## DYNAMIC REGION RRT: APPLICATION TO KINODYNAMIC SYSTEMS

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by

### ANDREW BREGGER

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Dr. Nancy Amato

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### ABSTRACT

#### Dynamic Region RRT: Application to Kinodynamic Systems

Andrew Bregger Department of Computer Science and Engineering Texas A&M University

Research Advisor: Dr. Nancy Amato Department of Computer Science and Engineering Texas A&M University

In the general motion planning problem the robot must satisfy basic constraints such as avoiding obstacles and remaining within the boundary of the environment. Kinodynamic motion planning is a type of planning where additional constraints must be satisfied. Kinodynamic planning is a more realistic planning problem as the robot must operate under constraints such as friction, gravity, velocity, and acceleration while avoiding obstacles. Sampling-based methods are often used to solve these types of problems. These methods generate robot configurations throughout the environment in order to eventually connect them to form a valid path from the start position to the goal. Rapidly-exploring Random Trees (RRT) are types of sampling-based methods appears when planning in an environment with a narrow passage or cluttered space. In these problems it is unlikely to generate a sample in the narrow spaces and the robot does not explore these locations. Dynamic Region-biased Rapidly-exploring Random Trees (DRRRT) is a method that addresses these issues by guiding an RRT with dynamic sampling regions along an embed-

ded graph of the workspace. DRRRT is effective in general motion planning problems, but faces issues in kinodynamic problems. Oftentimes, a sample is generated near an obstacle that is valid, but is found to be unrecoverable because if the robot were to move from that state with any of the available controls it would collide with an obstacle. This often occurs in environments with narrow spaces and tight turns such as a maze.

In this work, we address the address the problems DRRRT faces in the kinodynamic problem with a series of improvements. First, we use the embedded graph to bias the direction that the tree extends to keep the robot moving along the graph. Second, also using the embedded graph we limit the candidates while neighborhood finding so that the entire tree is not searched each time a sample is chosen. Lastly, instead of uniformly selecting which region to be sampled, a bias is applied to the regions according to a heuristic designed to promote more successful regions.

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#### 1. INTRODUCTION AND LITERATURE REVIEW

Sampling-based motion planning is the task of determining a valid path through an environment from an initial state to a goal state by randomly selecting a state within the environment. This path is represented by a collection of states, or configurations, that are described by a set of parameters representing the location and orientation of the robot. This problem has applications in many fields, such as robotics, video games/animations, computer-aided design, and bio-informatics.

One method for solving motion planning problems is the Rapidly-exploring Random Tree (RRT) [1]. RRT is effective in single query scenarios and non-holonomic systems. Non-holonomic systems or kinodynamic systems are systems that must obey kinematic, dynamic, and force constraints [2]. The past configurations will determine the current velocities, accelerations, and momentum that are associated with the robot at that instant in time. In many environments there exists a narrow passage. Narrow passages are sections of the environment that have small sampling area. This causes a problem when sampling because there becomes of its small probability of selection. Dynamic Region-biased RRT (DRRRT) addresses this issue.

RRT is used as a basis for DRRRT [3], which uses an embedding graph to represent the topology and homotopy of the environment. Regions are moved along the graph and sampling is biased within these regions. The embedding graph is generated by decomposing the environment and building a graph from the resulting decomposition. However, this graph can often be jagged and can cause the region to be partially inside of an obstacle.

When considering a non-holonomic systems there are a few problems which DRRRT does not address. In DRRRT much of the running time is spent in neighborhood finding. When a new sample is chosen the nearest neighbor in the tree must be selected so that the tree can extend from the neighbor to the new sample. This results in a search over the entire tree. To limit this we introduce a topological bucketing neighborhood finder that limits this search to a smaller set of candidates associated with the embedding graph.

