



43rd Turbomachinery 30th Pump SYMPOSIA

GEORGE R. BROWN CONVENTION CENTER
HOUSTON, TX | SEPT. 22 - 25, 2014

COUPLED TORSIONAL-LATERAL ANALYSIS

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Consulting



Outline

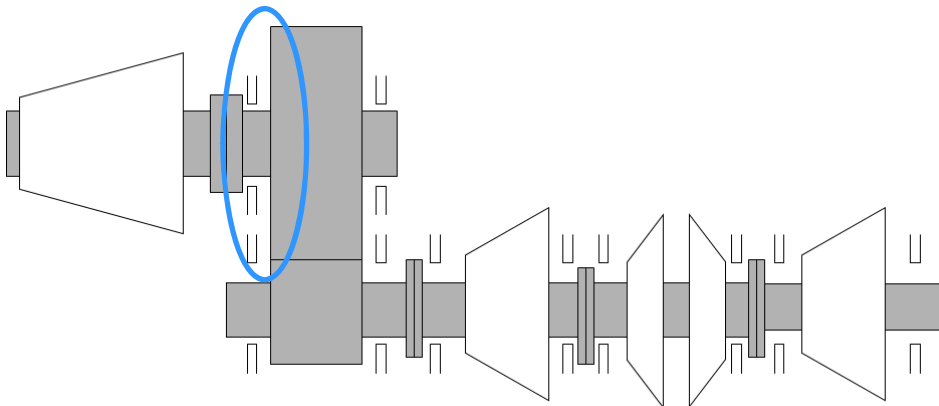
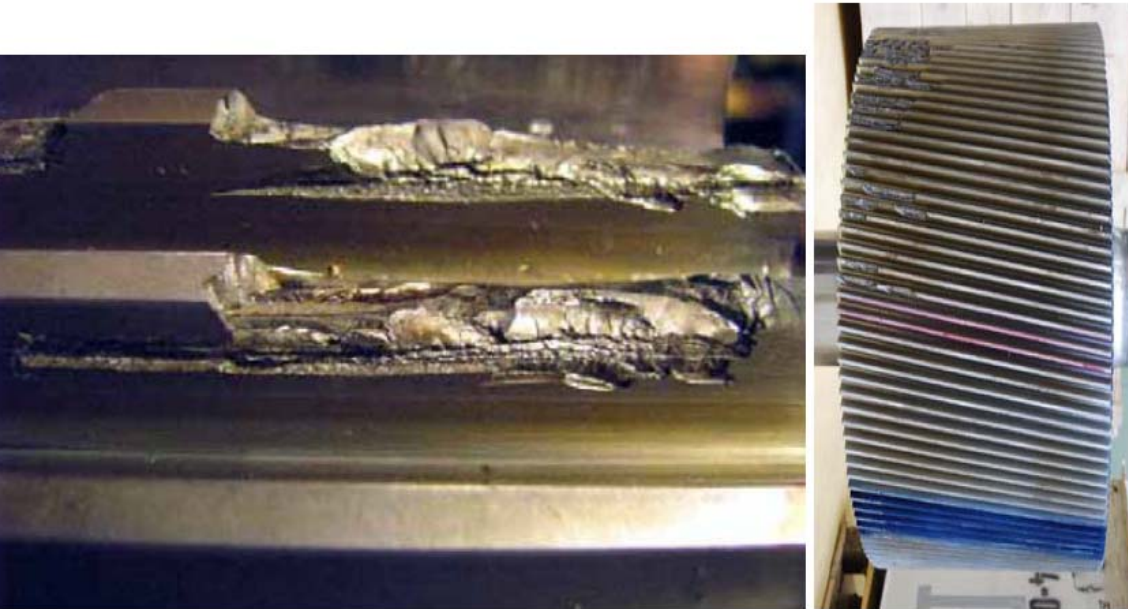
- Background
- Measurements on gear casing
- Calculations
 - Static
 - Dynamic
- Comparing measurements
- Discussion

Background

- North sea platform production modification
- Two compressor trains were upgraded from 18 MW -> 21 MW
- Main modifications:

| Property | Modified | Original |
|-----------------|----------------|----------------|
| Power [MW] | 21.30 | 18.25 |
| Speed in [rpm] | 3600 | 3600 |
| Speed out [rpm] | 10718 | 10894 |
| Module | 5.6 | 6.4 |
| Z1 | 44 | 38 |
| Z2 | 131 | 115 |
| Type | Single helical | Single helical |

