

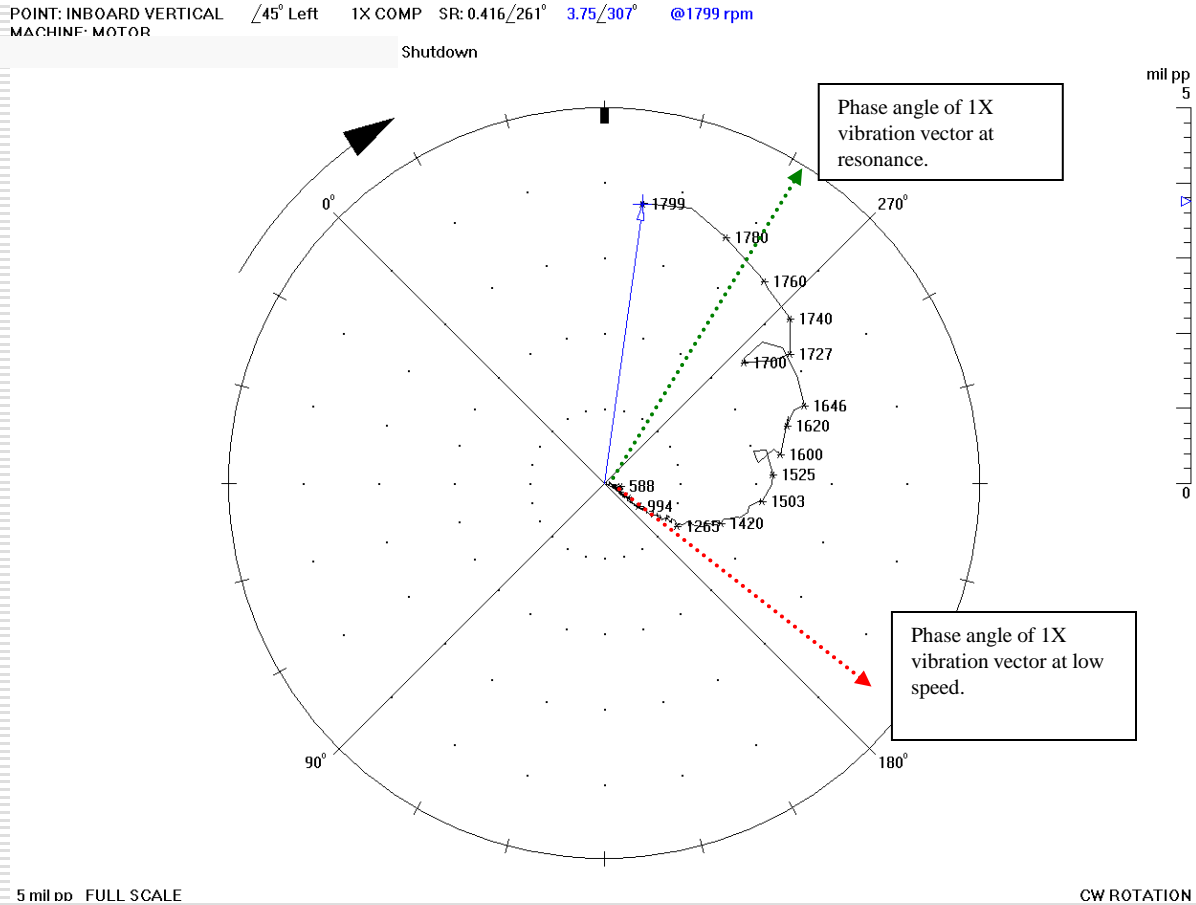
# Mechanical Behavior of a 9.7 MW Induction Motor Under Fault Conditions – A Case History

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# 1X Polar Plot – Shutdown – 45L