Another issue pertains to the dynamics introduced by a non-holonomic problem. In a non-holonomic problem configurations may also consist of velocity parameters. The simple approach is to generate these velocities randomly. We introduce a method to bias the randomly generated velocity along the embedding graph provided by DRRRT to improve exploration. Lastly, we introduce a region weighting scheme. When generating a new sample, DRRRT must select a region to sample from. Previously, this was done uniformly over all regions and the environment. We aim to improve this by assigning each region a probability of being selected depending on the region's sampling history. If a region generates more successful samples its probability of being selected for future samples will increase <sup>1</sup>.

We demonstrate the method on autonomous drones. To do this, we must simulate the physics of a flying drone; however, due to limitations in the physics engine we am only able to apply gravity and not give the robot the ability to move itself in the direction of gravity. Gravity must be the only force that is able to move the robot in that direction. To show the viability of this method, we perform experiments on two simple environments with a helicopter robot. The method is compared to the old DRRRT without the changes, RRT, and SyCloP, another workspace planner, in a uniform grid an a small maze.

<sup>&</sup>lt;sup>1</sup>This work is done in collaboration with Ben Smith. The methods are the same between our theses. The differences are in our applications and results. I am applying these methods to drones, while he is applying them to autonomous vehicles.

#### 2. RELATED WORK

In this chapter, we discuss the important background information for the motion planning problem and other work related to this method.

#### 2.1 Motion Planning

Motion planning is the task of finding a path through some environment from a start to a goal position. Traditionally, this path must fit constraints such as avoiding the obstacles and boundaries of the environment and allowing the object or robot to move along it without collision. In this paper, we discuss motion planning for holonomic and non-holonomic robots. A holonomic robot is a robot where all of its degrees of freedom (DOFs) are controllable. The DOFs of a robot parameterize its position and orientation. They include the robot's position, rotation, and joint angles if applicable. A non-holonomic robot is one where not all DOFs are controllable, such as a car, which cannot move laterally without first turning. The motion planning problem is often represented by the workspace and configuration space or  $C_{space}$ .

The workspace of a motion planning problem is the environment which consists of obstacles and a boundary.  $C_{space}$  is the set of all configurations of a given robot. A configuration is one unique set of values for a robot's DOFs. For a simple robot in a 2-d world one configuration could be  $q = \langle x, y, \theta \rangle$  where x and y are the robot's position in the world and  $\theta$  is its rotation angle.  $C_{space}$  also consists of two subsets, free space ( $C_{free}$ ) and obstacle space ( $C_{obst}$ ).  $C_{obst}$  is the set of configurations in  $C_{space}$  that are in collision with an obstacle in the workspace and  $C_{free}$  is the set of configurations in  $C_{space}$  that are not in collision. With this information we can represent the motion planning problem as finding a continuous path of configurations in  $C_{free}$  from the start to goal configurations.

#### 2.2 Sampling-based Planning

One common and effective technique for addressing the motion planning problem is sampling-based planning. The goal of sampling-based planning is to construct a graph that represents  $C_{free}$  by generating sample configurations in  $C_{free}$ . These samples are then connected to form a graph or roadmap. Once the roadmap is constructed, the start and goal configurations can be connected to the closest point on the roadmap and a path can be found. One example of sampling-based planning is the Rapidly-exploring Random Tree [1], which is further explained in the next section.

### 2.3 Rapidly-exploring Random Trees (RRTs)

Rapidly-exploring Random Trees are a type of sampling based planning algorithm that are effective single query motion planning problems. That is problems consisting of only one start and one goal configuration. Rapidly-exploring Random Tree solves a problem by iteratively expanding outwards from root configuration  $(q_{root})$ . For each iteration, a random configuration  $(q_{rand} \in C_{space})$  is generated. Then the nearest configuration to  $q_{rand}$ in the tree  $(q_{near})$  is found and is extended from  $q_{near}$  in the direction of  $q_{rand}$  some distance  $\Delta D$ . The end position of the extension becomes a new configuration  $(q_{new})$  which is added to the tree if and only if there is a valid path between  $q_{near}$  and  $q_{new}$ .

