Pseudogap in Fe₂VGa: NMR evidence

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We report the results of a 51 V and 69 Ga nuclear magnetic resonance (NMR) study of Fe₂VGa at temperatures between 4 and 450 K. The presence of magnetic antisite defects is deduced from the NMR linewidth, which displays a Curie-law temperature dependence. The absence of associated NMR shifts indicates the material to be intrinsically nonmagnetic. At low temperatures the NMR spin-lattice relaxation rate exhibits Korringa behavior, indicating a small carrier density at the Fermi level. At elevated temperatures, the Knight shifts and NMR relaxation rates go over to a thermally activated response, a semiconductor-like behavior. These results are consistent with pseudogap features identified by recent band structure calculations. The Fermi level density of states deduced from NMR is considerably smaller than given by the specific heat coefficient, γ . The electronic properties are compared to the isostructural semimetal Fe₂VAI.

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I. INTRODUCTION

The physics of d-electron intermetallics with electronic gaps or pseudogaps near the Fermi level continues to attract attention. Such gaps, in materials containing localized magnetic orbitals, may be due to hybridization or to Kondo-type singlet formation, and there is a continuous range of behavior between these two extremes. Recently, the Heusler-type Fe₂VAl compound has been of interest due to its unusual transport and thermodynamic properties,² resembling those of the 3d Kondo insulator FeSi in many ways.³ Nuclear magnetic resonance⁴⁻⁶ (NMR) and optical conductivity⁷ for Fe₂VAl have confirmed that this material possess a pseudogap in the Fermi-level density of states (DOS). Similarly, the isostructural compound Fe₂VGa is predicted from band-structure calculations to be semimetallic, 8,9 with a small indirect band overlap at the Fermi level. Transport measurements¹⁰ indicate a possible metal-insulator transition in this material at low temperatures. However, transport measurements are subject to extrinsic effects, due mainly to incomplete ordering of the Fe and V sublattices.

NMR is a local probe which can provide intrinsic information, despite the presence of impurities and incomplete ordering. In this investigation, we thus employed NMR techniques to probe the electronic characteristics in Fe₂VGa. Measurements extending from 4.2 K to 450 K allowed us to examine the nature of the pseudogap in this material. The results support the assignment of Fe₂VGa as a band semimetal, with a finite DOS at the Fermi level within a pseudogap.

II. EXPERIMENTAL DETAILS

The sample studied here was prepared from 99.97% Fe, 99.7% V and 99.9% Ga by mixing appropriate amounts of elemental metals. They were placed in a water-cooled copper crucible and then were melted several times in an Ar arcmelting furnace. The resulting ingot was annealed in a vacuum-sealed (10^{-5} torr) quartz tube at 600 °C for two days, and then further annealed at 400 °C for more than 12 h followed by furnace cooling. The same preparation tech-

nique has been used in other studies of this material, ¹¹ which is known to form in a single-phase L2₁ (Heusler-type) structure. The sample was powdered for NMR measurements, with a grain size of $50-100~\mu m$. Wavelength dispersive spectroscopy showed these grains to be uniform in composition, with an approximate 1 at. % deficit of Ga. No signs of a second phase were seen in this analysis.

A Cu $K\alpha$ x-ray analysis on a powdered sample from the annealed ingot was consistent with the expected L2₁ structure, with four strong reflections indexed to (220), (400), (422), and (440) planes. The determined lattice parameter, a = 5.77 Å, is equal to that reported in the literature, 10,12,13 with no other phases apparent in the spectrum. X-ray powder intensities calculated by standard means were in very good agreement with the observed intensities. However, calculated intensities were also found to be relatively insensitive to ordering on the Fe and V sublattices, due to the nearness Fe and V in the Periodic Table. Thus with a single wavelength x-ray measurement the order parameter for L2₁ order is difficult to obtain; 13 a better measure is provided by the NMR results described below, which indicate the Fe concentration on V sites to be a few percent, which is also consistent with deductions based on magnetization measurements.¹⁰

NMR experiments were performed using a 9-T homebuilt pulse NMR spectrometer. ⁵¹V and ⁶⁹Ga NMR spectra were detected at approximately 101 and 91 MHz, respectively, in constant field. The powder mixed with granular quartz was placed in a plastic vial for 4 to 300 K measurements, while we put the specimen in a Teflon tube for high temperature purposes. Both sample holders showed no observable ⁵¹V and ⁶⁹Ga NMR signals.

