

AN INTELLIGENT HUMAN-TRACKING ROBOT BASED-ON KINECT SENSOR

A Thesis

by

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## ABSTRACT

This thesis provides an indoor human-tracking robot, which is also able to control other electrical devices for the user. The overall experimental setup consists of a skid-steered mobile robot, Kinect sensor, laptop, wide-angle camera and two lamps. The Kinect sensor is mounted on the mobile robot to collect position and skeleton data of the user in real time and sends it to the laptop. The laptop processes these data and then sends commands to the robot and the lamps. The wide-angle camera is mounted on the ceiling to verify the tracking performance of the Kinect sensor. A C++ program runs the camera, and a java program is used to process the data from the C++ program and the Kinect sensor and then sends the commands to the robot and the lamps. The human-tracking capability is realized by two decoupled feedback controllers for linear and rotational motions. Experimental results show that although there are small delays (0.5 s for linear motion and 1.5 s for rotational motion) and steady-state errors (0.1 m for linear motion and  $1.5^\circ$  for rotational motion), tests show that they are acceptable since the delays and errors do not cause the tracking distance or angle out of the desirable range ( $\pm 0.05\text{m}$  and  $\pm 10^\circ$  of the reference input) and the tracking algorithm is robust. There are four gestures designed for the user to control the robot, two switch-mode gestures, lamp crate gesture, and lamp-selection and color change gesture. Success rates of gestures recognition are more than 90% within the detectable range of the Kinect sensor.

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## CHAPTER I

### INTRODUCTION AND LITERATURE REVIEW

Electronic devices are ubiquitous these days. With the development of computer vision technology and depth cameras, the ways people interact with the electrical devices are being improved. Low-cost depth cameras have been researched for years with newly available techniques, and the development of software and algorithms for them enhances their functions. The release of low-cost depth cameras allows more and more people to enjoy the benefit of this technology.

#### **1.1 Design objectives**

The objective of this thesis is to develop a human-tracking intelligent robot to improve the way that humans interact with electronic devices. This robot is designed mainly for the household and is capable of doing the following:

1. Tracking the designated person quickly and smoothly on a flat wooden floor or carpet, maintaining a safe distance to that person
2. Recognizing specific predetermined postures by the person being tracked quickly and accurately
3. Controlling other electronic devices wirelessly based on the motion-commands by the person being tracked.

#### **1.2 Human tracking**

There are several sensors that can be used for human tracking. Ultrasonic sensors

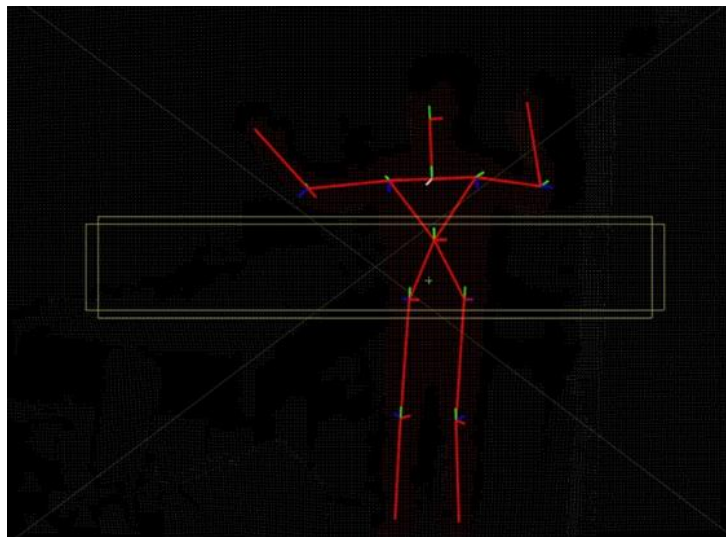
transmit and receive ultrasonic waves and determine the distance to an object by calculating the time interval between sending the signal and receiving the echo. They are used to track a human and avoid obstacles by developing an ultrasonic-sensor array [1]. However, ultrasonic sensors cannot distinguish humans from objects. RGB cameras, which can deliver the three basic color components (red, green, and blue), are frequently used some image processing software for object detection and tracking. For example, OpenCV, Matlab, and Point Cloud Library (PCL) can be used for image processing. However, 3D motion sensors (or depth sensors) are very likely to supersede other sensors in human tracking due to their reliability and depth sensing ability.

A 3D motion sensor is a device that can capture motions in 3D [2], [3]. There are two popular commercial 3D motion sensors, Kinect from Microsoft and Xtion PRO Live from Asus. The Kinect sensor has high resolution (1–75mm) [4] and is more adaptable than the Xtion PRO Live. Human-tracking is easy to realize with 3D motion sensors because they usually come with a software development kit (SDK) that processes color, depth, and skeleton data. With these data, it is convenient to create human-tracking applications.

### **1.3 Gesture recognition**

Gesture recognition is an application based on skeleton tracking. Skeleton tracking is a key function of the 3D motion sensor that allows the sensor to recognize humans. As shown in Figure 1-1, a human is being tracked by a Kinect sensor, and his skeleton image with a coordinate in each joint is shown on the computer monitor in real time. By locating these joints, the distance between of two joints and the angle of three

joints can be calculated. While a specific gesture has a certain distance between two joints and angle ranges of three joints, gesture recognition can be realized by setting the combination of angle ranges and distance between these joints and defining them. For the Kinect sensor, up to six people can be recognized and up to two people can be tracked in detail within the detectable field of the sensor.



**Figure 1-1 Skeleton image shown on a computer while a human is being tracked**

## **1.4 Applications**

Motion-control techniques are applied in a variety of areas listed below.

### **1.4.1 Home entertainment**

The Xbox 360 Kinect Sensor may not be the first application of motion control

but must be the most popular application. The Xbox 360 Kinect Sensor is a motion sensing input device by Microsoft for the Xbox 360 video game console. Based on a Kinect sensor for the Xbox 360 console, it enables users to control and interact with the console without touching any game controller, only through a natural user interface using gestures and spoken commands.

**1.4.2 Automotive**

Toyota has unveiled the ‘Smart Insect’ concept at CEATEC technology show 2012 in Japan. The fully electric car, as shown in Figure 1-2, is decked out with a Kinect sensor by Microsoft. The on-board motion sensors allow the car to recognize its owner based on face and body shapes and predict the owner's behavior by analyzing movement. For example, it can detect the approaching of the owner and determine when to open the door.



**Figure 1-2 Toyota’s fully electric car equipped with Kinect sensors [5]**

The front and rear displays are set to show a welcome message when the owner approaches the car. The car is equipped with a speaker on the hood of the car and dashboard-mounted microphones on the front and back, so voice recognition is also included for opening the car door and other functions [5].

Mercedes' Dynamic & Intuitive Control Experience (DICE) built a concept cabin by installing a series of proximity sensors to detect arm and hand movements. With those sensors users can control everything from music, navigation, and social functionality to a heads-up display that comprises the entire windshield [6], as shown in Figure 1-3.



**Figure 1-3 Mercedes-Benz gesture-control concept [6]**

### **1.4.3 Television**

TCL Multimedia (TCL), one of China's leading TV and consumer electronics



brands, begins to use Hillcrest's Freespace motion software for its Smart TVs. The Freespace gesture recognition engine enables motion, gesture, and cursor control for the user to navigate and interact with the smart TV content. It includes the TV menus, Web browser, games, and a wide variety of applications [7].

#### **1.4.4 Mobile devices**

Depth sensors are also applied in mobile devices. Earlier this year, Google introduced its Project Tango smartphone, a mobile device equipped with a depth sensor, a motion tracking camera, and two vision processors that enable the phone track its position in space and create 3D maps in real time [8]. The device is not only a phone but also a good sensor for robot since it is the base capability for most of the robots to navigate and locate themselves in the real world.

### **1.5 Thesis overview**

The thesis consists of six chapters: Introductions, Design and System Architecture, Control System Design, Human-Robot Interaction Design, Simulation and Experimental Results, Conclusions and Future work.

The thesis begins with the first chapter, giving an introduction to human-tracking mobile robot and applications. This introduction also covers thesis overview and significance of thesis contributions.

In the second chapter, the hardware and software components of the system are described. This chapter presents the function of each hardware and software components and clarifies how they work with each other.

The third chapter details the control system design. In this chapter, a mathematical model is derived and analyzed. Based on these analyses, two proportional-integral-derivative (PID) controllers and a lead-lag compensation are designed. Finally, all these controllers are simulated and evaluated.

The fourth chapter introduces the design of human-robot interaction. This chapter mainly describes the functions expected from the mobile robot and how they are coded.

The fifth chapter describes the experiments designed for both human tracking and gesture recognition. Along with this, the experimental results are also given and discussed.

The final chapter entails the conclusions of the thesis and provides an insight into the experiments with suggestions for improvements.

## **1.6 Thesis contributions**

A structure was built on the mobile robot by Enrique Zarate, a former undergraduate student in our lab, to carry the Kinect sensor. A mathematical model was developed by identifying necessary parameters. The robot's motions were decoupled into linear motion and rotational motion. Based on this model, a proportional-integral-derivative (PID) controller was designed for the rotational motion control, and a PID, lead, lag, and a lead-lag controllers were designed for the linear motion control. A wide-angle camera was installed on the ceiling of the lab. A C++ program was written to process the video stream of the camera and track the position of the user and the robot. Two lamps controlled by Arduino boards were developed. Java programs were written for the Arduino boards. The Kinect sensor was used to obtain 3D position data and

skeleton data of the user being tracked. A Java program was written to process these data from the Kinect sensor and the camera and then send commands to the Arduino board. The controllers were implemented in the main Java program to process these position data. Gestures to command the robot were designed and included in the main Java program. Experiments were conducted to evaluate the performance of the tracking ability and the gesture recognition of the robot.

## CHAPTER II

### DESIGN AND SYSTEM ARCHITECTURE

In this chapter, the hardware and software of the robot are introduced, and then the functions of these components and how they work with each other are clarified.

#### **2.1 Hardware components**

##### **2.1.1 Skid-Steered mobile robot**

Skid-steered mobile robots are widely used due to their robust mechanical structure and high maneuverability. Although much research was conducted on dynamic modeling and tracking control of differential-driven mobile robots, not as much research has been done on skid-steered mobile robots. A kinematic model for an ideal differential-driven wheeled robot cannot be categorized as a skid-steered robot because the effects of skidding and slipping of robot wheels are minimal. Recently, many researchers developed mathematical models of skid-steered mobile robots, considering the effect between wheels and the ground. Yi et al. [9] proposed a pseudo-static friction model. Although a skid-steered mobile robot usually assumes all wheels on the same side share the same speed, a dynamic model with different angular velocities of four wheels was developed [10]. In [11], the kinematic model included the effects of slippage without dynamics computations in the loop. In this research, a model proposed in [12] was simplified and adopted since the model in that paper is described in terms of the

angular velocity of the wheels, which is beneficial and easy for control.

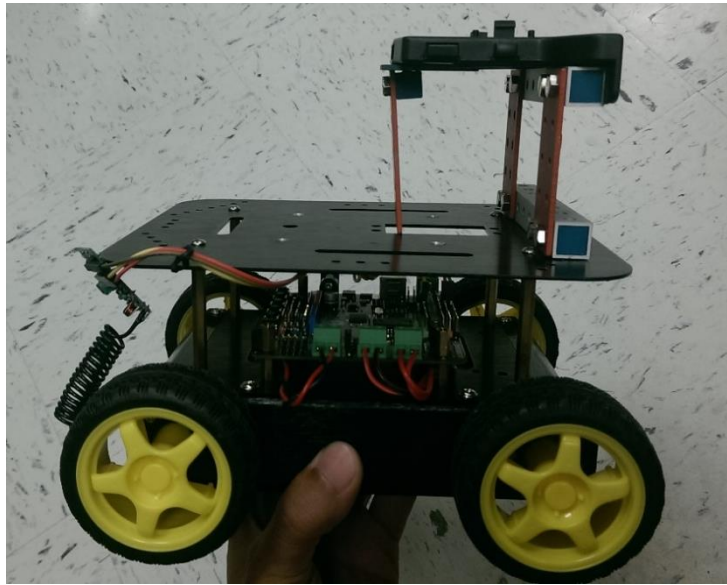
Based on the aforementioned models, researchers also developed control algorithms. In [13], a tuning fuzzy vector field orientation (FVFO) feedback control method was proposed for a skid-steered mobile robot using flexible fuzzy logic control (FLC). In [14], a robust backstepping tracking control was proposed based on a Lyapunov redesign for a skid-steered mobile robot.

Most of the skid-steered mobile robots have four wheels [9], [10] and [12]. However, some of them have two wheels [14], and six wheels [15]. The majority of skid-steered mobile robots are wheeled [9], [10], [12], [14]–[16], but some are tracked [13], [17] to handle the tough terrain. In this research, a four-wheeled skid-steered mobile robot is used.

Figure 2-1 is the skid-steered mobile robot that is used in the research. It was built by Enrique Zarate, a former undergraduate student in our lab. This mobile robot was controlled by an Arduino board and was actuated by four motors. Two motors on each side are in parallel connection, which means wheels on the same side rotate in the same direction and have the same angular velocity. On a flat surface, the vehicle has two degrees of freedom (translation and rotation).

### **2.1.2 Kinect sensor**

The Kinect sensor, seen Figure 2-2, is a motion sensing device by Microsoft. It was originally designed for video gaming. However, developers also created applications for human-robot interaction [18].



**Figure 2-1 The skid-steered mobile robot used in the research**



**Figure 2-2 The Kinect sensor**

Microsoft released a version of the Kinect sensor especially for windows. The sensor contains two cameras (one RGB camera and one IR camera), a microphone array,

and a tilt motor as well as a software package that processes color, depth, and skeleton data. Thus, users are able to create interactive applications that based on the recognition of natural movements, gestures, and voice commands.

### **2.1.3 Assemble of the Kinect sensor**

To mount the Kinect sensor on the robot, the top of the robot needs a structure that can keep the Kinect sensor tight all the time. Also, this structure should be able to be installed on the robot. There is nothing better than using a Kinect TV mount to attach a Kinect sensor without disassembling it because there is nothing but two holes designed to fit with that mount on the bottom of a Kinect sensor. However, the Kinect TV mount is not designed to mount the Kinect sensor on the robot. Therefore, the mount was modified to the one as shown in Figure 2-3.



**Figure 2-3 The structure to carry the Kinect sensor**

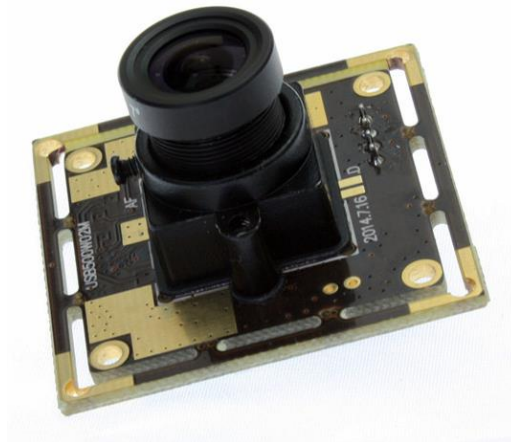
The best height of the Kinect sensor for human-tracking is about 0.5–1.5 m, but the robot is just of 0.15 meter's height. On the one hand, the tilt angle of the Kinect sensor can be adjusted for sensing. However, the performance will become worse as the tilt angle becomes large. On the other hand, a higher structure can be built to allow a smaller tilt angle. However, the higher the Kinect sensor is mounted, the more unstable the robot will become. With the best-fit sensing angle found experimentally, a structure was built on top of the mobile robot to carry the Kinect sensor, as shown in Figure 2-3.

#### **2.1.4 A wide-angle camera**

The wide-angle camera used in the research, as shown in Figure 2-4, is a USB camera from ELP, a manufacturer of surveillance system. The camera is come with a 5-megapixel (MP) complementary metal–oxide–semiconductor (CMOS) sensor and a 3.6 mm lens. This configuration is ideal for the research because: 1) although 5 MP is a very entry-level configuration for a camera, it is able to stream image clear enough for the research. Higher resolution than 5 MP would be a waste; 2) the camera is supposed to be mounted on the ceiling of the lab (3-m height), so theoretically  $4.6$  (horizontal)  $\times$   $3.5$  (vertical)  $m^2$  of floor area can be captured by the 3.6 mm lens. In case larger space is need for experiments, a 2.1mm lens can also be purchased.

Another important characteristic of the camera is its 30 frames per second (FPS) frame rate. Since the camera is to be mounted on the ceiling, a long USB extension cable is need to connect the camera to the computer. Tests show that the long cable will not slow down the frame rate under 30 FPS. The camera's object detectable distance is between 5 cm to 100 m, which is good enough for the research.





**Figure 2-4 the wide-angle camera (ELP-USB500W02M-L36) [19]**

### **2.1.5 Devices to be controlled**

Any electrical device installed with a receiver can be controlled by the robot. In the research, two lamps are built to indicate the remote control ability of the robot. The lamp is made up with an Arduino board, a XBee receiver, two LEDs (one RGB LED and one white LED), resistors and wires. The white LED is used to indicate whether the power of the lamp is on or off. It is on to inform a user that it is waiting for the robot's commands. The RGB LED adopted in the research has full colors. It is used to indicate the color of the lamp.

## **2.2 Software components**

### **2.2.1 Processing**

Processing is an open-source programming language and integrated development

environment (IDE) built on the Java language but using a simplified syntax and graphics programming model, which is the reason it was adopted to compile the main program. In this research, a program is needed to process data from various sources (the Kinect and the camera), and communicate with Arduino boards (robot and lamps). It is easy to communicate Processing with Arduino, which is also Java based, through serial port. Besides, there are libraries for the Processing to process data from the Kinect and camera. Therefore, Processing is the best choice to write the main program in the research.

### **2.2.2 OpenNI**

OpenNI (Open Natural Interaction), an industry-led, non-profit organization, was created by PrimeSense, a company which developed the technology behind the Kinect's 3D imaging and worked with Microsoft to develop the Kinect device [20]. In this research, OpenNI will be used as middleware to access the Kinect data streams and the skeleton/hand tracking capability and as a library in Processing to obtain data from the Kinect sensor.

### **2.2.3 Arduino IDE**

The Arduino IDE is a cross-platform application written in Java, and derives from the IDE for the Processing programming language and the Wiring projects [21]. In this research, it was used to compile program for Arduino board inside the robot and the lamps. Arduino IDE has a useful tool for debugging and monitoring serial ports, called Serial Monitor. The Serial Monitor is a useful tool that acts as a separate terminal that

communicates by receiving and sending Serial Data. That makes the Arduino IDE effective.

#### **2.2.4 MATLAB**

MATLAB is a high-level language, providing interactive environments for numerical computation, visualization, and programming, that was developed by MathWorks. MATLAB allows matrix manipulations, plotting of functions and data, implementation of algorithms, creation of user interfaces, and interfacing with programs written in other languages, for example, C++ and Java. MATLAB, in this research, serves as a tool to tune the controllers designed for human-tracking, simulate motion response of the robot, and analyze the experimental results.

#### **2.2.5 OpenCV**

Open Source Computer Vision (OpenCV) is a library of programming functions mainly for real-time image processing. It can be used in, for example, C, C++, and Java interfaces and supports operating system such as Windows, Linux, and Mac OS. In the research, the OpenCV library was included in the C++ program to process the video stream from the wide-angle camera. The OpenCV is mainly used for camera calibration and color tracking. Pinhole cameras have come to our daily life for a long time. They are compact and cheap. However, this cheapness comes with its price. Cheap cameras come with significant distortion, especially in a wide-angle camera. Luckily, this problem can be fix by calibration and some remapping. Furthermore, calibration relates the image units (pixels) and the length units in real world (for example meters). That is the reason

OpenCV is adopted in the research.

### **2.2.6 Visual Studio 2010**

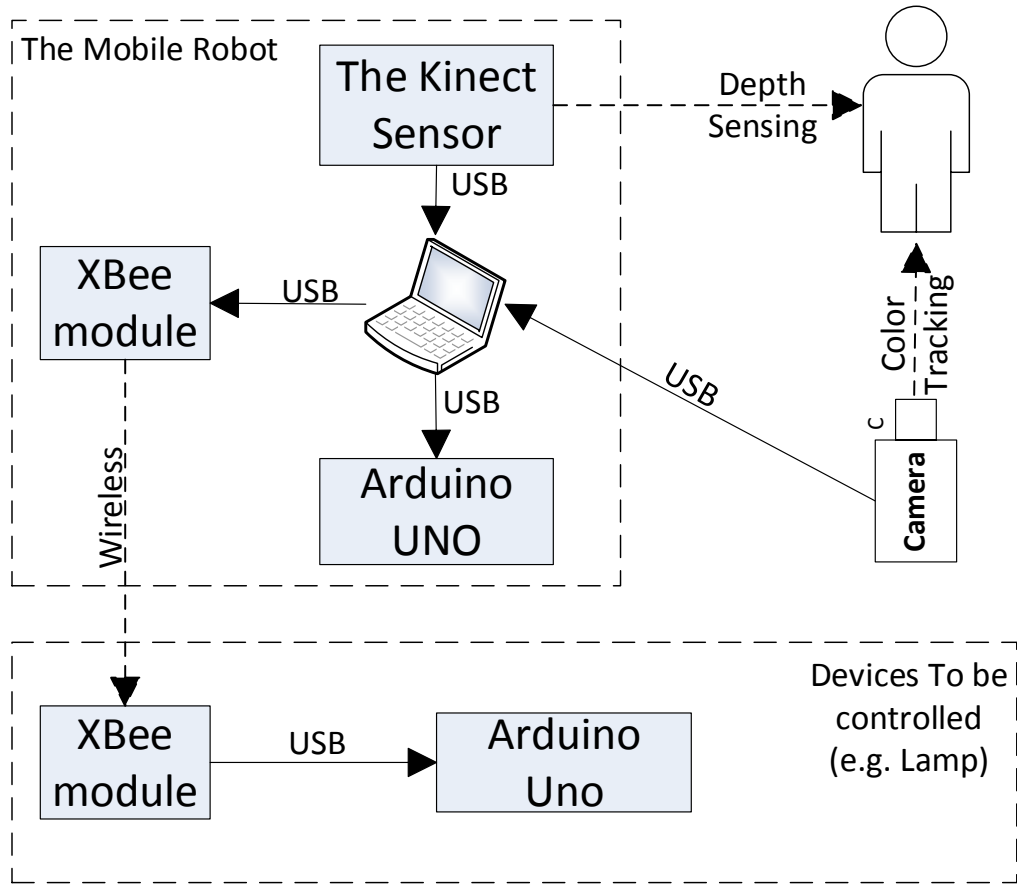
Microsoft Visual Studio is an integrated development environment (IDE) from Microsoft. It is a popular IDE for the C++ programming language on the Microsoft Windows operating system. The reason Visual Studio is chosen for the research is that OpenCV is adopted as a helpful library to process image from the wide-angle camera. Visual Studio is recommended to build applications with OpenCV on the Microsoft Windows operating system.

## **2.3 Connection**

The overall experimental system consists of three devices, as shown in Figure 2-5, a mobile robot, wide-angle camera, and digitally controlled lamp. The communication between the mobile robot and the lamp is developed by a pair of XBee radio modules. For the mobile robot, the XBee modules, Kinect sensor, Arduino board and wide-angle camera are connected to the laptop through four USB data cables. For the digital lamp, the other XBee module is connected to the Arduino board.

Figure 2-6 presents a diagram illustrating how the software components work together. The camera is operated by a C++ program running with Visual Studio. This program tracks a user and the mobile robot (to track specific colors) and sends translational and angular data to the Processing program. As the C++ program runs, it setups for the connection with the Processing program, but it does not start tracking until the Processing program is ready to receive data. When the Processing program runs, it

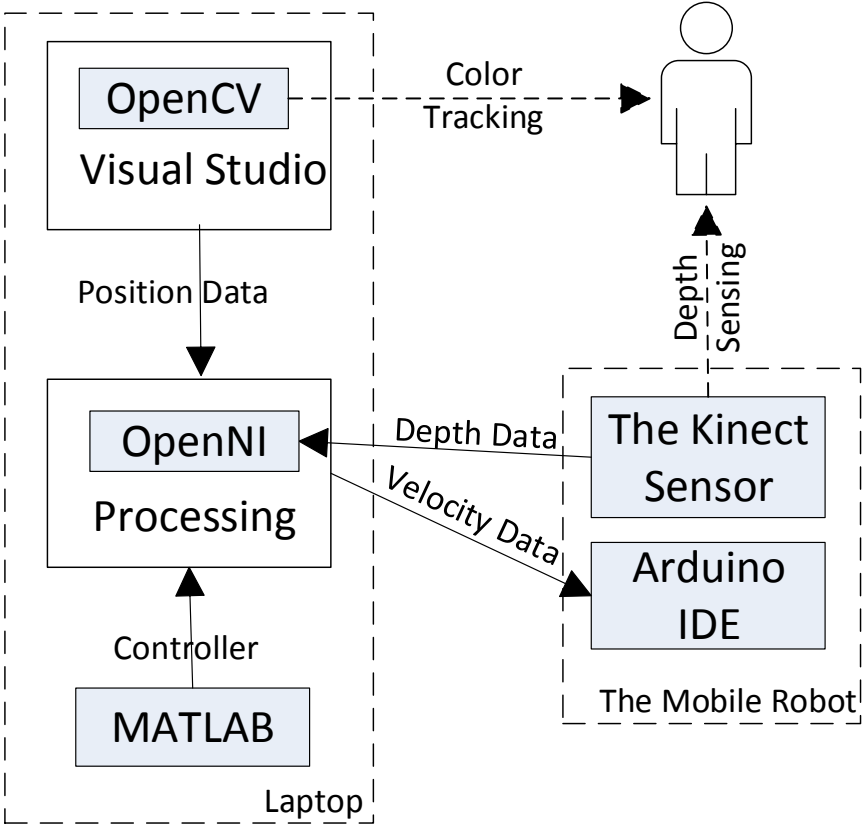
makes a connection to the C++ Program. Once the connection is established successfully, the camera start working and the whole system begins operating.



**Figure 2-5 Communication among various devices**

There are two mode of the system, human-tracking mode and motion-control mode. For the human-tracking mode, the Kinect sensor keeps detecting and sends depth data to the laptop through a USB data cable. Then the Processing program, running in

the laptop, keeps receiving depth data by the OpenNI, and translational and angular data by a socket, processes these data using the controller designed in Matlab, and sends command data to the Arduino board on the robot through a serial port. The command data are information about the velocities of the wheels on difference sides. The Arduino board generates pulse width modulation (PWM) signal of appropriate duty cycle to different motors based on the command data. Then the motors on the left side and the right sides generate appropriate torques so that the robot can track the designated person.



**Figure 2-6 Cooperation among software components**

For the motion-control mode, the Kinect sensor keeps detecting and sends positional data of joints of the person being tracked to the laptop. The Processing program processing these data and sends PWM signals to the Arduino boards of the lamps through the Xbee modules. Then the Arduino boards process these signals to control LEDs in the lamps.