One specific type of RRT is Reachability-guided RRT (RGRRT) [4]. A reachable set is defined as a set of configuration that can be reached by a robot given its controls and configuration. A control is a force that can be applied to a robot to move it from one configuration to another. RGRRT uses the reachable set to bias the sampling. When generating samples, if  $q_{rand}$  is closer to  $q_{near}$  than any configuration in the reachable set  $q_{rand}$  is discarded. This approach allows to the RRT to better sample the unexplored space of the environment.



(a) Example embedding graph



(b) Execution of Dynamic Region-biased RRT.

Figure 2.1: The embedding graph (2.1a) represents paths of exploration through the workspace. These are explored by dynamic sampling regions that guide RRT growth (2.1b).

### 2.4 Dynamic Region-biased RRT

In this paper, we extend Dynamic Region-biased RRT (DRRRT) [3] to better support kinodynamic motion planning problems. Dynamic Region-biased RRT is based on RRT with some key differences. DRRRT computes a representation of the workspace topology and uses dynamic sampling regions to guide an underlying RRT planner. The representation of the workspace topology is known as an embedding graph (Magenta lines in Figure 2.1a). The embedding graph is a skeleton of the workspace represented by an undirected graph. Next the embedding graph is converted to a directed graph from the start to goal a flow graph. This represents the exploration direction of the robot from the start to goal. A region is a bounded volume in the workspace such as a bounding box or a bounding sphere (Green circle in Figure 2.1b). After computing the flow graph, a region is created at the beginning of the graph and is guided along the graph to the goal. If the flow graph splits, representing different paths, or homotopies, through the workspace, multiple regions are dynamically created to explore each path. At each iteration of the algorithm a region or the environment is chosen and a sample is generated within that region or environment. Finally, the underlying RRT extends to this new sample if it is valid.

## 2.5 Synergistic Combination of Layers of Planning

Synergistic Combination of Layers of Planning [5] (SyCLoP) addresses the problem of non-holonomic planning. In SyCLoP, the workspace is decomposed to construct a model of the problem. At each iteration of the algorithm a high-level planner searches this model for a feasible path which can be used to guide an underlying tree structure. They test their method on robots with high-dimensional dynamics including a unicycle, a flying unicycle, and a tractor trailer in environments with multiple narrow passages and a maze.

#### 3. METHOD DESCRIPTION

#### 3.1 Topological Bucketing

Algorithm 1 Algorithms for tree extension with topological bucketing.

```
1: function EXTENDWITHREGION(Region r, Tree t)
2:
         q_{rand} \leftarrow \text{Sample}(r) // \text{Or BiasedSample...}
         candidates \leftarrow FindCandidates(r)
 3:
         q_{near} \leftarrow \text{FindNearestNeighbor}(candidates)
 4:
         q_{new} \leftarrow \text{Extend}(t, q_{rand}, q_{near})
 5:
         if q_{new} \in \mathcal{C}_{free} then
 6:
             BucketMap[r.Center()].Append(q_{new})
 7:
         end if
 8:
 9: end function
10: function FINDCANDIDATES(Region r)
         p \leftarrow r.\text{GetCenter}()
11:
         candidates \leftarrow BucketMap[p]
12:
         e \leftarrow r.\text{GetSkeletonEdge}()
13:
         d \leftarrow 0
14:
         while d < threshold do
15:
             d += distance(p, e.PointBefore(p))
16:
             p \leftarrow e.\text{PointBefore}(p)
17:
             candidates.Append(BucketMap[p])
18:
         end while
19:
         return candidates
20:
21: end function
```

One bottleneck in Dynamic Region-biased RRT is in neighborhood finding. This is caused by using a brute force method which searches the entire tree for the nearest configuration. To improve on this approach we would like to utilize the information provided by the embedding graph to limit the candidates for neighborhood finding. The solution to this is topological bucketing. The algorithm for this method is given in Algorithm 1. The embedding graph structure consists of vertices with edges connecting them. These edges have various edge points or intermediates along it, on which the region is centered (Magenta line and points in Figure 4.1a). When generating a sample we add the sample to a 'bucket' (Defined by blue lines in Figure 3.1) associated with the edge point at the center of the region. In doing this each successful sample is mapped to its nearest edge point. When finding the nearest neighbor, instead of searching the entire tree, we can use the buckets as input to the neighborhood finder and effectively reduce the size of the input.

