial y} \right)_{y=0} = \frac{qB\mu}{0.00633kA} \dots\dots\dots (A.4)$$

The above condition is a direct application of Darcy's law for fluid flow in porous media.

Outer Boundary Condition: (No flow boundary)

$$\left(\frac{\partial p}{\partial y} \right)_{y=y_e} = 0 \dots\dots\dots (A.5)$$

Pseudo-steady state behavior is characterized by a constant pressure gradient with respect to time given by,

$$\frac{\partial p}{\partial t} = \text{constant} \dots\dots\dots (A.6)$$

From the definition of compressibility we get,

$$c = -\frac{1}{V} \frac{\partial V}{\partial p} \dots\dots\dots (A.7)$$

From eqn (3.8) we get,

$$\frac{\partial p}{\partial t} = -\frac{1}{cV} \frac{\partial V}{\partial t} \quad \dots\dots\dots (A.8)$$

where,

$$V = \phi Ah \quad \dots\dots\dots (A.9)$$

Substituting eqn 3.11 into eqn. 3.10 gives,

$$\frac{\partial p}{\partial t} = -\frac{qB}{c\phi Ah} \quad \dots\dots\dots (A.10)$$

The above equation obtained can also be used in terms of field units without applying any conversion factor.

Substituting eqn 3.12 into eqn. 3.3 gives,

$$\frac{\partial^2 p}{\partial y^2} = \frac{\phi\mu c_i}{0.00633k} \left(\frac{-qB}{c\phi Ah} \right) \quad \dots\dots\dots (A.11)$$

The area of the rectangular geometry perpendicular to the flow is given as,

$$A = 4x_f h \quad \dots\dots\dots (A.12)$$

Substituting eqn 3.14 into eqn. 3.13 gives,

$$\frac{\partial^2 p}{\partial y^2} = \frac{-qB\mu}{0.00633ky_e(4x_f h)} \quad \dots\dots\dots (A.13)$$

In the above equation the flow rate q has units in $\frac{ft^3}{D}$ which is converted to stock tank barrel units. Also we multiply divide the above equation by 2π to obtain the diffusivity equation in the form similar to the radial flow equation.

$$\frac{\partial^2 p}{\partial y^2} = -\frac{\pi}{2} \frac{141.2 qB\mu}{khx_f y_e} \quad \dots\dots\dots (A.14)$$

To solve the diffusivity equation we convert it into dimensionless form using the following dimensionless groups,

$$y_D = \frac{y}{y_e} \quad \dots\dots\dots (A.15)$$

$$p_D = \frac{kh(p_i - p)}{141.2 qB\mu} \quad \dots\dots\dots (A.16)$$

$$t_D = \frac{0.00633 kt}{\phi\mu c_i y_e^2} \quad \dots\dots\dots (A.17)$$

Substituting eqns. 3.17, 3.18 and 3.19 into eqn 3.16 we obtain the dimensionless form of the diffusivity equation as,

$$\frac{\partial}{\partial y_D} \left(\frac{\partial p_D}{\partial y_D} \right) = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \quad \dots\dots\dots (A.18)$$

Similarly the initial and boundary conditions in terms of the dimensionless variables are given as,

Initial Condition: (Uniform Pressure Distribution)

$$p_D(r_D, t_D < 0) = 0 \quad \dots\dots\dots (A.19)$$

Inner Boundary Condition: (Constant well rate)

$$\lim_{y_D \rightarrow 0} \left(\frac{\partial p}{\partial y} \right) = -\frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \quad \dots\dots\dots (A.20)$$

Outer Boundary Condition: (No flow boundary)

$$\left(\frac{\partial p}{\partial y} \right)_{y=1} = 0 \quad \dots\dots\dots (A.21)$$

Integrating eqn. 3.20 gives,

$$\left(\frac{\partial p_D}{\partial y_D} \right) = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) y_D + c_1 \quad \dots\dots\dots (A.22)$$

Integrating the above equation once again with respect to y_D gives,

$$p_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \frac{y_D^2}{2} + c_1 y_D + c_2 \quad \dots\dots\dots (A.23)$$

Apply the outer boundary condition, eqn. 3.23 to eqn. 3.25

$$c_1 + \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) = 0 \quad \dots\dots\dots (A.24)$$

$$\therefore c_1 = -\frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \quad \dots\dots\dots (A.25)$$