## CHAPTER III

### CONTROL SYSTEM DESIGN

#### **3.1 Mathematical modeling**

In this section, critical parameters are measured and calculated, and the kinematic and dynamic model of the mobile robot are developed.

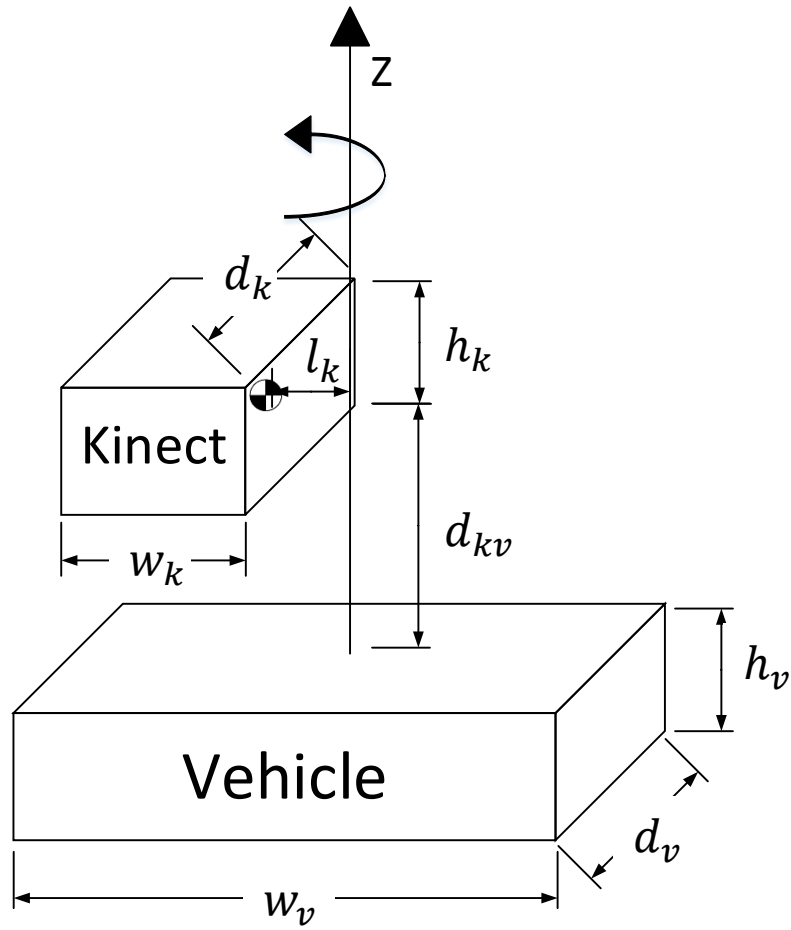
##### **3.1.1 Model description**

The mobile robot used in this research is a skid-steered mobile robot. A skid-steered mobile robot is a vehicle that steers by controlling the relative velocities of the wheels or tracks on the left and right sides. Also, all the wheels or tracks always point to the longitudinal axis of the vehicle. So, there is always slippage while a skid-steered vehicle turns. There has been so much research on this type of mobile robot. After some study, the model in [12] was adopted and revised.

##### **3.1.2 Definitions of parameters**

The robot is not of a regular shape, so it is not easy to calculate its moment of inertia. To calculate the moment of inertia of the robot, the shape of it is simplified to two solid cuboids representing the Kinect sensor and the vehicle, respectively. The solid cuboid representing the Kinect sensor is of the mass  $M_k$ , width  $w_k$ , depth  $d_k$ , and height  $h_k$ , as shown in Figure 3-1.





**Figure 3-1 Dimension definitions of the vehicle**

$l_k$  denotes the distance between the center of mass of the cuboid and the rotation axis, and  $d_{kv}$  denotes the distance between the Kinect sensor and the vehicle body. Since the Kinect sensor does not rotate about an axis through the body's center of mass. According to the parallel axis theorem, the moment of inertia of the Kinect sensor should be:

$$I_k = \frac{1}{12} M_k (w_k^2 + d_k^2) + M_k l_k^2 \quad (3.1)$$

The solid cuboid representing the vehicle is of the mass  $M_v$ , width  $w_v$ , depth  $d_v$ , and height  $h_v$ . In this case, the moment of inertia of the vehicle is:

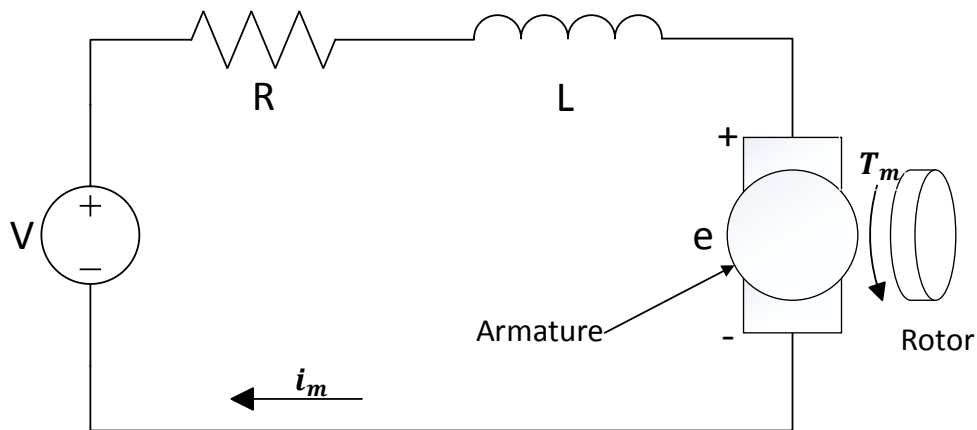
$$I_v = \frac{1}{12} M_v (w_v^2 + d_v^2) \quad (3.2)$$

Therefore, the total moment of inertia of the robot is:

$$I = I_k + I_v \quad (3.3)$$

A schematic diagram of a DC motor system is shown in Figure 3-2. In a permanent-magnet DC motor, the developed torque is proportional to the armature current  $i_m$  with a torque constant  $K_t$  as shown in the relation below.

$$T_m = K_t i_m \quad (3.4)$$



**Figure 3-2 The electric circuit of the armature**

The datasheet of the motor does not list the torque constant of the DC motor. Instead, it gives the torque  $T_a = 0.012 \text{ kg-m}$  at 3 V. Therefore, the current through each motor of the vehicle at 3 V equals to the armature voltage divided by the armature resistance.

$$I_a = \frac{V_a}{R_m} = 1.36 \text{ A} \quad (3.5)$$

So the torque constant can be calculated by dividing torque by the current.

$$K_t = \frac{T_a}{I_a} = \frac{0.012 \times 9.81 \text{ N} \cdot \text{m}}{1.36 \text{ A}} = 0.0865 \text{ N-m / A} \quad (3.6)$$

In the Processing IDE, the range of the motor's velocity  $p_v$  is 0–255, assuming that it is proportional to the motor's angular velocity. Then

$$i_m = k_i \cdot p_v \quad (3.7)$$

$$k_i = \frac{1.36}{255} = 0.0053 \text{ A}$$

$\alpha$  is a terrain-dependent that related to rolling resistance  $\mu_r$ . Experiments show that the large the rolling resistance, the large the value of  $\alpha$  [12]. Referring to [12],  $\alpha$  was set to 1.5 for a lab surface. Both the frame rate of the Kinect sensor and the camera are denoted by  $TS$ . Table 3.1 lists all the important parameters of the robot.

### 3.1.3 Kinematics

In this section, the kinematics model of the robot is developed. Table 3.2 gives all the variables that used in the mathematical modeling of the robot.

**Table 3.1 Summarizes the key parameters of the robot**

Mass of the vehicle	$M_v = 1.0741 \text{ kg}$
Mass of the Kinect sensor	$M_k = 0.4646 \text{ kg}$
Vehicle width	$w_v = 0.172 \text{ m}$
Vehicle length	$d_v = 0.199 \text{ m}$
Kinect width	$w_k = 0.254 \text{ m}$
Kinect depth	$d_k = 0.064 \text{ m}$
Mass of center of Kinect to the rotate axis	$l_k = 0.023 \text{ m}$
Moment inertia of the robot	$I = 0.0091 \text{ kg} \cdot \text{m}^2$
Motor armature resistor	$R_m = 2.2 \Omega$
Motor voltage	$V_a = 3 \text{ V}$
Motor torque at 3 V	$T_a = 0.012 \text{ kg} \cdot \text{m}$
Motor current at 3 V	$I_a = 1.36 \text{ A}$
Gear ratio	$G_r = 1:120$
Torque constant	$K_t = 0.0865 \text{ N} \cdot \text{m} / \text{A}$
PWM constant	$K_i = 0.0053 \text{ A}$
Friction coefficient	$\mu_f = 0.3$
Rolling resistance coefficient	$\mu_r = 0.03$
Radius of the wheel	$r = 0.028 \text{ m}$
Terrain-dependent parameter	$\alpha = 1.5$
Frame rate	$TS = 1 / 30 \text{ FPS}$

**Table 3.2 Define the variables of the robot to be used in the rest of thesis**

Vehicle displacement in longitudinal direction	$y$
Vehicle rotation	$\varphi$
Vehicle velocity in longitudinal direction	$V_y$
Vehicle angular velocity	$\dot{\varphi}$
Rotation of the left wheel	$\theta_L$
Rotation of the right wheel	$\theta_R$
Angular velocity of wheels on the left side	$\omega_L = \dot{\theta}_L$
Angular velocity of wheels on the right side	$\omega_R = \dot{\theta}_R$
Input torque of the left motors	$T_L$
Input torque of the right motors	$T_R$
PWM value	$P_v$

There are two motor in each side to drive two wheels separately. So the total torque in each side is:

$$T_L = T_R = 2 \frac{T_m}{G_r} \quad (3.8)$$

Substitute  $T_m$  with equation (3.4)

$$T_L = 240k_t k_i P_v \quad (3.9)$$

There are some assumptions for developing the mathematical model:

1. The vehicle is symmetric about the  $x$  and  $y$  axes.

2. The center of mass is at the geometric center.
3. There is point contact between the wheels and the ground.
4. Wheels on the same side share the same angular velocity.
5. The robot is running on a ground with flat surface and its four wheels are always in contact with the surface of the ground.

For vehicles that satisfy the assumptions, an experimental kinematic model of a skid-steered wheeled vehicle that is developed in [12] is given by

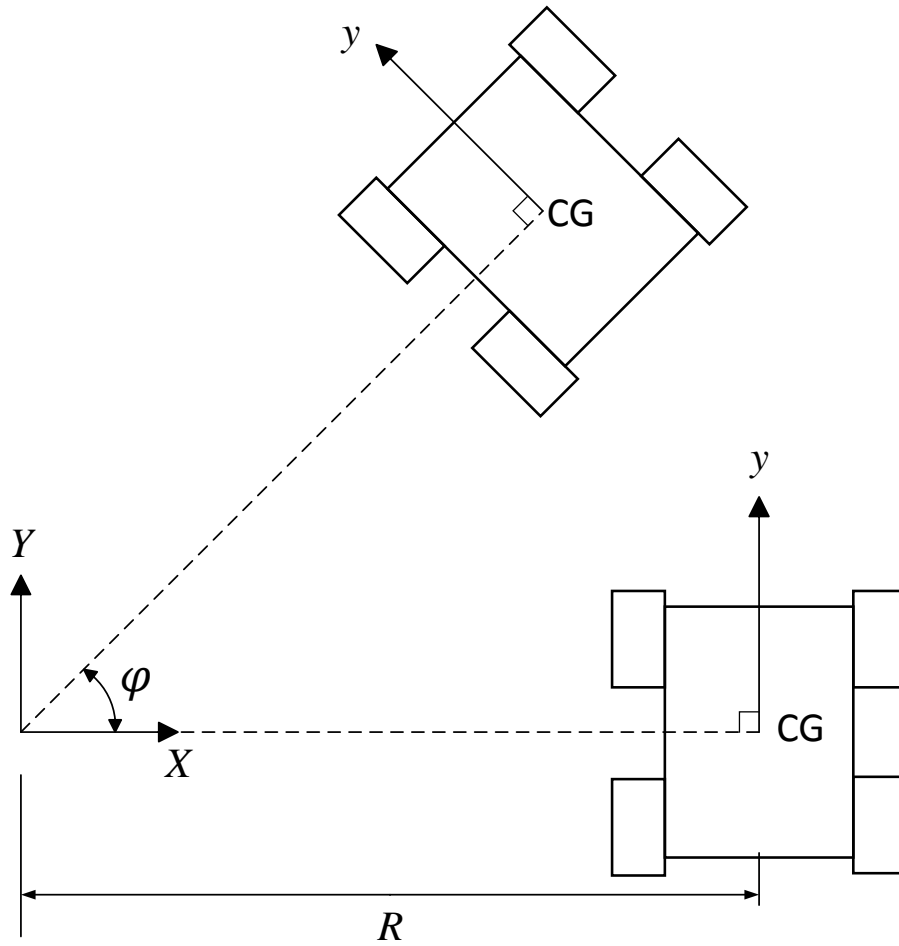
$$\begin{bmatrix} V_y \\ \dot{\phi} \end{bmatrix} = \frac{r}{\alpha w_v} \begin{bmatrix} \frac{\alpha w_v}{2} & \frac{\alpha w_v}{2} \\ -1 & 1 \end{bmatrix} \begin{bmatrix} \omega_L \\ \omega_R \end{bmatrix}. \quad (3.10)$$

Figure 3-3 shows a schematic diagram for the circular motion of the robot.

Assuming the robot is on the  $x$ -axis and at the beginning, and the distance between the origin and the robot is  $R$ . Then the robot moves to the second position on the top. The angle the robot rotates is  $\varphi$ , while  $y$  is the displacement in the longitudinal direction.

### 3.1.4 Dynamic modeling

This section develops the dynamic model of a skid-steered vehicle for the case of circular 2D motion. In contrast to dynamic models described in terms of the velocity vector of the vehicle [16], the dynamic model modified is described in terms of the angular velocity vector of the wheels. In this way the model structure is particularly beneficial and easy for control since the wheel velocities are directly commanded by the control system.



**Figure 3-3 Schematic diagram for circular motion of the mobile robot**

The dynamic model is given by

$$M\ddot{q} + C(q, \dot{q}) + G(q) = \tau \quad (3.11)$$

where  $q = [\theta_L \ \theta_R]^T$  is the angular displacement of the left and right wheels,  $\dot{q} = [\omega_L \ \omega_R]^T$  is the angular velocity of the left and right motors,  $M$  is the mass matrix,  $C(q, \dot{q})$  is the resistance term, and  $G(q)$  is the gravitational term.

The robot moves on a 2D surface (the robot only has three degree of freedom), so the model follows from [16], which is showed in the local  $x$ - $y$  coordinates, and  $M(q)$  in (3.11) is given by

$$M = \begin{bmatrix} \frac{mr^2}{4} + \frac{r^2I}{\alpha w_v^2} & \frac{mr^2}{4} - \frac{r^2I}{\alpha w_v^2} \\ \frac{mr^2}{4} - \frac{r^2I}{\alpha w_v^2} & \frac{mr^2}{4} + \frac{r^2I}{\alpha w_v^2} \end{bmatrix} \quad (3.12)$$

Where

$$m = M_v + M_k \quad (3.13)$$

represents the total mass of the robot. Since only planar motion are considered,  $G(q) = 0$ .  $C(q, \dot{q})$  denotes the resistance resulting from the interaction between the wheels and terrain, including the rolling resistance, sliding frictions, and the locomotion resistance. Based on the analysis in [12] and considering that the model is only used to derive the feedback controller, the resistance term  $C(q, \dot{q})$  is simplify to a linear term,

$$C(\dot{q}) = \begin{bmatrix} r(\mu_r + \mu_f) & -r\mu_f \\ -r\mu_f & r(\mu_r + \mu_f) \end{bmatrix} \dot{q} \quad (3.14)$$

assuming that the resistance is proportional to the angular velocity.  $\mu_r$  and  $\mu_f$  are respectively the rolling resistance coefficient and the friction coefficient. Therefore, (3.11) becomes

$$\begin{bmatrix} \frac{mr^2}{4} + \frac{r^2I}{\alpha w_v^2} & \frac{mr^2}{4} - \frac{r^2I}{\alpha w_v^2} \\ \frac{mr^2}{4} - \frac{r^2I}{\alpha w_v^2} & \frac{mr^2}{4} + \frac{r^2I}{\alpha w_v^2} \end{bmatrix} \ddot{q} + \begin{bmatrix} r(\mu_r + \mu_f) & -r\mu_f \\ -r\mu_f & r(\mu_r + \mu_f) \end{bmatrix} \dot{q} = \begin{bmatrix} \tau_L \\ \tau_R \end{bmatrix} \quad (3.15)$$

Multiplying both side by  $M^{-1}$  yields



$$\ddot{q} = \begin{bmatrix} -r(\mu_r + \mu_f) \left( \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} \right) & r\mu_f \left( \frac{\alpha w_v^2}{4r^2 I} - \frac{1}{mr^2} \right) \\ r\mu_f \left( \frac{\alpha w_v^2}{4r^2 I} - \frac{1}{mr^2} \right) & -r(\mu_r + \mu_f) \left( \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} \right) \end{bmatrix} \dot{q} \quad (3.16)$$

$$+ \begin{bmatrix} \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} & \frac{1}{mr^2} - \frac{\alpha w_v^2}{4r^2 I} \\ 1 & \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} \end{bmatrix} \begin{bmatrix} \tau_L \\ \tau_R \end{bmatrix}$$

In state-space matrix form:

$$\begin{bmatrix} \dot{\theta}_L \\ \ddot{\theta}_L \\ \dot{\theta}_R \\ \ddot{\theta}_R \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & -r(\mu_r + \mu_f) \left( \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} \right) & 0 & r\mu_f \left( \frac{\alpha w_v^2}{4r^2 I} - \frac{1}{mr^2} \right) \\ 0 & 0 & 0 & 1 \\ 0 & r\mu_f \left( \frac{\alpha w_v^2}{4r^2 I} - \frac{1}{mr^2} \right) & 0 & -r(\mu_r + \mu_f) \left( \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} \right) \end{bmatrix} \begin{bmatrix} \theta_L \\ \dot{\theta}_L \\ \theta_R \\ \dot{\theta}_R \end{bmatrix} \quad (3.17)$$

$$+ \begin{bmatrix} 0 & 0 \\ \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} & \frac{1}{mr^2} - \frac{\alpha w_v^2}{4r^2 I} \\ 1 & \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} \\ \frac{\alpha w_v^2}{4r^2 I} + \frac{1}{mr^2} & \frac{1}{mr^2} - \frac{\alpha w_v^2}{4r^2 I} \end{bmatrix} \begin{bmatrix} \tau_L \\ \tau_R \end{bmatrix}$$

$$\begin{bmatrix} y \\ \varphi \end{bmatrix} = \frac{r}{\alpha w_v} \begin{bmatrix} \frac{\alpha w_v}{2} & 0 & \frac{\alpha w_v}{2} & 0 \\ -1 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \theta_L \\ \dot{\theta}_L \\ \theta_R \\ \dot{\theta}_R \end{bmatrix}$$

Then, the transfer function will be

$$\begin{bmatrix} Y_y \\ Y_\varphi \end{bmatrix} = \begin{bmatrix} G_{11} & G_{12} \\ G_{21} & G_{22} \end{bmatrix} \begin{bmatrix} T_L \\ T_R \end{bmatrix} \quad (3.18)$$

where

$$G_{11}(s) = G_{12}(s) = \frac{23.21s + 653.2}{s^3 + 44.07s^2 + 448.3s} = 23.21 \frac{(s + 28.14)}{s(s + 15.93)(s + 28.14)}$$

$$G_{22}(s) = -G_{21}(s) = \frac{337.7s + 5380}{s^3 + 44.07s^2 + 448.3s} = 337.7 \frac{(s + 15.93)}{s(s + 15.93)(s + 28.14)}$$

after substituting all parameter values.

## 3.2 System analysis

### 3.2.1 Stability

As the results shown in the last section, plant  $G_{11}(s)$  equals to plant  $G_{12}(s)$  while plant  $G_{22}(s)$  equals to negative  $G_{21}(s)$ . That means the torque input from the left wheels has the same effect with the torque input from the right wheels to the translation output  $Y_y$ . The torque input from the left wheels has opposite effect with the torque input from the right wheels to the rotation output  $Y_\varphi$ .

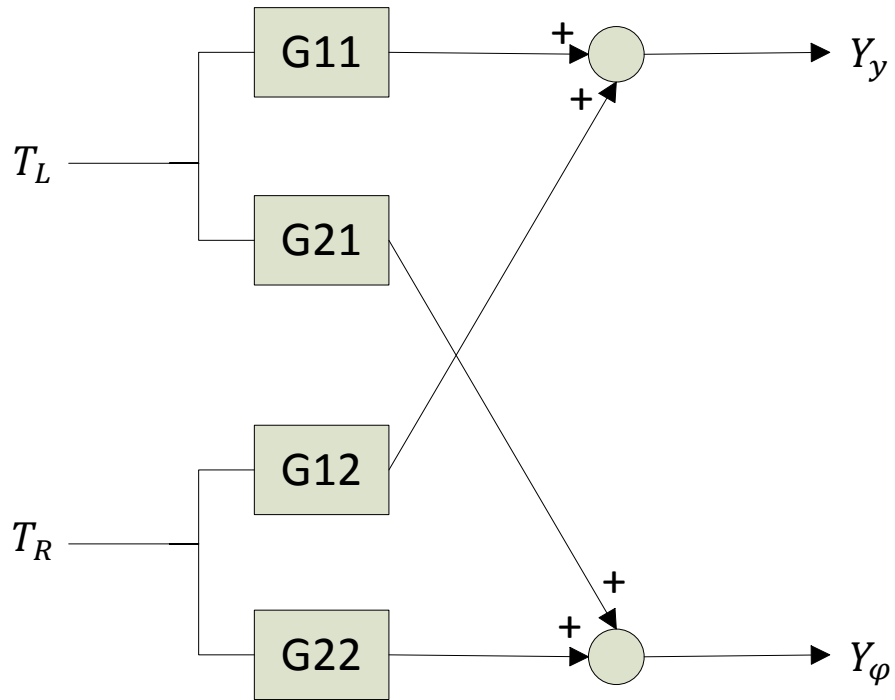
The control system of the skid-steered mobile robot is a multi-input multi-output (MIMO) system, as shown in Figure 3-4. Originally, the system should be analyzed by MIMO control techniques. However, it can also be analyzed by single-input single-output (SISO) control techniques.

First, let us just consider the mobile robot moving in a straight line only, without turning. That means  $Y_\varphi$ , the angular displacement output equals zero. Since plant  $G_{22}(s)$  equals to negative plant  $G_{21}(s)$ , torque  $T_L$  should equal to torque  $T_R$ . Then the displacement of the robot in one degree of freedom can be derive as following:

$$Y_y = G_{11}(s)T_L + G_{12}(s)T_R = 2G_{11}(s)T_L$$

Therefore, the plant of the system only has linear motion will be:

$$G_y(s) = \frac{Y_y}{T_L} = 2G_{11}(s) \quad (3.19)$$



**Figure 3-4 The block diagram of the system**

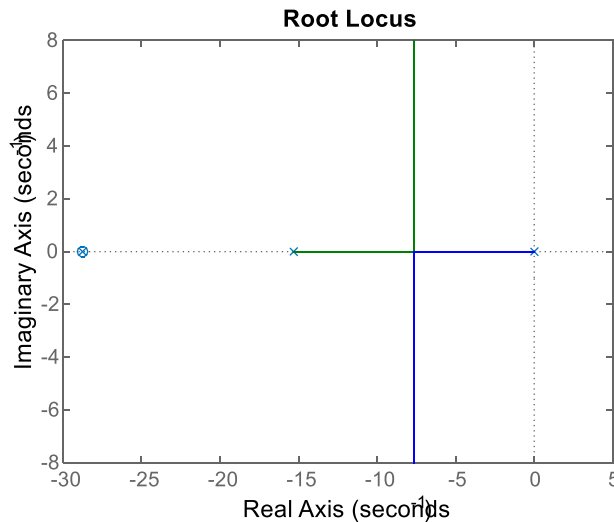
In another case, let us just consider the mobile robot rotating about the geometry center of it only. That means  $Y_y$  equals to zero. While  $G_{11}(s)$  equals to  $G_{12}(s)$ ,  $T_L$  should equal to negative  $T_R$ . Then the rotational angle of the robot can be derive as following:

$$Y_\varphi = G_{21}(s)T_L + G_{22}(s)T_R = 2G_{22}(s)T_R$$

$$G_\varphi(s) = \frac{Y_\varphi}{T_R} = 2G_{22}(s) \quad (3.20)$$

Figure 3-5 shows the root locus for linear motion only. As indicate in this diagram, there are one zero and three poles on the real axis. The pole at 28.14 cancels the effect of the zero at the same place. No pole on the right-half s-plane, but there is one

pole at the origin. That means the open-loop system is marginal stable.



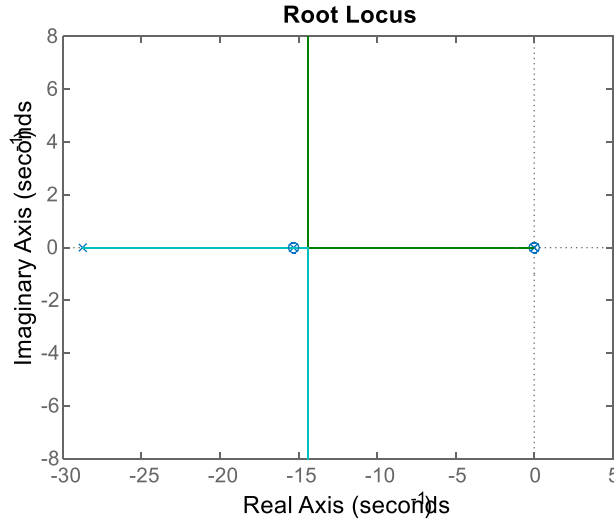
**Figure 3-5 The Root locus of the system for linear motion only**

The root locus of the open-loop system for rotation only is shown in Figure 3-6. This is also a marginally stable system because one of the poles is on the origin. There are three poles and one zero. All of them are on the real axis. The pole at 15.93 cancels the effect of the zero at the same place.

### 3.2.2 Open-loop dynamics

In this section ODE (Ordinary Differential Equation) is used to demonstrate the connection between the step response of the open-loop analysis result and the physical phenomena of the robot because different results can be seen clearly by changing the

initial conditions and constrains.