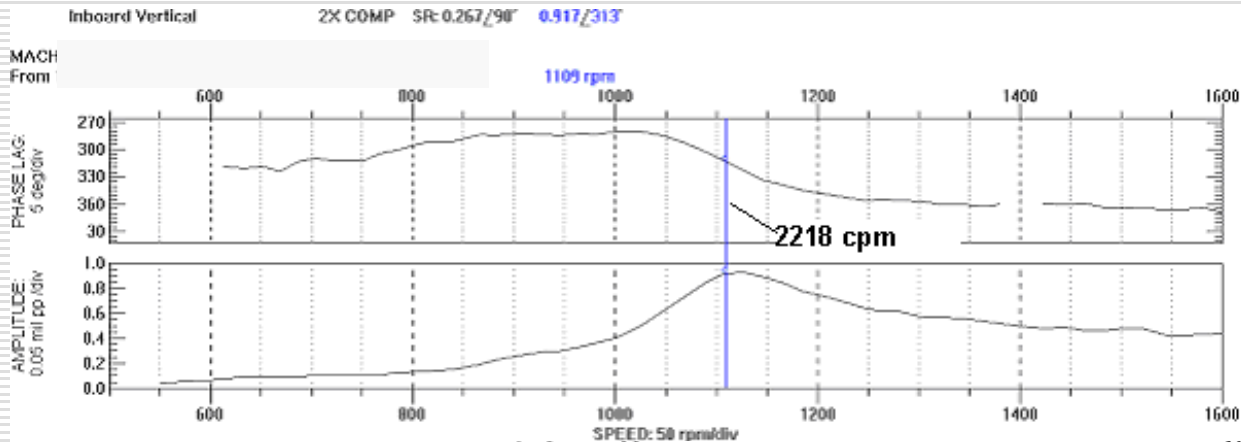


# 2X Bode Plot – Shutdown Data

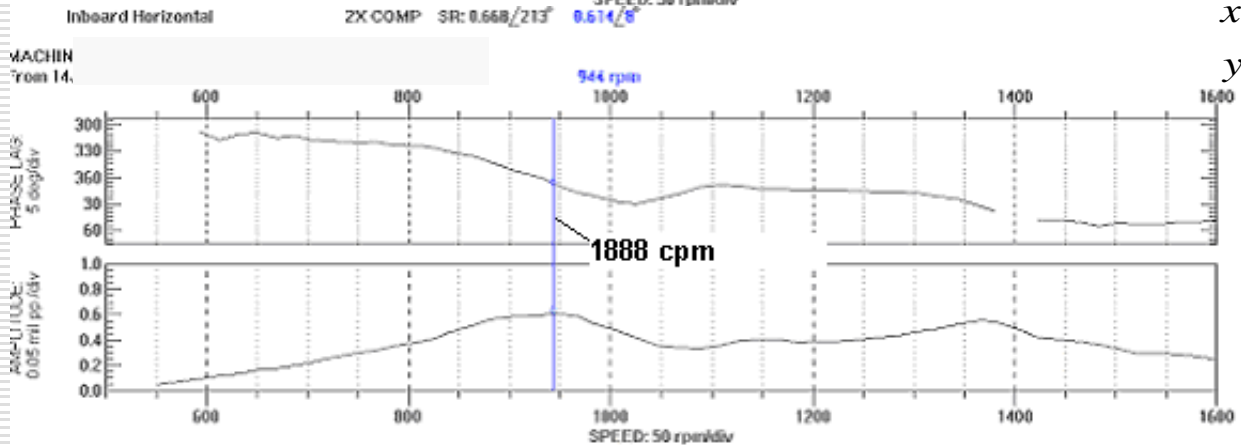
## Plot A = True Vertical

## Plot B = True Horizontal

Plot A



Plot B



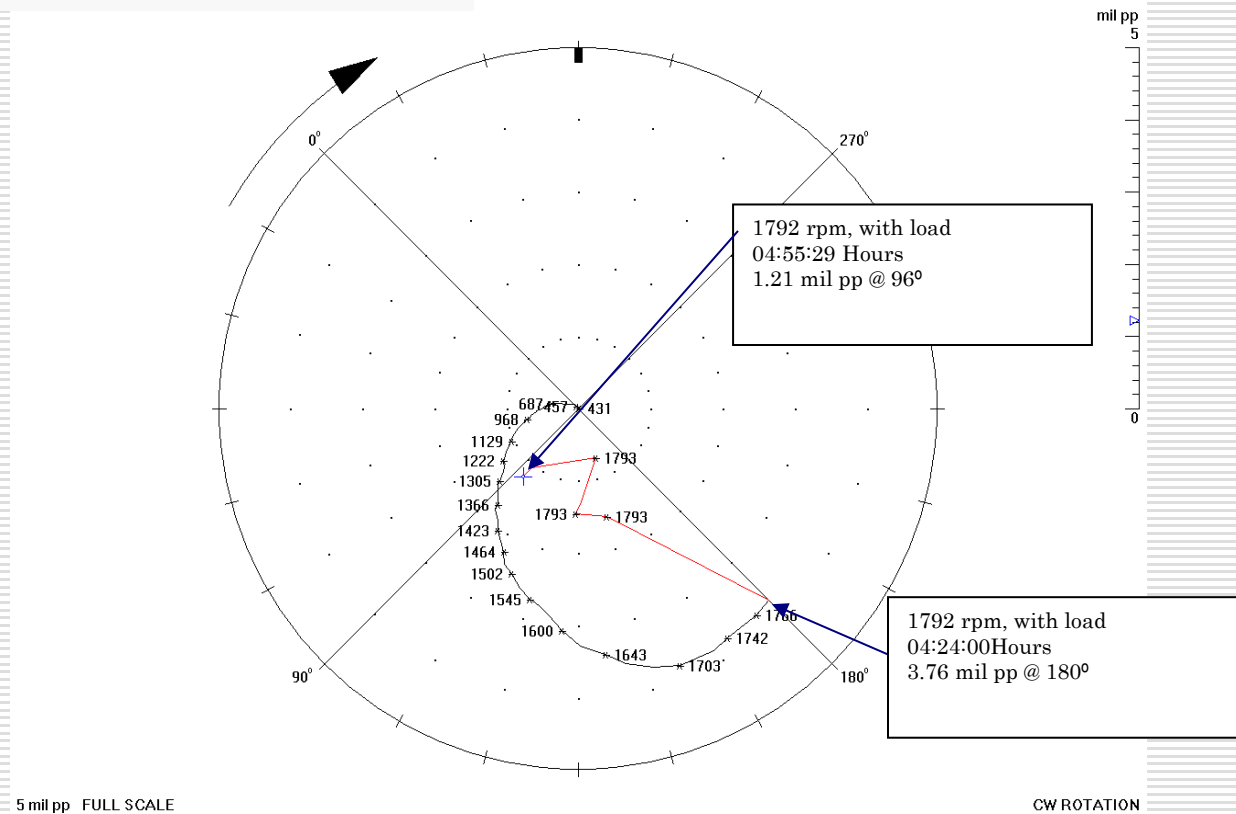
$$x = X \cos \theta + Y \sin \theta$$

$$y = -X \sin \theta + Y \cos \theta$$