Substituting eqn. 3.27 into eqn. 3.25 gives

$$p_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(\frac{y_D^2}{2} - y_D \right) + c_2 \dots\dots\dots (A.26)$$

Substituting eqns. 3.14, 3.18 and 3.19 into eqn. 3.12 gives,

$$\frac{\partial p_D}{\partial t_D} = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \dots\dots\dots (A.27)$$

Integrating the above equation with respect to t_D gives the average reservoir pressure as,

$$\bar{p}_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) t_D \dots\dots\dots (A.28)$$

From eqn (28) we get,

$$\bar{p}_D = \left[\frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(\frac{y_D^3}{6} - \frac{y_D^2}{2} \right) + c_2 y_D \right]_0^1 \dots\dots\dots (A.29)$$

$$\therefore \bar{p}_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(\frac{1}{6} - \frac{1}{2} \right) + c_2 \dots\dots\dots (A.30)$$

From eqn. 3.32 and eqn. 3.30 we get the value of c_2 as,

$$c_2 = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(t_D + \frac{1}{3} \right) \dots\dots\dots (A.31)$$

Hence the dimensionless pressure solution for an infinite conductivity fracture is given as,

$$p_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(\frac{y_D^2}{2} - y_D \right) + \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(t_D + \frac{1}{3} \right) \dots\dots\dots (A.32)$$

The dimensionless time variable defined in eqn. 3.19 is in terms of the reservoir length y_e . Hence the above equation can be written as,

$$p_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(\frac{y_D^2}{2} - y_D \right) + \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(t_{Dy_e} + \frac{1}{3} \right) \dots\dots\dots (A.33)$$

But from the definition of t_D ,

$$t_{Dy_e} = \frac{0.00633 kt}{\phi \mu c_t y_e^2} = \left(\frac{x_f}{y_e} \right)^2 t_{Dx_f} \dots\dots\dots (A.34)$$

$$\therefore \left(\frac{y_e}{x_f} \right) t_{Dy_e} = \left(\frac{x_f}{y_e} \right) t_{Dx_f} \quad \dots\dots\dots (A.35)$$

Hence the general solution for the dimensionless pressure is given as,

$$p_D = \frac{\pi}{2} \left(\frac{y_e}{x_f} \right) \left(\frac{y_D^2}{2} - y_D \right) + \frac{\pi}{2} \left(\frac{x_f}{y_e} \right) t_{Dx_f} + \frac{\pi}{6} \left(\frac{y_e}{x_f} \right) \quad \dots\dots\dots (A.36)$$

The solution at the well bore with $y_D = 0$ is given as,

$$p_{wD} = \frac{\pi}{2} \left(\frac{x_f}{y_e} \right) t_{Dx_f} + \frac{\pi}{6} \left(\frac{y_e}{x_f} \right) \quad \dots\dots\dots (A.37)$$

The average reservoir pressure is obtained from eqn. 3.30 while the pressure at the well bore is obtained from eqn. 3.39 by substituting into the definition for dimensionless pressures and generating the corresponding pressures. These pressures are then used to obtain the PI for constant rate condition as,

$$J_{CR} = \frac{kh}{141.2 B\mu \left[\frac{\pi}{6} \left(\frac{y_e}{x_f} \right) \right]} \quad \dots\dots\dots (A.38)$$

The general definition for PI in terms of the dimensionless PI is given as,

$$J_{CR} = \frac{kh}{141.2 B\mu} J_D \quad \dots\dots\dots (A.39)$$

Comparing eqns. 3.40 and 3.41 we obtain the maximum dimensionless PI as,

$$J_{D, \max} = \frac{6}{\pi} \quad \dots\dots\dots (A.40)$$

APPENDIX B

The following data file is used to simulate a case where 15 laterals penetrate the reservoir at a depth of 365 ft from the top of the reservoir.

--

 -- Office Simulation File - Multilateral Well Architecture is used to drain the field