Background



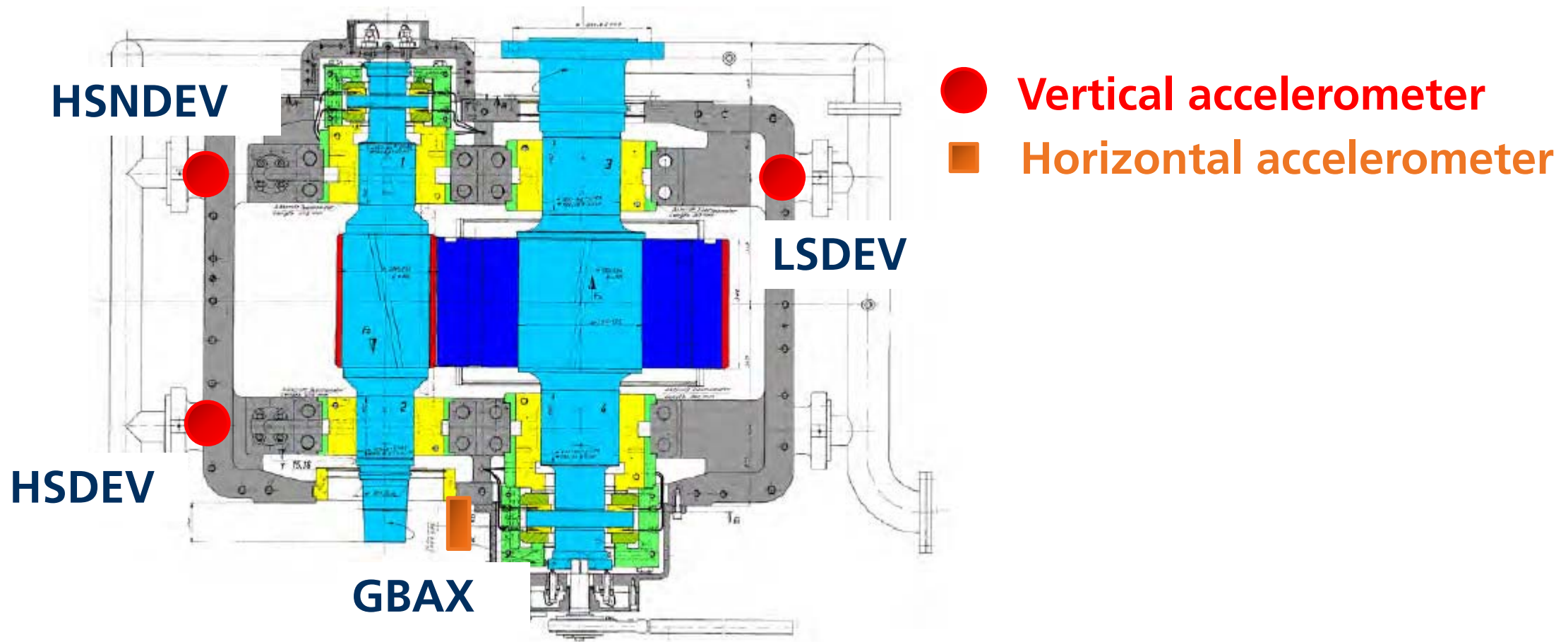
Problems encountered:

- Two consecutive gearbox failures within few weeks after commissioning
- ~ 500-1000 operating hours before failure
- Severe gearbox casing vibrations and excessive noise levels recorded
- Turbine side on bull gear experienced fractured teeth and cracks on the load surfaces

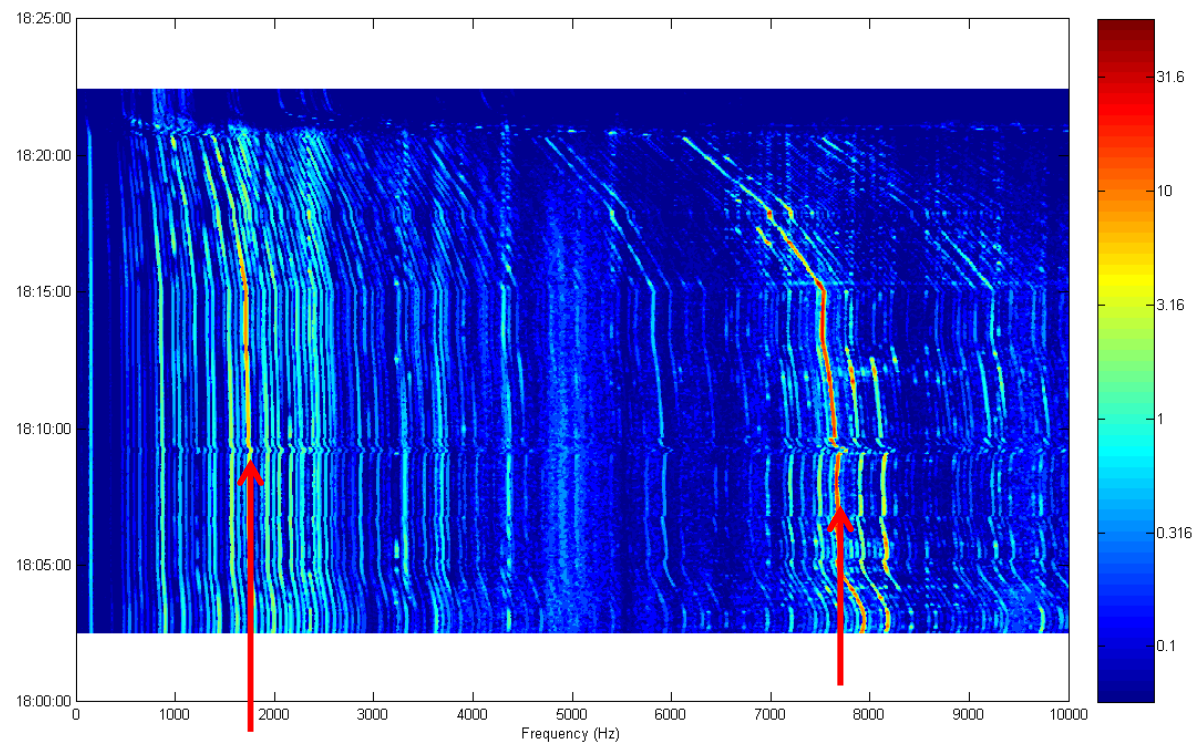
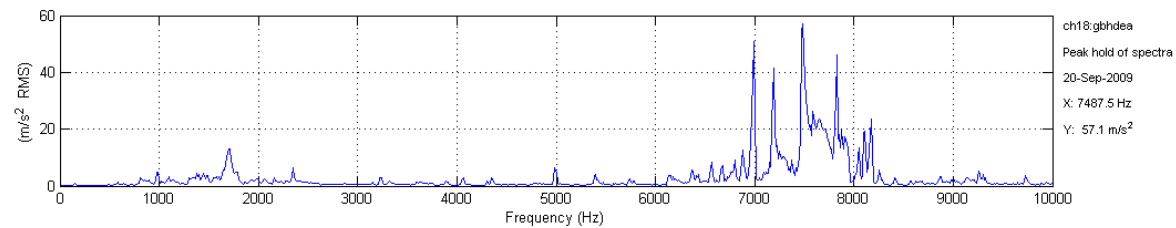
Actions taken:

