Structural and electronic properties of Au on TiO₂(110)

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The structure and electronic properties of 1-ML Au supported on $TiO_2(110)$ have been theoretically investigated using the full potential linearized augmented plane-wave method. Based on total-energy and atomic-force calculations, the preferential adsorption site for the Au adatom is predicted to be the atop site above the fivefold surface Ti atom, with a bond length of $d_{\text{Au-Ti}} = 2.66\,\text{Å}$ and an adsorption energy of $-1.49\,\text{eV}$ per adatom. The adsorption of Au enhances the binding energies of the valence bands and core levels of the surface Ti and O atoms, the Au d bands are destabilized with metallic gap states appearing near the Fermi level. This Au-substrate interaction leads to a more active Au site for the Au/TiO₂(110) system compared to the Au(001) surface, in agreement with recent experimental observations.

I. INTRODUCTION

Metal-oxide systems, especially those involving TiO₂, have recently received considerable attention because of their technological importance as photocatalysts, chemical sensors, and heterogeneous catalysts. 1,2 Accordingly the growth of various metals such as Cr, Fe, Cu, Hf, and Pt on TiO₂ has been investigated.^{3–8} Although gold has long been considered to be catalytically inactive, recently it has become a subject of intensive research because of its demonstrated unusual catalytic properties when highly dispersed, i.e., <10 nm clusters. For example, the Au/TiO2 system has been shown to exhibit excellent properties as a chemical gas sensor and catalyst for room-temperature CO oxidation. 9-11 Highly dispersed Au on supports such as TiO2 also exhibits an extraordinary high activity for low-temperature catalytic combustion and reduction of nitrogen oxides. Valden and co-workers 12-15 have studied in detail the structure and catalytic properties of Au on TiO2 concluding that CO oxidation on Au/TiO₂(110) is structure sensitive and that the unusual activity of the Au is likely due to quantum size effects in the highly dispersed Au clusters.

The adsorption and growth mode of Au on $TiO_2(110)$ within the submonolayer regime is a key to understanding the Au-TiO₂(110) interfacial interaction and the unusual catalytic activity of supported Au. Zhang, Persaud, and Madey¹⁶ have studied the growth of Au on TiO₂(001) using low-energy ion scattering, x-ray photoelectron spectroscopy XPS, and low-energy electron diffraction and found that initially Au grows quasi-two-dimensionally (2D). No evidence of a significant chemical interaction was found between the Au adlayer and the TiO₂ substrate. Using the full potential linear muffin-tin orbital (FP-LMTO) method, the electronic structure of 5d transition metals (Ta to Au) on an unrelaxed TiO₂(110) surface was studied by Thiên-Nga and Paxton¹⁷ considering only one adsorption site (the atop site above the fivefold titanium surface atom). However, it is known that the TiO₂(110) is significantly reconstructed; ^{18,19} therefore the actual Au adsorption site on the relaxed surface could differ considerably from the unrelaxed surface. Thus it is important to consider the role of the substrate relaxations in altering the adsorption site and electronic properties of Au on $TiO_2(110)$.

In this paper, the full potential linearized augmented plane-wave (FLAPW) method²⁰ was used to study the adsorption of 1-ML Au on the relaxed ${\rm TiO_2(110)}$. It is found that the Au adatoms prefer the atop site above the fivefold surface Ti atom, with a bond length of $d_{\rm Au-Ti}=2.66\,{\rm Å}$ and an adsorption energy of -1.49 eV per adatom. The chemical properties of an Au site in ${\rm Au/TiO_2(110)}$ appear to be very different from those in ${\rm Au(001)}$. The Au d band in ${\rm Au/TiO_2(110)}$ is very close to the Fermi level (E_f) and metallic states appear within the ${\rm TiO_2}$ band gap, leading to the enhanced chemical reactivity of the ${\rm Au/TiO_2(110)}$ system.

A brief description of the model and computational method is first presented, followed by first-principles results and discussion of bulk ${\rm TiO_2}$, the bare ${\rm TiO_2}(110)$ surface, and the ${\rm Au/TiO_2}(110)$ system.