--

RUNSPEC

TITLE

VERSION 1 Jabillos - 62x21x11

START

30 'DEC' 1987 /

FIELD

GAS

OIL

WATER

DISGAS

SAVE

'UNFORMATTED' /

MONITOR

RSSPEC

DIMENS

-- NX NY NZ

62 21 11 /

WELLDIMS

-- MX CON/WELL GRPS WLL/GRP

1 671 1 1/ -- Maximum number of connections

WSEGDIMS

1 723 63/ -- DIMENSION OF MULTISEGMENT WELL

 GRID

EQUALS

```

-- PROP  VALUE  IX1  IX2  JY1  JY2  KZ1  KZ2

'DX' 322.58 1    62    1    21    1    11 /
'DY' 476.19 1    62    1    21    1    11 /
'DZ' 68.18   1    62    1    21    1    11 /
'TOPS' 14500 1    62    1    21    1    1 /
-- CRETACEOUS-01 RESSERVOIR , 750 FT
'PERMX' 86.6 1    62    1    21    1 11/
'PERMY' 28.67 1    62    1    21    1 11/
'PERMZ' 2.6   1    62    1    21    1 11/
'PORO' .12   1    62    1    21    1 11/

```

/

GRIDFILE

2 /

INIT

EDIT

PROPS

PMAX

```

-- Maximum Simulation Pressure
11200 1* 1* 1*
/

```

DENSITY

```

-- Fluid Densities at Surface Conditions
-- sto  wat  gas (lbm/ft3)
54.637  62.4  0.068432
/

```

ROCK

```

-- Rock Properties
7000 3e-006
/

```

PVCO

```

-- Live Oil PVT Properties (Dissolved Gas)
-- pbub  Rs  Bo  vis  coil  cvis
-- psia  mcf/stb  rb/stb  cp  1/psi  1/psi
500 0.054 1.045 7666 1.5296e-005 2.022e-005
714.286 0.0558333 1.0474 7366.34 1.5296e-005 2.022e-005
1428.57 0.125625 1.08002 1251.99 1.5296e-005 2.022e-005
2142.86 0.215357 1.124 212.79 1.5296e-005 2.022e-005

```

| | | | | | |
|---------|----------|---------|----------|-------------|------------|
| 2857.14 | 0.335 | 1.18504 | 36.166 | 1.5296e-005 | 2.022e-005 |
| 3571.43 | 0.5025 | 1.27335 | 6.1468 | 1.5296e-005 | 2.022e-005 |
| 4285.71 | 0.75375 | 1.4094 | 1.04472 | 1.5296e-005 | 2.022e-005 |
| 4642.86 | 0.933214 | 1.50811 | 0.430698 | 1.5296e-005 | 2.022e-005 |
| 5000 | 1.1725 | 1.64093 | 0.177561 | 1.5296e-005 | 2.022e-005 |

/

PVZG

-- Dry Gas PVT Properties (using Z-factors)

-- press z-fac gas vis

-- psia cp

--

290

/

| | | |
|------|-------|------|
| 500 | 0.922 | 0.03 |
| 1000 | 0.922 | 0.03 |
| 2000 | 0.893 | 0.03 |
| 3000 | 0.902 | 0.03 |
| 4000 | 0.935 | 0.03 |
| 5000 | 1 | 0.03 |

/

PVTW

-- Water PVT Properties

-- p Bw cw vis cvis

| | | | | | | |
|--------|--------|--------|----|------|-------|------|
| psia | rb/stb | 1/psi | cp | | vis | cvis |
| 4789.7 | 1 | 3e-006 | | 0.15 | 1/psi | 0 |

/

STONE1

--

SWFN

-- Water Saturation Functions

| | | |
|------|---------|------|
| sw | krw | pcow |
| 0.14 | 0 | 0 |
| 0.16 | 0.00025 | 0 |
| 0.2 | 0.00085 | 0 |
| 0.3 | 0.0083 | 0 |
| 0.4 | 0.035 | 0 |
| 0.5 | 0.049 | 0 |
| 0.6 | 0.106 | 0 |
| 0.64 | 0.134 | 0 |
| 0.7 | 0.19 | 0 |
| 0.8 | 0.32 | 0 |
| 0.9 | 0.493 | 0 |
| 1 | 1 | 0 |

/

-- Gas rel perm and cap pressure
SGFN

| -- | sg | krp | pcgo |
|----|------|--------|------|
| | 0 | 0 | 0 |
| | 0.05 | 8e-006 | 0 |
| | 0.1 | 1e-005 | 0 |
| | 0.2 | 0.0025 | 0 |
| | 0.3 | 0.0133 | 0 |
| | 0.4 | 0.0434 | 0 |
| | 0.5 | 0.1082 | 0 |
| | 0.6 | 0.2285 | 0 |
| | 0.73 | 0.5107 | 0 |
| | 0.86 | 1 | 0 |