- Full RCA initiated. This concluded poor final grinding as primary cause of failures
- Contributory causes had to be investigated as part of the RCA
- Torsional/Lateral vibration analysis was initiated by LRC as part of the RCA

Measurements



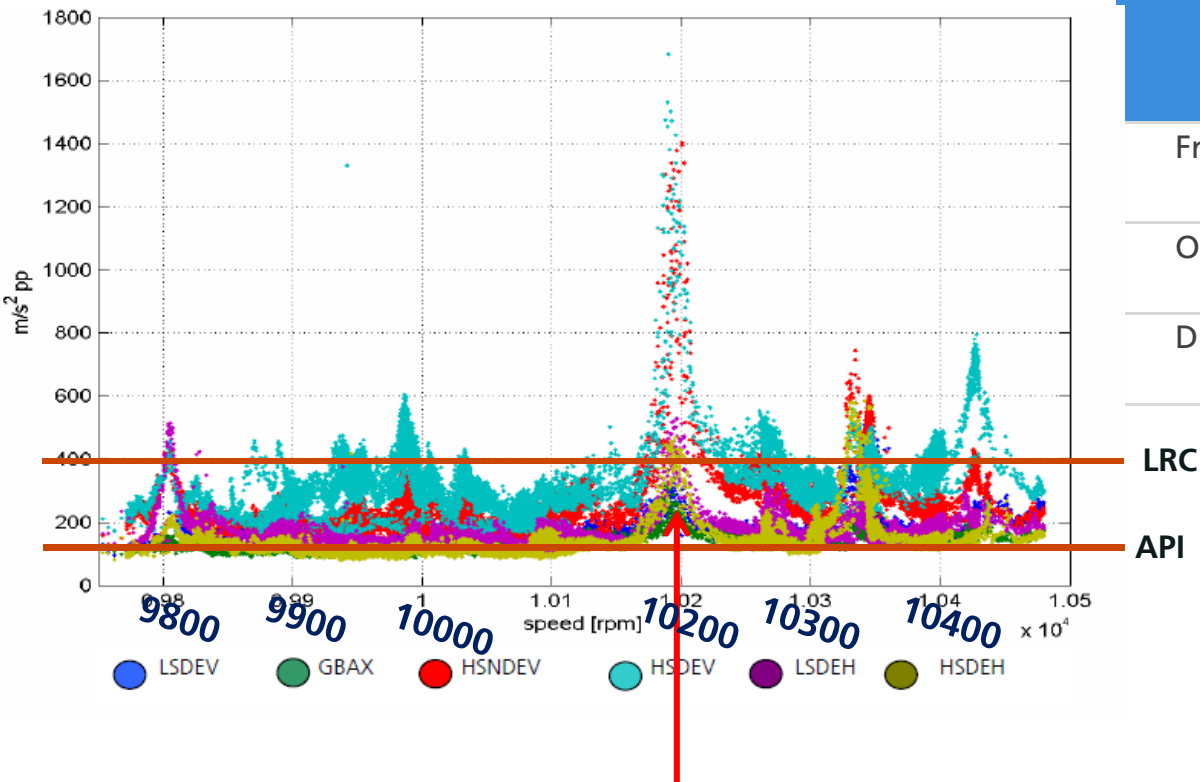
Measurements



~1700 Hz

Gear mesh frequency (7000-8000 Hz)