Knight shifts were determined from the position of the maximum of each spectrum with respect to an aqueous AlCl₃ solution reference, using 11.093, 10.219, and 11.193 MHz/T as the gyromagnetic ratios ($\gamma_n/2\pi$) for ²⁷Al, ⁶⁹Ga, and ⁵¹V, respectively. The spin-lattice relaxation rates (T_1 's) were measured using the inversion recovery method. We recorded the signal strength by integrating the spin echo FFT of the ⁵¹V and ⁶⁹Ga lines. For the recovery of the -1/2 \leftrightarrow +1/2 central transition, the T_1 's were extracted by fitting to differ-

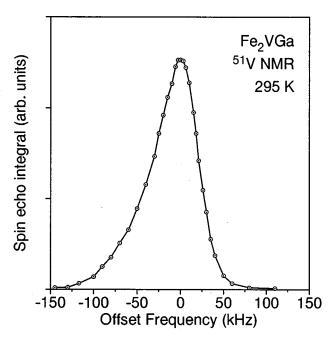


FIG. 1. Room-temperature ^{51}V NMR powder pattern of Fe₂VGa.

ent multiexponential curves, ¹⁴ as appropriate for I = 7/2 ⁵¹V and I = 3/2 ⁶⁹Ga, with T_1 as a parameter.

III. RESULTS

A 51 V room-temperature powder pattern is shown in Fig. 1, measured from spin-echo integration versus frequency. The 69 Ga lineshape exhibits similar behavior. The ordered L2₁ structure contains an equal number of V and Ga sites, both with local octahedral symmetry. For this situation, quadrupole splitting vanishes, and a single narrow line is expected for both 51 V and 69 Ga, as indeed was observed. From the pulse-length dependence of the spin echo, we find that the center of both lines responds as a $^{-1/2} \leftrightarrow ^{+1/2}$ central transition, while the shoulders have somewhat longer 90 ° pulse lengths, characteristic of satellite transitions randomly broadened by defects. 15 Thus we treated the center of the line as a central transition.

A. NMR linewidths

We have found the NMR linewidths to be temperature-dependent, with a Curie-type behavior consistent with the presence of local magnetic defects. As a measure of the NMR line shape, we obtained the full width at half maximum (FWHM) of the ⁵¹V NMR line, which is plotted against temperature in Fig. 2. The data can be fit to a temperature-independent width plus a term proportional to 1/*T*, as plotted by the dotted curve in Fig. 2. Such 1/*T* behavior can be produced by dilute paramagnetic impurities, as previously established. ^{16,17} Since the overall shift of the NMR line does not exhibit Curie-type 1/*T* behavior (as described below), dipole coupling to the paramagnetic impurities is indicated, since dipole broadening has zero spatial

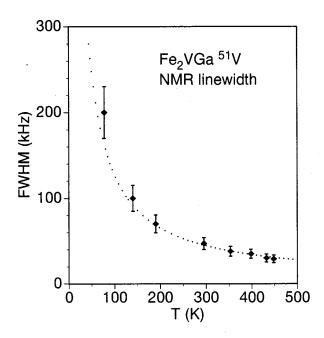


FIG. 2. ⁵¹V FWHM linewidth of Fe₂VGa vs temperature. Dotted curve: Curie-type behavior described in the text.

average, and hence gives no net shift. Dipole coupling can dominate in low-carrier-density materials, rather than the RKKY interaction which often dominates for impurities in metals.