/

SOF3

-- Oil Saturation Functions

| -- | Soil | krpw | krpg |
|----|------|--------|--------|
| | 0 | 0 | 0 |
| | 0.1 | 0.01 | 0.0001 |
| | 0.2 | 0.0194 | 0.0054 |
| | 0.3 | 0.028 | 0.009 |
| | 0.36 | 0.03 | 0.016 |
| | 0.4 | 0.039 | 0.035 |
| | 0.5 | 0.084 | 0.05 |
| | 0.6 | 0.173 | 0.1 |
| | 0.7 | 0.302 | 0.28 |
| | 0.8 | 0.615 | 0.54 |
| | 0.84 | 0.81 | 0.716 |
| | 0.86 | 1 | 1 |

/

REGIONS

SOLUTION

EQUIL

-- Equilibration Data Specification

14875 11200 16250 0 13000 0 1 1 -20

/

RSVD

| -- | depth | Rs (mcf/stb) |
|----|-------|--------------|
| | 12000 | 1.14504 |
| | 14350 | 0.874212 |
| | 14646 | 0.7475 |
| | 14700 | 0.619152 |

| | |
|-------|-----------|
| 14800 | 0.538511 |
| 14880 | 0.330833 |
| 14960 | 0.244157 |
| 15000 | 0.0558333 |
| 16500 | 0.0558333 |

/

-- Switch echo output off
NOECHO

DATUM
14875 /

RPTSOL
-- Initialisation Print Output
'FIP=2' 'EQUIL' 'VOIL' /

SUMMARY

RPTSMRY
1
/

RPTONLY

FPR

WBHP
/

FOIP

FOPR

FWPR

FGPR

FOPT

RUNSUM

EXCEL

SEPARATE

 SCHEDULE

DRSDT
0.0003 1* /

RPTRST
BASIC=2 VISC /

TUNING
1* 31 8* /
11* /
4* 31 5* /

RPTSCHED
'RESTART=2' 'FIP=2' 'WELLS=4' 'CPU=1' 'TUNING' /

WSEGITER

--ITERMAX
50 /

WELSPECS
-- NAME GRP I J BHPDTH
WELL1 'ESTE' 1 11 14875 'OIL' /
/

COMPDAT
-- Well I J K K Flag
-- Name (up) (down)

| | | | | | | | | |
|-------|----|----|---|---|-----------|------|----|-----|
| WELL1 | 1 | 11 | 4 | 4 | 'SHUT' 2* | 3.00 | 3* | X / |
| WELL1 | 62 | 11 | 4 | 4 | 'SHUT' 2* | 3.00 | 3* | X / |

| | | | | | | | | |
|-------|---|----|---|---|---------|-----|----|-----|
| WELL1 | 3 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 3 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 3 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 3 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 3 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 3 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |

| | | | | | | | | |
|-------|---|----|---|---|---------|-----|----|-----|
| WELL1 | 7 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 7 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 7 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 7 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 7 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
| WELL1 | 7 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |

| | | | | | | | | |
|-------|----|----|---|---|---------|-----|----|-----|
| WELL1 | 11 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y / |
|-------|----|----|---|---|---------|-----|----|-----|

| | | | | | | | | | |
|-------|----|----|---|---|---------|-----|----|---|---|
| WELL1 | 11 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 11 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 11 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 11 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 11 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 15 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 15 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 15 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 15 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 15 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 15 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 19 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 19 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 19 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 19 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 19 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 19 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 23 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 23 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 23 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 23 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 23 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 23 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 27 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 27 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 27 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 27 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 27 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 27 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 32 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 32 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 32 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 32 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 32 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 32 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 36 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 36 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 36 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 36 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 36 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 36 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 40 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 40 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 40 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |

| | | | | | | | | | |
|-------|----|----|---|---|---------|-----|----|---|---|
| WELL1 | 40 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 40 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 40 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 44 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 44 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 44 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 44 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 44 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 44 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 48 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 48 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 48 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 48 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 48 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 48 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 52 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 52 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 52 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 52 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 52 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 52 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 56 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 56 | 12 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 56 | 13 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 56 | 14 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 56 | 15 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 56 | 16 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 60 | 11 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 60 | 10 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 60 | 9 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 60 | 8 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 60 | 7 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |
| WELL1 | 60 | 6 | 4 | 4 | OPEN 2* | 0.3 | 3* | Y | / |