Measurements



Requirements

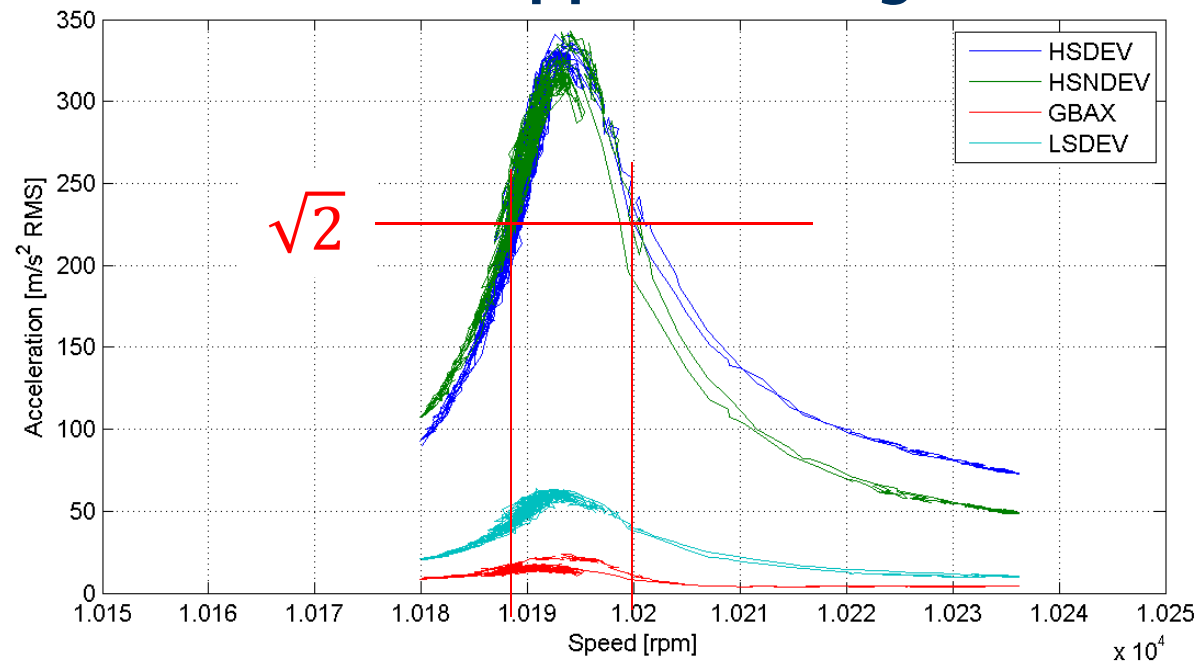
| API613 5 th Ed. | Velocity (RMS) | Acceleration (P-P) |
|----------------------------|----------------|------------------------------------|
| Frequency range | 10 – 2500 Hz | 2500 – 10 000 Hz |
| Overall | 2.9 mm/s | 8 g (~ 80 m/s ²) |
| Discrete frequency | 1.8 mm/s | - |

