# GAS VISCOSITY AT HIGH PRESSURE AND HIGH TEMPERATURE

A Dissertation

by

**KEGANG LING** 

Submitted to the Office of Graduate Studies of Texas A&M University in partial fulfillment of the requirements for the degree of

DOCTOR OF PHILOSOPHY

December 2010

Major Subject: Petroleum Engineering

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Major Subject: Petroleum Engineering

### **ABSTRACT**

Gas Viscosity at High Pressure and High Temperature. (December 2010)

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Chair of Advisory Committee: Dr. Gioia Falcone

Gas viscosity is one of the gas properties that is vital to petroleum engineering. Its role in the oil and gas production and transportation is indicated by its contribution in the resistance to the flow of a fluid both in porous media and pipes. Although viscosity of some pure components such as methane, ethane, propane, butane, nitrogen, carbon dioxide and binary mixtures of these components at low-intermediate pressure and temperature had been studied intensively and been understood thoroughly, very few investigations were performed on viscosity of naturally occurring gases, especially gas condensates at low-intermediate pressure and temperature, even fewer lab data were published. No gas viscosity data at high pressures and high temperatures (HPHT) is available. Therefore this gap in the oil industry still needs to be filled.

Gas viscosity at HPHT becomes crucial to modern oil industry as exploration and production move to deep formation or deep water where HPHT is not uncommon. Therefore, any hydrocarbon encountered there is more gas than oil due to the chemical reaction causing oil to transfer to gas as temperature increases. We need gas viscosity to optimize production rate for production system, estimate reserves, model gas injection, design drilling fluid, and monitor gas movement in well control. Current gas viscosity correlations are derived using measured data at low-moderate pressures and temperatures, and then extrapolated to HPHT. No measured gas viscosities at HPHT are

available so far. The validities of these correlations for gas viscosity at HPHT are doubted due to lack of experimental data.

In this study, four types of viscometers are evaluated and their advantages and disadvantages are listed. The falling body viscometer is used to measure gas viscosity at a pressure range of 3000 to 25000 psi and a temperature range of 100 to 415 °F. Nitrogen viscosity is measured to take into account of the fact that the concentration of nonhydrocarbons increase drastically in HPHT reservoir. More nitrogen is found as we move to HPHT reservoirs. High concentration nitrogen in natural gas affects not only the heat value of natural gas, but also gas viscosity which is critical to petroleum engineering. Nitrogen is also one of common inject gases in gas injection projects, thus an accurate estimation of its viscosity is vital to analyze reservoir performance. Then methane viscosity is measured to honor that hydrocarbon in HPHT which is almost pure methane. From our experiments, we found that while the Lee-Gonzalez-Eakin correlation estimates gas viscosity at a low-moderate pressure and temperature accurately, it cannot give good match of gas viscosity at HPHT. Apparently, current correlations need to be modified to predict gas viscosity at HPHT. New correlations constructed for HPHT conditions based on our experiment data give more confidence on gas viscosity.

# **DEDICATION**

To my family for their love and support

### **ACKNOWLEDGMENTS**

During these four years at Texas A&M University I have tried my best to adhere to the requirements of being a qualified graduate student. I got tons of help in the process of pursuing my Ph.D. degree. I want to acknowledge these people for their generosity and kindness.

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# **CHAPTER I**

### INTRODUCTION

### 1.1 Viscosity

Viscosity is a fundamental characteristic property of fluids. Viscosity, which is also called a viscosity coefficient, is a measure of the resistance of a fluid to deform under shear stress resulting from the flow of fluid. It is commonly perceived as "thickness", or resistance to flow. Viscosity describes a fluid's internal resistance to flow and may be thought of as a measure of fluid friction, or sometime can also be termed as a drag force.

In general, in any flow, layers move at different velocities and the fluid's viscosity arises from the shear stress between the layers that ultimately oppose any applied force. To understand the definition of viscosity, we consider two plates closely spaced apart at a distance *y*, and separated by a homogeneous substance as illustrated in Figure 1-1.

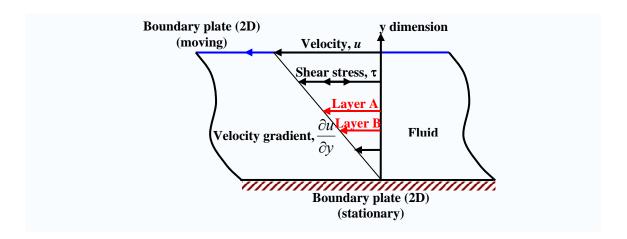


Figure 1-1. Laminar shear in fluids, after Wikipedia viscosity (2010)

Figure 1-2 is an amplification of the flow between layers A and B in Figure 1-1.