Electronic structure calculations for Fe $_2$ VGa indicate the material to be nonmagnetic in the ordered L2 $_1$ configuration, 8,9 but with Fe atoms assuming a magnetic moment when placed on the V site. A calculated value 9 for the moment of such wrong-site Fe atoms is 3.2 μ_B . Furthermore, a field-dependent specific heat study of isostructural Fe $_2$ VAl indicated the presence of defects with a moment of 3.7 μ_B , which were associated with such antisite Fe atoms. 18 We attribute the broadening observed here to this type of defect, and have used the value 3.7 μ_B to estimate their concentration.

Broadening by random paramagnetic impurities has been treated rigorously only in the dilute limit, ¹⁷ although Monte Carlo methods have been used for higher concentrations, ¹⁹ demonstrating a change from Lorentzian to Gaussian lineshapes as one goes from dilute to more concentrated situations. We find the central portions of the Fe₂VGa lines to be close to Gaussian in shape, and therefore outside of the dilute limit, in contrast to results obtained for Fe₂VAl, which shows Lorentzian lineshapes for both ⁵¹V and ²⁷Al. ^{4,5} As an approximate measure, however, we have taken the dipole broadening function as calculated in the dilute limit by Walstedt and Walker, 17 and compared to the FWHM observed here. The result, which is the dotted curve in Fig. 2, gives an impurity concentration f = 4% per formula unit. This result can be compared to f = 0.4% found by specific heat methods in Fe₂VAl. 18 The temperature-independent portion of the linewidth obtained in this fit is 3 kHz, corresponding to a relatively small contribution due to sample inhomogeneities other than the magnetic defects.

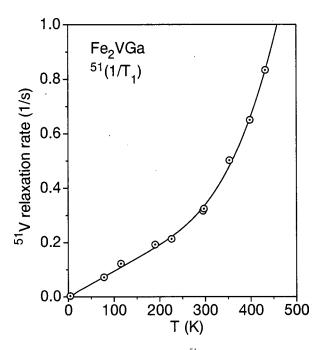


FIG. 3. Temperature-dependent ⁵¹V spin-lattice relaxation rates for Fe₂VGa. Solid curve: fit to the Korringa plus activated behavior.

Although the dilute-limit broadening function gives only an approximate value in the present case, the concentration of these defects is clearly larger in Fe₂VGa than Fe₂VAl, consistent with the deviation from Lorentzian shape observed here. Endo *et al.* ¹⁰ assumed a moment equal to 5 μ_B per antisite defect, and obtained a concentration of 2.6% per formula unit from magnetization measurements in similarly prepared Fe₂VGa, quite consistent with the present result. From magnetization and specific heat studies of these systems, we have further concluded that superparamagnetic clusters of these defects are also present, ²⁰ having considerably larger effective moments, but these are quite dilute and do not affect the NMR results described here.

B. Spin-lattice relaxation rates

Figure 3 shows the 51 V spin-lattice relaxation rates, denoted $^{51}(1/T_1)$, measured as a function of temperature. At low temperatures, $^{51}(1/T_1)$ is proportional to the temperature, a characteristic signature of the Korringa relaxation process due to metallic electrons. From a straight-line fit to the data below 250 K, we obtained $^{51}(1/T_{1K}T) = 9.4 \times 10^{-4} \text{ s}^{-1}\text{K}^{-1}$, where the subscript *K* denotes the Korringa process. Normally, the spin contribution to $1/T_{1K}T$ is proportional to the Fermi-level DOS. Comparison to the experimental value for V metal, 21 $1/T_1T = 1.27 \text{ s}^{-1}\text{K}^{-1}$, shows the Fe₂VGa value to be small, consistent with electronic structure calculations^{8,9} indicating a small band overlap at the Fermi level in this material.

 T_1 measurements for 69 Ga (not shown) produced results similar to those for 51 V: $1/T_1$ linear in T at low temperatures, and increasing much more rapidly at higher temperatures. A fit to the low-temperature data yielded $^{69}(1/T_{1K}T) = 6.5 \times 10^{-3} \text{ s}^{-1}\text{K}^{-1}$, about 7 times larger than $^{51}(1/T_{1K}T)$.