10200 rpm = GMF @ 7480 Hz
Levels up to 1600 m/s² (~ 160 g) p-p

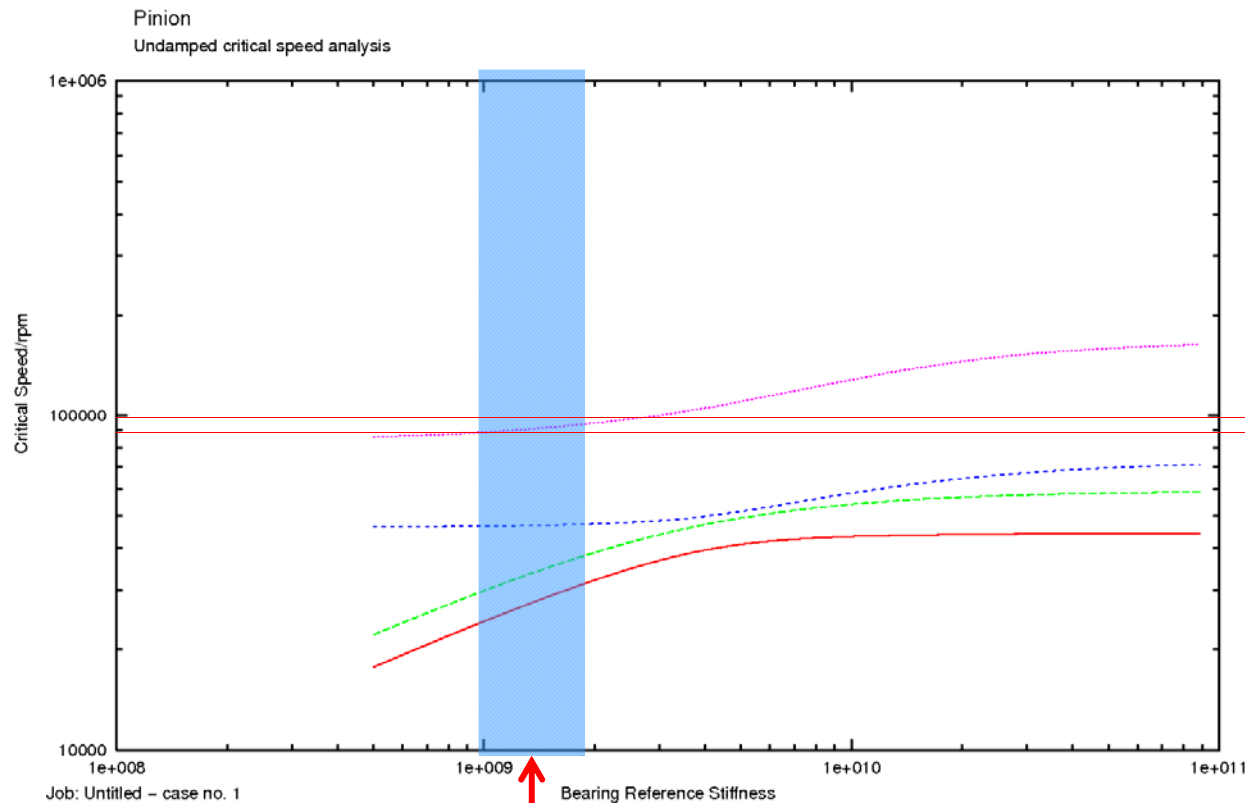
Measurements

**Amplification factor
 $Q \approx 700$**

44X filter applied on signal



Pinion mode excitation



Bearing stiffness range
~1 – 2.5 E+9 N/m
(~6 - 14 E+7 lb/in)

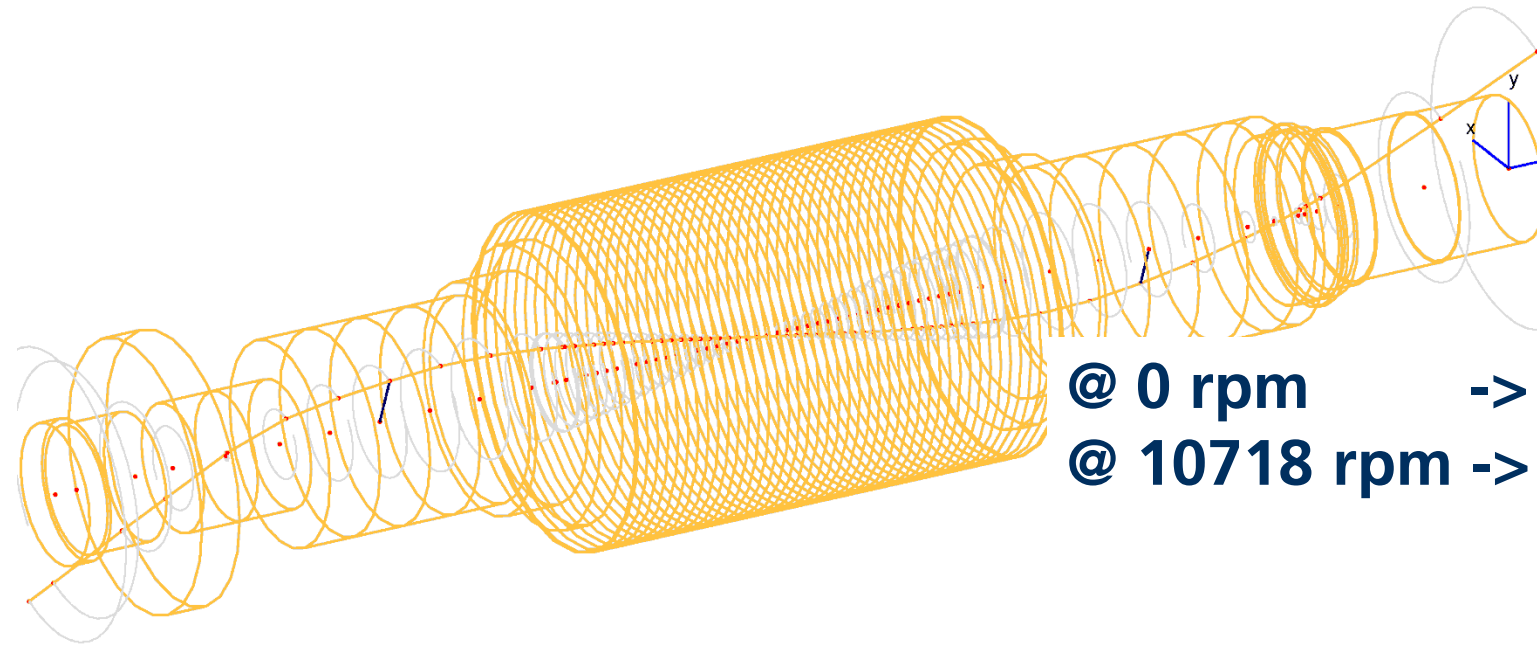
88000 – 97000 cpm
(1470 – 1620 Hz)

1X = 10 718 rpm
8X = 85 744 rpm
9X = 96 462 rpm
10X = 10 7180 rpm

Pinion mode excitation

Damped eigenvalue analysis
elements, nodes , mode no. 8: 1313.8 Hz, log. dec = -6.149
Speed: 10718 (1)