**Figure 3-6 The Root locus of the system for rotational motion only**

The state space form can be rewrite as:

$$\begin{aligned}
 \frac{d^2\theta_L}{dt^2} &= -r(\mu r + \mu_f) \left( \frac{\alpha B^2}{4r^2 I} + \frac{1}{mr^2} \right) \frac{d\theta_L}{dt} + r\mu_f \left( \frac{\alpha B^2}{4r^2 I} - \frac{1}{mr^2} \right) \frac{d\theta_R}{dt} \\
 &\quad + \left( \frac{\alpha B^2}{4r^2 I} + \frac{1}{mr^2} \right) \tau_L + \left( \frac{1}{mr^2} - \frac{\alpha B^2}{4r^2 I} \right) \tau_R \\
 \frac{d^2\theta_R}{dt^2} &= r\mu_f \left( \frac{\alpha B^2}{4r^2 I} - \frac{1}{mr^2} \right) \frac{d\theta_L}{dt} - r(\mu r + \mu_f) \left( \frac{\alpha B^2}{4r^2 I} + \frac{1}{mr^2} \right) \frac{d\theta_R}{dt} \\
 &\quad + \left( \frac{1}{mr^2} - \frac{\alpha B^2}{4r^2 I} \right) \tau_L + \left( \frac{\alpha B^2}{4r^2 I} + \frac{1}{mr^2} \right) \tau_R
 \end{aligned} \tag{3.21}$$

Assume the input torque  $\tau_L$  and  $\tau_R$  are constants, then its derivatives are zero. To

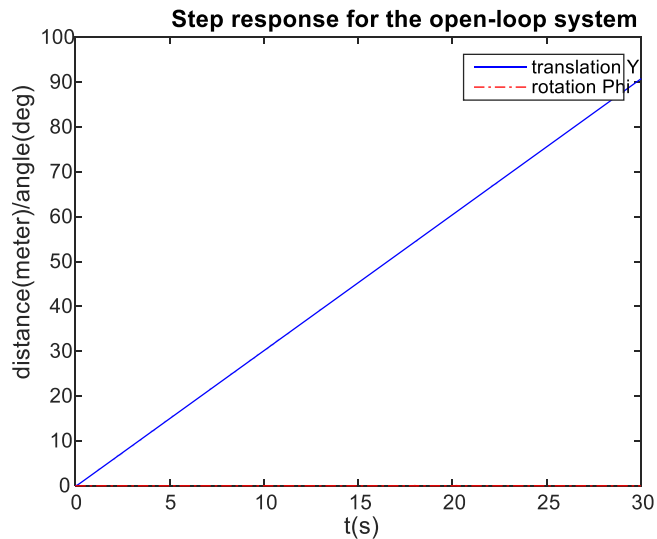
obtain the first set of step response, initial conditions were set as:  $\theta_L(0) = 0$ ,  $\frac{d\theta_L}{dt}(0) = 0$ ,  $\theta_R(0) = 0$ ,  $\frac{d\theta_R}{dt}(0) = 0$ ,  $T_L(0) = 1$ ,  $T_R(0) = 1$

Then ode45 is used in Matlab to solve  $\theta_L$  and  $\theta_R$ . The inputs for the ode45 are set as  $T_L(0) = 1$ ,  $T_R(0) = 1$ ,  $\frac{dT_L}{dt} = 0$ , and  $\frac{dT_R}{dt} = 0$ . This means the torques generated by the left and right wheels are constant and the same. Since the output of the system is:

$$y = \frac{r}{2}(\theta_L + \theta_R)$$

$$\varphi = \frac{r}{\alpha B}(\theta_R - \theta_L)$$

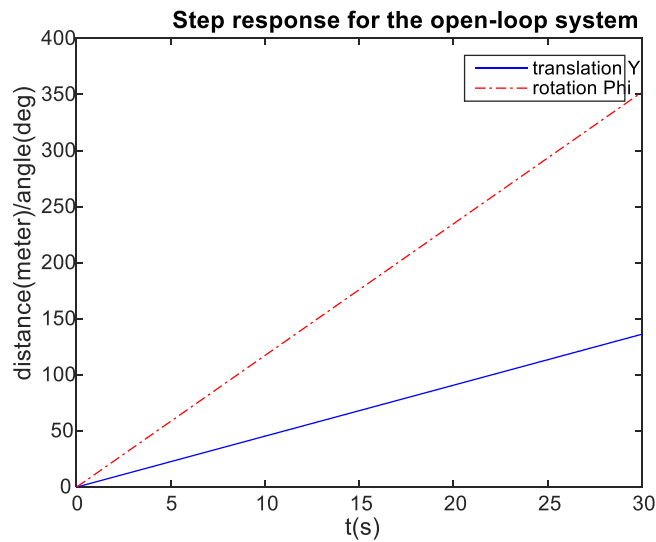
A diagram about  $y$  and  $\varphi$  verse  $t$  is plotted in Figure 3-7. As you can see the displacement  $y$  keep increase linearly because the torques are constants, while rotation  $\varphi$  is zero because torques from both sides are the same.



**Figure 3-7 Step response with same torque input**

To obtain the second set of result, inputs are modified as  $T_L(0) = 2$ ,  $T_R(0) = 1$ ,  $\frac{dT_L}{dt} = 0$  and  $\frac{dT_R}{dt} = 0$ . In this case, the torque generated by the left wheels is twice as much as the torque generated by the right wheels and they are still constants.

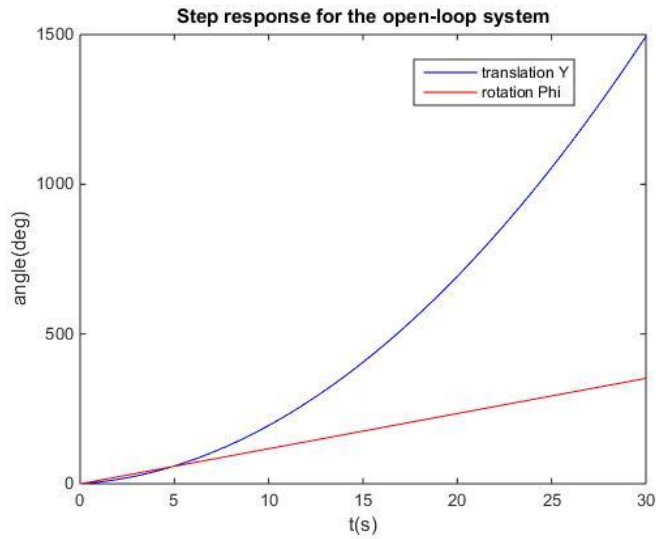
Figure 3-8 shows that the translation  $y$  still keeps increasing linearly, and so as the rotation  $\varphi$ . That makes sense, the robot keeps rotating because the torques from two sides are different.



**Figure 3-8 Step response with different torque input**

To obtain the third set of results, the inputs are modified again. They are set as  $T_L(0) = 2$ ,  $T_R(0) = 1$ ,  $\frac{dT_L}{dt} = 1$ , and  $\frac{dT_R}{dt} = 1$ . Based on the input of last test, the changing rate of torques from both sides are set to be the same constant of 1. That means

the torques will increase at the same rate and they are no long constants. As you can see in Figure 3-9 the robot runs faster and faster, while rotate angle keeps increasing linearly because the torques increase at the same rate.



**Figure 3-9 Step response with different proportional torque input**

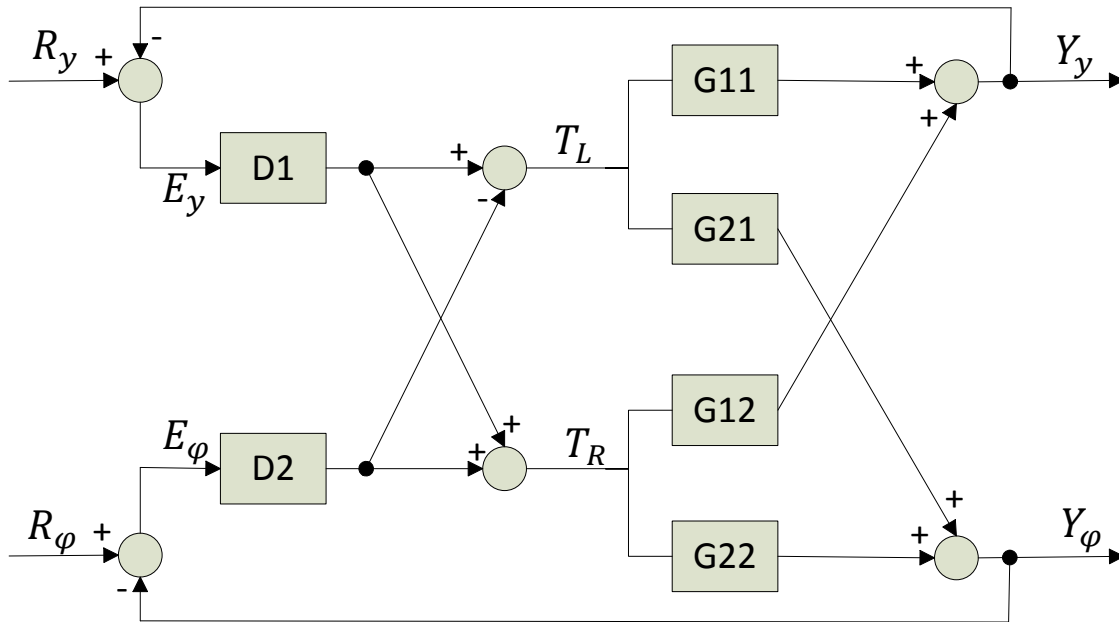
### 3.3 Classical control design

#### 3.3.1 PID controller

Based on the analysis in section 3.1, the block diagram of the control system of the robot is developed, as shown in Figure 3-10.  $R_y$  and  $R_\phi$  are respectively the reference input of displacement and rotation.  $e_y$  and  $e_\phi$  are respectively the error of



linear motion and rotational motion.  $D_{siso1}$  and  $D_{siso2}$  are respectively the PID controller for linear motion and rotational motion.



**Figure 3-10 The block diagram of the system with controller**

There is a critical factor that must be considered for the requirement of the controller. Kinect sensors are designed to be working in a stationary position, so they can decide which object is moving, which is not. However, in this research, the Kinect sensor is mounted on the mobile robot. That means the Kinect sensor will move with the mobile robot. If the robot moves too quickly (especially in rotational motion), the Kinect sensor will lose the tracking of a designated person. Therefore, the first requirement for the two controllers is not to overshoot in the step response. The second

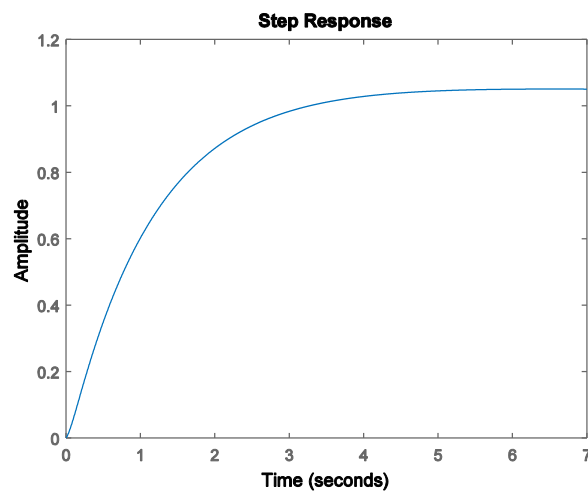
requirement is reducing the settling time as much as possible because the slow response of the robot may also have it lose the tracking of a designated person.

To tune the controllers to meet the requirements aforementioned, SISOTOOL in Matlab is used. For a PID controller, there is a gain and two zeros need to be tune. The gain is decided based on the physical limitation of the vehicle (maximum linear speed) and the Kinect sensor (maximum rotational speed). Zeros are tuned to reduce the overshoot. The two controllers for linear motion ( $D_{siso1}$ ) and rotation ( $D_{siso2}$ ) are developed respectively after tuning.

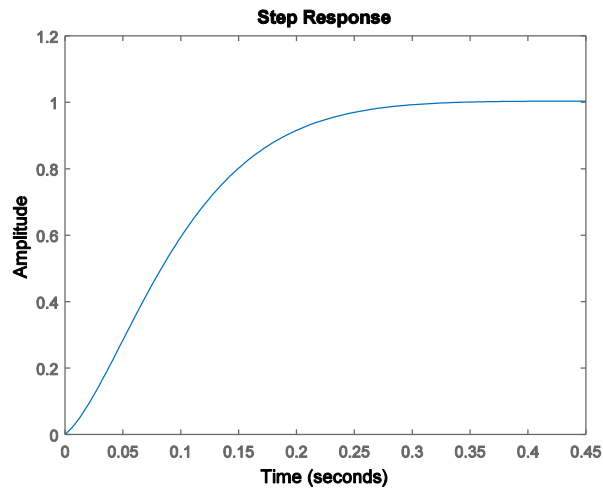
$$D_{siso1} = 0.3064 + \frac{0.018}{s} + 0.006732s$$

$$D_{siso2} = 0.862 + \frac{0.02}{s} + 0.0086s$$

The step response of the closed-loop system include the two PID controller are given in Figure 3-11 and Figure 3-12.



**Figure 3-11 Step response of the closed-loop system (linear motion)**



**Figure 3-12 Step response of the closed-loop system (rotation)**

The linear motion controller, worked well, its response was slow. For the rotational motion controller, the response was pretty good. The experimental performance of these two controllers will be evaluated in Chapter V.

### **3.3.2 Lead-lag controller**

Due to the PID controller for linear motion has a slow response, a lead-lag controller is designed for linear motion in this section. Based on the previously analysis the Phase Angle of the open-loop system is good enough ( $79.4^\circ$ ), so the lag compensation is chosen. In this section, a lag compensator such that the system has a Phase Margin of  $80^\circ$  and a velocity error constant of  $K_v = 1.746$  m/s is designed.

#### **1) System type and error constant**

The plant of the system (linear motion only):

$$G_y(s) = \frac{46.42s + 1306.4}{s^3 + 44.07s^2 + 448.3s}$$

The system is Type 1. Application of the Final Value Theorem to the error formula gives the result

$$\begin{aligned} e_{ss} &= \lim_{s \rightarrow 0} \cdot sE(s) = \lim_{s \rightarrow 0} \cdot s \frac{1}{1 + G_y} R(s) = \lim_{s \rightarrow 0} \cdot s \frac{1}{1 + \frac{46.42s + 1306.4}{s(s^2 + 44.07s + 448.3)}} \frac{1}{s^2} \\ &= 0.34 \text{ m} \end{aligned}$$

$$K_v = \frac{1}{e_{ss}} = 2.91 \text{ m/s}$$

The steady-state error is 0.34 m, and the velocity error constant is 2.91 m/s.

## 2) Determine the control gain to meet the steady-state error requirements

Let  $G_{y'}(s)$  be the new plant of the system, which multiplied the lag gain.

$$G_{y'}(s) = K_{lag}G_y(s)$$

$$K_v = \lim_{s \rightarrow 0} \cdot sG_{y'}(s) = 1.746 \text{ m/s}$$

$$K_v = \lim_{s \rightarrow 0} \cdot s \frac{K_{lag}(46.42s + 1306.4)}{s(s^2 + 44.07s + 448.3)} = 1.746 \text{ m/s}$$

The control gain of the lag compensation would be

$$K_{lag} = 0.6$$

## 3) Determine the new crossover frequency $\omega_{cr}$

The Bode plot of the system  $G_{y'}(s)$  is plotted by Matlab, as shown in Figure 3-13. To have a new Phase Margin of  $93.9^\circ$ , the crossover frequency should be

$$\omega_{cr} = 1.1 \text{ rad/s}$$

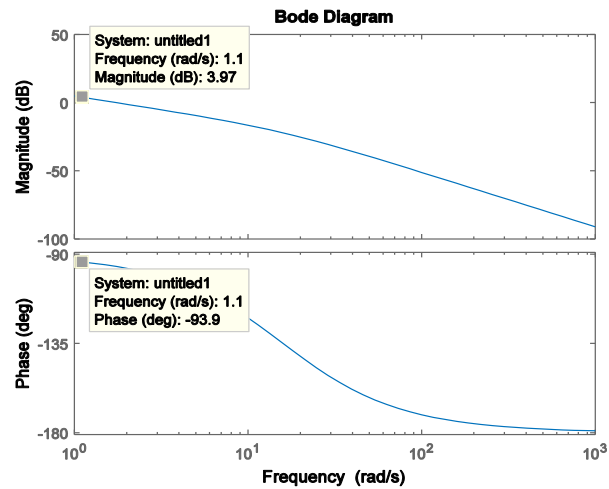


Figure 3-13 Bode plot of the plant with control gain (linear motion)

4) Place zero 1 decade below  $\omega_{cr}$

$$\frac{1}{T} = \frac{1}{10} \omega_{cr}$$

$$T = 9.091 \text{ s}$$

5) Calculate  $\alpha$

According to Figure 3-13

$$20 \log_{10}(\alpha) = 3.97$$

So

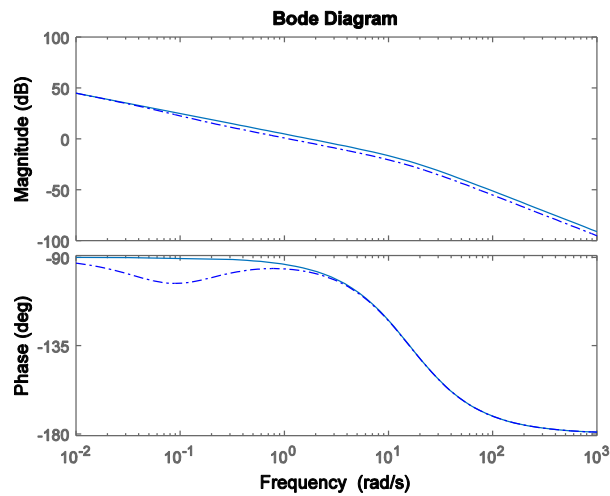
$$\alpha = 1.58$$

6) Verify design

The lag compensation will be

$$C_{lag}(s) = K_{lag} \left( \frac{Ts + 1}{\alpha Ts + 1} \right) = 0.6 \frac{9.091s + 1}{1.58 \times 9.091s + 1} = 0.38 \frac{s + 0.11}{s + 0.07}$$

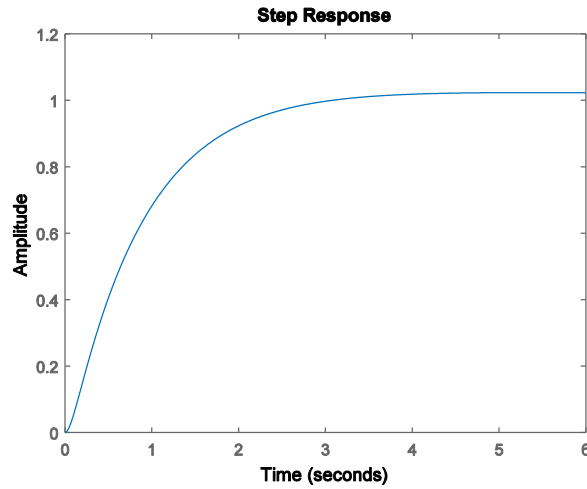
Figure 3-14 shows the Bode plot of the two systems. The solid line represents the open-loop system  $G_{y'}(s)$ . The dash-dotted line represent the system utilizing the lag compensation  $C_{lag}(s)G_{y'}(s)$ .



**Figure 3-14 Bode plot for lag compensation**

Figure 3-15 shows the step response of the closed-loop system utilizing the lag compensation. There is a small error about 0.02 m, which is not desired.

To have a better performance, a lead compensation such that the system has a phase margin of 80° and a velocity error constant of  $K_v = 4.37$  m/s is also designed.



**Figure 3-15 Step response of the system with lag compensation**

**1) Determine the control gain to meet the steady-state error requirements**

$G_{y''}(s)$  is defined as

$$G_{y''}(s) = K_{lead}G_y(s)$$

$$K_v = \lim_{s \rightarrow 0} \cdot sG_{y''}(s) = 1.746 \text{ m/s}$$

$$K_v = \lim_{s \rightarrow 0} \cdot s \frac{K_{lead}(46.42s + 1306.4)}{s(s^2 + 44.07s + 448.3)} = 4.37 \text{ m/s}$$

The control gain of the lag compensation would be

$$K_{lead} = 1.5$$

**2) Determine the phase margin of the uncompensated system**

$$1 = |G_{y''}(j\omega_c)| = \left| \frac{69.63j\omega_c + 1959.6}{-j\omega_c^3 - 44.07\omega_c^2 + 448.3j\omega_c} \right|$$

$$\omega_c = 4.225 \text{ rad/s}$$

$$\begin{aligned}\angle G_{y''}(j\omega_c) &= \angle \frac{69.63j\omega_c + 1959.6}{-j\omega_c^3 - 44.07\omega_c^2 + 448.3j\omega_c} \\ &= \angle(69.63j\omega_c + 1959.6) - \angle j\omega_c - \angle(-\omega_c^2 + 44.07j\omega_c + 448.3) \\ &= 8.538^\circ - 90^\circ - 23.391^\circ = -104.853^\circ\end{aligned}$$

$$PM = 75.147^\circ$$

### 3) Determine the amount of phase lead needed

$$\phi_{lead} = \phi_{PM,desired} - \phi_{PM,current} + \epsilon$$

$$\phi_{lead} = 80^\circ - 75.147^\circ + 10^\circ = 14.853^\circ$$

### 4) Calculate $\alpha$

$$\alpha = \frac{1 - \sin(\phi_{lead})}{1 + \sin(\phi_{lead})} = \frac{1 - \sin(13.989^\circ)}{1 + \sin(13.989^\circ)} = 0.592$$

### 5) Determine the frequency where we will add the maximum phase

$$20 \log_{10} |G_{y''}(j\omega_{max})| = -10 \log_{10} \frac{1}{\alpha}$$

$$20 \log_{10} \left| \frac{69.63j\omega_{max} + 1959.6}{-j\omega_{max}^3 - 44.07\omega_{max}^2 + 448.3j\omega_{max}} \right| = -10 \log_{10} \frac{1}{\alpha}$$

$$\omega_{max} = 5.38 \text{ rad/s}$$

### 6) Calculate T

$$T = \frac{1}{\omega_{max}\sqrt{\alpha}} = 0.2416 \text{ s}$$

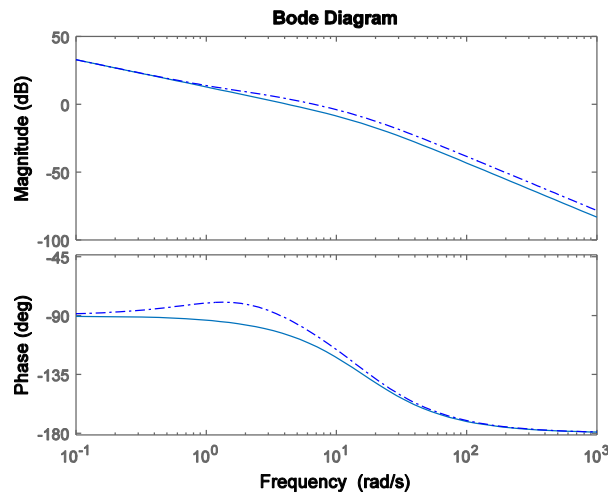
### 7) Verify design

Therefore the lead compensation is

$$C_{lead}(s) = K_{lead} \left( \frac{Ts + 1}{\alpha Ts + 1} \right) = 2.53 \frac{s + 4.14}{s + 6.99}$$



Figure 3-16 shows the Bode plot of the two systems. The solid line is the open-loop system  $G_{y''}(s)$ . The dash-dotted line is the system utilizing the lead compensation  $C_{lead}(s)G_{y''}(s)$ . The step response of the closed-loop system with the lead compensation is shown in Figure 3-17. As shown in the figure, the response is quick.



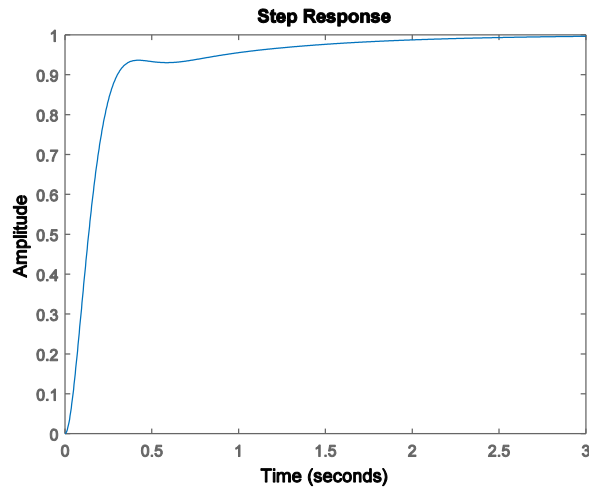
**Figure 3-16 Bode plot for the lead compensation**

To eliminate the steady-state error of the lag compensation and also have a better performance, a lead-lag controller is designed by adding a new lag compensation to the lead compensation. The gain of the lead-lag controller is set to be 0.9 based on analysis of the step response of the system.

**1) Determine the new crossover frequency  $\omega_{cr}$**

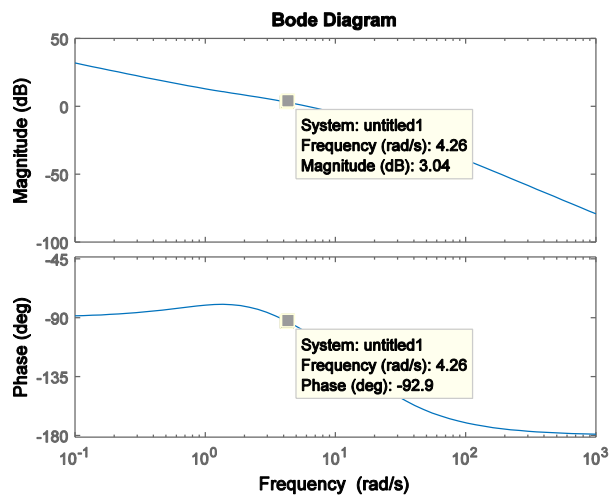
$G_{y'''}(s)$  is defined as

$$G_{y'''}(s) = K_{lead-lag} C_{lead}(s) G_y(s)$$



**Figure 3-17 Step response of the system with the lead compensation**

The Bode plot of the system  $G_{y'''}(s)$  is plotted by Matlab, as shown in Figure 3-18. The low crossover frequency yields a large steady-state error, and the high crossover frequency makes little effect to the system.