A set of “virtual” transducers was created by mathematically transforming the actual vector data from two perpendicular probes at 45L and 45R via the following coordinate transform:

# Typical 1X Vector Response During Startup and First 30 Minutes of Steady State Operation

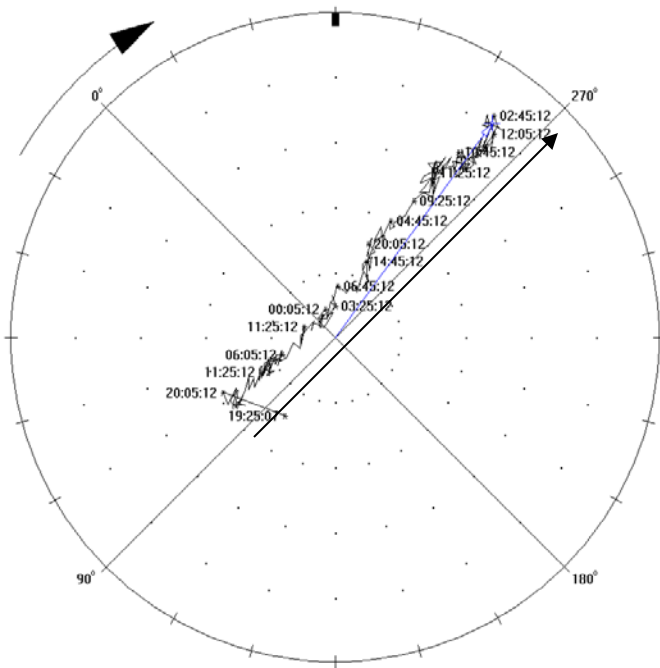
POINT: INBOARD VERTICAL /45° Left 1X COMP SR: 1.23/201° (man) 1.21/96° @1793 rpm