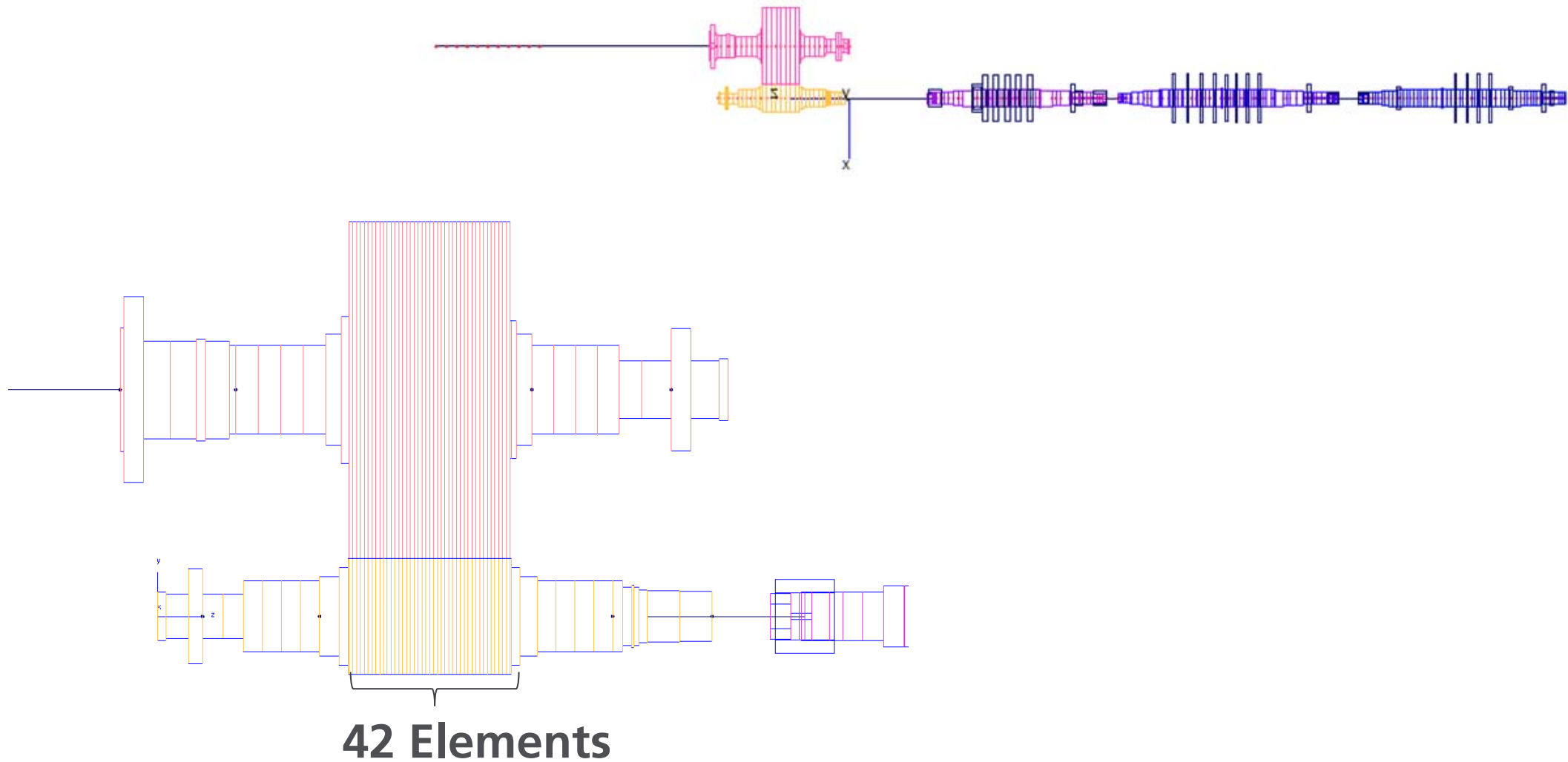
Pinion



@ 0 rpm -> 77 460 cpm (1291 Hz)
@ 10718 rpm -> 78 840 cpm (1314 Hz)

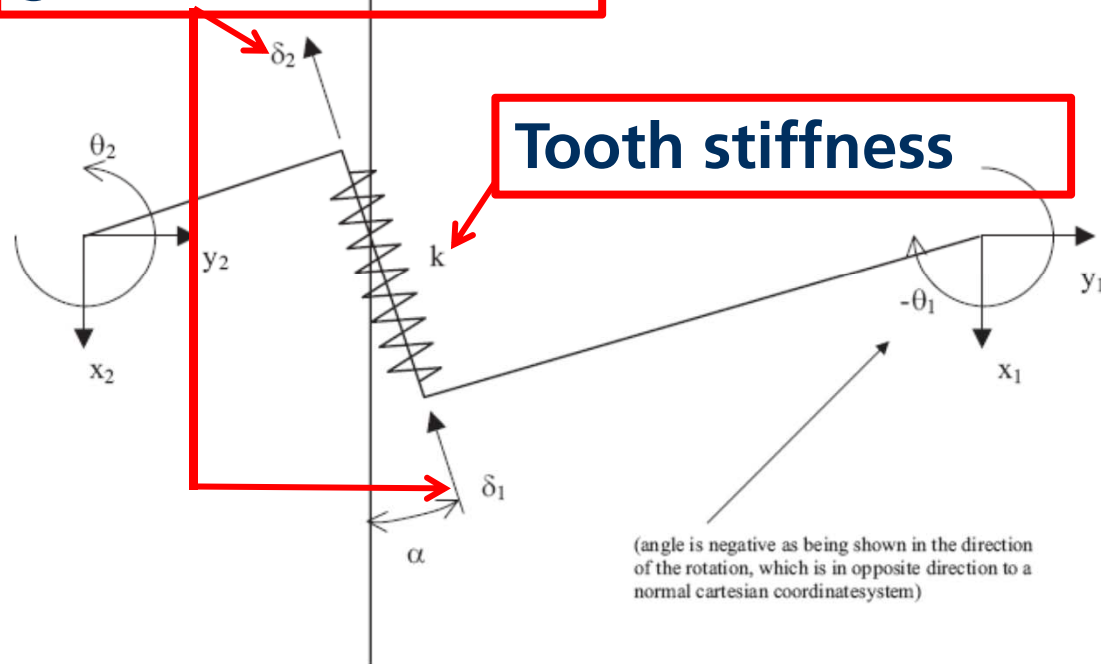
1X = 10 718 rpm
7X = 75 026 rpm
8X = 85 744 rpm
9X = 96 462 rpm
10X = 10 7180 rpm