However, the hyperfine coupling for Ga-s orbitals is approximately 70 times larger than the V-d core polarization term, ²² so the corresponding Fermi-surface weight in Ga-s orbitals is considerably smaller than in V-d orbitals. This is also consistent with calculations, ^{8,9} which have indicated the carriers to be in small pockets dominated by Fe and V d orbits.

An earlier report⁶ showed a larger, non-Korringa-like $^{51}(1/T_1)$ in Fe₂VGa at low temperatures. A local moment contribution due to defects was inferred,⁶ but such a contribution to our data is apparently smaller than the Korringa term, because of sample and/or magnetic field dependence. Note that in a previous study⁴ we found the 27 Al $(1/T_1)$ in Fe₂VAl to be smaller than $^{51}(1/T_1)$, with a non-Korringa temperature dependence indicating $^{27}(1/T_1)$ to be dominated by local moments, while $^{51}(1/T_1)$ is dominated by Korringa relaxation.

Relaxation due to paramagnetic defects is caused by fluctuating moments, often producing a Debye peak in the nuclear T_1^{-1} due to the slowing down of fluctuations.²³ This explains the peak in $^{27}(1/T_1)$ for Fe₂VAl.⁴ Values of T_1 due to this mechanism will be nearly equivalent for different nuclei with similar gyromagnetic ratios.²³ By contrast, in Fe₂VGa we have different rates for ⁵¹V and ⁶⁹Ga, and both are linear in T at low temperatures, the hallmark of a Korringa process. The light nucleus ²⁷Al has a smaller hyperfine coupling to conduction electrons, allowing paramagnetic relaxation to be relatively more important. Because $1/T_1$ terms are additive, any unresolved paramagnetic contribution to $^{51}(1/T_1)$ and $^{69}(1/T_1)$ will in principle cause an overestimation of the Korringa term, and the resulting DOS. However, for the reasons described above, it is clear that the Korringa process is the most important for both ⁵¹V and ⁶⁹Ga.

Above 250 K, $^{51}(1/T_1)$ rises rapidly, with an activated temperature dependence. This is the characteristic behavior for semiconductors, 24 with the increase in relaxation rate due to an increase in the number of carriers because of thermal excitation across an energy gap. It is easy to reconcile the metallic behavior observed at low temperatures with the high-temperature semiconducting behavior by assuming a two-band model, with one band overlapping the Fermi level while the second band is separated from the Fermi level by an energy gap, $\Delta \epsilon$. In this case, the relaxation rate is given by 24

$$\frac{1}{T_1 T} = \frac{1}{T_{1K} T} + C_1 T e^{-\Delta \epsilon / k_B T},\tag{1}$$

where $1/T_{1K}T$ is the Korringa value obtained above, and the second term is due to the band edge separated from the Fermi level. This form assumes an effective-mass approximation for the band edge, with C_1 a constant depending upon the effective mass, as well as other factors. We fixed the $^{51}T_{1K}$ value obtained from the low-temperature fit, and found that Eq. (1) gives good agreement with the data, shown as the solid curve in Fig. 3. The result of the least-squares fit is $\Delta\epsilon = 0.11$ eV.

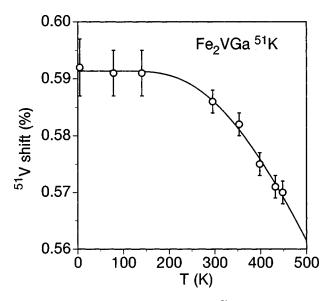


FIG. 4. Temperature dependence of ⁵¹V Knight shifts of Fe₂VGa. Solid curve: fit to Eq. (2).

C. Knight shifts

The temperature dependence of the 51 V Knight shift (denoted ^{51}K) is displayed in Fig. 4. The characteristics of this behavior are a temperature-independent shift observed at low temperatures, and a shift to lower frequencies with increasing temperature above 250 K, which can be fit to an activated curve. The 69 Ga Knight shift (^{69}K) exhibits a similar trend, not shown here.