II. THE MODEL AND COMPUTATIONAL METHOD

The film version FLAPW method²⁰ has no shape approximation for charge, potential, and wave functions in the muffin-tin, interstitial, and vacuum regions. The local-density approximation (LDA) formalism of Hedin and Lundqvist²¹ was used to describe the exchange-correlation potential and energy.

In the muffin-tin region, spherical harmonics with a maximum angular momentum of 8 are used to expand the charge, potential, and wave functions. In the interstitial region, plane waves with energy cutoffs of 324 Ry (for the charge and potential) and 16 Ry (for the variational bases) were employed. The Ti 3p3d4s and O 2s2p states were treated as valence states. The equilibrium structures were determined using total-energy and atomic forces, with a criterion that required the force on each atom to be less than 2×10^{-3} hartree/a.u. Sixteen k points in the irreducible part of the two-dimensional Brillouin zone [for the TiO₂(110) clean surface and the Au/TiO₂(110) systems] were used for the

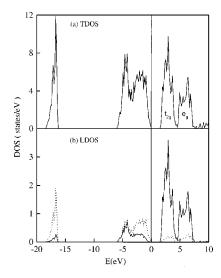


FIG. 1. The total (TDOS) (a) and local (b) density of states (LDOS) of the bulk TiO₂. The solid and dotted lines in panel (b) represent the LDOS of Ti and O, respectively. The solid vertical line at zero denotes the Fermi level.

integrals in reciprocal space. Test calculations for bulk ${\rm TiO_2}$ and clean ${\rm TiO_2}(110)$ surface with larger energy cutoffs showed that this approach is reasonable.

III. BULK TiO₂ AND THE TiO₂(110) CLEAN SURFACE

For bulk TiO₂, isotropic compressibility was assumed, i.e., the internal structural parameter u remains constant (0.305), and a and c scale isotropically. LDA calculations show that the total energy reaches its minimum at the experimental observed lattice constant values: 23 a = 4.594 Å and $c = 2.952 \,\text{Å}$. The calculated bulk modulus B is 228 GPa, very close to the experimental observed value (239 GPa).²⁴ In contrast, the calculated lattice constant using the generalized gradient approximation²⁵ (GGA) was found to be 2% larger than the experimental value.²³ Since the LDA method is known to describe Au better than GGA, LDA was used in the present studies. The calculated total and local density of states (DOS) for bulk TiO₂ in the equilibrium geometry are shown in Fig. 1. The states from higher to lower stability have O 2s(-18 to -16 eV), O 2p(-6 to 0 eV), and Ti 3d(2 to 7.5 eV) character, respectively.

 ${
m TiO_2}$ is an insulator with a LDA-predicted band gap of 1.8 eV, a value smaller than the experimental value of 3.0 eV for well-known reasons. Noting the local DOS (LDOS) in panel (b), it is apparent that the uppermost valence states consist primarily of the O 2p component, while the Ti 3d component dominates the conduction band. There is obvious hybridization between the Ti 3d and the O 2p states, especially in the energy range -6 to 0 eV. The Ti 3d bands are separated into t_{2g} and e_g subbands because of the strong octahedral crystal field. These results agree well with Paxton's FP-LMTO data. 26

The $TiO_2(110)$ surface is the most thermodynamically stable TiO_2 surface, and has been studied extensively by various experimental and theoretical extensively by various experimental and theoretical extensively by various experimental extensively and theoretical extensively by various experimental extensively and theoretical extensively extensively by various experimental extensively extensive extensi

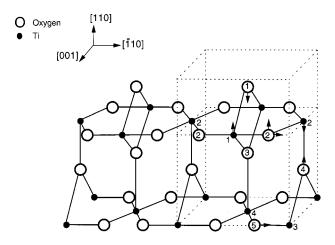


FIG. 2. The schematic geometry of the bulk-terminated $\text{TiO}_2(110)$ - (1×1) (only the upper half of the three-layer slab is drawn; the part in the dashed-line box is the upper-half unit cell used in our calculations). Small solid circles represent Ti and large open circles are for O.

et al. ¹⁸ The observed large surface relaxations, up to 0.27 Å, agree with ab initio pseudopotential total-energy calculations ¹⁹ especially for the positions of the surface titanium atoms.