**Figure 3-18 Bode plot of the plant with the lead compensation (linear motion)**

Finally, the crossover frequency is determined to be

$$\omega_{cr} = 4.26 \text{ rad/s}$$

**2) Place zero 1 decade below  $\omega_{cr}$**

$$\frac{1}{T} = \frac{1}{10} \omega_{cr}$$

$$T = 2.3474 \text{ s}$$

**3) Calculate  $\alpha$**

According to Figure 3-18

$$20 \log_{10}(\alpha) = 0.315$$

$$\alpha = 1.4174$$

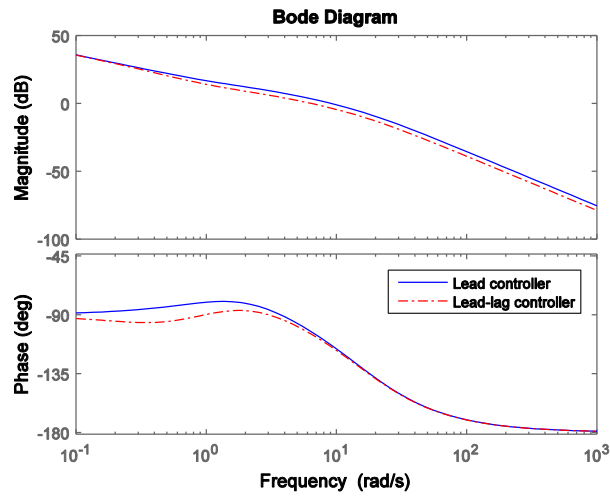
**4) Verify design**

The lead-lag compensation will be

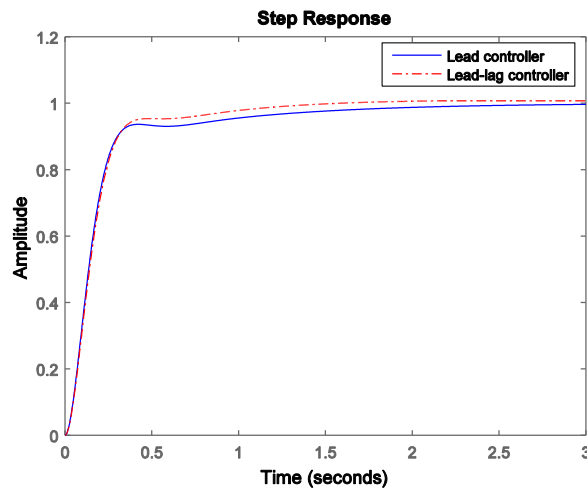
$$C_{lead-lag}(s) = C_{lead}(s)K_{lead-lag} \left( \frac{Ts + 1}{\alpha Ts + 1} \right) = 1.606 \frac{(s + 4.14)(s + 0.426)}{(s + 6.99)(s + 0.301)}$$

Figure 3-19 shows the Bode plot of the two systems. The solid line represents the open-loop system  $G_{y'''(s)}$ . The dash-dotted line represents the system utilizing the lead-lag compensation  $C_{lead-lag}(s)G_{y'''(s)}$ .

Figure 3-20 shows the step response of the closed-loop system with the lead-lag compensation. The overshoot generated by the lag compensation has been eliminated, and the steady-state error of the lead compensation is attenuated.



**Figure 3-19 Bode plot for the lead-lag compensation**

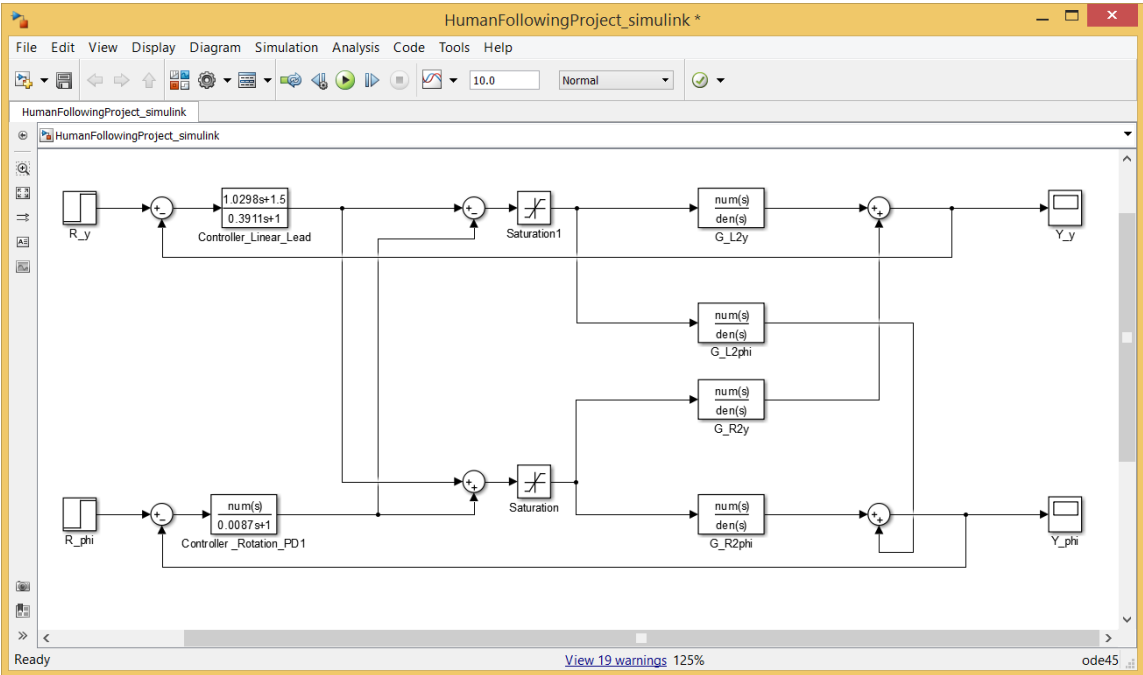


**Figure 3-20 Step response of the system with lead-lag compensation**

### 3.4 Simulation

In this section, Simulink is used to simulate the performance of the controllers designed in the last section. Figure 3-21 is the architecture of the system in Simulink.

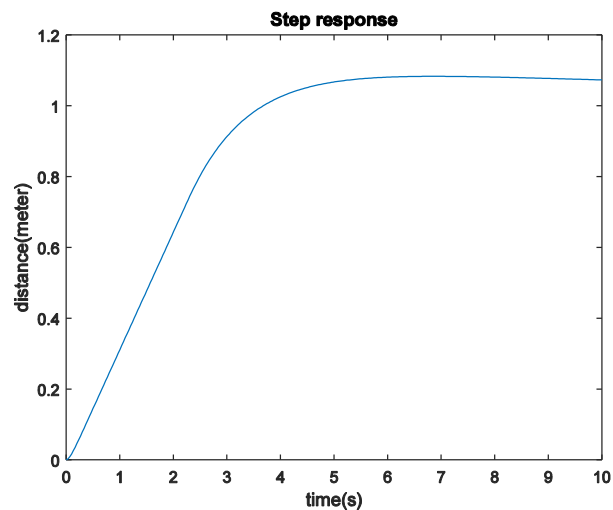
There are two feedback loops in the system, linear motion control on the top and rotational motion control in the bottom. From left to the right are the reference, controller, saturation constraint, plant and output. The saturation constraint blocks are added because there is a physical limitation of the robot's output. The motors of the robot cannot output an unlimited torque to achieve an unlimited responding time. Therefore, step responses and the results of the simulation, will be more close to the practice with saturation constraint blocks.



**Figure 3-21 The system simulated in Simulink**

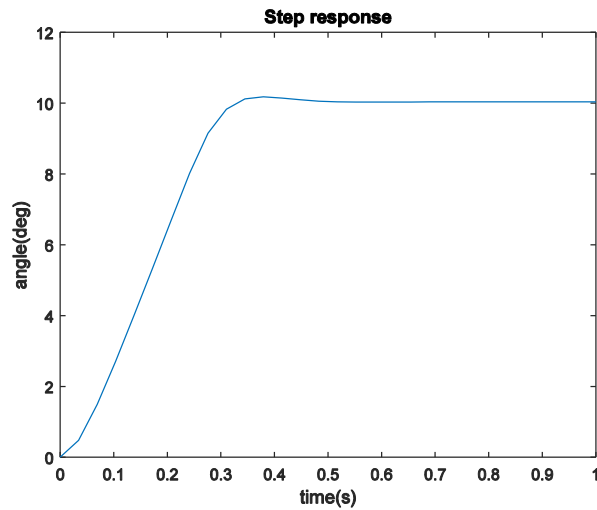
### 3.4.1 PID controller

Figure 3-22 shows the result of the simulation of the PID controller for linear motion control. The rise time is about 3 s, which is slightly slower than the previous analysis (2.3-s rise time), and the steady-state error is about 0.09 m, which is larger than the previous analysis (0.05-m steady-state error). In the first 2.5 seconds, the response is linear. This is because it is at the robot's maximum output, and the saturation constraint block limits the torque output.



**Figure 3-22 Simulation result of PID controller for linear motion**

Figure 3-23 shows the result of the simulation of the PID controller for rotational motion control. The result matches the previous analysis well. The rise time is about 2.3 s, and there is with a  $0.03^\circ$  overshoot, which is very small and acceptable.



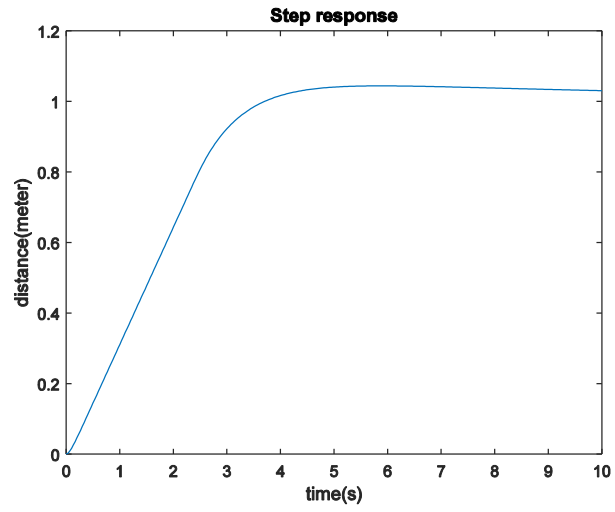
**Figure 3-23 Simulation result of PID controller for rotational motion**

### 3.4.2 Lead-lag controller

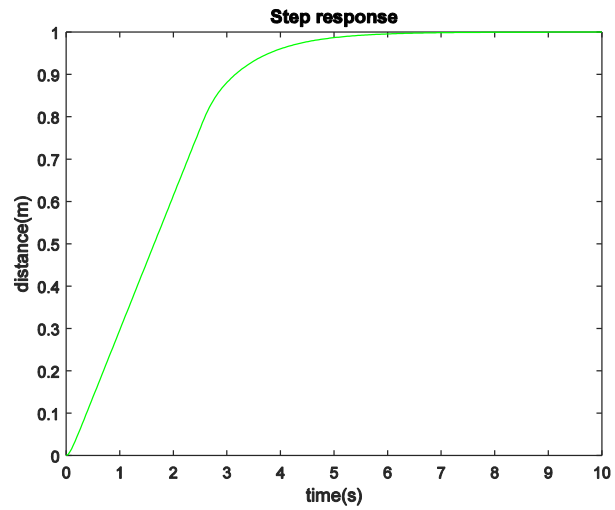
The simulation result of the system with the lag compensation designed for linear motion control in the last section is shown in Figure 3-24. With saturation constraint the steady-state error here is larger than the one analyzed in last section. The steady-state error is about 0.04 m, which is better than that of the PID controller.

Figure 3-25 is the simulation result of the lead controller for linear motion. The rise time is about 2.6 s, and the steady-state error is zero, which makes it better than the other controllers.

Figure 3-26 is the simulation result of the lead-lag controller for linear motion control. It is similar with the result of the lead controller, which also has a 2.6-s rise time and zero steady-state error.

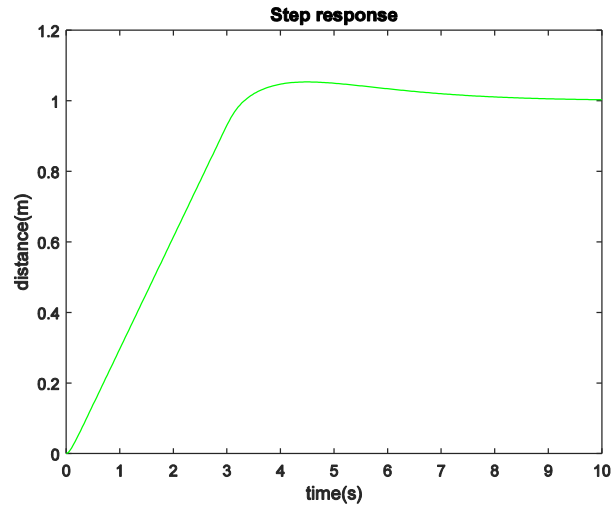


**Figure 3-24 Simulation result of the lag compensation for linear motion**



**Figure 3-25 Simulation result of the lead compensation for linear motion**





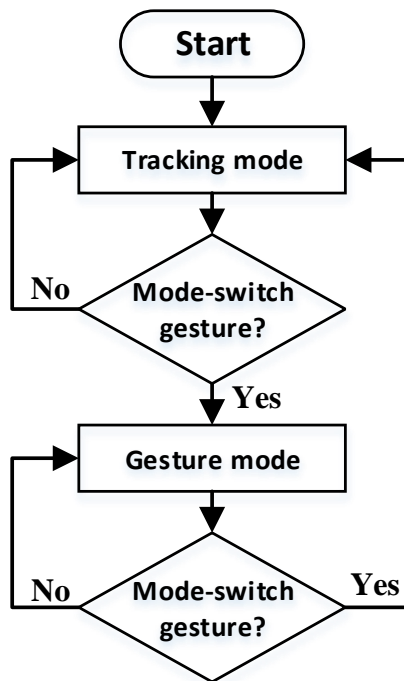
**Figure 3-26 Simulation result of the lead-lag compensation for linear motion**

### 3.5 Technical discussion and evaluation

In this chapter, five controllers were designed, one for the rotation control and four for the linear motion. For the rotation control, the PID controller is good enough for the system. It has a tiny overshoot and a short rise time. For the linear-motion control, the PID controller has a 0.09-m steady-state error, and the lag compensation have a 0.04-m steady-state error, while the lead and lead-lag controller have a better performance (2.6-s rise time, no overshoot, and no steady-state error).

CHAPTER IV  
HUMAN-ROBOT INTERACTION DESIGN

In this chapter, the human-robot interaction system, shown in Figure 4-1, is presented. There are two modes of the interaction system: the human-tracking mode and the gesture-control mode. The default mode is the human-tracking mode because it is the premise for the robot to receive gesture-based commands from the user since the Kinect sensor has to face the user, and the user should be in the detectable range. In section 4.1 the human-tracking mode is discussed. Section 4.2 elaborates the gesture-control mode.



**Figure 4-1** Flowchart of the whole interaction system

As shown in Figure 4-1, the system will begin with the human-tracking mode. Once the system detects the mode-switch gesture, it will shift to gesture-control mode. If not, it will keep tracking the user. Once the system shifts to the gesture-control mode, detecting the mode-switch gesture can exit the gesture-control mode.

## **4.1 Human tracking**

In this section, two human-tracking algorithms are developed for the onboard Kinect sensor and the wide angle camera mounted on the ceiling, respectively. Both data captured by the Kinect sensor and the camera can be adopted for feedback control loop.

### **4.1.1 Human tracking with the Kinect sensor**

#### **4.1.1.1 Human detection**

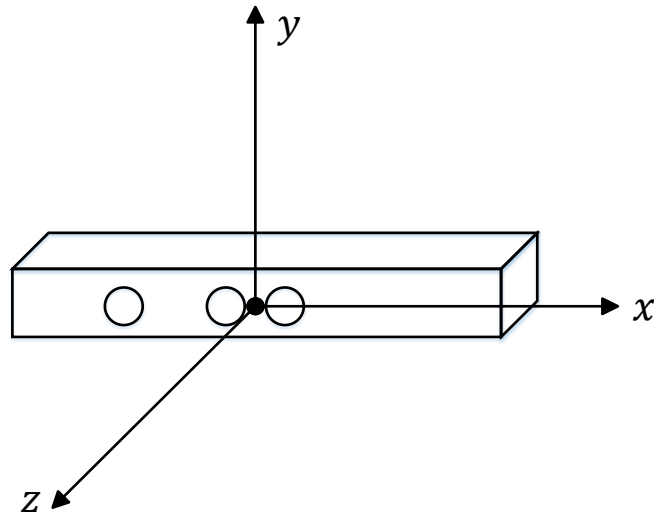
The human detection based on a Kinect sensor relies upon the OpenNI, a middleware introduced before, for two reasons. On the one hand, the real capabilities of the Kinect sensor can be fully assessed, using the framework designed for it. On the other hand, this approach allows to save time because coding for skeleton tracking is not necessary with the OpenNI library.

The reference coordinates defined by the Kinect sensor are shown in Figure 4-2. This is a right-handed coordinate system that place a Kinect at the origin with the positive  $z$ -axis extending in the direction in which the Kinect is facing. The positive  $y$ -axis extends upward, and the positive  $x$ -axis extends to the left.

#### **4.1.1.2 Human-tracking**

Due to physical limitations, given a mobile robot with a Kinect sensor, only one

target can be tracked at a time (although the Kinect sensor is able to track up to six users). The 3D coordinates of the center of mass of the user is obtained by using a set of functions provided by OpenNI.



**Figure 4-2 Reference coordinates of the Kinect sensor**

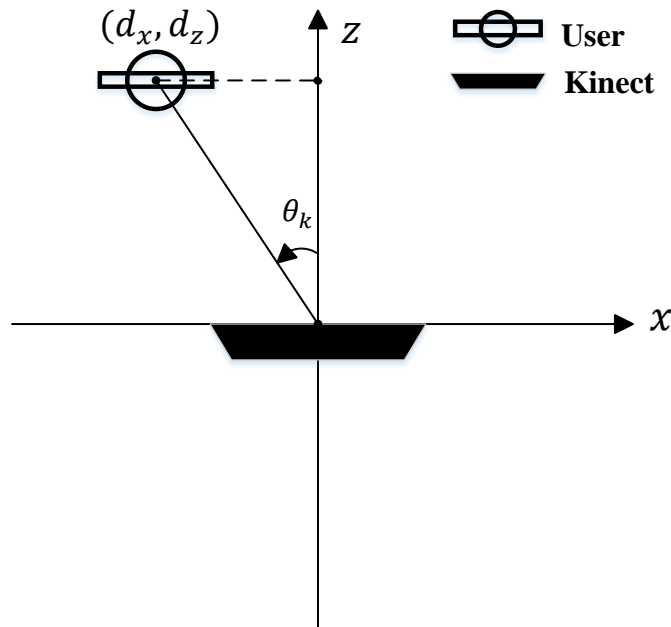
Once the spatial coordinates of the user are obtained, the distance and angle offset are need to be computed, in order to run and reorient the mobile robot according to the motion of the user. In this research, only 2 dimensions are considered ( $x$  and  $z$ ). Considering the reference coordinate shown in Figure 4-2, and by means of basic geometry (see Figure 4-3 and Figure 4-4) the absolute distance of the user (neglect  $y$  dimension) calculated as follows:

$$d_a = (\sqrt{d_x^2 + d_z^2} - \tan(\varphi_k)) \cos(\varphi_k) \quad (4.22)$$

Where  $d_a$  is the distance to the user,  $\varphi_k$  is the angle between the center line of the

Kinect sensor and the horizontal line, and  $d_x$  and  $d_z$  indicate the distance of the user along the  $x$ - and  $z$ -axes. Then the angle between the  $z$ -axis and the user  $\theta_k$  would be

$$\theta_k = \text{atan}\left(\frac{d_x}{d_z}\right) \quad (4.2)$$



**Figure 4-3 The top view of the user in the Kinect's coordinates**

A graphical user interface (GUI) was designed, as shown in Figure 4-5, to indicate the error distance in real time (on the left) and to adjust the reference input by adjusting a slider (on the right).

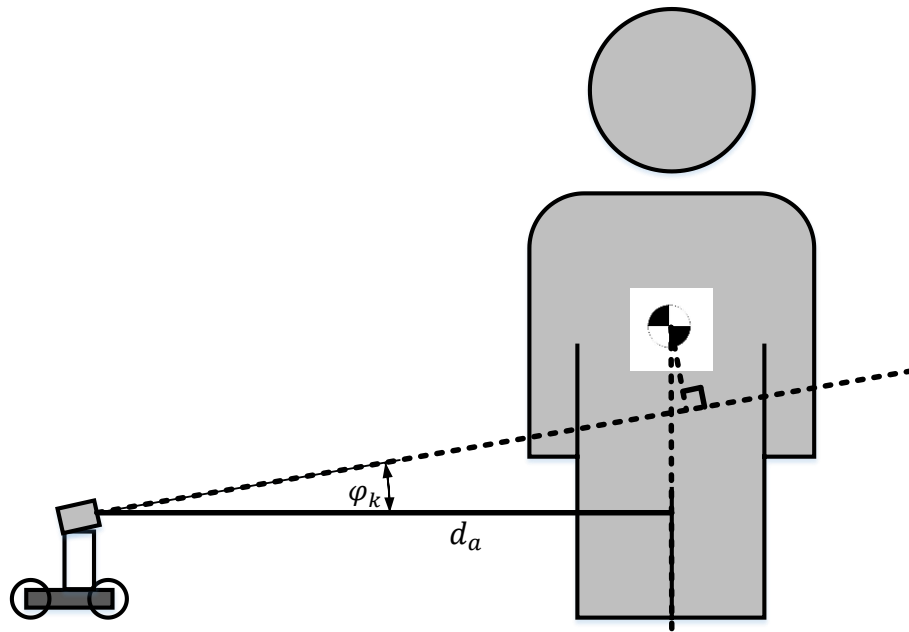


Figure 4-4 The front view of the user in the Kinect's coordinates

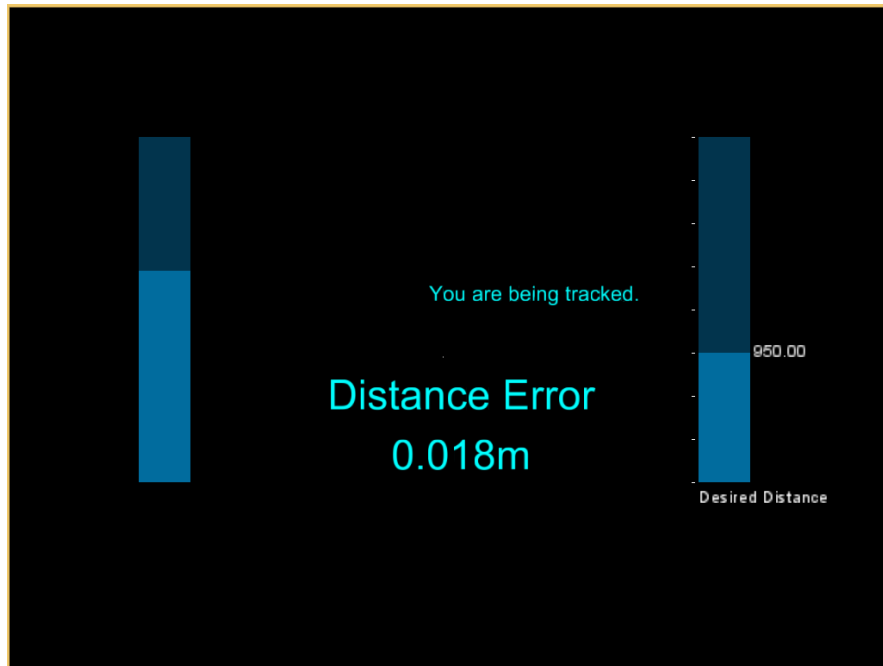


Figure 4-5 Graphical user interface for tracking mode

## **4.1.2 Human tracking with the wide-angle camera**

### **4.1.2.1 Object detection**

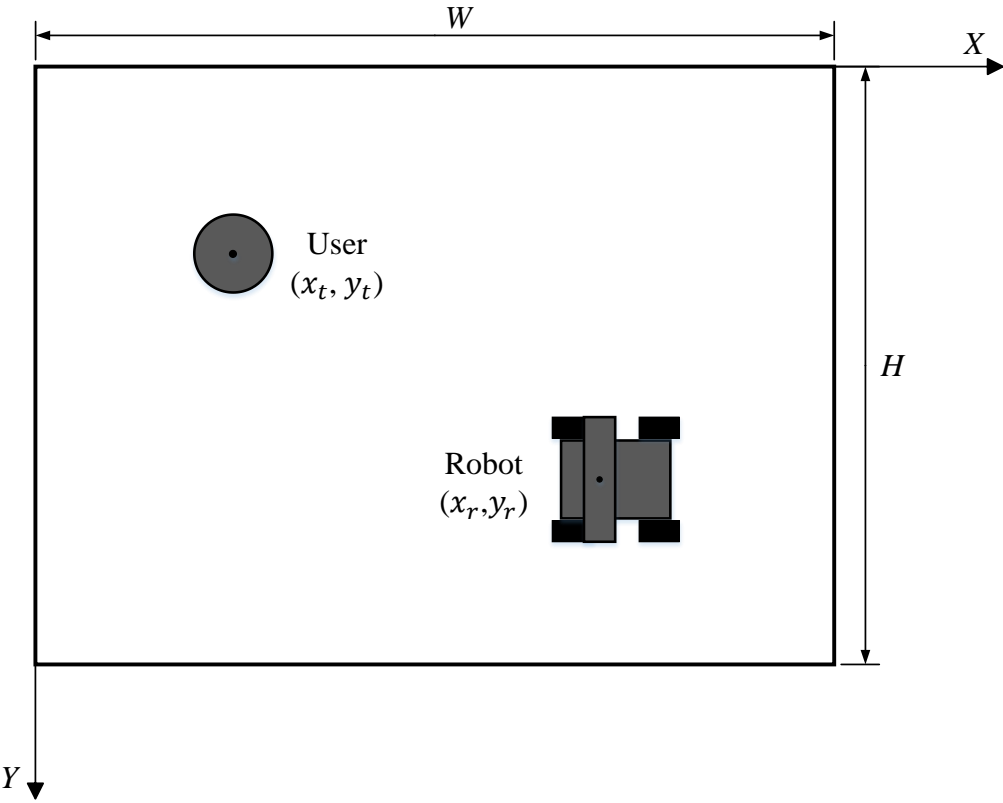
In this research, the object detection based on the camera is realized by the color detection function of OpenCV. OpenCV does provide human-tracking algorithm for developers. However, color detection and tracking is simpler and more reliable. Therefore, the color tracking function provided by OpenCV is adopted in this research. To track of the user and the robot by applying the color tracking algorithm only, the user is asked to put on a cap with specific color, and the robot is decorated with two tapes in different color. All the colors assigned to the user and the robot are not to be spotted easily in a lab environment to avoid the camera mistaking other objects as the interested objects.

### **4.1.2.2 Human tracking**

OpenCV processes images by pixels, so the position of the interested colors also presented by pixels. For instance, Figure 4-6 is a sample image with frame width  $W$  and frame height  $H$ . The positions of the user and the robot are  $(x_t, y_t)$  and  $(x_r, y_r)$ , respectively. The unit of  $W$ ,  $H$ ,  $x_t$ ,  $y_t$ ,  $x_r$  and  $y_r$  is pixel. To get a high frame rate, the frame size is set to  $640 \times 480$ . So the  $W$  here is 640 pixels and the  $H$  is 480 pixels.

The camera-based human-tracking subsystem runs by a C++ program. In this program three specific colors are being tracked, the green color of the hat that the user puts on, the yellow color that decorated on the Kinect sensor, and the pink-color tape that decorated on the rear of the robot, as shown in Figure 4-7. The figure was captured by the camera mounted on the ceiling while tracking. The robot and the user was located

by two red circles with coordinates beside, and denoted by caption “robot” and “user” respectively. The program will keep locating these three colors. To calculate the distance between the user and the robot, the coordinates in pixel should be transformed to be of a unit of length.