Thermal Vector = 3.83 mil pp @ 18°  
 Motor Coupled to Gearbox/Compressor  
 Under Load

# 1X Vector Change vs. Time

POINT: INBOARD VERTICAL /45° Left 1X COMP SR: 0.987/187° 4.08/279° @06:05:12  
MACHINE: MOTOR  
From 28JUN1991 19:25:07.1 To 05JUL1991 06:45:12.7 Shutdown



- ❑ Acceptance Region Trend Plot from 28 June – 5 July
- ❑ Depicts the change in the 1X vibration vector vs. time
- ❑ Similar vector changes occurred from:
  - 27 April through 14 June
  - 14 June through 21 June
  - 21 June through 28 June
  - 28 June through 5 July
  - 5 July through 14 July

1X Vector Change from 28 June Through 5 July =  
5.14 mil pp @ 272°

# FIELD BALANCING: 27 APRIL 1991

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$$\overrightarrow{\text{Vibration}} = \frac{\sum \vec{F}}{\sum \vec{K}}$$

# Influence Vector / Synchronous Dynamic Stiffness Vector

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$$\vec{H}_{average} = 0.015 \text{ milpp} / \text{gram} \angle 101^\circ$$

$$\frac{1}{\vec{H}_{average}} = \frac{\text{mass}}{\text{displacement}} \sim \frac{\text{force}}{\text{displacement}}, \text{ e.g. stiffness}$$

Multiply mass by  $r\Omega^2$  and divide by gravitational constant to convert from mass to force units.

# Influence Vector / Synchronous Dynamic Stiffness Vector

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$$\vec{K}_{DS} = \frac{1}{0.5\vec{H}} \times \frac{r\Omega^2}{g_c}$$

Where:

$\vec{H}$  = influence vector

$r$  = calibration mass radius, 12.5 in

$\Omega$  = Rotational speed, radians/second, 187.66 rad/sec

$g_c$  = Gravitational Constant;

386 (in - lb<sub>m</sub>)/(lb<sub>f</sub> - sec<sup>2</sup>),

or 1 (m - Kg)/(N - sec<sup>2</sup>)

Note: The factor of 0.5 is included in the denominator in order to convert mils pp to mils peak. Stiffness is usually defined such that both the force and the displacement units are 0 to peak, not peak to peak, with typical engineering units expressed as either lb<sub>f</sub>/in or N/m. The gravitational constant is necessary in order to **properly** convert from mass units to force units.



# Influence Vector / Synchronous Dynamic Stiffness Vector

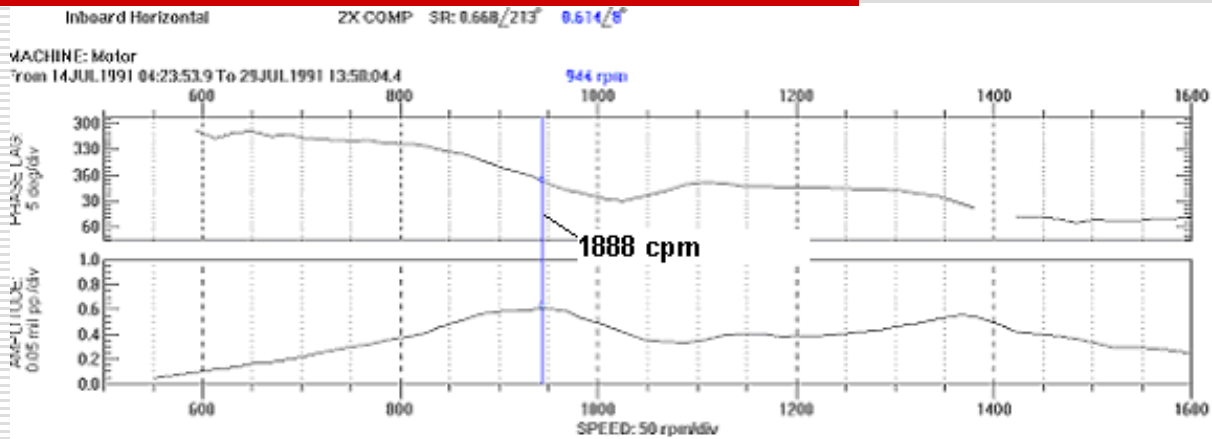
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$$\vec{K}_{DS} = \frac{1}{0.5\bar{H}} \times \frac{r\Omega^2}{g_c}$$