This dissertation follows the style and format of the SPE Journal.

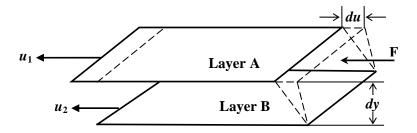


Figure 1-2. Laminar shear of a fluid film

Assuming that the plates are very large, with a large area A, such that edge effects may be ignored, and that the lower plate is fixed, let a force F be applied to the upper plate. Then dynamic viscosity is the tangential force per unit area required to slide one layer, A, against another layer, B, as shown in Figure 1-2. Employing Newton's law, if this force causes the substance between the plates to undergo shear flow, the applied force is proportional to the area and velocity of the plate and inversely proportional to the distance between plates. Combining three relations the results the equation,  $F/A = \mu(\partial u/\partial y)$ , where  $\mu$  is the proportionality factor called the absolute viscosity. The reciprocal of viscosity is the fluidity that is denoted as  $\varphi=1/\mu$ .

The absolute viscosity is also known as the dynamic viscosity, and is often shortened to simply viscosity. The equation can be expressed in terms of shear stress,  $\tau = F / A = \mu (\partial u / \partial y)$ . The rate of shear deformation is  $\partial u / \partial y$  and can be also written as a shear velocity or shear rate,  $\gamma$ . Hence, through this method, the relation between the shear stress and shear rate can be obtained, and viscosity,  $\mu$ , is defined as the ratio of shear stress to shear rate and is expressed mathematically as follows:

$$\mu = \frac{\tau}{\gamma} = \frac{\tau}{\frac{\partial u}{\partial y}} \tag{1.1}$$

where

 $\tau$  = Shear stress

 $\gamma$  = Shear rate

 $\mu$  = Viscosity

Common units for viscosity are Poise (named after French physician, Jean Louis Poiseuille (1799 - 1869)), equivalent to dyne-sec/cm<sup>2</sup>, and Stokes, Saybolt Universal. In case of Poise, shear stress is in dyne/cm<sup>2</sup> and shear rate in sec<sup>-1</sup>. Because one poise represents a high viscosity, 1/100 poise, or one centipoise (cp), is common used in petroleum engineering.

In the SI System, the dynamic viscosity units are N-s/m<sup>2</sup>, Pa-s or kg/m-s where N is Newton and Pa is Pascal, and, 1 Pa-s = 1 N-s/m<sup>2</sup> = 1 kg/m-s. In the metric system, the dynamic viscosity is often expressed as g/cm-s, dyne-s/cm<sup>2</sup> or poise (P) where, 1 poise = dyne-s/cm<sup>2</sup> = g/cm-s = 1/10 Pa-s.

In petroleum engineering, we are also concerned with the ratio of the viscous force to the inertial force, the latter characterized by the fluid density  $\rho$ . This ratio is characterized by the kinematic viscosity, defined as follows:

$$\upsilon = \frac{\mu}{\rho} \tag{1.2}$$

In the SI system, kinematic viscosity uses Stokes or Saybolt Second Universal units. The kinematic viscosity is expressed as m<sup>2</sup>/s or Stokes, where 1 Stoke= 10<sup>-4</sup> m<sup>2</sup>/s. Similar to Poise, stokes is a large unit, and it is usually divided by 100 to give the unit called Centistokes.

1 Stoke = 100 Centistokes.

1 Centistokes =  $10^{-6}$  m<sup>2</sup>/s

Fluids are divided into two categories according to their flow characteristics: 1) if the viscosity of a liquid remains constant and is independent of the applied shear stress and

time, such a liquid is termed a Newtonian liquid. 2) Otherwise, it belongs to Non-Newtonian fluids. Water and most gases satisfy Newton's criterion and are known as Newtonian fluids. Non-Newtonian fluids exhibit a more complicated relationship between shear stress and velocity gradient than simple linearity (Figure 1-3).

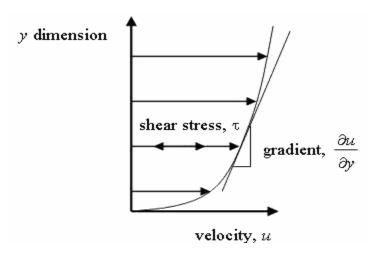


Figure 1-3. Laminar shear of for non-Newtonian fluids flow, after Wikipedia viscosity (2010)