/

WELSEGS

-- RECORD 1

-- Well Depth of Lenght Down Vol1 Len&Dep

-- Name Node Tubing

WELL1 14865 10 1* INC /

-- First Last Branch Outlet Lnth Depth Diam Ruf-

-- Seg Seg Number Seg Change ness

-- Main Stem

2 2 1 1 10 10 0.30 1.0E-3 2* /

| | | | | | | | | | |
|-----|-----|----|----|--------|---|------|--------|----|---|
| 3 | 63 | 2 | 2 | 322.58 | 0 | 3.00 | 1.0E-3 | 2* | / |
| 64 | 69 | 3 | 5 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 70 | 75 | 4 | 9 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 76 | 81 | 5 | 13 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 82 | 87 | 6 | 17 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 88 | 93 | 7 | 21 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 94 | 99 | 8 | 25 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 100 | 105 | 9 | 29 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 106 | 111 | 10 | 34 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 112 | 117 | 11 | 38 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 118 | 123 | 12 | 42 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 124 | 129 | 13 | 46 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 130 | 135 | 14 | 50 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 136 | 141 | 15 | 54 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 142 | 147 | 16 | 58 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |
| 148 | 153 | 17 | 62 | 476.2 | 0 | 0.3 | 0.001 | 2* | / |

/

COMPSEGS

-- Name

WELL1 /

| -- I | J | K | Brn | Start | End | Dir | End |
|------|---|---|-----|--------|--------|------|-------|
| -- | | | No | Length | Length | Pent | Range |

-- Main Horizontal branch

| | | | | | | | |
|----|----|---|----|-------|----|---|------|
| 1 | 11 | 4 | 2 | 10.00 | 1* | X | 62 / |
| 3 | 11 | 4 | 3 | 1* | 1* | Y | 6 / |
| 7 | 11 | 4 | 4 | 1* | 1* | Y | 16 / |
| 11 | 11 | 4 | 5 | 1* | 1* | Y | 6 / |
| 15 | 11 | 4 | 6 | 1* | 1* | Y | 16 / |
| 19 | 11 | 4 | 7 | 1* | 1* | Y | 6 / |
| 23 | 11 | 4 | 8 | 1* | 1* | Y | 16 / |
| 27 | 11 | 4 | 9 | 1* | 1* | Y | 6 / |
| 32 | 11 | 4 | 10 | 1* | 1* | Y | 16 / |
| 36 | 11 | 4 | 11 | 1* | 1* | Y | 6 / |
| 40 | 11 | 4 | 12 | 1* | 1* | Y | 16 / |
| 44 | 11 | 4 | 13 | 1* | 1* | Y | 6 / |
| 48 | 11 | 4 | 14 | 1* | 1* | Y | 16 / |
| 52 | 11 | 4 | 15 | 1* | 1* | Y | 6 / |
| 56 | 11 | 4 | 16 | 1* | 1* | Y | 16 / |
| 60 | 11 | 4 | 17 | 1* | 1* | Y | 6 / |

/

WCONPROD

| -- Name | Flag | Control | Coilmax | Limits | BHP |
|---------|--------|---------|----------|--------|-----|
| WELL1 | 'OPEN' | 'ORAT' | 63000.00 | / | |

/

```
TSTEP
6*30
/
WCONPROD
-- Name Flag Control Qoilmax      Limits BHP
  WELL1 'OPEN' 'ORAT'  59000.00 /
/

TSTEP
6*30
/

WCONPROD
-- Name Flag Control Qoilmax      Limits BHP
  WELL1 'OPEN' 'ORAT'  49000.00 /
/

TSTEP
6*30
/

WCONPROD
-- Name Flag Control Qoilmax      Limits BHP
  WELL1 'OPEN' 'ORAT'  40000.00 /
/

TSTEP
6*30
/

WCONPROD
-- Name Flag Control Qoilmax      Limits BHP
  WELL1 'OPEN' 'ORAT'  32000.00 /
/

TSTEP
6*30
/

WCONPROD
-- Name Flag Control Qoilmax      Limits BHP
  WELL1 'OPEN' 'ORAT'  27000.00 /
/

TSTEP
6*30
/

END
```

VITA

Manoj Sarfare holds a B.E. degree in petrochemical engineering from Maharashtra Institute of Technology, Pune, India. He worked with Dr. Peter Valkó as a Research Assistant on the industry funded project on Reservoir Applications of Advanced Multilateral Well Technology.

His current address: Texas A&M University

Attn.: Dr. Peter. P. Valkó

Harold Vance Department of Petroleum Engineering

3116 TAMU

College Station, TX 77843-3116

USA