**Figure 4-6 A schematic of a camera view**

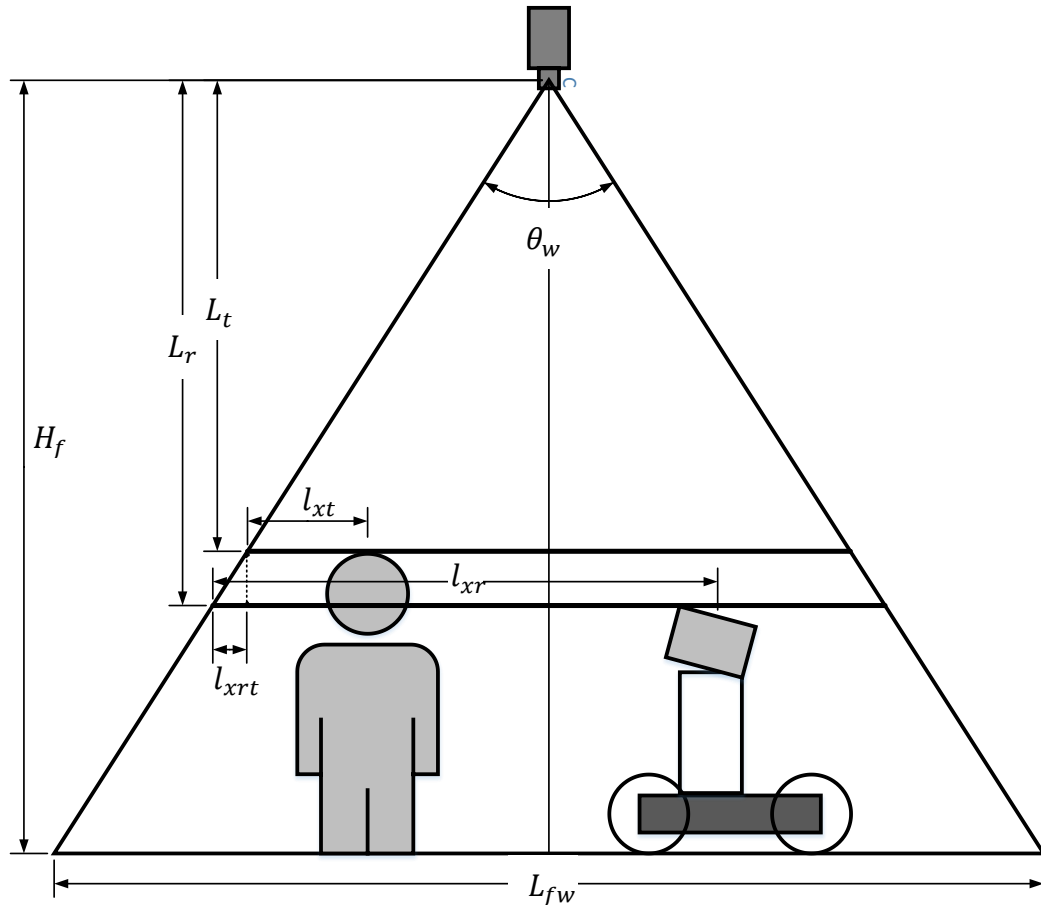




**Figure 4-7 Tracking by the camera**

#### **4.1.2.2.1 Distance calculation**

Figure 4-8 is a schematic diagram to clarify how a camera captures a picture. The schematic diagram is drawn as a front view. That means the length of the view here is related to the width of the frame. To calculate the angle of the view in this direction, the maximum length of the floor that the camera can capture in the direction related to frame width is measured as  $L_{fw}$ . The height of the camera (from the floor to the camera) is measured as  $H_f$ .



**Figure 4-8 A schematic of camera capturing in front view**

So the capture angle of the camera in this direction can be calculated by

$$\tan\left(\frac{\theta_w}{2}\right) = \frac{L_{fw}}{2H_f} \quad (4.3)$$

Assume that the user is of height  $H_t$ . The height from the camera to the user's hat is

$$L_t = H_f - H_t. \quad (4.4)$$

Then the real length that the camera captures at the height of a user is

$$2L_t \cdot \tan\left(\frac{\theta_w}{2}\right). \quad (4.5)$$

Hence, the actual length from the left edge to the user in the  $x$  direction can be calculate by multiply the maximum length in that height with the percentage of pixel

$$l_{xt} = 2L_t \tan\left(\frac{\theta_w}{2}\right) \frac{x_t}{W}. \quad (4.6)$$

The actual length of the robot in the  $x$  direction can be obtained in the same way

$$l_{xr} = 2L_r \tan\left(\frac{\theta_w}{2}\right) \frac{x_r}{W}. \quad (4.7)$$

The height of the robot is longer than that of the user, and the coordinate is calculated from the left edge. So to calculate the distance between the user and the robot in the  $x$  direction, the longer part in the left edge,  $l_{xrt}$ , should be known.

$$l_{xrt} = (L_r - L_t) \tan\left(\frac{\theta_w}{2}\right) \quad (4.8)$$

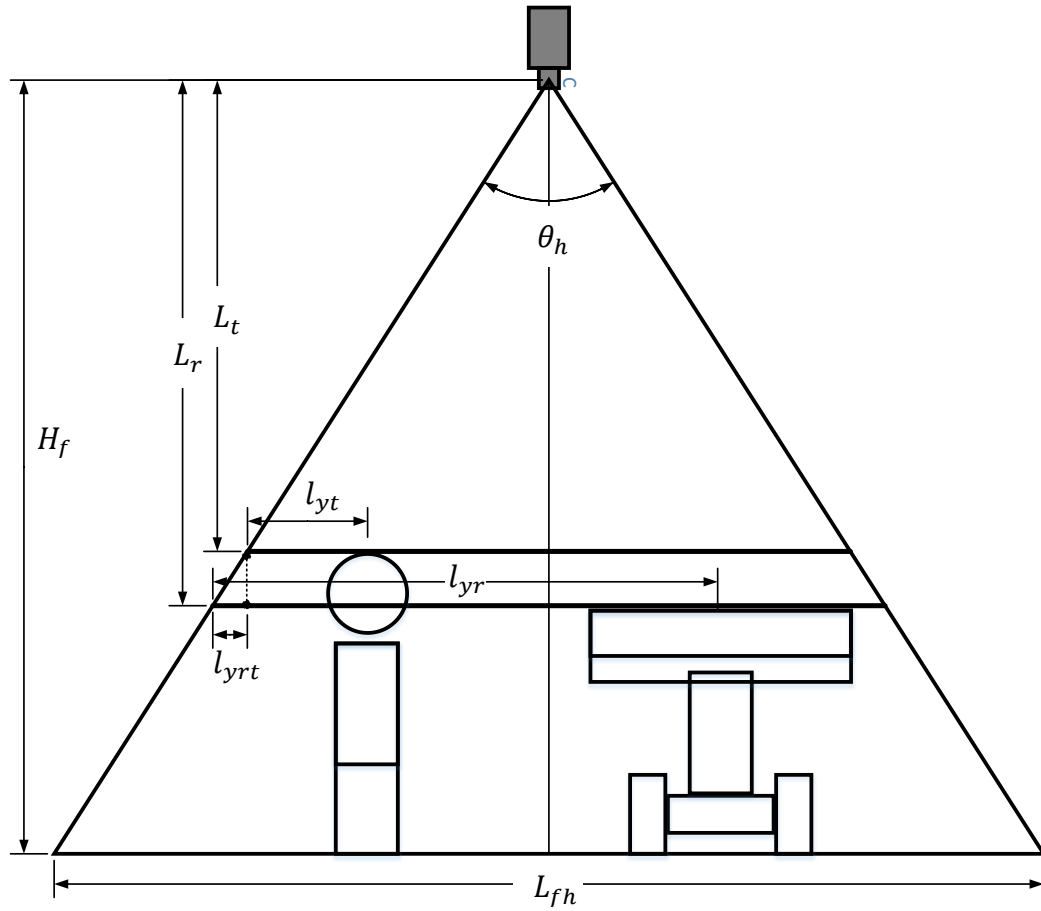
Finally, the distance between the user and the robot in the  $x$  direction can be obtained by

$$l_{xa} = l_{xr} - l_{xt} - l_{xrt} \quad (4.9)$$

Figure 4-9 is a left view, so all the horizontal length in the diagram are in the  $y$  direction. All the processes are the same with in the  $x$  direction. First, obtain the capture angle in this direction

$$\tan\left(\frac{\theta_h}{2}\right) = \frac{L_{fh}}{2H_f} \quad (4.10)$$

Then calculate the length of the user ( $l_{yt}$ ) and the robot ( $l_{yr}$ ) to the left edge in the  $y$  direction.



**Figure 4-9 A schematic of camera capturing in left view**

$$l_{yt} = 2L_t \tan\left(\frac{\theta_h}{2}\right) \frac{y_t}{W} \quad (4.11)$$

$$l_{yr} = 2L_r \tan\left(\frac{\theta_h}{2}\right) \frac{y_r}{W} \quad (4.12)$$

Next, the actual distance between the user and the robot in the y direction.

$$l_{yrt} = (L_r - L_t) \tan\left(\frac{\theta_h}{2}\right) \quad (4.13)$$

$$l_{ya} = l_{yr} - l_{yt} - l_{yrt} \quad (4.14)$$

Finally, the distance between the user and the robot in 2D is

$$l_a = \sqrt{l_{xa}^2 + l_{ya}^2} \quad (4.15)$$

#### 4.1.2.2.2 Angle offset calculation

The angle offset calculation is based on the rule of cosine. There are two points of the robot being tracked by the camera, the Kinect sensor on the front and the paper board on the rear, as shown in Figure 4-10. The position of the Kinect sensor is taken as the position of the robot, and the position of the paper board is to calculate the orientation of the robot.

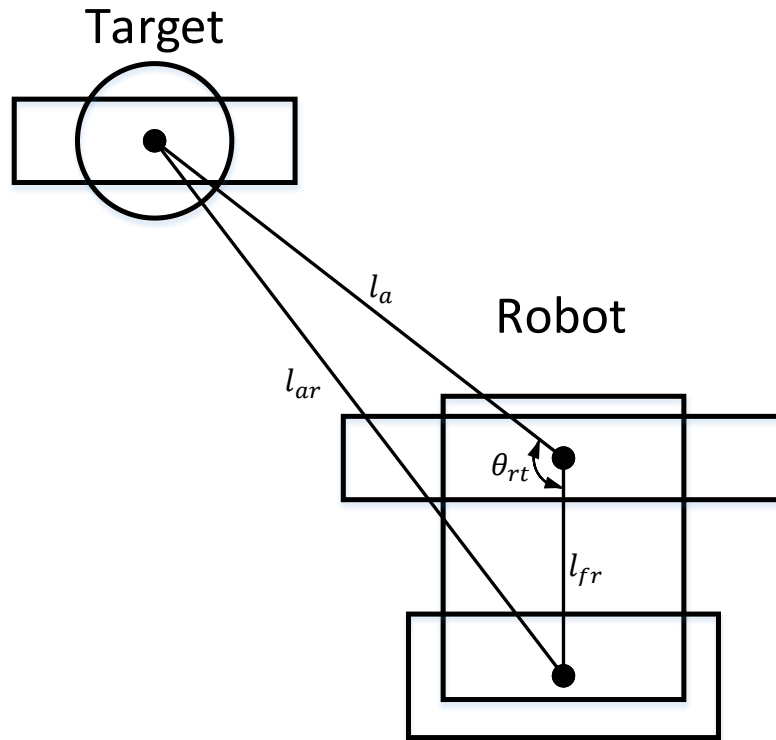
According to the rule of cosine, the angle offset  $\theta_{rt}$  is given by

$$\theta_{rt} = \arccos\left(\frac{l_a^2 + l_{fr}^2 - l_{ar}^2}{2l_a l_{fr}}\right) \quad (4.16)$$

#### 4.1.3 The whole process of tracking

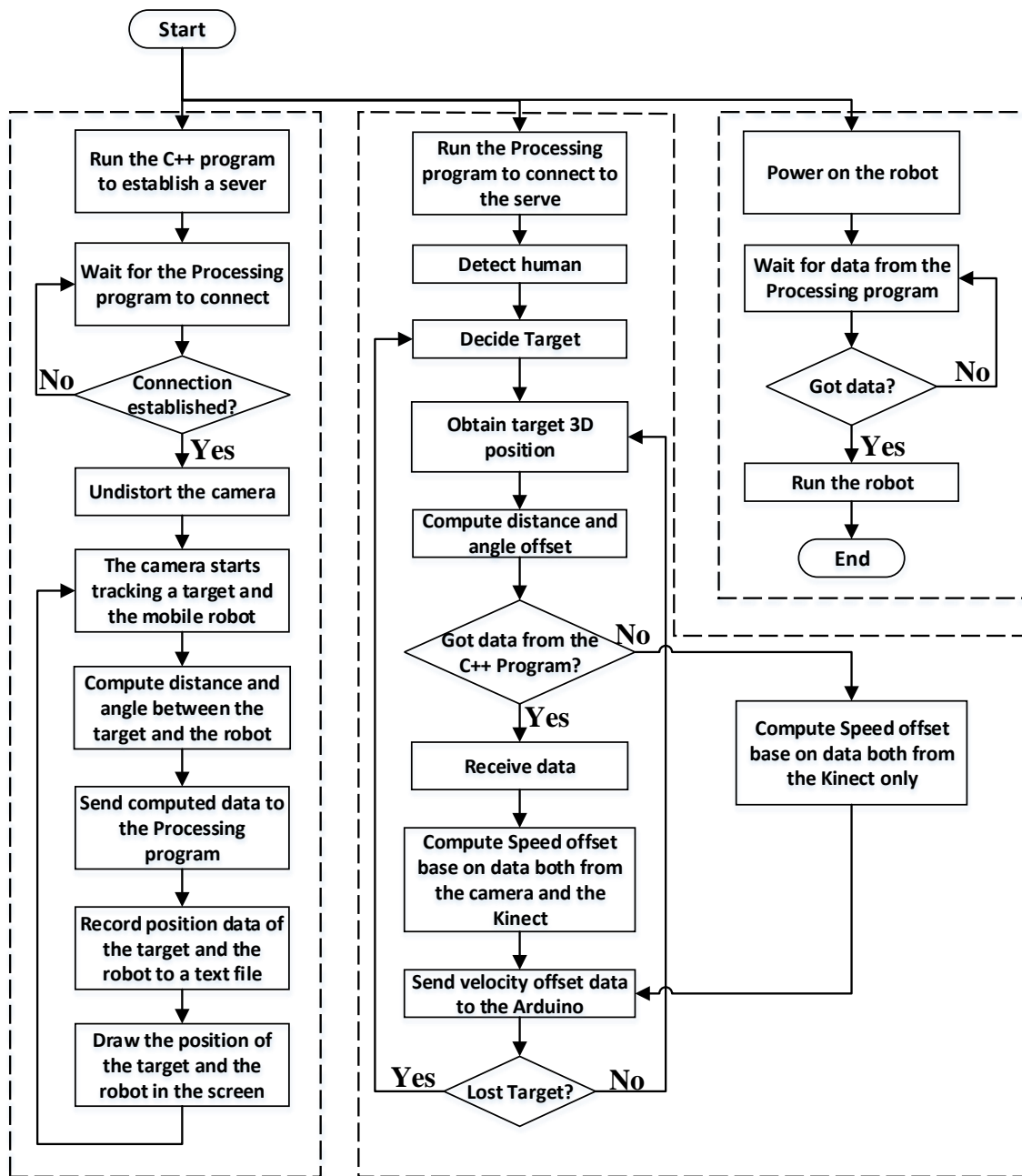
There are three individual programs involving the tracking process, the C++ program operating the wide-angle camera, Processing program running the Kinect sensor, and Arduino program governing the mobile robot. They are shown in the left, middle, and right columns in Figure 4-11, respectively. To start the system, first power on the robot, and the Arduino program will run automatically. Second, run the C++ program, and a data communication server will be established. However, at this moment the camera is not yet tracking. The C++ program will not move to next step until the Processing program makes a connection to it successfully. Finally, run the Processing

program. Once the connection is established, the whole system works normally.



**Figure 4-10 A schematic of camera capturing in top view**

For the C++ program, at first, it reads camera calibration data, which are the output of a camera calibration program. Second, after processing these data, the camera starts tracking three specific colors and outputs their coordinates in pixel. Third, it computes the distance and angle between the user and the robot according to the algorithm discussed above. Forth, it sends these data to the Processing program for further computation.



**Figure 4-11 Flowchart of the human-tracking system**

Fifth, it records the position data of the user and the robot as a text file for further

analysis. Sixth, it draws three different color circles in a captured video to indicate the location of the user and the robot. Then, it goes back and repeats tracking processes.

For the Processing program, after connected to the C++ server, the system will detect a human within the Kinect sensor's detectable range. The first detected person becomes the user to be tracked. Then the processing program obtains the position of the user's center of mass. After computing the distance and angle offset, the system determines whether the C++ program is sending data. If yes, then the system processes data from both the camera and the Kinect sensor. If not, the system processes data from the Kinect sensor only. These distance and angle data are processed by one of the controllers designed in the last chapter to calculate the desired velocity offset for the robot to track the user. Then these velocity offset data are sent to the Arduino program. Next, the system checks if the user has lost tracking or not. If the robot lost tracking of the user, it tries to detect human again. If not, it repeats to obtain the position of the user and keeps tracking.

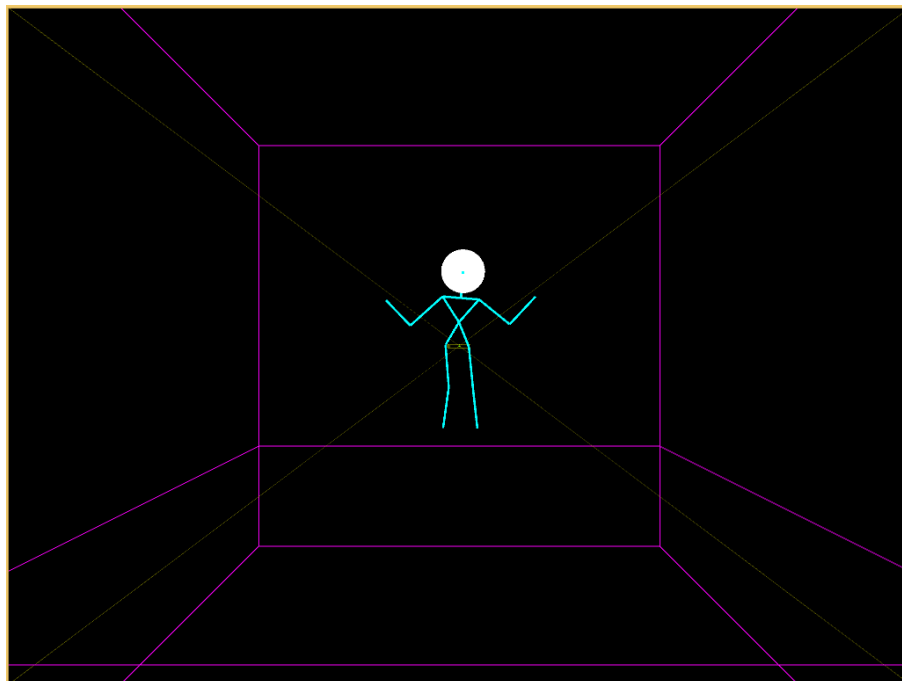
For the Arduino program, it just simply waits for the velocity offset data from the Processing program. Once it receives the data, it runs the robot.

## **4.2 Gesture control**

In chapter 1, several gesture recognition techniques and applications were presented. According to the motivations for a user-friendly robot to interact with, in this chapter, the implementation of the gesture-control system is presented. To achieve a practical gesture-based interaction system, four gestures are defined, aiming to implement a vision-based gesture recognizer. Within the whole set of defined gestures,



the system is designed to recognize only body gestures since hand gestures are unrecognizable. Figure 4-12 shows the GUI designed for the gesture-control mode. A virtual stage, Kinect sensor, and the skeleton of the user are drawn in the program window.



**Figure 4-12 GUI for gesture controlling mode**

#### **4.2.1 Skeleton tracking**

Figure 4-13 shows the skeleton that the Kinect sensor tracks. The Kinect sensor tracks all the joints of the body and OpenNI is used as a middleware to access these data. These data contain geometry information of all the joints of the skeleton.

## 4.2.2 Gesture definition

This section presents the gestures the system is able to recognize. The vocabulary consists of the four gestures presented below:

- Switch to controlling
- Switch to tracking
- Lamp creation
- Lamp selection and color control

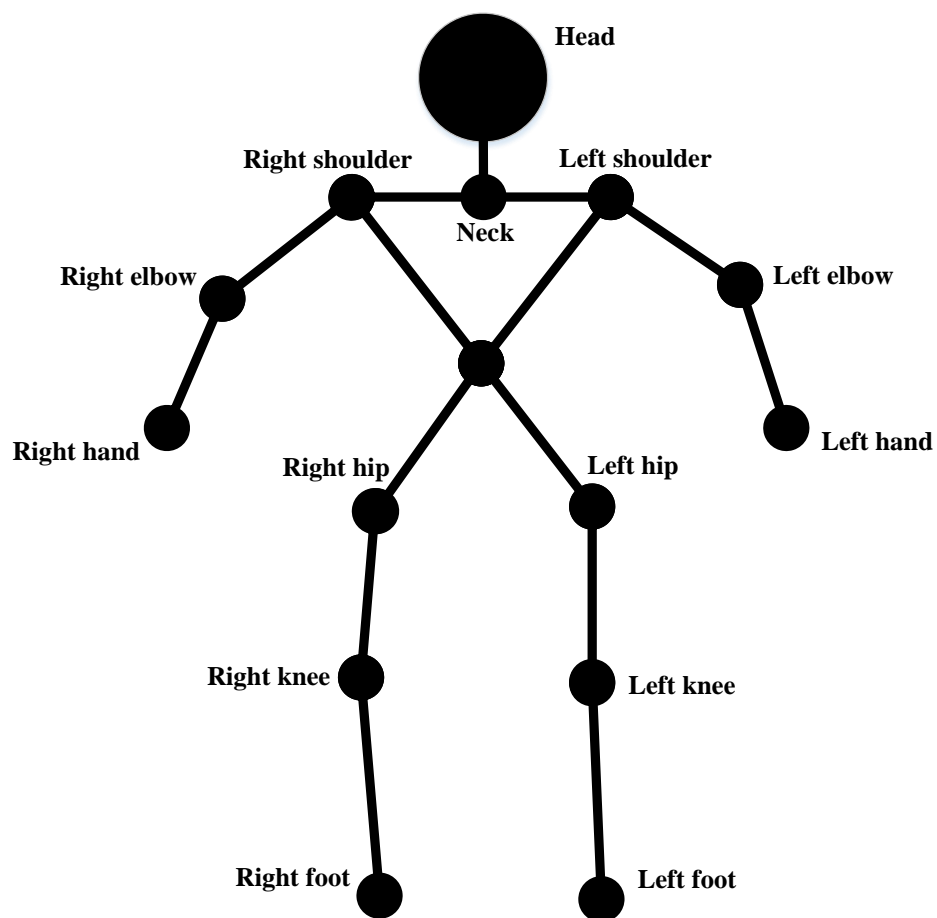


Figure 4-13 The Skeleton that the Kinect sensor tracks

The gestures are defined by stipulating some angles of joints. Part of these gestures are referred to [22]. The three gestures are just designed to show the robot's interaction capability, it is easy to increase the number of recognizable gestures by adding definitions.

#### Gesture 1: Switch to controlling

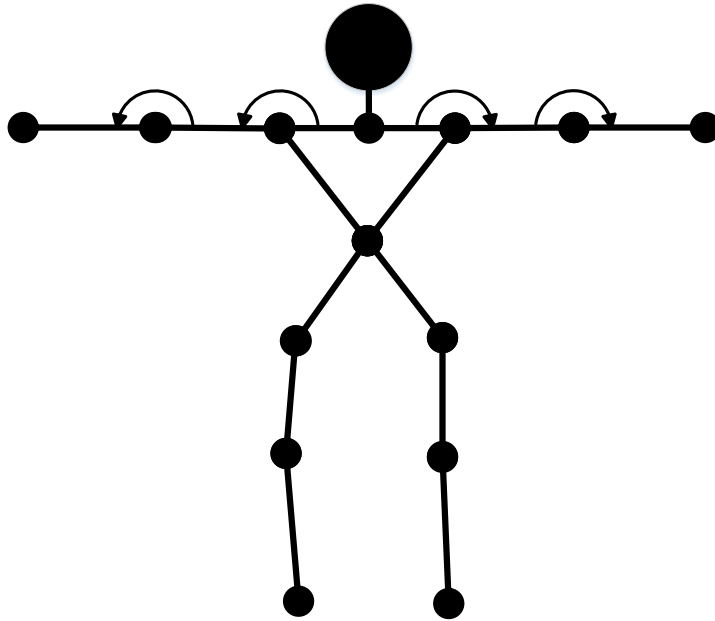
This gesture is used to switch from the tracking mode to the gesture controlling mode. The gesture requires the user to raise his/her arms laterally. The gesture is chosen for three reasons: first, it is easy to execute. Second, it is easy to be recognized by the sensor because there is no overlap of the body. Third, people do not raise their arms that high while they are walking, so it is hard to be mistaken.

To inform the robot that the user is performing this switch gesture, four angles of joints are stipulated to be close to  $180^\circ (\pm 10^\circ)$ , as shown in Figure 4-14. Therefore, whenever all these angles are met the requirement of the stipulation, actions of this mode-switch gesture is triggered.

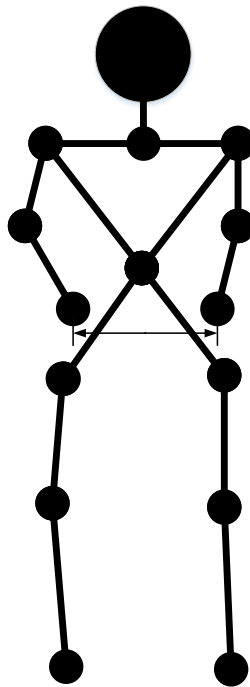
#### Gesture 2: Switch to tracking

This gesture is used to switch from the gesture controlling mode to the tracking mode. The gesture requires that the user expose his/her arms in front of the Kinect sensor and make them closer.

To inform the robot that the user is performing this switch gesture, the distance between the user's hands must be closer than 0.01 m, as shown in Figure 4-15. Therefore, whenever the distance meets the requirement of the stipulation, actions of this mode-switch gesture is triggered.