In the present study the $TiO_2(110)$ substrate is modeled by a three-layer slab shown in Fig. 2 (only the upper half of the slab is shown). The atoms in the model are fully relaxed according to their atomic forces; however, the in-plane symmetry in the 2D unit cell obtained from the ideally terminated rutile (110) surface is preserved. The calculated atomic displacements from their positions in the ideally terminated structure of TiO₂(110)-(1×1) are listed in Table I, along with previous experimental 18 and theoretical (ab initio pseudopotential method) results. 19 The major relaxations occur along the surface normal with the fivefold Ti [denoted as T(2) and the sixfold Ti [denoted as Ti(1)] moving inward and outward by 0.15 and 0.13 Å, respectively. The bridging oxygen [denoted as O(1)] and the in-plane oxygen [denoted as O(2)] move inward and outward by \sim 0.06 and 0.13 Å, respectively. The O(2) and O(5) atoms relax laterally by 0.06 and 0.05 Å, respectively, along the $[\bar{1}10]$ direction as indicated in Fig. 2. The relaxed TiO₂(110) is found to be puckered, agreeing well with earlier theoretical results for a fivelayer slab¹⁹ as well as with x-ray diffraction data.¹⁸ Note that, for O(1), a large discrepancy still exists between our theory and the x-ray diffraction result¹⁸ (-0.06 Å vs $-0.27\pm0.08\,\text{Å}$). To check the possibility of local minimum or existence of metastable state, we carry out calculations using the experimental position 18 for O(1). As a result, this structure gives a much higher total energy (by 0.67 eV/cell) than does the theoretically optimized structure for the clean TiO₂(110) surface.

The total density of states (TDOS) of the slab and the LDOS of the surface atoms for the relaxed $TiO_2(110)$ surface are shown in Fig. 3. It is noteworthy that the band gap of the surface layer is reduced by 0.8 eV relative to the bulk crystal, and that an electrostatic shift occurs between the fivefold and sixfold Ti atoms. The DOS features of the O(1) 2s states are destabilized by approximately 1 eV relative to the O(2) 2s

TABLE I. The calculated atomic displacements of Ti and O atoms from the ideally terminated structure of $TiO_2(110)$ - (1×1) for the clean and Au adsorbed $TiO_2(110)$ systems, accompanied by the earlier experimental (Ref. 18) and theoretical [ab initio pseudopotential (p.p.) method] (Ref. 19) results of the clean surface. A negative (positive) value indicates that atoms move toward (away from) the surface for the perpendicular displacement. The \parallel denotes the movements along [$\overline{1}10$] direction for a lateral displacement. The actual directions of the movement are shown by arrows in Fig. 2. An asterisk indicates that the atom position was frozen in the calculation.

	Au/TiO ₂ (110)				
Atom type	Expt. (Ref. 18)	p.p. method (Ref. 19)	Present	A site	C site
Ti(1)	0.12±0.05	0.13	0.13	0.11	0.11
Ti(2)	-0.16 ± 0.05	-0.17	-0.15	-0.14	-0.10
Ti(3)	-0.09 ± 0.04	-0.08	0.00	0.00	0.00
Ti(4)	0.07 ± 0.04	0.07	0.00	0.00	0.00
O(1)	-0.27 ± 0.08	-0.07	-0.06	-0.05	-0.06
O(2)[110]	0.05 ± 0.05	0.13	0.13	0.08	0.10
$O(2)[\overline{1}10]_{\parallel}$	-0.16 ± 0.08	*	-0.06	-0.04	-0.06
O(3)	0.05 ± 0.08	-0.08	-0.05	-0.04	-0.05
O(4)	0.00 ± 0.08	0.02	-0.004	-0.003	0.02
O(5)[110]	0.02 ± 0.06	-0.03	0.00	0.00	0.00
$O(5)[\bar{1}10]_{\parallel}$	-0.07 ± 0.06	*	-0.06	-0.03	-0.05

states. Satellite surface state features, also found by Paxton and Thiên-Nga,²⁶ appear at the bottom of the conduction band.