$$\vec{K}_{DS_{avg}} = \left[ \left( \frac{1}{0.0075 \text{ mil / gram @ } \angle 101^\circ} \right) \left( \frac{1 \text{ lb}_m}{454 \text{ grams}} \right) \times \left( \frac{1000 \text{ mil}}{1 \text{ in}} \right) \left( \frac{12.5 \text{ in}}{386 \text{ in-lb}_m / \text{lb}_f \text{-sec}^2} \right) \frac{(187.66 \text{ rad/sec})^2}{1} \right]$$

$$\vec{K}_{DS_{avg}} = 334,926 \text{ lb}_f / \text{in}$$

# Dynamic Stiffness / Rotor Resonance



$$\Omega_{res} = \sqrt{K_{DS} / M} \qquad \Omega_{res} = \sqrt{\frac{334,926 \text{ lb}_f / \text{in} \left( 386 \text{ in-lb}_m / \text{lb}_f \text{-sec}^2 \right)}{4200 \text{ lb}_m}}$$

$$\Omega_{res} = 175.4 \text{ rad/sec}$$

$$\Omega_{res} = 27.9 \text{ rev/sec}$$

$$\Omega_{res} = 1675 \text{ rev/min}$$

# FIELD BALANCING:

## 14 June

- Seven weeks later, on Friday, 14 June, the Wet Gas Compressor Train was shut down due to high motor 1X vibration readings

$$\vec{H}_{1,1} = \frac{\vec{C}_A}{W_A} \quad ?$$

$$\text{Increase in } \vec{Vibration} = \frac{\sum \vec{F}}{\sum K} \text{ due to:}$$

$$\vec{K}_{DS} = \frac{1}{0.5H} \times \frac{r\Omega^2}{g_c} \quad ?$$

$$\Omega_{res} = \sqrt{K_{DS} / M} \quad ?$$

# What Do We Know?

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- Significant changes in the 1X steady state vibration response occurred from 14 June through 14 July
- Five subsequent balance corrections required after the initial in situ field balancing on 27 April:
  - 14 June
  - 21 June
  - 28 June
  - 5 July
  - 14 July