Torsional-Lateral Calculations

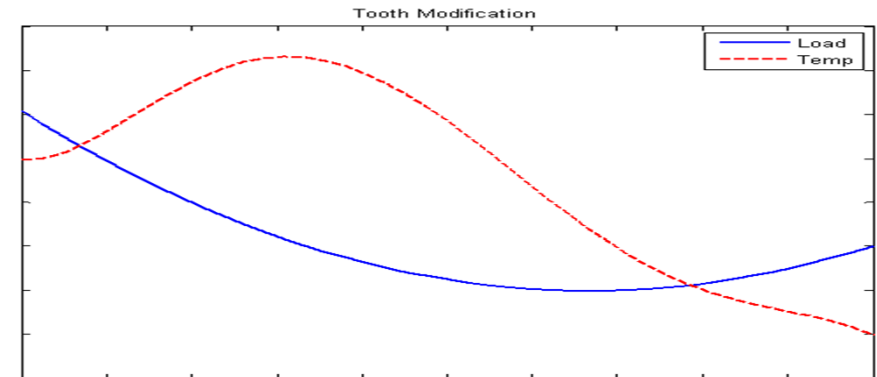


Torsional-Lateral Calculations

Displacement in gear contact



Tooth stiffness



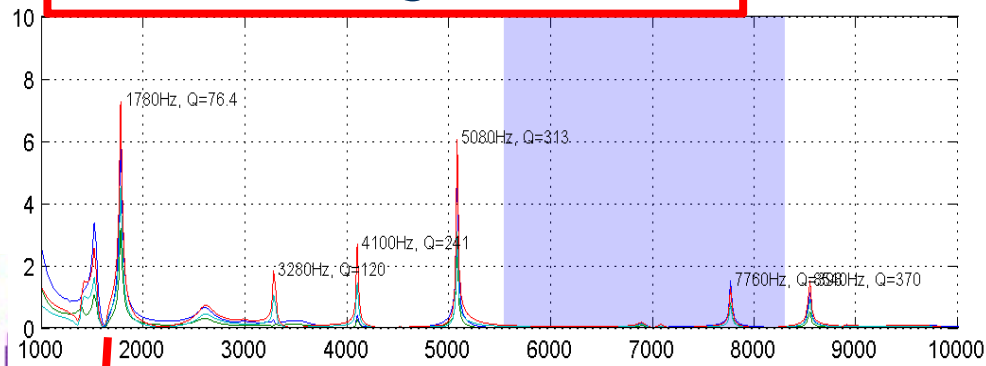
$$\delta_1 = -r_1\theta_1 - x_1 \cos(\alpha) - y_1 \sin(\alpha)$$

$$\delta_2 = r_2\theta_2 - x_2 \cos(\alpha) - y_2 \sin(\alpha)$$

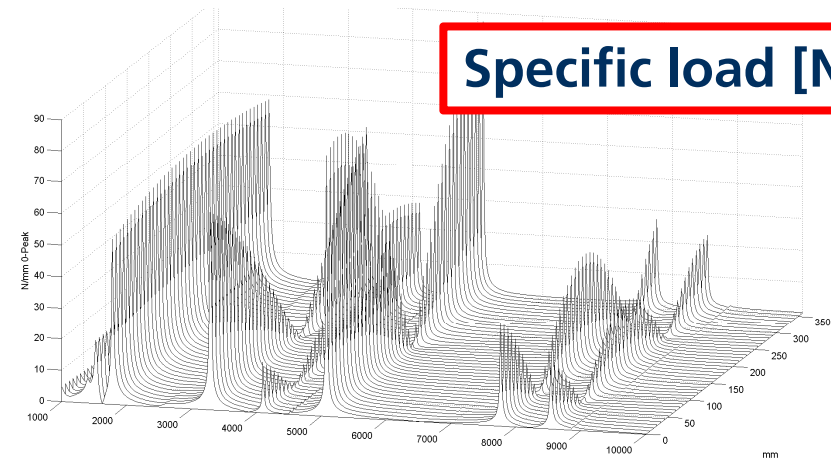
$$P_i = \begin{cases} k(\delta_{1i} - \delta_{2i} - \delta_{ci}) & \delta_{1i} - \delta_{2i} > \delta_{ci} \\ 0 & \delta_{1i} - \delta_{2i} \leq \delta_{ci} \end{cases} \quad i = 1..43$$