IV. THE ADSORPTION OF GOLD

The adsorption of 1 ML (one Au atom per surface unit cell) of Au atoms on the relaxed $TiO_2(110)$ surface was studied by placing an Au adatom on each side of the relaxed $TiO_2(110)$ slab. Three possible adsorption sites, A (on top of the fivefold Ti), B (on top of the sixfold Ti), and C (above the bridge of two in-plane O atoms along the $[\bar{1}10]$ direction), shown in Fig. 4, were considered. The positions of the

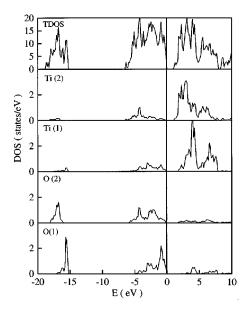


FIG. 3. The TDOS and LDOS of the ${\rm TiO_2}(110)$ clean surface. The solid vertical line at zero denotes the Fermi level.

adsorbed Au and the substrate atoms were optimized according to their atomic forces. The adsorption energies [defined as $E_{\text{ad}} = \frac{1}{2} (E_{\text{Au/TiO}_2} - E_{\text{TiO}_2} - 2E_{\text{Au}})$, with $E_{\text{Au/TiO}_2}$, E_{TiO_2} , and $E_{\rm Au}$ representing the total energies of the adsorbed system, the clean TiO₂(110) surface, and a free Au monolayer, respectively] were -1.49 eV/atom, -1.00 eV/atom, and -1.41 eV/atom for the three adsorption geometries (A, B, C), respectively. Overall, these adsorption energies are less than comparable values for metal/metal systems, but larger than those values found for metals adsorbed on MgO(001).³⁴ In contrast, an unreasonably large adsorption energy (~8.5 eV/ atom) for the broken row adsorption (corresponding to 0.5 ML Au) was found by Thiên-Nga and Paxton from their FP-LMTO calculations for Au adsorption on the unrelaxed TiO₂(110) surface.¹⁷ Comparatively, the least favorable adsorption site is B, where the adsorption energy is only -1.0eV/atom. The A site is probably the most favorable adsorption site, followed closely by the C site (-1.49 eV/adatom)and -1.41 eV/adatom, respectively). Obviously at elevated temperatures, i.e., a few hundred Kelvin, adsorption on either A and C sites is likely. The Au results are very similar to

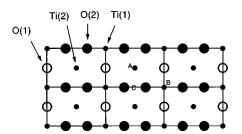
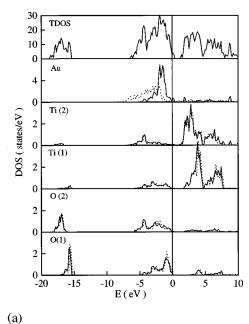


FIG. 4. Schematic geometry (top view) of the $TiO_2(110)$ surface, with three possible adsorption sites considered in our studies marked as A, B, and C, respectively. The small solid circles represent the surface Ti, the large solid and open circles represent the in-plane O [O(2)] and the bridge O [O(1)], respectively.



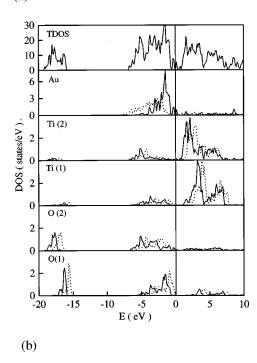


FIG. 5. The TDOS and LDOS of the $Au/TiO_2(110)$ system for (a) A-site adsorption and (b) C-site adsorption. The dotted lines represent the LDOS for the Au(001) and $TiO_2(110)$ clean surfaces. The solid vertical line at zero denotes the Fermi level.

those found for Pt and Pd on $TiO_2(110)$, although both Pt and Pd have a greater preference for the A site. ^{35,36}

The atomic displacements from the ideally terminated structure of $\text{TiO}_2(110)$ - (1×1) in the equilibrium structures of the A and C adsorption sites of $\text{Au/TiO}_2(110)$ are shown in Table I. The adsorption of Au only slightly alters the relaxation of the TiO_2 substrate, even for the nearest-neighbor Ti and O atoms. On the A site, Au causes the nearest-neighbor O(2) to move inward by ~ 0.05 Å; Ti(1) also moves inward by 0.02 Å accompanied by a shift of the O(2). The bond lengths between the Au adatom and its nearest neighbors,