Below 250 K, ${}^{51}K$ and ${}^{69}K$ are 0.59% and 0.07%, respectively. The temperature-independence of these shifts is characteristic of nonmagnetic materials, and indicates that despite the paramagnetic local-moment defects identified through the linewidths, the bulk of the material is nonmagnetic. Using the measured values of T_{1K} , the Korringa relation²² can be used to estimate the expected temperatureindependent metallic contributions to these shifts, 0.005% and 0.013% for ⁵¹V and ⁶⁹Ga, respectively. While electronelectron interactions can enhance such shifts, the shifts observed here can be attributed largely to an orbital mechanism. The orbital shift is a paramagnetic chemical shift due to orbitals away from the band edges, and is not associated with conducting states. For comparison, ⁶⁹Ga chemical shifts in III-V zinc-blende semiconductors range up to 0.03%, ²⁵ while a ⁵¹V orbital shift of approximately 0.63% in A15structure V₃Ga is apparent from NMR in the superconducting state, where the spin susceptibility is zero.26 Thus the large value for ${}^{51}K$ does not signify strongly metallic behavior.

Above 250 K, ^{51}K shifts to lower frequencies with increasing temperature. A negative ^{51}V shift reflects an increase in the spin susceptibility, due to the negative V-hyperfine coupling for the core-polarization mechanism. 22 Thus, the decrease in ^{51}K can be attributed to a thermally activated increase in the density of carriers, also responsible for the increase in T_1 . The Knight shift in this case can be written 24

$$K = K_o + C_2 \sqrt{T} e^{-\Delta \epsilon / k_B T}, \tag{2}$$

where K_o is a combination of orbital and temperature-independent metallic shifts, C_2 is a negative constant, and $\Delta \epsilon$ is the excitation energy as defined before. The solid curve in Fig. 4 represents a fit to Eq. (2), yielding $\Delta \epsilon = 0.095$ eV, consistent with the result obtained via spin-lattice relaxation.

IV. DISCUSSION

Magnetic properties of $Fe_{3-x}V_xGa$ and $Fe_{3-x}V_xAl$ are quite similar, except that Fe_{3-r}V_rGa maintains a larger moment in the nominally nonmagnetic composition x = 1, and a Curie temperature of 15 K was deduced from features observed in the bulk magnetization of this composition. 10 The nature of this transition is particularly interesting in light of the apparent metal-insulator transition and large giant magnetoresistance observed near T_c. ^{10,27} However, from the absence of additional shifts or splitting of the low-temperature NMR lines, ordered Fe₂VGa appears nonmagnetic. The transition must be a property of the defects, and not, for instance, a bulk transition induced by the presence of defects. A calculation for ordered Fe₂VGa indicated a residual moment of 0.03 μ_B per Fe compensated by -0.06 μ_B on V, but frozen moments of this size will broaden or shift the 51V NMR resonance by about 5.8 MHz, given the hyperfine coupling²⁸ $H_{hf}^d = -86$ kG. Such shifts are not observed here, indicating ordered Fe₂VGa to be nonmagnetic.

A further question is whether Fe₂VGa is nonmagnetic due to hybridization effects, or another mechanism such as Kondo lattice behavior. Indeed, the reported value of γ , the T-linear specific heat coefficient, is 20 mJ/mol K², corresponding to an electronic mass enhancement of order 100 over calculated values. The Korringa contribution to $^{51}(1/T_1)$ can provide a measure of $g(\epsilon_f)$, as reported previously for Fe₂VAl. For d-spin relaxation in metals, the 51 V term is 22

$$(T_{1K}T)^{-1} = 2hk_B[\gamma_n H_{hf}^d g_V(\epsilon_f)]^2 q,$$
 (3)