Algorithm 1 explains this process. In Algorithm 1:1-9 a random sample is first generated and its candidates are found. Then these candidates are used as input to a brute force neighborhood finder. A standard RRT extend is then called from the random sample to the new configuration returned by the neighborhood finder. In Algorithm 1:6-8 the new configuration is added to the bucket associated with the current region's center. Here the bucket map is an associative container that associates a region's center point with a set of configurations or a bucket (Figure 4.1b). Finding the candidates of a random sample is done in Algorithm 1:10-21.

In order to determine which buckets to search over we initially set the candidates (Red outline in Figure 3.1c) to be the bucket associated with the current region's center (Algorithm 1:11-12). Then we traverse the embedding graph backwards for a distance d < threshold, adding the configurations in each bucket to the candidates set (Algorithm 1:15-19). For our purposes we set *threshold* to be the maximum distance that the extender can extend.

In using this approach we observe two advantages over the standard brute force search method. First, the size of the input that the neighborhood finder must search over is reduced from the entire tree to a small portion of the tree stored in the nearest buckets. Second, the configurations in the candidates set are more likely to be near the newly sampled configuration as they come from the buckets which are at most a distance d < threshold

away from the sampled configuration.



(a) Embedded graph defines (b) Congifuration added to (c) Traversing the embedded buckets closest bucket graph for candidates

Figure 3.1: Example progression of Bucket Neighborhood finder: (a) Embedded graph (magenta) and buckets (blue outline); (b) RTT growth and assositation with buckets; (c) collection of candidate set (red outline).

#### 3.2 Velocity Sampling

In kinodynamic motion planning each configuration can have DOF values that represent more than position, such as, velocity. When generating a random configuration one approach for giving it velocity is to generate a random linear velocity for the configuration. Although this method is fast, it can often lead to configurations which can only travel in an unhelpful direction. For example, it is possible for a velocity to be generated which directs a configuration backwards into the tree instead of towards unexplored free space (Yellow arrow in Figure 4.1a). This is another problem we can address using the information provided by the embedding graph.

The embedding graph represents the workspace topology and provides us with a guide from the start to the goal. The embedding graph also consists of multiple intermediate points along each edge which can be used to represent the direction of the graph (Red arrow in Figure 4.1a). These directions can be used to bias randomly generated velocities to be 'along' the embedding graph. This approach is shown in Algorithm 2.

Algorithm 2 Algorithm for biasing velocity along skeleton.

1: **function** BIASEDSAMPLE(Region *r*) 2:  $q_{rand} \leftarrow \text{Sample}(r)$  $e \leftarrow r.\text{GetSkeletonEdge}()$ 3: 4:  $p \leftarrow r.\text{GetCenter}()$ 5:  $dir \leftarrow unit(e.PointAfter(p) - p)$  $coeff \leftarrow q_{rand}$ .LinearVelocity()  $\cdot dir$ 6: if coeff < alpha then 7: while coeff < alpha do 8: 9:  $q_{rand} \leftarrow \text{Sample}(r)$  $coeff \leftarrow unit(q_{rand}.LinearVelocity()) \cdot dir$ 10: end while 11: 12: end if return *q<sub>rand</sub>* 13: 14: end function

First, in Algorithm 2:2-4 a random configuration is generated from the current region with a random velocity. Then, from the region we obtain the current skeleton edge and point. With this information we can compute the direction of the skeleton, *dir*, as the unit vector between the current point and the next point on the skeleton. Next, we set *coef f* to be the dot product between the unit vector of the configuration's linear velocity and the direction of the skeleton. In Algorithm 2:7-12 the goal is to minimize the difference between the configurations velocity and the skeleton direction by using the properties of the dot product. If the two velocities are in opposite directions then the dot product will return -1, provided the vectors are unit vectors. If the two velocities are parallel the dot product will return 1. We use a parameter,  $\alpha$ , to maximize the dot product of the two directions and generate a velocity which is along the skeleton within some bounds. This is shown in Algorithm 2:8-9 where a new configuration and velocity is generated until the dot product between the velocity and the skeleton direction becomes larger than  $\alpha$  and acceptable to use.