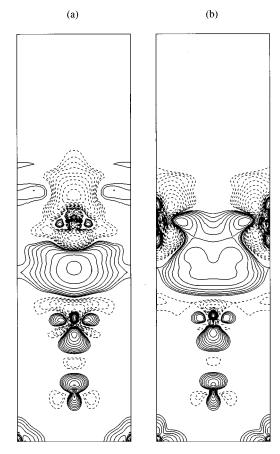


FIG. 6. The calculated charge density difference obtained by subtracting the superposition of the charge densities of Au monolayer and $\text{TiO}_2(110)$ from that of $\text{Au/TiO}_2(110)$ (a) for A-site adsorption, (b) for C-site adsorption. Contours are shown in the vertical ($\bar{1}10$) plane and start from 1×10^{-3} e/a.u.², and increase successively by a factor of $\sqrt{2}$. Dashed lines indicate negative differences.

Ti(2) and O(2), are 2.66 and 3.11 Å, respectively. In contrast, with total-energy minimization for the unrelaxed $TiO_2(110)$ surface, a shorter Au-Ti(2) bond length (2.57 Å) was reported by Thiên-Nga and Paxton. The For Au adatoms on the C site, the nearest-neighbor Ti(2) [O(2)] atoms move outward (inward) by 0.05 Å (0.03 Å) from its corresponding position within the $TiO_2(110)$ clean surface. The Ti(1) site also shifts inward by 0.02 Å because of the change of the O(2) position. On the C site, the bond lengths between the Au adatom and its nearest Ti(2) and O(2) atoms are 2.95 and 2.65 Å, respectively.

The TDOS and LDOS for Au adsorption on the A and C sites are shown in Figs. 5(a) and 5(b), respectively. In Fig. 5(a), compared to the DOS of the $TiO_2(110)$ clean surfaces, Au adsorption on the A site induces no substantial change for the Ti and O sites. On the other hand, the Au d bands are now very close to E_f , which are mainly in the energy range of -5 to 0 eV, with a small feature lying just above the Fermi energy [i.e., a metal-induced gap state (MIGS)]. As discussed below, this is caused by charge polarization in the interfacial region and a subsequent increase of the potential in the adlayer. Such a large energy shift of the Au 5d band toward the E_F , as discussed by Hammer and Norskøv, 37 and

TABLE II. The binding energies of the core states with respect to the Fermi level (in eV, $4f_{7/2}$ for Au, $2p_{3/2}$ for Ti and $1s_{1/2}$ for O) for the Au/TiO₂ (110) systems in the *A*- and *C*-site cases. Results of relaxed (unrelaxed) TiO₂ (110) and Au (001) clean surfaces are also given.

Atom	Au on A site	Au on C site	Clean surface
Au	75.08	74.67	76.20 (75.99)
Ti(2)	437.83	437.91	437.24 (438.23)
O(2)	503.47	503.58	502.75 (503.57)
O(1)	501.70	502.47	501.68 (501.53)

also the induced gap state are expected to strongly alter the surface chemical properties of $Au/TiO_2(110)$ from those of the Au(001) clean surface.

For Au adsorption on the C site, the TDOS curve in Fig. 5(b) show that the gap is filled by many MIGS's, resulting mainly from the interaction between the Au atom and the nearest Ti(2) and O(2) atoms. Another major feature in Fig. 5 is the adsorbate-induced band bending, which can be clearly seen from the downward shifts of the Ti(1) and O(1) bands from the Fermi level. This band bending was observed by Zhang, Persaud, and Madey. 16

To investigate the bonding mechanisms, the charge density differences obtained by subtracting the superposition of charge densities of the Au monolayer and the $TiO_2(110)$ clean surface from that of $Au/TiO_2(110)$ are plotted in Fig. 6. For adsorption of Au on the A site, Fig. 6(a) shows that electrons deplete from both the interfacial Au and Ti(2) sites and accumulate in the region between them. This suggests the formation of covalent bonds between Au and Ti(2).