**Figure 4-14 Scheme of the gesture to switch to gesture controlling mode**

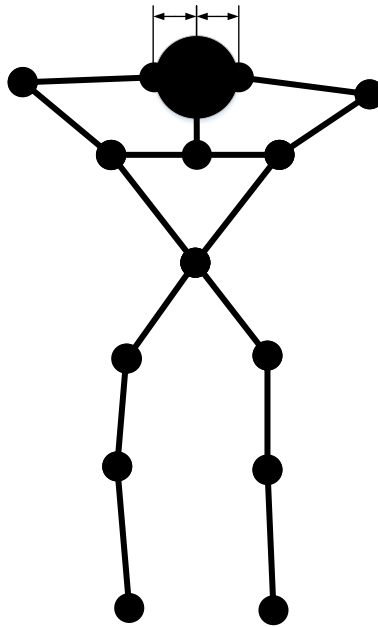


**Figure 4-15 Scheme of the gesture to switch to tracking mode**

### Gesture 3: Lamp creation

This gesture is to create a virtual lamp in the reference coordinates of the Kinect. In other words, it is use to tell the Kinect where the lamp is located. Since the object recognition application has not been added to the system yet, this is a practical way to locate a lamp in the Kinect coordinates. Once this gesture is recognized, the position of the center of mass of the user will be recorded and regarded as the position of the lamp, and a rectangle will be drawn in the GUI window to indicate the location of the lamp.

This gesture requires the user to touch his/her head with hands. To define this gesture in the program, the distance between each hand to the head of the user will be evaluated, as shown in Figure 4-16. If the distances are around 0.1 m ( $\pm 0.05$  m), the lamp creation gesture is triggered.

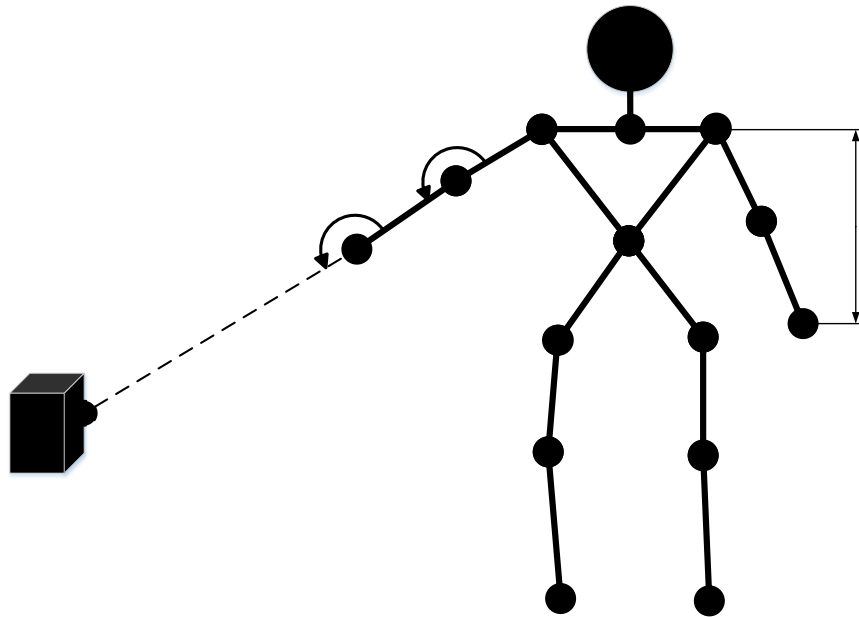


**Figure 4-16 Scheme of the lamp creating gesture**

#### Gesture 4: Lamp selection and color control

This gesture is used to tell the robot which lamp the user selected and to change the color of the lamp. When the system recognizes that the user points to one of the lamps created before with his/her right hand, the rectangle in the GUI turns white to indicate that the lamp is selected. In the meantime, the color of that lamp will be changed according to the height of the user's left hand.

For this gesture, the user is required to use his/her right hand to point to the virtual lamp, which is located at the position that the user performed the lamp creation gesture. To adjust the color of the lamp, the user needs to raise his/her left hand. The color of the lamp is changed according to the level of the user's left hand, as shown in Figure 4-17.



**Figure 4-17 Scheme of the lamp selecting and color changing gestures**

### 4.2.3 Gesture control

For the gesture-control system, as shown in Figure 4-18, at the beginning, the system tracks the user's skeleton. Then the system decides whether the user is performing the gesture for switching to gesture controlling mode or not. If yes, it switches to the human-tracking mode. If not, it evaluates specific joint angles and joint distances to see if the user is touching his/her head or pointing to a lamp. If the user is touching his/her head, the system creates a virtual lamp at the position of the user's center of mass. If the user is pointing to a lamp, it turns white that lamp in the GUI and changes the color of the lamp based on the level of the user's left hand.

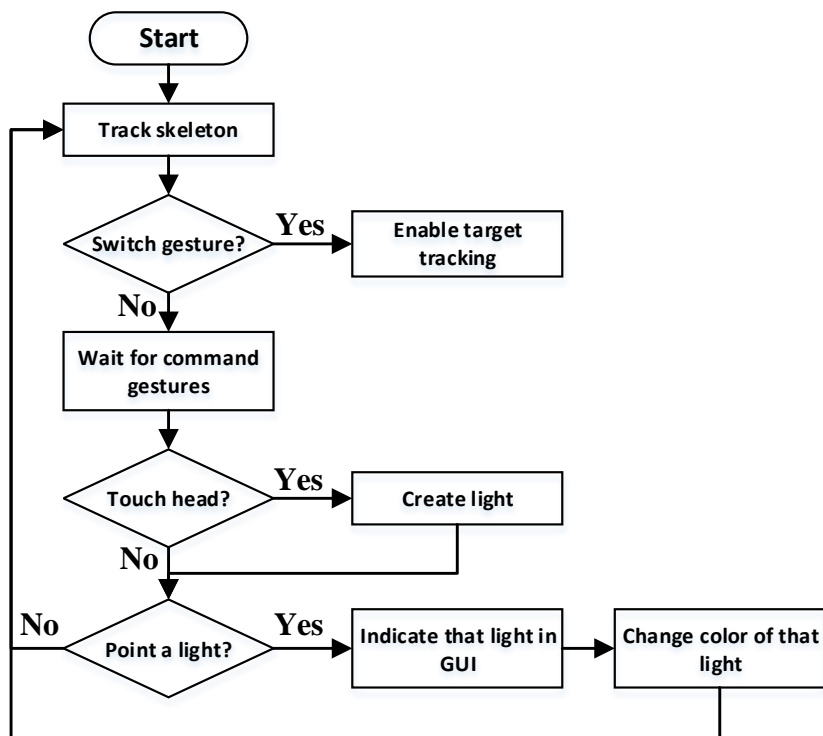


Figure 4-18 Flowchart of the gesture-control system

## CHAPTER V

### EXPERIMENTAL RESULTS

In this chapter the performance of the robot is evaluated by analyzing the obtained results. Two types of experiments are performed, in order to evaluate the following aspects of the robot:

1. Robustness of the human-tracking subsystem
2. Reliability of the gesture-control subsystem

The experimental platform is shown in Figure 5-1. The figure is captured by the wide-angle camera mounted on the ceiling. The camera is used to capture the position of the robot and the user. The Kinect sensor was decorated with yellow tape, while the user to be tracked is asked to put on a green hat. The C++ program was set to track these two colors. The black marks on the floor are to indicate distance and angle between the user and the robot. The three marks on the left are to denote the distance (from left to the right are 2, 1.5 and 1 m, respectively). The four marks on the right are to denote the angle (from top to the bottom are  $20^\circ$ ,  $15^\circ$ ,  $10^\circ$ , and  $0^\circ$ ). The robot will be placed on designated mark, and the user is standstill on a designated mark either in every test. In each of the following experiments, the experimental setup is first detailed and then the results of the test are discussed.





**Figure 5-1 Experimental platform**

## **5.1 Human-tracking evaluation**

In this section experiments performed on the sole human-tracking subsystem are presented in order to evaluate the robustness of such system with respect to analyzing the time response diagrams.

### **5.1.1 Experimental design**

There are four experiments to evaluate the robot's tracking performance. The first one is to test the linear motion of the robot exclusively. The second one is to test the rotational motion of the robot exclusively. The third one is to test both linear motion and rotational motion at the same time. The fourth one is 2D trajectory tracking. Although

the robot is connected to the laptop with wires during the experiments, it can move freely on the floor, and the influence of the wires is minimal and neglected.

### 5.1.1.1 Linear motion

For this experiment, a set of tests is carried out to obtain the linear response data of the four controllers developed in Chapter III to various distances. The experiment is executed with one subject acting as the user to be tracked by the robot. As shown in Figure 5-2, the robot is placed on the 2-m mark or 1.5-m mark (2-m mark in Figure 5-2) on the floor of the lab, and facing the  $0^\circ$  mark, while the user is asked to face the robot and stand still in front of it during the tests.



**Figure 5-2 Configuration of the linear motion experiment**

Each distance is performed four times (performed by four different controllers), for an overall execution of eight times. During the experiment the distance between the robot and the user is recorded by both the Kinect sensor and the camera. The reference distance input is set to be 1 m. Therefore, when the tracking begins, the robot will rush to the user and then stop at the 1-m mark in front of the user. Since the robot is placed 2 or 1.5 m away from the user, two step responses with amplitude of 1 and 0.5 m are obtained.

#### **5.1.1.2 Rotational motion**

For the rotational motion experiment, a set of tests is carried out to obtain the rotational response data of the PID controller to different angles. This experiment is also executed with one user to be tracked by the robot. The robot is placed on 2-m mark, as shown in Figure 5-3.

The user is asked to stand still in front of the robot on three different marks,  $10^\circ$ ,  $15^\circ$  and  $20^\circ$  ( $15^\circ$  in Figure 5-3). The test is performed once per angle. During the experiment the angle between the robot and the user is recorded by the Kinect sensor only. The reason the angle calculated by the camera is not adopted is it has an error about  $30^\circ$ , which is unacceptable. The error is large because the two points of the robot tracked by the camera is too close.

The reference angle input is set to be  $0^\circ$ . Therefore, when the tracking begins, the robot turns and faces the user straightly. Since the user is standing on the  $10^\circ$ ,  $15^\circ$ , or  $20^\circ$  mark, 3 step responses with the amplitudes of  $10^\circ$ ,  $15^\circ$ , and  $20^\circ$  will be obtained.



**Figure 5-3 Configuration of the rotation experiment**

### **5.1.1.3 Overall performance**

In this experiment, two set of tests is carried out to obtain the rotational response data of the lead and lead-lag controller, respectively. The robot is placed on the 2-m mark. The user is asked to stand still in front of the robot on the 15° mark. During the experiment the distance and angle between the robot and the user is recorded by the Kinect sensor and the camera. The reference angle input is set to be 0°, and the reference distance input is set to be 1 m. Therefore, when the tracking begins, the robot runs and turns to the user simultaneously.

### **5.1.1.4 2D trajectory tracking**

This experiment is to show the tracking capability of the robot. The laptop

connected to the robot is placed on top of a moveable chair. In order to reduce the influence of the wire tension to the robot, the chair is moved by a volunteer following the robot wherever the robot moves. The user is ask to walk randomly within the view of the wide-angle camera. The robot is set to track the user and maintain a 1-m safe distance. During the experiment, the positional data of the user and the robot are recorded by the camera, and Matlab is used to generate trajectories of the user and robot.

### **5.1.2 Results**

In this section the results from the four experiments are presented. The results from the Kinect sensor alone and from the wide-angle camera are compared in the linear-motion experiments. The experimental results of the first three experiments are presented by giving step responses. For the linear-motion control, only results performed by the lead-lag controller are presented, since it is the best. For the rotational motion control, all the results are performed by the PID controller, since it is the only controller developed for the rotational motion. All the responses in time domian are obtained by Matlab.

#### **5.1.2.1 Linear motion**

The experimental result of the linear motion control is presented by collecting distance data by the wide-angle camera and the Kinect sensor and comparing them with the simulation result. In this section, each step response consists of three lines. The solid line represents the distance detected by the wide-angle camera, which is more reliable and can be considered the real distance. The dash-dotted line represents the distance detected by the Kinect sensor. The dashed line represents the simulation result.

### 5.1.2.1.1 Performed by the Kinect sensor only

In these set of experiments only the data sent by the Kinect sensor were adopted for feedback control. The data recorded by the camera are used only as a reference.

Figure 5-4 shows the linear-motion experimental result of the system performed by the Kinect sensor (the camera is not included in the feedback loop) with initial distance at 1 m.

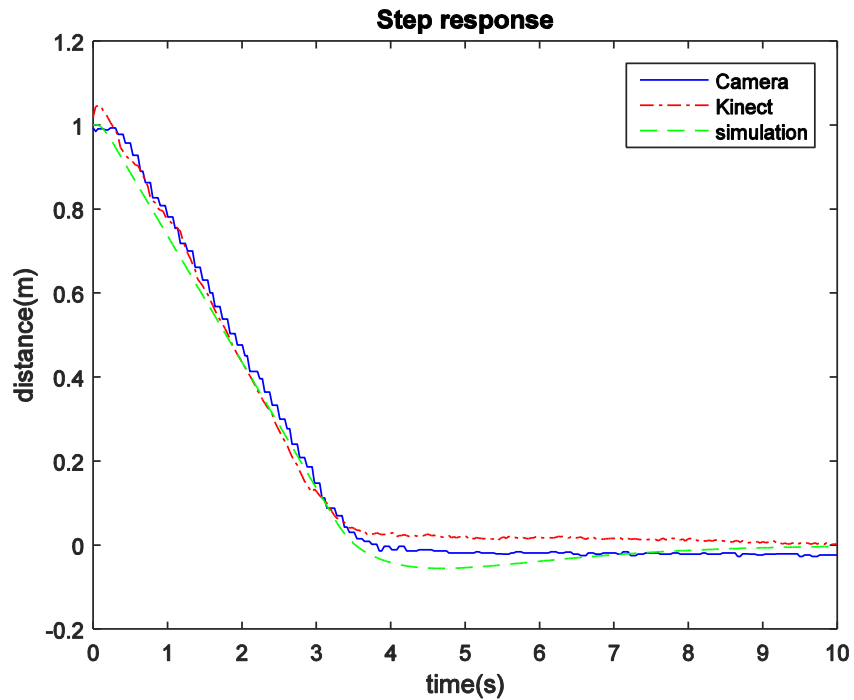


Figure 5-4 Experimental result of the lead-lag controller (1 m)

In the first 3.3 seconds, the experimental result match well with the simulation result. After 3.3 s, there is a small error (about 0.001 m) of the data captured by the

Kinect sensor. The Kinect sensor locates the center of mass of the user actually. However, it cannot calculate the precise position of the user sometime while it is too close to the user and cannot capture the whole body of the user. Apart from this error, comparing the data of the Kinect to the simulation result, there is a small error as well. The error is caused by the physical limitation of the robot's hardware. Since there is a dead-zone in the torque output of the robot due to friction, the robot would not move if the duty ratio of the PWM signal is smaller than 5%. However, a 0.05-m steady-state error is acceptable for tracking in our application.

Figure 5-5 shows the linear motion experimental result of the system performed by the Kinect sensor with initial distance at 0.5 m. As shown in the figure, there is some delay and small oscillations (range of 0.04 m) between 2–3 s. Actually, the robot was not shaking, the oscillations is generated by the method accessing to the position of the user.

#### **5.1.2.1.2 Performed by the wide-angle camera**

In this set of experiments only the data captured by the camera is adopted for feedback control. The data recorded by the Kinect sensor are used only as a reference.

Figure 5-6 shows the linear-motion experimental result of the system performed by the camera with the initial distance at 1 m. The experimental result match with the simulation result well, with little delay (0.3 s), which may be caused by the uncertainty of the system including the friction between the wheels and the lab floor.

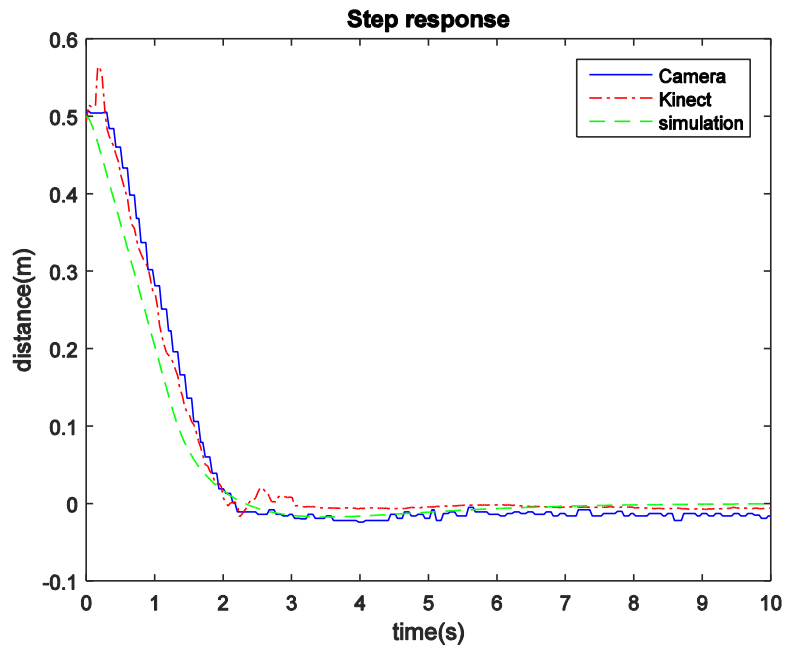


Figure 5-5 Experimental result of the lead-lag controller (0.5 m)

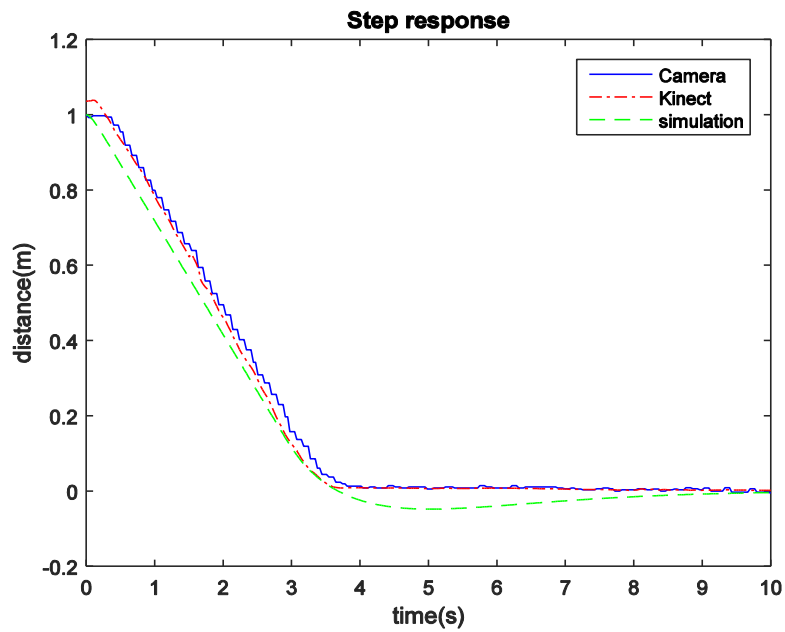
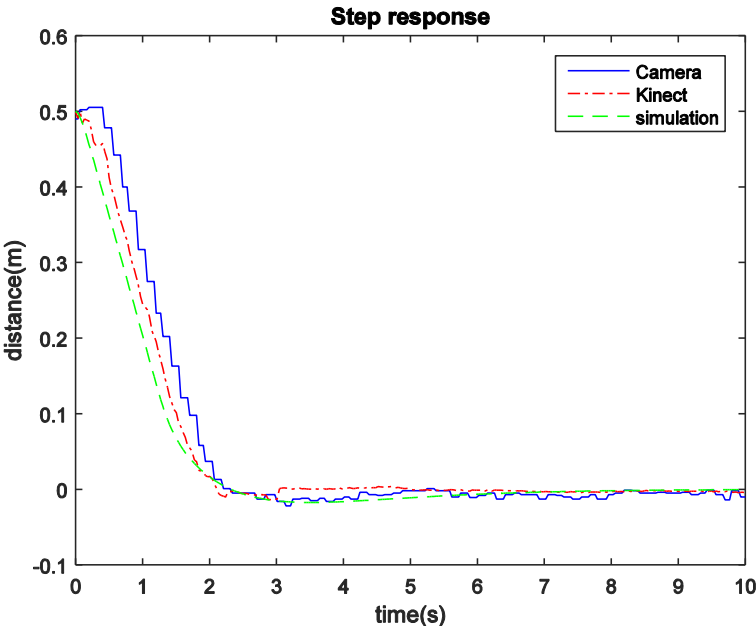


Figure 5-6 Experimental result of the lead-lag controller (1m)



Figure 5-7 shows the linear-motion experimental result of the system performed by the camera with the initial distance at 0.5 m. As shown in the figure, the experimental result matches the simulation result well, except small oscillations occurring in 4–10 s, which is of the range of 0.03 m. The oscillations are caused by the motion of the user, since no one can really stand still. One may also find that there is a small delay in the response of the camera, compared with the response recorded by the Kinect sensor. Actually, the delay was caused by the communication between the Processing program and the C++ program. The C++ program records the data captured by the camera and then sends them to the Processing program, and then combines them with the data recorded by the Kinect sensor. Therefore, sometimes there is a small delay in the camera's data.



**Figure 5-7 Experimental result of the lead-lag controller (0.5m)**

### 5.1.2.2 Rotational motion

After initial tests, it turned out that the angle calculated by the camera's data was not precise for steering. This error was more than  $30^\circ$ . The reason for the error is that the two points of the robot chosen for tracking is too close. Therefore in this section, the angle data from the camera are eliminated. The dashed line denotes the data recorded by the Kinect sensor, and the solid line represents the simulation result.

Figure 5-8 shows the rotation experimental result performed by the Kinect sensor with the initial angle of  $10^\circ$ . There were some delay and a small overshoot, but the steady-state error was quite small (about  $0.3^\circ$ ). The experimental result of the system for  $15^\circ$  rotation is shown in Figure 5-9. There is a 0.2-s delay, while the steady-state error are still small.

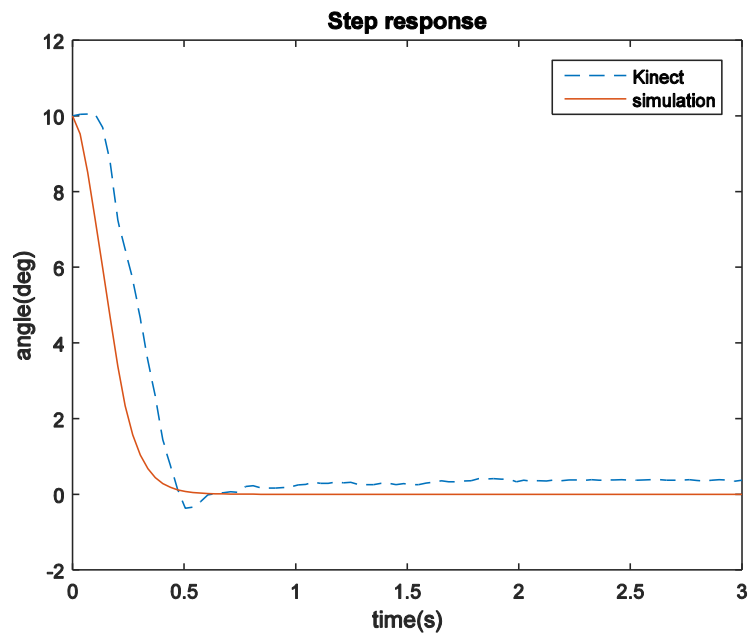
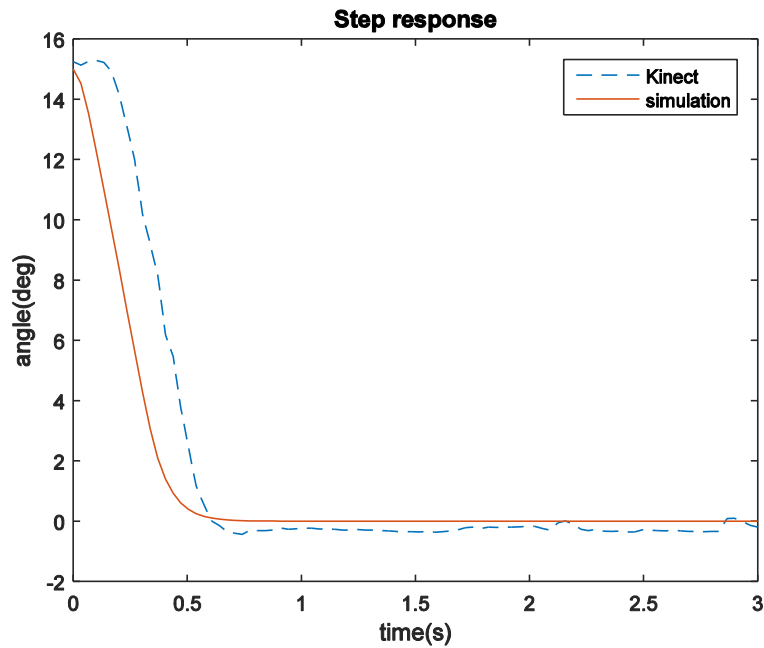


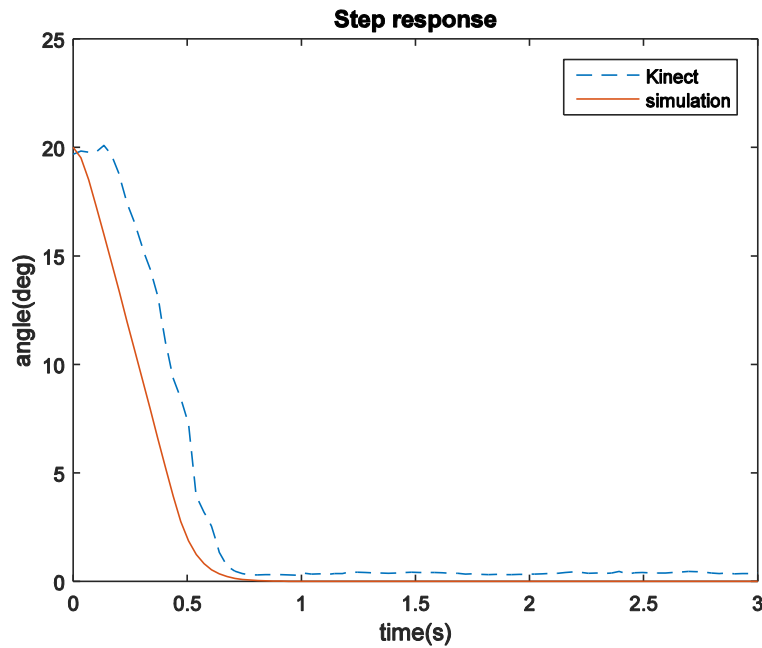
Figure 5-8 Experimental result of the PID controller for rotation ( $10^\circ$ )



**Figure 5-9 Experimental result of the PID controller for rotation (15°)**

Figure 5-10 shows the experimental result of the system for 20° rotation. There is still a 0.2–0.3-s delay. The delay of the rotation maybe caused by the uncertainty of the system including the friction between the wheels and the lab floor.

For the rotational motion experiments, the results shares common phenomena, small response delay (about 0.2 s) and very small steady-state error (smaller than 1°). Tests proved that the small delay does not affect tracking.