## Balance Summary Data: April 27 - July 14, 1991

Run No.	Data Type	Date	Day of the Week	Elapsed Time	Speed (rpm)	BP	Mass Added (gms)	Mass Angle	+	Outboard 45L (vertical xducer) (mil pp @ Φ)	Outboard 45R (horz xducer) (mil pp @ Φ)	Inboard 45L (vertical xducer) (mil pp @ Φ)	Inboard 45R (horz xducer) (mil pp @ Φ)
1	Initial	27-Apr-91	Saturday	0 Days	1792	A	118	300°	+	2.90 @ 225°	0.70 @ 346°	3.80 @ 211°	1.90 @ 325°
	Final	27-Apr-91				B	118	300°	+	0.30 @ 4°	0.50 @ 99°	0.60 @ 151°	0.40 @ 307°
2	Initial	14-Jun-91	Friday	48 Days	1792	A	130	15°	+	4.17 @ 313°	1.84 @ 69°	4.16 @ 302°	2.08 @ 46°
	Final	14-Jun-91				B	130	15°	+	0.52 @ 340°	0.44 @ 106°	0.56 @ 234°	0.72 @ 338°
3	Initial	21-Jun-91	Friday	7 Days	1792	A	150	0°	+	4.32 @ 289°	1.98 @ 42°	3.77 @ 280°	2.10 @ 39°
	Final	21-Jun-91				B	150	0°	+	0.88 @ 137°	0.22 @ 212°	1.44 @ 165°	1.36 @ 293°
4	Initial	28-Jun-91	Friday	7 Days	1792	A	179	330°	+	4.50 @ 269°	1.36 @ 15°	5.07 @ 258°	2.50 @ 350°
	Final	28-Jun-91				B	179	330°	+	1.11 @ 72°	0.51 @ 182°	1.14 @ 113°	1.26 @ 263°
5	Initial	5-Jul-91	Friday	7 Days	1792	A	159	345°	+	3.86 @ 281°	1.19 @ 22°	4.10 @ 266°	1.93 @ 345°
	Final	5-Jul-91				B	159	345°	+	0.73 @ 184°	0.45 @ 182°	1.69 @ 178°	1.93 @ 190°
6	Initial	14-Jul-91	Sunday	9 Days	1792	A	160	315°	+	3.23 @ 240°	1.25 @ 334°	3.85 @ 224°	2.39 @ 315°
	Final	14-Jul-91				B	160	315°	+	0.79 @ 123°	0.60 @ 245°	1.49 @ 149°	2.02 @ 268°

## Balance Summary Data Sheet

Notes:

- BP = Balance Plane; A=Outboard; B= Inboard
- The "+" sign = mass added
- The "-" sign = mass removed
- All vibration data is shaft relative displacement data
- Mass added at a 12.5 inch balance radius
- Mass angle is referenced to the 45L (vertical) transducer

# 1X Vector Change vs. Time

<b>CHANGE IN 1X VIBRATION VECTOR vs TIME</b>					
<b>From</b>	<b>To</b>	<b>Outboard 45L (vertical xducer) (mil pp @ <math>\Phi</math>)</b>	<b>Outboard 45R (horz xducer) (mil pp @ <math>\Phi</math>)</b>	<b>Inboard 45L (vertical xducer) (mil pp @ <math>\Phi</math>)</b>	<b>Inboard 45R (horz xducer) (mil pp @ <math>\Phi</math>)</b>
27-Apr-91	14-Jun-91	3.99 @ 310°	1.43 @ 59°	4.69 @ 306°	2.18 @ 56°
14-Jun-91	21-Jun-91	4.01 @ 283°	1.83 @ 30°	3.40 @ 287°	1.86 @ 59°
21-Jun-91	28-Jun-91	5.13 @ 276°	1.57 @ 17°	5.34 @ 274°	2.10 @ 23°
28-Jun-91	5-Jul-91	4.86 @ 275°	1.68 @ 16°	5.14 @ 272°	2.15 @ 20°
5-Jul-91	14-Jul-91	2.89 @ 252°	1.66 @ 341°	2.94 @ 248°	3.84 @ 339°
<b>TOTAL 1X VECTOR CHANGE vs TIME</b>					
27-Apr-91	14-Jul-91	19.97 @ 280°	7.45 @ 20°	11.20 @ 294°	10.35 @ 20°

Table 2

# Conclusions

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- Analysis of field balancing data in order to determine the Influence and Synchronous Dynamic Stiffness properties of the rotor / bearing system provides powerful insight into the origin(s) of a change in rotor vibration.
- Coupled with other forms of direct and indirect data, operating risks are minimized and the proper machinery asset management is provided.
- Synchronous perturbation is an inherent part of every field balancing exercise.
- By synchronously perturbing the rotor system with a know centrifugal force, the response of the system to the synchronous perturbation force can be directly measured.
- Since the rotor response (vibration) is always equal to the summation of the dynamic forces that act on the rotor / bearing system divided by the complex dynamic stiffness of the system, it becomes apparent that an increase in rotor vibration may be due to:
  - An increase in the dynamic forces
  - A decrease in the complex dynamic stiffness
  - Both
- From this information, both the Synchronous Dynamic Stiffness and Influence Vectors can be determined.
- Along with other direct and indirect (calculated) forms of machinery data, both the Synchronous Dynamic Stiffness and Influence Vectors are evaluated and trended over time.