where $g_V(\epsilon_f)$ is the V partial d-spin contribution, q is a factor equal to the reciprocal of the degeneracy, 21 and H_{hf}^d is the core polarization hyperfine field. $H_{hf}^d = -86\,$ kG, calculated for V metal, 28 provides a good estimate for this parameter. Furthermore, band-structure calculations 8,9 indicate an e_g orbital symmetry for electron pockets which would dominate the 51 V relaxation. These pockets have degeneracy of 2, giving q=1/2. Using these parameters we obtain $g_V(\epsilon_f)=0.085\,$ states/eV atom, which can be compared to $g_V(\epsilon_f)=0.023\,$ states/eV atom measured this way in Fe₂VAl. 5 Weht and Pickett 8 calculated $g(\epsilon_f)=0.1\,$ total states/eV atom for Fe₂VAl, and have indicated that Fe₂VGa possesses a larger band overlap at ϵ_f . The measured values are thus in reasonable agreement.

While Eq. (3) assumes the electrons to be noninteracting, electron-electron interactions can lead to an enhancement of $1/T_{1K}T$. This enhancement can take a number of forms; in spin fluctuation theory²⁹ the enhancement is proportional to

the enhancement of the magnetic susceptibility or to its square root, and the enhancement of $1/T_{1K}T$ would be expected to be significant in cases where the enhancement of γ is significant. For cases in which the relaxation is dominated by local moments, the Korringa relation no longer holds. The $^{51}(1/T_{1K}T)$ observed for Fe₂VGa is in reasonable agreement with the results of band theory with no enhancement term, indicating hybridization to play a dominant role in this case.

Away from ϵ_f , a conduction-band edge having little dispersion in reciprocal space between the X and Γ points is calculated to lie approximately 0.1 eV above ϵ_f in Fe₂VGa (measured from Fig. 11 in Ref. 9). The separation of this band edge from ϵ_f is in very satisfactory agreement with the values, $\Delta \epsilon = 0.11$ eV and 0.095 eV, obtained from the activated behavior of T_1 and the Knight shift, respectively. Therefore, thermal excitation of carriers to this band at high temperatures provides a good explanation for the behavior of both T_1 and the Knight shift.

The measured values for $\Delta \epsilon$ are not equal, with the activation energy obtained from T_1 slightly exceeding the value obtained from the Knight shift. A larger difference appears in one-dimensional spin-gap systems, where the T_1 activation energy exceeds the gap obtained from Knight shifts by a factor of approximately 1.5, compared to a ratio very close to 1 for most materials.³⁰ This may result from the separation of singlet and triplet excitations in these materials, among other possibilities.³¹ An explanation for the ratio observed here, 1.15, would be a tendency towards similar spin excitations in Fe₂VGa, and hence the possible influence of Kondo-type interactions. (In Fe₂VAl the ratio is 1.3, measured independently both by ⁵¹V and ²⁷Al NMR.⁴) Another possible explanation is nonparabolicity of the band edge, modifying the energy dependence of the DOS, giving correction terms in Eqs. (1) and (2).²⁴ Further experiments to address this issue would be most interesting. In either case, the measurements do not depart significantly from expectations based on band theory, again indicating hybridization to be the dominant interaction. Thus we characterize Fe₂VGa as a hybridization-gap semimetal.

There remains an inconsistency between the small $g(\epsilon_f)$ deduced from NMR and the large observed γ . The reported value, 20 mJ/mol K^2 corresponds to an electronic mass enhancement of order $100,^{27}$ compared to the value from NMR relaxation rates. However, it is likely that a considerable portion of the observed γ results from extrinsic effects, leading to a Schottky-type enhancement, and *false heavy Fermion* behavior, as found in Fe₂VAl. ¹⁸ To provide further information, a magnetic study focusing on magnetic defects and clusters is underway.

V. CONCLUSIONS

NMR measurements have provided a local picture of the electronic properties of Fe₂VGa, indicating that despite the presence of magnetic antisite defects, Fe₂VGa is essentially nonmagnetic, with properties quite similar to those calculated via band-structure methods. Both the Knight shifts and spin lattice relaxation rates are understood in terms of semimetallic characteristics, with a small band overlap at ϵ_f falling within a pseudogap formed by nearby bands. No large enhancement of the Korringa relaxation process was found, indicating the pseudogap to be due to hybridization, rather than Kondo, effects.

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