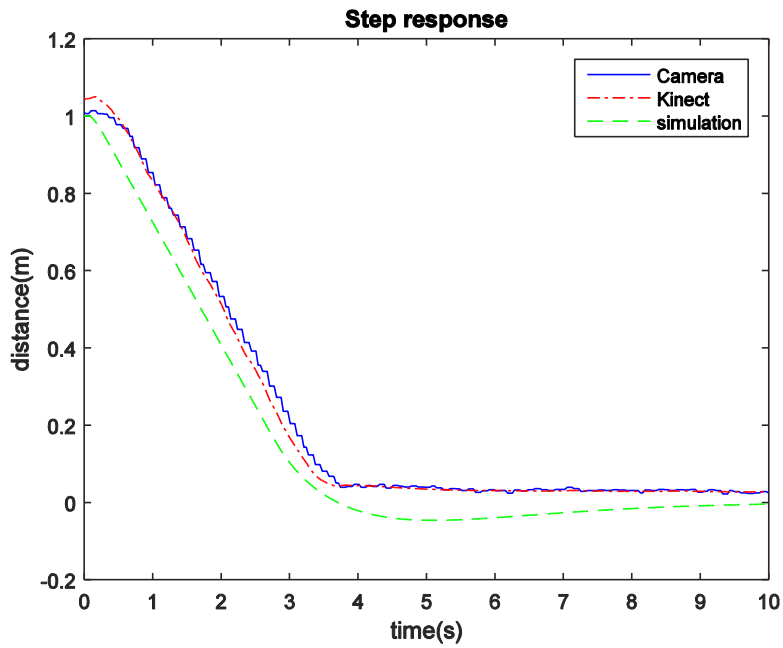


**Figure 5-10 Experimental result of the PID controller for rotation (20°)**

### 5.1.2.3 Combined experiments

In this section, experimental results with two initial angles 10° and 15° are given. For each test, a step response of distance and a step response of angle are shown. The Kinect is the only sensor included in the feedback control loop, while the camera is used only for reference. The lead-lag controller is used for linear motion control, and the PID controller is used for rotational motion control.

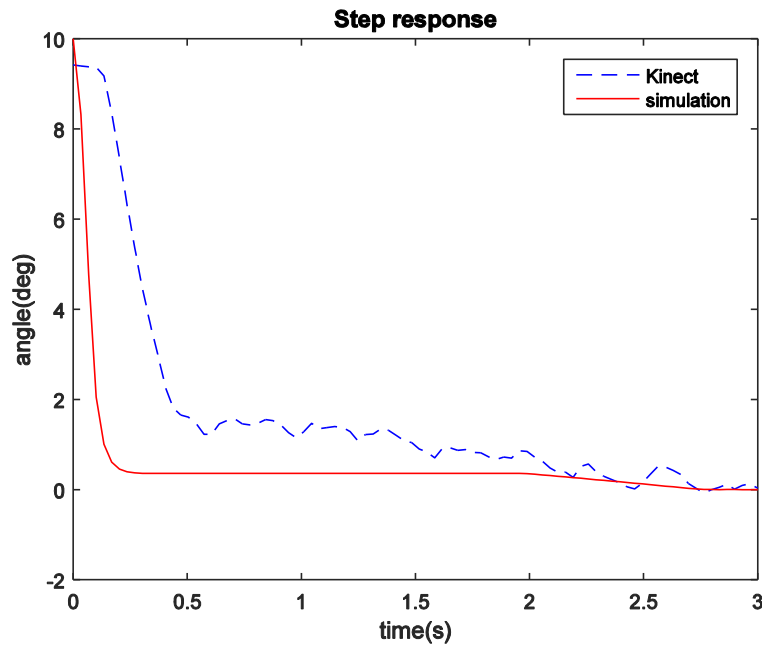
Figure 5-11 shows the distance response of the system with initial distance of 1 m and initial angle of 10°. The experimental result matches the simulation result well, with a small delay (about 0.4 s) and a small steady-state error (about 0.04 m).



**Figure 5-11 Experimental result of the combined performance with the initial distance of 1 m and initial angle of  $10^\circ$  (distance response)**

Figure 5-12 shows the angle response of the system with initial distance of 1 m and initial angle of  $10^\circ$ . The experimental result matches the simulation result well, with a small delay (about 0.4 s) and small oscillations.

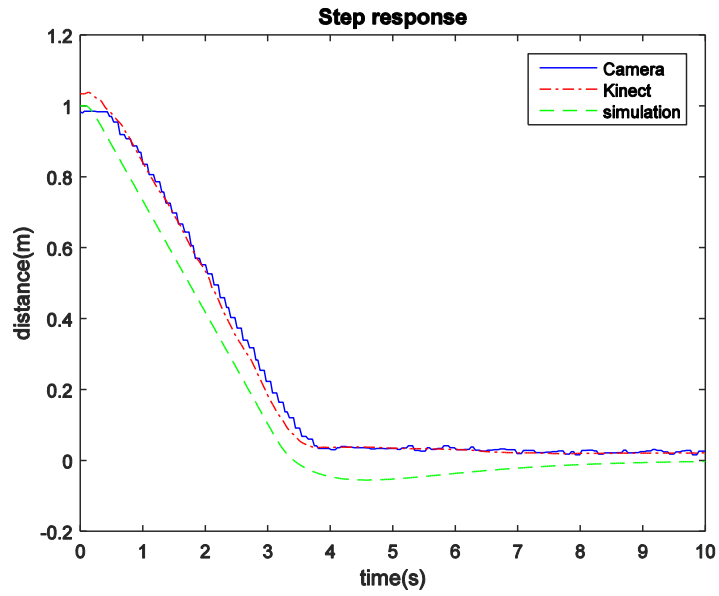
Figure 5-13 shows the distance response of the system with initial distance of 1 m and initial angle of  $15^\circ$ . The experimental result matches the simulation result well, with a small delay (about 0.4 s) and a small steady-state error (about 0.04 m).



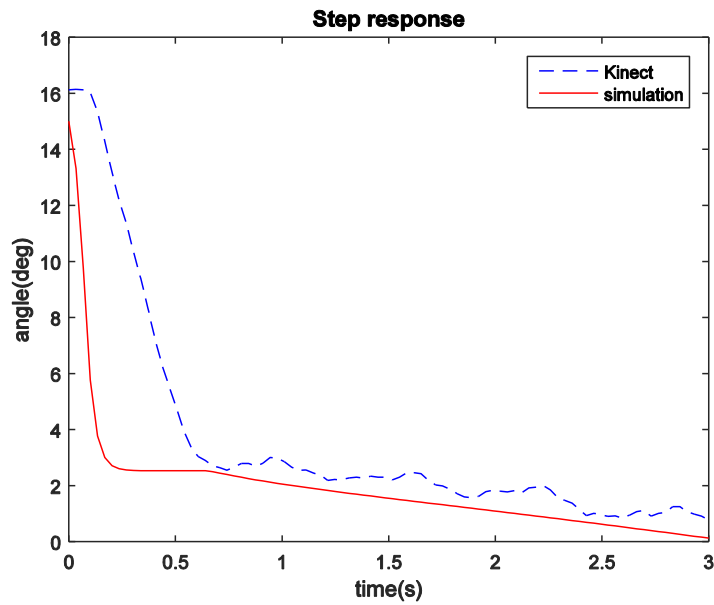
**Figure 5-12 Experimental result of the combined performance with the initial distance of 1 m and the initial angle of  $10^\circ$  (angle response)**

Figure 5-14 shows the angle response of the system with initial distance of 1 m and initial angle of  $10^\circ$ . The experimental result matches the simulation result well, with a delay (about 0.5 s at maximum) and small oscillations. Although the results in this set of experiments does not fit the simulation result perfectly, tests show that these delays and steady-state errors are acceptable.

To ensure the delays and steady-state errors occurring in tracking are acceptable, experiments to determine the range of the distance and the angle between the robot and the user were carried out. The range of the distance was about 0.8–1.8 m, and the range of the angle was  $\pm 18^\circ$ . Hence, the delays and steady-state errors are acceptable since they do not drive the robot out of the controllable range.



**Figure 5-13 Experimental result of combination performance with the initial distance of 1 m and the initial angle of 15° (distance response)**



**Figure 5-14 Experimental result of the combined performance with the initial distance of 1 m and the initial angle of 15° (angle response)**

### 5.1.2.4 2D trajectory tracking

Figure 5-15 shows the trajectories of the robot and the user captured by the camera. The positional data were processed by Matlab. There are 181 data points for each trajectory adopted for this plot. The camera captures positional data at 30 FPS. Therefore, the duration of the trajectories should be 6 s. There are markers of 0.5-s intervals on the trajectories. Recall the reference coordinates of the Kinect sensor given in Figure 4-2. The displacements in the  $z$ -axis (longitudinal direction of the robot) are clearly shown in the trajectories. In contrast, the displacements in the  $x$ -axis are not conspicuous, since the angular displacements of the robot cannot be represented in this trajectories.

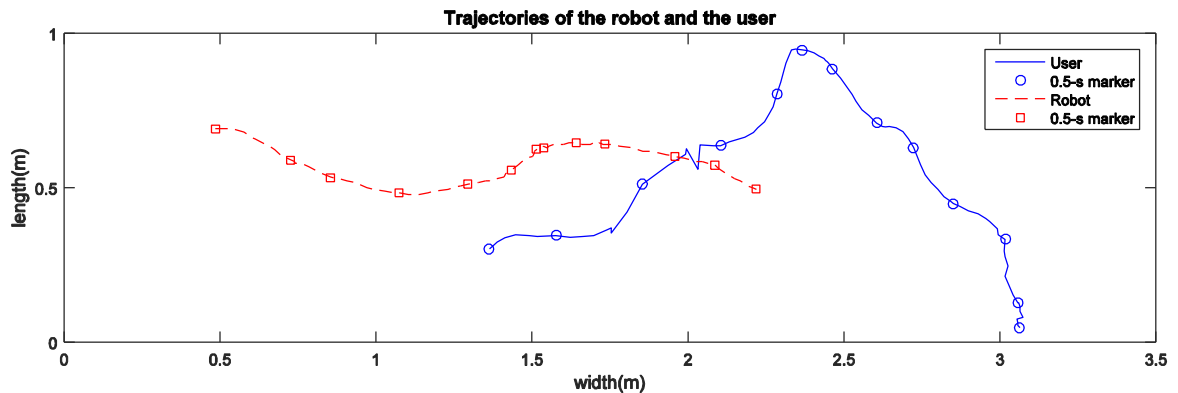


Figure 5-15 Trajectories of the robot and the user

## 5.2 Gesture recognition evaluation

This section is dedicated to the experiments executed to assess the reliability of



the gesture-recognition subsystem through the assessment of the recognition success rate with respect to the four gestures presented in Chapter IV, two mode-switch gestures, and a lamp creation gesture, lamp selection and color change gesture.

### **5.2.1 Experimental design**

For these tests, ten people, aged 26 years old on average, were asked to perform all the gestures that the robot is able to recognize. The pool of the ten people consisted of six males and four females, who had no previous experience either the Kinect or motion capture. Each experiment is articulated as follows.

- The robot is placed on the floor, and the human-tracking system is disabled.
- Subject training: first, the subjects learn the gesture vocabularies and understand how to execute each of them. Then, they perform a training run consisting of eight executions, two for each gesture;
- Evaluation run: this step consists of 12 executions, three for each gesture. The subjects are asked to perform one of the three gestures, in order for the calculation of the recognition success rate without any memory effect, which can affect the evaluation.

### **5.2.2 Results**

Table 5.1 shows the experimental results of the gesture recognition. It is the average success rates of the individual testing from 1.5 or 2 m away. Every gesture was recognized well in 0° and 10°. When the test goes to 15° all the success rates of gestures decreased in different percentages. When it went to 20°, the user was out of the Kinect's

detectable range. For the test from 2 m away, every gesture was recognized well in 0° and 10°. As the angle increased from 10° to 20°, the success rates of all the gestures decreased in different percentages. The reason that the success-rate decrease was that the Kinect sensor could not track the crucial part of the body that triggered the motion. In other words, the critical body part was out of the Kinect sensor's best detectable range. According to these data, when the robot is serving in a distance between 1.5 to 2 m, the user was not supposed to have an angle more than 20° about the robot.

**Table 5.1 Success rate of the gesture recognition**

	1.5 m				2 m			
	0°	10°	15°	20°	0°	10°	15°	20°
Mode-switch 1	100%	100%	83%	NA	100%	100%	93%	83%
Mode-switch 2	100%	100%	90%	NA	100%	100%	100%	93%
Lamp creation	100%	100%	87%	NA	100%	100%	97%	90%
Lamp selection	100%	100%	80%	NA	100%	100%	93%	83%
Color change	100%	100%	93%	NA	100%	100%	100%	93%

## CHAPTER VI

### CONCLUSIONS AND FUTURE WORK

#### 6.1 Conclusions

The challenging aim of natural human-robot interaction (NHRI) is to design desirable robotic platforms, which can be mass-consumption products. The existing device with NHRI function can be classified into two groups based on the type of users. The first group of devices was designed for the general public. Usually, these devices have very limited function and are unmovable and affordable. For example, the Kinect for the Xbox 360 console. The Kinect sensor here is just an input for the video game console. It cannot be used for other devices since it is unmovable. The other group of devices was designed for specialists and is unsuitable for inexperienced operators. These devices are usually used in special scenarios, like in an earthquake site or in a laboratory. They are high-tech, expensive, and unaffordable in general.

The affordable and reliable robotic system developed in this research achieved the goal that has the potential for wide usage and easy to interface. First, the robot showed its ability to interact with other electrical devices wirelessly. In the research, this ability was demonstrated by controlling lamps' power and their color. Besides, the robot's human-tracking ability was evaluated in Chapter V, and showed it was robust within the detectable range of the Kinect sensor. Therefore, with wireless communication module, the robot could control most of electrical devices.

Second, a natural interface means less human effort needed for the interaction, for example, minimizing the complexity of the user interfaces. To this end, in this work a new approach for a mobile social robot was proposed, which provided the user a more natural communication interface. This was achieved without any wearable or graspable input device, rather equipping a robot with a motion sensor, and a vision-based gesture-driven interaction system. In addition, the interaction was quite simple and easy. Experiments in Chapter V confirmed the achievement of a gesture-driven interaction system usable by non-expert operators, which was one aim of the work. Moreover, in the research, the robot also showed its ability to acquire geometrical data. This means it may understand what you need before you “tell” it, and do what it can do. For example, in the research the robot turned on the lamp that the user came close to, and turned off the lamp that the user went away from. Gesturing is an easy and expressive way people communicate. Hence, a gesture-driven vision-based interaction system is an optimal choice for the purpose of developing a socially interactive robot.

Third, it is a potential mass-consumption product, for its low cost. The most expensive part of the robot is the Kinect sensor, which cost 249 US dollars.

In summary, the implementation of a friendly social robot exhibits good performances with respect to the objects presented in Chapter I.

## **6.2 Future work**

Although the goals were accomplished, the approach detailed in this thesis presents some aspects that can be implemented as future work.

First, there is a motor in the Kinect sensor to control the pan-tilt. However, it was

not used in the research since the framework of the motor was not yet released for Windows operating system. The Kinect sensor can always have a best view of the user by controlling the pan-tilt. Therefore, to make gesture recognition more robust, the best solution is to enable the pan-tilt.

Second, object recognition was not included in the research. The framework used for the Kinect is OpenNI, which is not support for object recognition. In the future, other frameworks may be utilized to implement object recognition, which will facilitate the human-robot interaction.

Third, it would be interesting to integrate additional human-oriented perception systems, for example, speech recognition. In this case, one could take advantage of the hardware already installed on the robot, the array of microphones of the Kinect.

Finally, the Kinect sensor is required to connect to a computer directly with the USB cable, without any wireless solution. That is why in this research the robot ran with a wire connected to a laptop. To increase the mobility of the robot, a single-board computer can be installed on the robot, such as Raspberry Pi. The Raspberry Pi is of about the same size with an Arduino board, and has been proved to cope with Kinect Sensor.

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## APPENDIX

### Processing Code

```
import SimpleOpenNI.*;
import processing.serial.*;
import controlP5.*;
import peasy.test.*;
import peasy.org.apache.commons.math.*;
import peasy.*;
import peasy.org.apache.commons.math.geometry.*;
import processing.opengl.*;
import processing.net.*;

SimpleOpenNI context; //for SimpleOpenNI library
Serial myPort4Robot; //for Serial communication
Serial myPort4Lamp;
ControlP5 cp5; //for user interface
Chart myChart;
Slider Slider1;
File lampsFile; //for lamp control
PeasyCam cam; //for 3D present
Client c; //for socket communication

String n1; // signs and numbers to send to Arduino board
String n2;
String n3;
String n4;
String sending; // combined n1, n2, n3, n4
PrintWriter output; // will show on the screen
int v;
int vl; // velocity of the left wheel
int vr; // velocity of the right wheel
int y; // distance between a target and robot
double theta; // angle between a target and robot
int ey1 = 0; // distance error
int ey2; // new distance error
double etheta1 = 0; // angular error
double etheta2; // new angular error
int u1 = 0;
int u2 = 0;
int u3 = 0;
int Ry = 1500; //reference y
int Rtheta = 0; //reference theta
double k = 0.0285; //  $1 * g * k_t * k_i = 2 * 120 * 0.0865 * (0.35 / 255) = 0.0285$ 
double kY = 0.033;
double kPhi = 1.25;
int maxY = 255; // maximum velocity output
```

```

int maxPhi = 150; // maximum angular output
int maxV = 255;
int minRun = 10; // minimum velocity output of the robot
int dl = 1; //direction of left motor, dl=1 means go forward
int dr = 0; //direction of right motor, dr =0 means go forward
int mode = 0; // mode1 is tracking, mode2 is gesture control
ArrayList<Lamp> lamps = new ArrayList<Lamp>(); // for saving lamps
int boundSize = 2400; // for the 3D PeasyCam
String input; // for socket communication
int data[];

// for user tracking
PVector bodyCenter = new PVector();
PVector bodyDir = new PVector();
PVector com = new PVector();
PVector com2d = new PVector();
color[] userClr = new color[] { color(255,0,0),
                                color(0,255,0),
                                color(0,0,255),
                                color(255,255,0),
                                color(255,0,255),
                                color(0,255,255)
                                };

// for slider in the UI
int sliderTicks1 = 100;
PFont f; //Declare PFont variable

////////////////////////////////////
void setup(){
  size(1024,768,P3D); // size of the image
  context = new SimpleOpenNI (this);

  // check the connection to Kinect sensor
  if(context.isInit() == false){
    println("Maybe your Kinect is not connected");
    exit();
    return;
  }
  context.setMirror(false); // disable mirror
  context.enableDepth(); // enable depth sensing
  context.enableUser(); // enable skeleton tracking
  //setup PeasyCam
  cam = new PeasyCam(this, 0, 0, 0, 3500);
  stroke(255,255,255);
  smooth();

// frameRate(30); //set framerate

//Initialize Serial Communication
String port4Robot = Serial.list()[0];

```

```

String port4Lamp = Serial.list()[1];
myPort4Robot= new Serial(this, port4Robot, 9600);
myPort4Lamp = new Serial(this, port4Lamp, 9600);

//CP5
PFont pfont = createFont("Arial",10,true); // use true/false for smooth/no-smooth
ControlFont font = new ControlFont(pfont,300);

//Initialize Control Slider
cp5 = new ControlP5(this);
cp5.addFrameRate()
    .setInterval(10)
    .setPosition(0,height - 10)
    .setSize(300,300)
    .setFont(font);
Slider1 = cp5.addSlider("Desired Distance")
    .setPosition(800,150)
    .setSize(60,400)
    .setRange(800,1200)
    .setNumberOfTickMarks(9)
    ;
Slider1.captionLabel()
    .setFont(font)
    .setSize(20)
    .toUpperCase(false)
    ;
Slider1.valueLabel()
    .setFont(font)
    .setSize(20)
    .toUpperCase(false)
    ;

//Initialize Chart
myChart = cp5.addChart("Error")
    .setPosition(150, 150)
    .setSize(60, 400)
    .setRange(-80, 80)
    .setView(Chart.BAR) // use Chart.LINE, Chart.PIE, Chart.AREA, Chart.BAR_CENTERED
    .setStrokeWeight(1.5)
    .setColorCaptionLabel(color(40))
    ;
myChart.captionLabel()
    .setFont(font)
    .setSize(20)
    .toUpperCase(false)
    ;
myChart.addDataSet("distanceError");
myChart.setData("distanceError", new float[1]);
cp5.setAutoDraw(false);

```

```

f = createFont("Arial",128,true); //Initialize Text
output = createWriter("Kinect.txt"); // Create a new file to save the position of the target
c = new Client(this, "136.0.0.1", 15935); // server's IP and port
}
////////////////////////////////////
void draw(){
  context.update(); // update the cam
  background(0,0,0); // background color
  int [] userList = context.getUsers(); // detect humans using Kinect

  // tracking or gesture control?
  if (mode==0){
    if (c.available() > 0) {
      input = c.readString();
      input = input.substring(0, input.indexOf("\n")); // Only up to the newline
      data = int(split(input, ' ')); // Split values into an array
    }
    if(context.isTrackingSkeleton(1)){
      //Displaying text
      textFont(f,128);
      fill(0,255,255);
      textAlign(CENTER);
      text("You are being tracked.",width/2,height-1000);

      context.getCoM(1,com); //get the center of mass of the target
      calculation(com,data[0],data[1]); // calculate the distance and angle offset and send command to
the Arduino board
      gui(); // show the GUI
      output.println(com.x+","+com.y+","+com.z+","+data[0]+","+data[1]); // Write the coordinate to the
file
//   println("Position:"+com.x+","+com.y+","+com.z+","+data[0]+","+data[1]);
    }
  } else if (mode==1){
    modeCheck4Gesture(1); // check if it is needed to shift to tracking mode
    // Draw the stage
    pushMatrix();
    translate(0, 0, boundSize/2);
    stroke(255, 0, 255);
    //stroke(50,200);
    noFill();
    box(boundSize);
    popMatrix();

    pushMatrix();
    translate(0, boundSize/4, boundSize/2);
    rotateX(PI/2);
    stroke(255, 0, 255);
    noFill();
    rectMode(CENTER);
    rect(0,0,boundSize,boundSize);

```

```

popMatrix();
////////////////////////////////////////flip
pushMatrix();
scale(-1,1,1);
scale(0.5);
rotateZ(radians(180));
rotateY(radians(360));
//image(context.userImage(),0,0);
if (context.getNumberOfUsers() != 0) {
  context.getCoM(1, com); // Get the Center of Mass
  for (int i = 0; i < lamps.size(); i++) {
    lamps.get(i).updateUserPos(com); // Update the lamps
  }
  userControl(1); // User control behaviors
  drawSkeleton(1);
  stroke(100,255,0);
  strokeWeight(1);
  beginShape(LINES);
  vertex(com.x - 15,com.y,com.z);
  vertex(com.x + 15,com.y,com.z);

  vertex(com.x,com.y - 15,com.z);
  vertex(com.x,com.y + 15,com.z);

  vertex(com.x,com.y,com.z - 15);
  vertex(com.x,com.y,com.z + 15);
  endShape();
}
for (int i = 0; i < lamps.size(); i++) {
  lamps.get(i).draw();
}
sendSerialData(); // send command to lamps
// modeCheck(1);
// draw the kinect cam
context.drawCamFrustum(); //Draw 3D PeasyCam
popMatrix();
}
}

//distance and orientation calculation
void calculation(PVector com, int data1, int data2)
{
  point(com.x,com.y,com.z);
  if (com.z < 600)
  {
    vl = 0;
    vr = 0;
    println("Stop");
  }
  else

```

```

{
double ratio = -com.x/com.z;
double theta = Math.toDegrees(Math.atan(ratio)); //new theta
println(theta);
y = (int)(sqrt(com.z*com.z+com.x*com.x-640000)*0.1+0.9*data1); //new y, adjust the ratio to adjust
the weight of the Kinect and the camera
int ey2 = y-Ry; //error of distance
myChart.push("distanceError", (ey2)); // update chart

//Displaying error
textFont(f,256);
fill(0,255,255);
textAlign(CENTER);
float ey22 = ey2;
text("Distance Error\n"+ey22/1000+"m",65,430);

double etheta2 = Rtheta-theta; //error of theta
ut1 = 1.904*ut11-0.9052*ut111+2.44*ey3-4.713*ey2+2.275*ey1; //new model u1 Lead-lag controller,
k=1.4, 0.015
ut2 = -0.3038*ut2+0.5004*etheta2-0.1351*etheta1; //update u2 sisotool

// transfer the input from torque to velocity value
u1 = (int)(ut1*kY/k);
u2 = (int)(ut2*kPhi/k);
println("u1:"+u1);
println("u2:"+u2);

// include physical limitation (maximum speed and maximum detectable angle)
if (abs(u1) > maxY)
{
u1 = (int)(Math.signum(u1)*maxY);
}
if (abs(u2) > maxPhi)
{
u2 = (int)(Math.signum(u2)*maxPhi);
}
println("u12:"+u1);
println("u22:"+u2);

//calculate the velocity to wheels on each side
vl = u1-u2;
vr = u1+u2;

// determine the wheel's rotate direction
if (vl > 0)
{
dl = 1;
}
else
{

```

```

    dl = 0;
    vl = -vl;
}
if (vr > 0)
{
    dr = 0;
}
else
{
    dr = 1;
    vr = -vr;
}

// include physical limitation (maximum speed and maximum detectable angle)
if (vl>maxV || vr>maxV)
{
    int u11 = round(u1/(abs((float)u1)+abs((float)u2))*maxV);
    int u22 = round(u2/(abs((float)u1)+abs((float)u2))*maxV);
    if (abs(u22)>maxPhi)
    {
        u22 = (int)(Math.signum(u22)*maxPhi);
        u11 = (int)(Math.signum(u11)*(maxV-maxPhi));
        if (u11 > u1)
            u11 = u1;
    }
    else if (abs(u11)>maxY)
    {
        u11 = (int)(Math.signum(u11)*maxY);
        u22 = (int)(Math.signum(u22)*(maxV-Y));
        if (u22 > u2)
            u22 = u2;
    }
}

//calculate the velocity to wheels on each side
vl = round(u11-u22);
vr = round(u11+u22);
}
ey1 = ey2; //old ey
ey2 = ey3;
ut111 = ut11;
ut11 = ut1;
etheta1 = etheta2; //old theta
}
modeCheck4Tracking(1); // check mode shift request

// transform interger into string
n1 = Integer.toString(dl);
n2 = Integer.toString(vl);
n3 = Integer.toString(dr);
n4 = Integer.toString(vr);