Since generating random samples is a relatively fast operation it is acceptable to re-

peatedly sample in this manner. Additionally,  $\alpha$  can be tuned to increase the likelihood to generate an acceptable velocity and decrease the total number of additional samples needed to find an acceptable velocity (Red outline in Figure 4.1b).



Figure 3.2: Motivation for Velocity Biasing: (a) general direction of embedded graph (red arrow) and the direction of new configuration (yellow arrow); (b) allowable direction for velocities (red outline).

### **3.3 Region Weighting**

At each iteration of Dynamic Region-biased RRT a region is chosen and a new configuration is generated from that region. Originally, this decision was made uniformly over all the regions and the entire environment itself. That is, each region, including the entire environment, had an equal chance of being chosen for sampling. We know that for the most part we want samples to be generated in a region, not the environment. Additionally, we want to choose regions which have a history of generating successful samples that help guide the RRT. To accomplish this we use a new region weighting scheme which computes a probability,  $p_i$ , for each region  $\langle r_0, r_1, \ldots, r_n \rangle$  and the environment. We also define a weight for each region  $w_i = s/t$ , where s is the number of successful samples generated in region i and t is the total samples generated in region i. The probability is defined to be:

$$p_i = (1 - \gamma) \frac{w_i}{\sum_{j=1} K w_j} + \gamma \frac{1}{K + 1}$$
(3.1)

where gamma is a constant in the range [0, 1] and K is the total number of current regions. The first term is determined by the ratio of the region's weight to the sum of all current regions' weights. This allows us to determine, to some extent, how well this region is performing. The second term represents uniform probability to select a region based on the input parameter  $\gamma$ . Here K + 1 is used to include the environment. If  $\gamma = 1$  then the probability is exactly uniform, and if  $\gamma = 0$  the probability is strictly based on the region's weight compared to the sum of all regions' weights. Since this probability is based on the weight of all current regions, we must dynamically update each region's probability when any region is added, deleted, or generates a sample.

Using this scheme we effectively bias sampling to regions which historically generate more successful samples, and thus, are more likely to be in areas of free space which have higher clearance between obstacles and more space for exploration.

#### 4. EXPERIMENTS AND RESULTS

### 4.1 Experiments

All methods were implemented in a C++ motion planning library developed at Parasol Lab at Texas A&M University. It uses a distributed graph data structure from the Standard Template Adaptive Parallel Library (STAPL) [6], a C++ library for parallel computing developed at Parasol Lab.

All experiments were performed on a desktop, at Parasol Lab, running CentOS 7 with Intel<sup>®</sup> Core<sup>TM</sup> i7-3770 at 3.40 GHz, 16 GB of RAM, and the GNU GCC compiler version 4.8.5.

#### 4.2 Results

The modified Dynamic Region-biased RRT was compared against the original Dynamic Region-biased RRT [3], a RRT [2], and SyCloP [5]. SyCloP is a method designed for kinodynamic motion planning that uses workspace information when planning. The new algorithm is demonstrated on a non-holonomic drone in two environments, a 4x4 maze and a 3x3 uniform grid. These environments are shown in Figure 4.2. In these environments a robot, which is a helicopter, has 6 DOF rigid body which uses a control set that allows for motion in the forward, backward, and up directions as well as pitch, roll, and yaw rotations. These controls do not allow for applying a control downwards, this is to allow gravity to force the robot to traverse down when there is not enough upward force to counter the act of gravity. To properly simulate the behavior of a drone, constraints were added to limit the rotation along the pitch and roll axes. Simulation of proper air resistance and drag are not currently simulated and are left for future work.

The experiments were ran until the query solved or the trial reached the vertex (20K) or time (6 minute) limits. 35 experiments were ran for each environment using modified

Dynamic Regions, original Dynamic Regions, RRT, and SyCloP. Of the 35 experiments, the fastest and slowest times were disregarded as outliers. The success rates of each trial are shown in Table 4.1 and the average run time (in seconds) and the standard deviation are shown in Figure **??**.