Results – Dynamic calculations

Pinion bearing force [N]



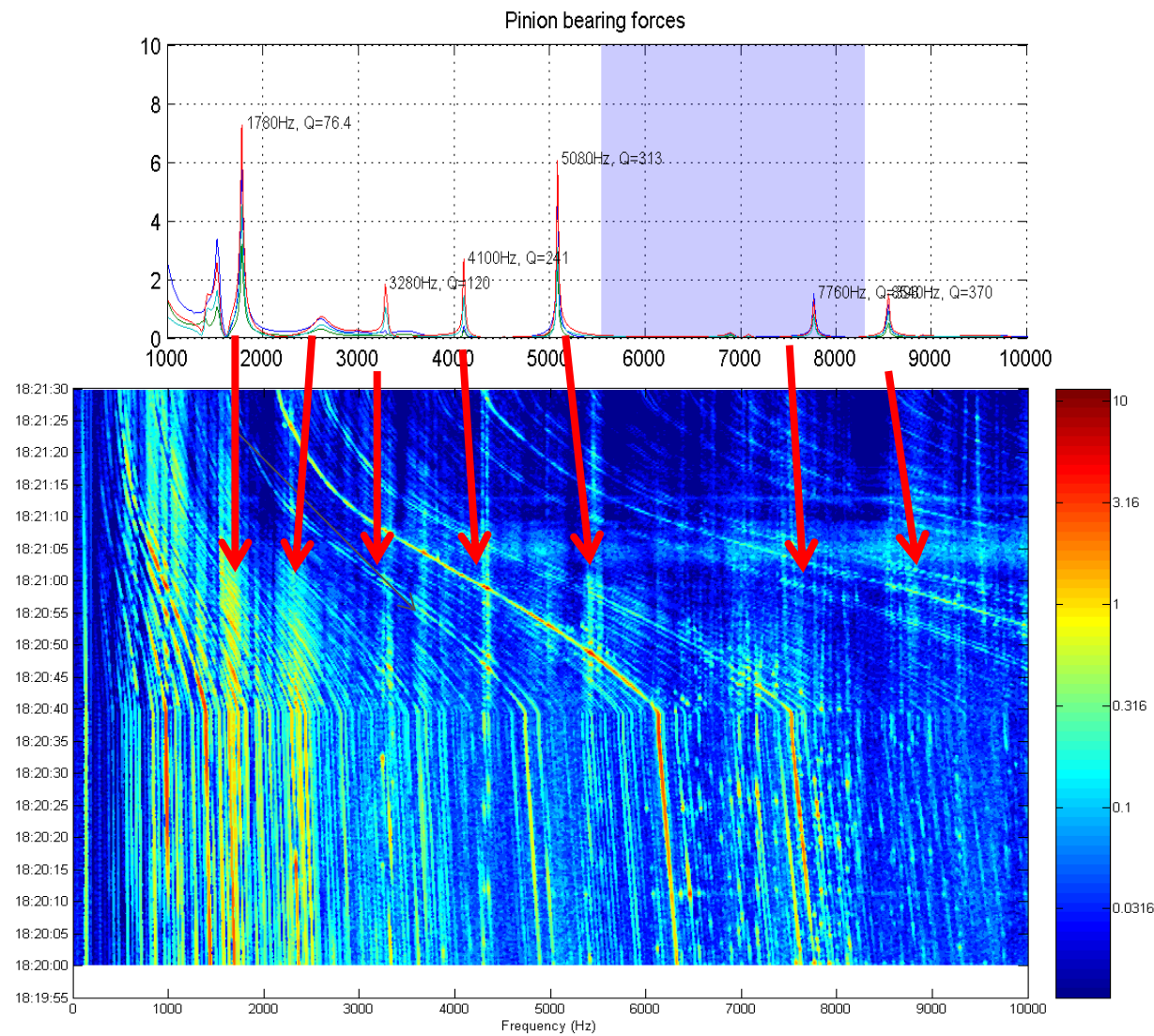
Specific load [N/mm]



1780 Hz

7760 Hz

Comparing with measurements



Conclusions

- The primary cause of failures was residual stress in tooth flanks from the manufacturing process. Contributory causes (such as torsional/lateral analysis) were investigated as part of the RCA.
- Spare gear set was sent onshore for a second “final grinding” to remove residual stress on the load flanks.
- The presented calculations were tuned with measurements from before and after modifications. The resulting loads were input to load flank fatigue calculations by the vendor.
- Fatigue calculations from before and after the machining could prove that the load flank fatigue life improved with the second grinding.
- Gear boxes are still in operation with no reported issues since commissioning March 2010 and June 2012 for the two trains, respectively.

Questions?