Comparatively, for the *C* site adsorption [Fig. 6(b)], more electrons deplete from the top of the Au adatom. Charge accumulations can be found in the Au adlayer along the [001] direction, which suggests the formation of a metallic bond in the Au adlayer. This feature corresponds to the states in the gap (MIGS's) [cf. the panels of TDOS and Au in Fig. 5(b)]. The pronounced charge polarization in the interfacial region is responsible for the metal-induced band bending shown in Fig. 5(b).

By referring to the core-level energies in Table II, it is found that the binding energies of the core levels of Ti and O are stabilized relative to the relaxed $\text{TiO}_2(110)$ clean surface. The Ti(2) $2p_{3/2}$ and O(2) $1s_{1/2}$ levels are shifted to higher binding energies by 0.59 eV (0.67 eV) and 0.72 eV (0.83 eV), respectively, for the *A* site (*C* site). The binding energies of the valence states are also stabilized [cf. Figs. 5(a) and 5(b)], especially for the *C* site. The charge depletion around these atoms is mainly responsible for these binding energy increases. Similar core-level shifts were observed via XPS by Zhang, Persaud, and Madey, ¹⁶ who found that the Ti 2p and O 1s core-level features shift to higher binding energies by $\sim 0.1-0.2$ eV.

For the Au adlayer, the Au $4f_{7/2}$ levels are predicted to be destabilized (*lower* binding energy) by 1.1 and 1.5 eV for the A and C sites, respectively, relative to the Au $4f_{7/2}$ levels for the Au(001) clean surface. The valence DOS of the Au adlayer also shifts toward E_f by \sim 1.8 eV relative to the Au(001) clean surface. These parallel shifts for the valence

and core states suggest that these arise from interfacial charge polarization and the subsequent potential shift in the adlayer. Recent XPS data of Luo, Kim, and Goodman, 38 indicate that the Au 4f core level shifts to higher binding energy (0.8 eV) relative to bulk Au as Au clusters on TiO2 become highly dispersed. XPS data of Zhang, Persaud, and Madey, 16 also show that the Au 4f feature for thin Au films (1.1 Å) on TiO₂ have higher core-level binding energies (0.4 eV) relative to thick Au films (52 Å). At first glance the higher Au $4f_{7/2}$ binding energies appear contradictory to the theoretical predictions. However, it is noteworthy that the Au 4f core-level shifts observed by Luo, Kim, and Goodman,³⁸ for Au clusters supported on SiO2, show a higher binding energy of 1.6 eV for highly dispersed clusters relative to bulk Au, an increase attributable to final-state effects due to finite cluster sizes. That the Au $4f_{7/2}$ core level shifts are 0.8 eV lower for small clusters of Au on TiO₂(110) compared to small clusters of Au on SiO₂ is consistent with there being an initial state contribution of ~ -1.0 eV for small clusters of Au on $TiO_2(110)$, close to the value predicted by the calculations (1.1-1.5 eV).

From Table II, the binding energies of the core levels are found to be structure sensitive, with clear differences between the core levels of the relaxed and the unrelaxed $TiO_2(110)$ clean surfaces. Noticeable differences are also evident between the core levels for the A and C adsorption sites, suggesting that different adsorption sites may be distinguishable using XPS.

V. SUMMARY

The structure and electronic properties of Au on TiO₂(110) have been studied using the full potential linearized augmented plane-wave (FLAPW) method. First, the adsorption of Au leads to small changes in the atomic and electronic structure of TiO₂. Second, total-energy and atomic-force calculations indicate two possible preferred adsorption sites (A and C) differing very slightly in energy (1.49 vs 1.41 eV). Third, the valence and core-level binding energies of the surface Ti and O are found to be stabilized, which is qualitatively observed experimentally. Finally, the Au 4f core-level shifts are predicted to be lower by 1.1-1.5eV compared to bulk Au, consistent with recent XPS measurements.³⁸ Due to the interfacial interaction and charge polarization, the Au d bands in $Au/TiO_2(110)$ are very near E_f , with numerous MIGS's induced within the band gap, which likely contributes substantially to the enhanced catalytic activity of Au/TiO₂(110) compared to bulk Au.

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