(a) 4x4 GridMaze

(b) 3x3 Grid

Figure 4.1: The experiment environments shown with a solved path for a helicopter. (a) 4x4 GridMaze (b) 3x3 Grid

### 4.3 Discussion

As Figure 4.2a shows, the new additions to DRRRT improve the performance compared to RRT and SyCloP. However, the original DRRRT method performed slightly better than the new DRRRT. We observed an decrease in the amount of time spent on neighborhood finding, but an increase in the overall run time. As of yet, we have no explanation for why this occurs.

Figure 4.2b shows the run times of all the methods on a 3x3 grid environment. The figure shows that all other method out performed DRRRT. Due to the simplicity of this problem, RRT performs very well. This method can solve this environment by navigating around the edge and potentially only make one turn on the outer corners. While the other methods are navigating through the interior of the environment, forcing the planner to

make more turns through the obstacles. Another possible cause for slower performance of both variants of DRRRT is exploration of non-optimal paths. In the 3x3 Grid, there are many different paths to the goal. Some of these paths have more turns and cover a larger distance then other paths. These turns are difficult to plan because selecting the correct control to apply is time consuming or may not exist. For the maze, the paths that do not lead to the goal are trimmed from the embedded graph making exploration of those paths less likely.

The error bars show that there is an inconsistency when solving these kinds of problems. This can be attributed to our method getting into an unrecoverable state, that the SyCloP method avoids. A configuration is known as an unrecoverable when computing a successful extension is difficult. When these states are reached it becomes difficult to continue sampling and progression through the environment halts. For DRRRT, we intend to address this issue by introducing reachability guidance. This is discussed in Section 5.1.



Figure 4.2: On-line planning times comparing the new Dynamic Region-biased RRT with the original Dynamic Region-biased RRT, RRT, and SyCloP in two non-holonomic problems. The average run times of all methods over 33 runs. The error bars show the standard deviation.

	New-Dynamic Regions	Old-Dynamic Regions	SyCloP	RRT
GridMaze	100%	100%	100%	100%
3x3 Grid	100%	100%	100%	100%

Table 4.1: The success rates for each method on all environments.

The discrepancy between the expected and the observed outcomes could be attributed to an error in the correctness of our implementation or an algorithmic error in the overall ideas of our improvements. In either case, this leads to our future work which is discussed in the next section.

#### 5. CONCLUSION

In this paper we introduced modifications to Dynamic Region-biasing RRT which improves performance for non-holonomic systems. These modifications are: topological bucketing for neighborhood finding, a biasing method for sampling the velocities, and a weighting scheme for region selection. We also show how the embedding graph's properties can be extended to improve non-holonomic problems. We demonstrate how these changes are applicable to non-holonomic robots; however, results indicate that there are areas for improvement.

### 5.1 Further Study

In the future, we will investigate the causes of the poor running times. Specifically, bucketing improves neighborhood finding times, however it appears to have an adverse effect on the overall runtime. Another area for improvement is in velocity biasing. In addition to biasing the direction of a configuration's velocity we would like to dynamically adapt the velocity to the current speed of the robot and the expected extension distance. This extension distance can also be dynamically updated based on the speed of the robot and the size and direction of local embedding graph edges. Currently the extension distance is constant for each environment. However, many environments (especially cluttered spaces) can have different regions of the environment which would need different extension distances. For example, an environment could have one region where the free space is large and open, but another region with a narrow passage. In the former case a larger extension distance would allow the robot to explore this more open space quickly, while a short extension distance would allow more turning to navigate tighter spaces in the latter case.

Additionally, we plan to introduce reachability guidance [4] into Dynamic Region-

biasing RRT. In reachability guidance, we use the controls of the robot to define what is able to be reached by the vertex that is extending, also known as a reachable set. We will be working on a method to compute or approximate the reachable set in-order to improve the extensions and reduce the chances of getting into an unreachable state.

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