```

```

// if n2 or n4 is less than 4 digits add a zero to the front of them.
while (n2.length() < 3){
  n2 = '0' + n2;
}
while (n4.length() < 3){
  n4 = '0' + n4;
}

sending = n1 + n2 + n3 + n4; //combine the four strings into one 8 digit one
myPort4Robot.write(sending); //write this to the serial port.
}

// draw the skeleton with the selected joints
void drawSkeleton(int userId)
{
  strokeWeight(5);

  // to get the 3d joint data
  drawLimb(userId, SimpleOpenNI.SKELETON_HEAD, SimpleOpenNI.SKELETON_NECK);

  drawLimb(userId, SimpleOpenNI.SKELETON_NECK, SimpleOpenNI.SKELETON_LEFT_SHOULDER);
  drawLimb(userId, SimpleOpenNI.SKELETON_LEFT_SHOULDER, SimpleOpenNI.SKELETON_LEFT_ELBOW);
  drawLimb(userId, SimpleOpenNI.SKELETON_LEFT_ELBOW, SimpleOpenNI.SKELETON_LEFT_HAND);

  drawLimb(userId, SimpleOpenNI.SKELETON_NECK, SimpleOpenNI.SKELETON_RIGHT_SHOULDER);
  drawLimb(userId, SimpleOpenNI.SKELETON_RIGHT_SHOULDER, SimpleOpenNI.SKELETON_RIGHT_ELBOW);
  drawLimb(userId, SimpleOpenNI.SKELETON_RIGHT_ELBOW, SimpleOpenNI.SKELETON_RIGHT_HAND);

  drawLimb(userId, SimpleOpenNI.SKELETON_LEFT_SHOULDER, SimpleOpenNI.SKELETON_TORSO);
  drawLimb(userId, SimpleOpenNI.SKELETON_RIGHT_SHOULDER, SimpleOpenNI.SKELETON_TORSO);

  drawLimb(userId, SimpleOpenNI.SKELETON_TORSO, SimpleOpenNI.SKELETON_LEFT_HIP);
  drawLimb(userId, SimpleOpenNI.SKELETON_LEFT_HIP, SimpleOpenNI.SKELETON_LEFT_KNEE);
  drawLimb(userId, SimpleOpenNI.SKELETON_LEFT_KNEE, SimpleOpenNI.SKELETON_LEFT_FOOT);

  drawLimb(userId, SimpleOpenNI.SKELETON_TORSO, SimpleOpenNI.SKELETON_RIGHT_HIP);
  drawLimb(userId, SimpleOpenNI.SKELETON_RIGHT_HIP, SimpleOpenNI.SKELETON_RIGHT_KNEE);
  drawLimb(userId, SimpleOpenNI.SKELETON_RIGHT_KNEE, SimpleOpenNI.SKELETON_RIGHT_FOOT);

  // draw body direction
  getBodyDirection(userId, bodyCenter, bodyDir);

  bodyDir.mult(200); // 200mm length
  bodyDir.add(bodyCenter);

  stroke(255,200,200);
  line(bodyCenter.x, bodyCenter.y, bodyCenter.z,
       bodyDir.x, bodyDir.y, bodyDir.z);
}

```



```

PVector joint_HEAD = new PVector();
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_HEAD, joint_HEAD);
strokeWeight(50);
stroke(255);
point(joint_HEAD.x, joint_HEAD.y, joint_HEAD.z);
strokeWeight(1);
}

void drawLimb(int userId,int jointType1,int jointType2)
{
PVector jointPos1 = new PVector();
PVector jointPos2 = new PVector();
float confidence;

// draw the joint position
confidence = context.getJointPositionSkeleton(userId,jointType1,jointPos1);
confidence = context.getJointPositionSkeleton(userId,jointType2,jointPos2);

stroke(0,255,255,confidence * 200 + 55);
line(jointPos1.x,jointPos1.y,jointPos1.z,
    jointPos2.x,jointPos2.y,jointPos2.z);
}

// mode shift from tracking to controlling
public void modeCheck4Tracking(int userId) {
// Hand Vectors
PVector rHand = new PVector();
PVector lHand = new PVector();

context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_RIGHT_HAND, rHand);
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_LEFT_HAND, lHand);

// if distance between both hand smaller than 0.08m then shift to controlling mode
if (lHand.dist(rHand) < 80){
    vl = 0;
    vr = 0;
    mode = 1;
}
}

// mode shift from controlling to tracking
public void modeCheck4Gesture(int userId) {
// define joints Vectors
PVector lHand = new PVector();
PVector lElbow = new PVector();
PVector rShoulder = new PVector();
PVector lShoulder = new PVector();

context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_LEFT_HAND, lHand);
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_LEFT_ELBOW, lElbow);

```

```

context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_RIGHT_SHOULDER, rShoulder);
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_LEFT_SHOULDER, lShoulder);

PVector shoulder = PVector.sub(rShoulder, lShoulder);
PVector lForearm = PVector.sub(lShoulder, lElbow);
PVector lArm = PVector.sub(lElbow, lHand);

float angleShoulderLForearm = PVector.angleBetween(shoulder, lForearm);
float angleLArmLForearm = PVector.angleBetween(lArm, lForearm);

if (angleShoulderLForearm*0.6+angleLArmLForearm*0.4 < PI/8){
  println("Shift");
  mode = 0;
}
}
// -----
// lamp events
void saveLamps() {
  String[] lines = new String[lamps.size()];
  for (int i = 0; i < lamps.size(); i++) {
    lines[i] = String.valueOf(lamps.get(i).pos.x) + " "
      + String.valueOf(lamps.get(i).pos.y) + " "
      + String.valueOf(lamps.get(i).pos.z) + " "
      + Integer.toString(lamps.get(i).getColor()[0]) + " "
      + Integer.toString(lamps.get(i).getColor()[1]) + " "
      + Integer.toString(lamps.get(i).getColor()[2]);
  }
  saveStrings(lampsFile, lines);
}

void loadLamps() {
  String lines[] = PApplet.loadStrings(lampsFile);
  for (int i = 0; i < lines.length; i++) {
    String[] coordinates = lines[i].split(" ");
    Lamp lampTemp = new Lamp(Float.valueOf(coordinates[0]),
      Float.valueOf(coordinates[1]),
      Float.valueOf(coordinates[2]));
    lampTemp.setColor(Integer.valueOf(coordinates[3]),
      Integer.valueOf(coordinates[4]),
      Integer.valueOf(coordinates[5]));
    lamps.add(lampTemp);
  }
}

// lamp creation, lamp selection and color change
private void userControl(int userId) {
  PVector head = new PVector();
  // Right Arm Vectors
  PVector rHand = new PVector();
  PVector rElbow = new PVector();

```

```

PVector rShoulder = new PVector();
// Left Arm Vectors
PVector lHand = new PVector();

// Head
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_HEAD, head);
// Right Arm
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_RIGHT_HAND, rHand);
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_RIGHT_ELBOW, rElbow);
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_RIGHT_SHOULDER, rShoulder);
// Left Arm
context.getJointPositionSkeleton(userId, SimpleOpenNI.SKEL_LEFT_HAND, lHand);

PVector rForearm = PVector.sub(rShoulder, rElbow);
PVector rArm = PVector.sub(rElbow, rHand);

// Lamp Control
if (PVector.angleBetween(rForearm, rArm) < PI / 8f) {
  for (int i = 0; i < lamps.size(); i++) {
    PVector handToLamp = PVector.sub(rHand, lamps.get(i).pos);
    if (PVector.angleBetween(rArm, handToLamp) < PI / 4) {
      PVector colors = PVector.sub(head, lHand);
      lamps.get(i).setColor((int) colors.x / 2,
        (int) colors.y / 2, (int) colors.z / 2);
      lamps.get(i).drawSelected();
    }
  }
}

// Lamp Creation
if (head.dist(rHand) < 200 && head.dist(lHand) < 200) {
  boolean tooClose = false;
  for (int i = 0; i < lamps.size(); i++) {
    if (com.dist(lamps.get(i).pos) < 200)
      tooClose = true;
  }
  if (!tooClose) {
    Lamp lampTemp = new Lamp(bodyCenter.x, bodyCenter.y,
      bodyCenter.z);
    lamps.add(lampTemp);
  }
}

// Serial Communcation for lamp
void sendSerialData() {
  for (int i = 0; i < lamps.size(); i++) {
    int ww = lamps.get(i).W;
    int rr = 255-lamps.get(i).R;
    int gg = 255-lamps.get(i).G;

```

```

    int bb = 255-lamps.get(i).B;
    myPort4Lamp.write('S');
    myPort4Lamp.write(i);
    myPort4Lamp.write(ww);
    myPort4Lamp.write(rr);
    myPort4Lamp.write(gg);
    myPort4Lamp.write(bb);
}
}

// GUI
void gui() {
    hint(DISABLE_DEPTH_TEST);
    cam.beginHUD();
    cp5.draw();
    cam.endHUD();
    hint(ENABLE_DEPTH_TEST);
}
// -----
// SimpleOpenNI user events

// if users are detected
void onNewUser(SimpleOpenNI curContext,int userId)
{
    println("onNewUser - userId: " + userId);
    println("\tstart tracking skeleton");

    context.startTrackingSkeleton(userId);
}

// if users are losted
void onLostUser(SimpleOpenNI curContext,int userId)
{
    // Displaying text
    // textFont(f,32);
    // fill(0,255,255);
    // textAlign(CENTER);
    // text("lost tracking.",width/2,200);
    println("onLostUser - userId: " + userId);
}

void getBodyDirection(int userId,PVector centerPoint,PVector dir)
{
    PVector jointL = new PVector();
    PVector jointH = new PVector();
    PVector jointR = new PVector();
    float confidence;

    // draw the joint position
    confidence = context.getJointPositionSkeleton(userId,SimpleOpenNI.SKEL_LEFT_SHOULDER,jointL);

```

```

confidence = context.getJointPositionSkeleton(userId,SimpleOpenNI.SKEL_HEAD, jointH);
confidence = context.getJointPositionSkeleton(userId,SimpleOpenNI.SKEL_RIGHT_SHOULDER, jointR);

// take the neck as the center point
confidence = context.getJointPositionSkeleton(userId,SimpleOpenNI.SKEL_NECK, centerPoint);

PVector up = PVector.sub(jointH, centerPoint);
PVector left = PVector.sub(jointR, centerPoint);

dir.set(up.cross(left));
dir.normalize();
}

```

## Matlab Code

### 1) Mathematical modeling and controller design

```

%% Parameters
Rm = 2.2; % motor resistor
Vm = 3;
Tm = 1.2;
Im = Vm/Rm;
Kt = Tm*9.81/100/Im; % Torque constant
Ki = 0.35/250; % I = duty*Ki
muf = 0.3; % friction coefficient
mur = 0.03; % rolling resistance coefficient
r = 0.028; % radius of wheel
Mv = 1.0741; % mass of the vehicle
Mk = 0.4646; % mass of the Kinect sensor
m = Mv+Mk; % mass of the robot(kg)
TS = 1/30; % 30 frames per second
alpha = 1.5; %expansion factor
Wv = 0.172; % vehicle width
Dv = 0.199; % vehicle depth
Wk = 0.254; % Kinect width
Dk = 0.064; % Kinect depth
Lk = 0.023; % center of mass of kinect to the rotate axis
I = 1/12*Mv*(Wv^2+Dv^2)+1/12*Mk*(Wk^2+Dk^2)+Mk*Lk^2; % moment inertia of vehicle
%% State space form
A = [0 1 0 0;
    0 -r*(mur+muf)*(alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2)) 0 -r*(mur+muf)*(-
alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2));
    0 0 0 1;
    0 -r*(mur+muf)*(-alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2)) 0 -
r*(mur+muf)*(alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2))];
B2 = [0 0;
    alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2) -alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2);
    0 0;
    -alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2) alpha*(Wv^2)/4/(r^2)/l+1/m/(r^2)];

```

```

C = r/alpha/Wv*[alpha*Wv/2 0 alpha*Wv/2 0;
-1 0 1 0];
D = zeros(2);
sys = ss(A,B2,C,D);
G = tf(sys)
%% Analyze the open-loop system
figure
rlocus(2*G(1,1)); % root locus (translation)
figure
rlocus(2*G(2,2)); % root locus (rotation)
figure
bode(2*G(1,1)); % bode diagram (translation)
figure
bode(2*G(2,2)); % bode diagram (rotation)
figure
step(2*G(1,1)); % step response (translation)
figure
step(2*G(2,2)); % step response (rotation)
%% Output data from Simulink
figure %distance
distance = simout(1:300);
t = linspace(0,length(distance)/30,length(distance));
plot(t,distance);
title('Step response');
xlabel('time(s)');
ylabel('distance(meter)');

figure %angle
angle = simout1(1:300)./pi.*180;
t2 = linspace(0,length(angle)/30,length(angle));
plot(t2,angle);
title('Step response');
xlabel('time(s)');
ylabel('angle(deg)');
%% controllers designed by sisotool
% sisotool(2*G(1,1)); % for linear motion
% sisotool(2*G(2,2)); % for rotation
Numssf = [0.39*0.30321 0.30321];
Denssf = [0.0033 1];
Numssr = [0.45128*0.03 0.45128];
Denssr = [0.0087 1];
Dssf = tf(Numssf,Denssf)% PD controller for linear motion
Dssr = tf(Numssr,Denssr)% PD controller for rotation
figure
step(2*G(1,1)*Dssf/(1+2*G(1,1)*Dssf))
figure
step(G(2,2)*Dssr/(1+G(2,2)*Dssr))
%% Lead compensator design
NumC1 = [1.0298 1.5]; %K=1.5, PM=80
DenC1 = [0.3911 1];

```

```

C1 = tf(NumC1,DenC1);
figure
bode(2*2*G(1,1)); % bode diagram for lead compensator(linear motion)
hold on
bode(C1*2*G(1,1),'-.');
figure
step(2*G(1,1)*C1/(1+2*G(1,1)*C1))
%% Lag compensator design
NumC2 = [50 28]; % Kl=2 , PM=100
DenC2 = [106.5 1];
C2 = tf(NumC2,DenC2)
figure
bode(2*2*G(1,1)); % bode diagram for lag compensator(translation)
hold on
bode(C2*2*G(1,1),'-.');
figure
step(2*G(1,1)*C2/(1+2*G(1,1)*C2))
%% Digitizaion
SYSDssf = c2d(Dssf,TS,'tustin') % PD controller for linear motion
SYSDssr = c2d(Dssr,TS,'tustin') % PD controller for rotation
SYSC1 = c2d(C1,TS,'tustin') % Lead controller for linear motion
SYSC2 = c2d(C2,TS,'tustin') % Lag controller for linear motion

```

## 2) Experimental data analyze

```

%import data from the txt file
Processing = 'xxx.txt'; %generated by Processing
CppUser = 'Cam_user'; % User position data generated by C++
CppRobot = 'Cam_robot'; % Robot position data generated by C++
A = importdata(Processing)
B = importdata(CppUser)
C = importdata(CppRobot)

KinectX = A(1:300,1); %user's x coordinate from Kinect
KinectY = A(1:300,3); %user's y coordinate from Kinect
CameraD = A(1:300,4); %distance measured from camera
CameraA = A(1:300,5); %angle measured from camera
CameraUserX = B(:,2); %user's x coordinate
CameraUserY = B(:,3); %user's y coordinate
CameraRobotX = C(:,2); %robot's x coordinate
CameraRobotY = C(:,3); %robot's y coordinate

%% trajectory recorded by the Kinect
a = 25;
c = linspace(1,10,length(KinectX));
figure
scatter(KinectX,KinectY,a,c,'filled')
%% trajectory recorded by the camera

```

```

figure
plot(CameraUserX, CameraUserY, 'b--+')
hold on
plot(CameraRobotX, CameraRobotY, 'r--o')

%% distance detected by the camera
figure
t = linspace(0, length(KinectY)/30, length(KinectY));
plot(t, CameraD/1000-1, 'b-');
%% distance detected by the Kinect
hold on
KinectD = sqrt(KinectX.^2+KinectY.^2-750^2);
plot(t, KinectD/1000-1, 'r-.');
%% distance simulated by simulink
hold on
distance = 1-simout(1:300);
t = linspace(0, length(distance)/30, length(distance));
plot(t, distance, 'g--');
title('Step response');
xlabel('time(s)');
ylabel('distance(meter)');
legend('Camera', 'Kinect', 'simulation');

%% angle recorded by the Kinect
figure
ratio = atan(KinectX(1:90)./KinectY(1:90));
angle = ratio*180/pi;
t2 = linspace(0, length(KinectY)/30*3/10, length(KinectY)*3/10);
plot(t2, angle, '--');
% angle simulated by simulink
hold on
angle = 10-simout1(1:90)./pi.*180;
plot(t2, angle, '-');
title('Step response');
xlabel('time(s)');
ylabel('angle(deg)');
legend('Kinect', 'simulation');

```

## C++ Code

```

#include <sstream>
#include <string>
#include <iostream>
#include <vector>
#include <stdio.h>
#include "opencv2/calib3d/calib3d.hpp"
#include <opencv2/core/core.hpp>
#include "opencv2/imgproc/imgproc.hpp"

```



```

#include <boost/asio.hpp>
#include <cmath>
#include <boost/lexical_cast.hpp>
#include "Object.h"
#include <fstream>

#define PI 3.141592653

using namespace std;

//initial min and max HSV filter values.
int hMin = 0;
int hMax = 256;
int sMin = 0;
int sMax = 256;
int vMin = 0;
int vMax = 256;

// frame width and height
const int frameWidth = 640;
const int frameHeight = 480;
//max number of objects to be tracked in the program
const int maxNumObjects=5;
//minimum and maximum size of an object
const int minObjectSize = 20*20;
//names that will appear at the top of each window
const string windowName = "Camera tracking";
const string windowName1 = "HSV Image";
const string windowName2 = "Thresholded Image";
const string trackbarWindowName = "Trackbars";

bool track = false; //disable tracking
string mystr; // data to be sent

//define coordinates for points to be track
int userPosX;
int userPosY;
int robotFPosX;
int robotFPosY;
int robotRPosX;
int robotRPosY;

//data to be sent to the Processing
string distanceS;
string angleS;

//output position data as text files
ofstream userPosition ("Cam_user.txt");
ofstream robotPosition ("Cam_robot.txt");

```

```

//settings for reading camera calibration data
class Settings
{
public:
    Settings() : cameraMatrix(), distCoeffs()
        {}
public:
    Mat cameraMatrix;
    Mat distCoeffs;

    void write(FileStorage& fs) const           //Write serialization
    {
        fs << "{" << "Camera_Matrix" << cameraMatrix
            << "Distortion_Coefficients" << distCoeffs
            << "}";
    }
    void read(const FileNode& node)           //Read serialization
    {
        node["Camera_Matrix" ] >> cameraMatrix;
        node["Distortion_Coefficients"] >> distCoeffs;
        node["square_Size" ] >> squareSize;
    }
};

//read camera calibration data
static void read(const FileNode& node, Settings& x, const Settings& default_value = Settings())
{
    if(node.empty())
        x = default_value;
    else
        x.read(node);
}

//function to convert int to string
string intToString(int number){
    std::stringstream ss;
    ss << number;
    return ss.str();
}

void createTrackbars(){
    namedWindow(trackbarWindowName,0); //create window for trackbars
    char TrackbarName[50]; //create memory to store trackbar name on window
    sprintf( TrackbarName, "hMin", hMin);
    sprintf( TrackbarName, "hMax", hMax);
    sprintf( TrackbarName, "sMin", sMin);
}

```

```

    sprintf( TrackbarName, "sMax", sMax);
    sprintf( TrackbarName, "vMin", vMin);
    sprintf( TrackbarName, "vMax", vMax);
    //create trackbars and insert them into window
    createTrackbar( "hMin", trackbarWindowName, &hMin, hMax, on_trackbar );
    createTrackbar( "hMax", trackbarWindowName, &hMax, hMax, on_trackbar );
    createTrackbar( "sMin", trackbarWindowName, &sMin, sMax, on_trackbar );
    createTrackbar( "sMax", trackbarWindowName, &sMax, sMax, on_trackbar );
    createTrackbar( "vMin", trackbarWindowName, &vMin, vMax, on_trackbar );
    createTrackbar( "vMax", trackbarWindowName, &vMax, vMax, on_trackbar );
}
void circleObject(vector<Object> theObjects,Mat &frame, Mat &imgLines){

    for(int i =0; i<theObjects.size(); i++){
    string object = theObjects.at(i).getType();
    if (object == "user"){
        userPosX = theObjects.at(i).getXPos();
        userPosY = theObjects.at(i).getYPos();
        robotFPosX = theObjects.at(i).getXPos();
        robotFPosY = theObjects.at(i).getYPos();
    }
    cv::circle(frame,cv::Point(theObjects.at(i).getXPos(),theObjects.at(i).getYPos()),10,cv::Scalar(0,0,
255));
    cv::putText(frame,intToString(theObjects.at(i).getXPos())+ " , " +
intToString(theObjects.at(i).getYPos()),cv::Point(theObjects.at(i).getXPos(),theObjects.at(i).getYPos()+20),
1,1,Scalar(0,255,0));
    cv::putText(frame,object,cv::Point(theObjects.at(i).getXPos(),theObjects.at(i).getYPos()-
30),1,2,theObjects.at(i).getColour());

    //Output data to text files
    if(track){
        userPosition << i << " , " << userPosX << " , " << userPosY <<endl;
        robotPosition << i << " , " << robotFPosX << " , " << robotFPosY <<endl;
    }
}
}
void trackFilteredObject(Mat threshold,Mat HSV, Mat &cameraFeed){

    vector <Object> users;

    Mat temp;
    threshold.copyTo(temp);
    vector< vector<Point> > contours;
    vector<Vec4i> hierarchy;
    //the function is used to find contours of filtered image
    findContours(temp,contours,hierarchy,CV_RETR_CCOMP,CV_CHAIN_APPROX_SIMPLE );
    //use moments method to find our filtered object
    double refArea = 0;
    bool objectFound = false;
    if (hierarchy.size() > 0) {

```

```

int numObjects = hierarchy.size();
//if number of objects greater than maxNumObjects we have a noisy filter
if(numObjects<maxNumObjects){
    for (int index = 0; index >= 0; index = hierarchy[index][0]) {

        Moments moment = moments((cv::Mat)contours[index]);
        double area = moment.m00;
        //if the size of the object is less than the minimum object size then it
is probably just noise

        //iteration and compare it to the area in the next iteration.
        if(area>minObjectSize){
            Object user;
            user.setXPos(moment.m10/area);
            user.setYPos(moment.m01/area);
            users.push_back(user);
            objectFound = true;
        }else objectFound = false;
    }
    if(objectFound ==true){
        //draw the object location on screen
        circleObject(users,cameraFeed,cameraFeed);}
    }else putText(cameraFeed,"TOO MUCH NOISE! PLASE ADJUST HSV
VALUES",Point(0,60),1,2,Scalar(0,0,255),2);
    }
}

void calculation()
{
    //calculate distance between user and robot in x direction
    float lx = 3.835*robotFPosX/frameWidth-1.729*userPosX/frameWidth-1.05;
    //calculate distance between user and robot in y direction
    float ly = 2.689*robotFPosY/frameHeight-1.213*userPosY/frameHeight-0.738;
    //calculate distance between user and robot
    float distance = sqrt(lx*lx+ly*ly);
    //convert distance into string
    distanceS = intToString(std::ceil(distance*1000));
    //calculate distance between user and robot rear in x direction
    float llx = 3.835*robotRPosX/frameWidth-1.729*userPosX/frameWidth-1.05;
    //calculate distance between user and robot rear in y direction
    float lly = 2.689*robotRPosY/frameHeight-1.213*userPosY/frameHeight-0.738;
    //calculate distance between user and robot rear
    float length = sqrt(llx*llx+lly*lly);
    //calculate the angle between the user and the robot orientaton
    float angle = acos((distance*distance+0.0361-length*length)/(2*distance*0.19));
    //convert the angle into string
    angleS = intToString(std::ceil(angle*1000));
}

int main(int argc, char* argv[])

```

```

{
    //if we would like to calibrate our filter values, set to true.
    bool calibrationMode = false;

    //calibration the camera
    Settings s;
    const string inputSettingsFile = argc > 1 ? argv[1] : "default.xml";
    FileStorage fs(inputSettingsFile, FileStorage::READ); // Read the settings
    if (!fs.isOpened())
    {
        cout << "Could not open the configuration file: \\" << inputSettingsFile << "\\" << endl;
        return -1;
    }
    fs["Settings"] >> s;
    fs.release(); // close Settings file

    //Matrix to store each frame of the camera feed
    Mat cameraFeed;
    Mat threshold;
    Mat HSV;

    if(calibrationMode){
        //create slider bars for HSV filtering
        createTrackbars();
    }
    //video capture object to acquire camera feed
    VideoCapture capture;
    //open capture object at location zero (default location for camera)
    capture.open(0);

    //initialize socket
    const int SERVER_PORT = 15935;
    boost::asio::io_service io_service;
    boost::asio::ip::tcp::endpoint endpoint(boost::asio::ip::tcp::v4(),SERVER_PORT);
    boost::asio::ip::tcp::acceptor acceptor(io_service, endpoint);
    boost::asio::ip::tcp::socket socket(io_service);
    std::cout << "Server ready"<< std::endl;
    acceptor.accept(socket);
    std::string message("Connected Successfully\n");
    boost::asio::write(socket, boost::asio::buffer(message));
    //start an infinite loop where camera feed is copied to cameraFeed matrix
    //all of the operations will be performed within this loop
    while(1){
        //store image to matrix
        capture.read(cameraFeed);
        Mat temp2 = cameraFeed.clone();
        undistort(temp2, cameraFeed, s.cameraMatrix, s.distCoeffs);

        //convert frame from BGR to HSV colorspace
        cvtColor(cameraFeed,HSV,COLOR_BGR2HSV);

```

```

    if(calibrationMode==true){
        //if in calibration mode, we track objects based on the HSV slider values.
        cvtColor(cameraFeed,HSV,COLOR_BGR2HSV);
        inRange(HSV,Scalar(hMin,sMin,vMin),Scalar(hMax,sMax,vMax),threshold);
        morphOps(threshold);
        imshow(windowName2,threshold);
        trackFilteredObject(threshold,HSV,cameraFeed);
    }else{
        //create some temp objects so that
        //we can use their member functions/information
        Object user("user"), robotF("robotF"), robotR("robotR");
        //first find users
        cvtColor(cameraFeed,HSV,COLOR_BGR2HSV);
        inRange(HSV,user.getHSVmin(),user.getHSVmax(),threshold);
        morphOps(threshold);
        trackFilteredObject(user,threshold,HSV,cameraFeed,imgLines);
        //then robotFs
        cvtColor(cameraFeed,HSV,COLOR_BGR2HSV);
        inRange(HSV,robotF.getHSVmin(),robotF.getHSVmax(),threshold);
        morphOps(threshold);
        trackFilteredObject(robotF,threshold,HSV,cameraFeed,imgLines);
        //then robotRs
        cvtColor(cameraFeed,HSV,COLOR_BGR2HSV);
        inRange(HSV,robotR.getHSVmin(),robotR.getHSVmax(),threshold);
        morphOps(threshold);
        trackFilteredObject(robotR,threshold,HSV,cameraFeed,imgLines);
    }
    calculation();
    while (distanceS.length() < 4){
        distanceS = "0" + distanceS;
    }
    while (angleS.length() < 4){
        angleS = "0" + angleS;
    }
    std::string message2(distanceS+" "+angleS+"\n");
    boost::asio::write(socket, boost::asio::buffer(message2));

    }
    //show frames
    imshow(windowName,cameraFeed);
    //delay 30ms so that screen can refresh.
    char key = (char)waitKey(30);
    if( key == 's'){
        track = true;
    }
}
return 0;
}

```