#### 1.2 Role of Gas Viscosity in Petroleum Engineering

The importance of gas viscosity in the oil and gas production and transportation is indicated by its contribution in the resistance to the flow of a fluid both in porous media and pipes. One of the most important things in petroleum engineer routine work is to calculate the pressure at any node in a production and/or transportation system. Since gas viscosity dictates the fluid flow from reservoir into the wellbore according to Darcy's law, and affects the friction pressure drop for fluid flow from bottomhole to the wellhead and in pipeline, we need gas viscosity to optimize the production rate for production system. Gas viscosity is also a key element that controls recovery of hydrocarbon in place or flooding sweep efficiency in gas injection. In drilling fluid design and well control gas viscosity must be known to understand the upward velocity

of gas kick. Gas viscosity is a vital factor for heat transfer in fluid. Right now as most of shallow reservoirs had been produced, increasing demand on oil and gas requires that more deep wells need to be drilled to recover tremendous reserves from deep reservoirs. As we drilled deeper and deeper we meet more high pressure and high temperature (HPHT) reservoirs. Although the hurdle pressure and temperature for HPHT always changes as petroleum exploration and production moves on, at this stage the Society of Petroleum Engineers defines high pressure as a well requiring pressure control equipment with a rated working pressure in excess of 10000 psia or where the maximum anticipated formation pore pressure gradient exceeds 0.8 psi/ft and high temperature as temperature of 150 °C (or 302 °F) and up. Most of HPHT reservoirs are lean gas reservoirs containing high methane concentration, some, for instance Puguang gas field in Sichuan, China, with trace to high nonhydrocarbon (Zhang et al., 2010) such as nitrogen, carbon dioxide, and hydrogen sulfide resulting from high temperature. Examples of HPHT reservoirs can be shown by Marsh et al. (2010), which is as follow.

Field Sector Operator Pressure Temperature o<sub>F</sub> psia 374 Elgin/Franklin North Sea (UK) **TOTAL** 15954.4 Shearwater North Sea (UK) SHELL 13053.6 356 10080.28North Sea (UK) 305.6 Devenick BP Erskine North Sea (UK) TEXACO 13996.36 347 Rhum North Sea (UK) BP 12400.92 302 Victoria North Sea (Norway) TOTAL 11603.2 392

Table 1-1. Examples of HPHT fields

#### 1.3 Methods to Get Gas Viscosity

In our research, we are interesting in gas viscosity. The mechanisms and molecular theory of gas viscosity have been reasonably well clarified by nonequlibrium statistical mechanics and the kinetic theory of gases. There are two approaches to get gas viscosity. One is direct measurement using gas samples, another is gas viscosity correlations.

Advantage of direct measurement is it gives reliable result so we can use it confidently. But it has the disadvantage of time consuming and cost expensive, and sometimes availability of measuring instrument. Gas viscosity correlations provide a simple and low cost method to predict gas viscosity if correlations are based on accurate lab data. Every precaution should be taken to obtain consistent and accurate data. Data from literatures should be verified before being employed. Inaccuracy and uncertainty in database will jeopardize the reliability of correlation.

### **CHAPTER II**

### LITERATURE REVIEW

### 2.1 Gas Viscosity Measuring Instrument

Instruments used to measure the viscosity of gases can be broadly classified into three categories:

- 1) Capillary viscometers
- 2) Falling (or rolling) ball viscometers
- 3) Vibrating viscometers

Other viscometers might combine features of two or three types of viscometers noted above, In general, during the measurement either the fluid remains stationary and an object moves through it, or the object is stationary and the fluid moves past it. The drag caused by relative motion of the fluid and a surface is a measure of the viscosity. The flow conditions must have a sufficiently small value of Reynolds number for there to be laminar flow.

Before the introduction to the three types of viscometer, knowledge in the derivation of gas viscosity equation (Poiseville's equation) will benefit our understanding of the principle of measurement. We can derive Poiseville's equation starting from the concept of viscosity. The situation we deal with is an incompressible fluid flows through a circular pipe with radius R and length L at a velocity of u(r). It is noted that the velocity is not uniform but varies with the radius, r. Figure 2-1 shows the schematic of fluid flow in a pipe.

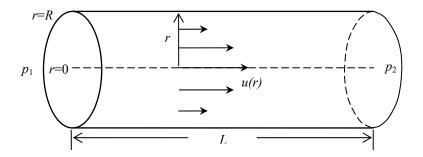


Figure 2-1. Schematic of fluid flow through a pipe

The Poiseville's equation will be valid only if the following assumptions hold:

- 1) Single phase incompressible fluid flows in the pipe.
- 2) Laminar flow is the only flow regime inside the pipe.
- 3) The fluid at the walls of the tube is assumed to be stationary, and the flow rate increases to a maximum at the center of the tube. No slippage happens during the flow (Figure 2-2).
- 4) The fluid is homogeneous.
- 5) Pipe is in horizontal position so that the effect of gravitational force on flow can be neglected.
- 6) Flow is steady-state.
- 7) Temperature is constant throughout the pipe.
- 8) Pipe is circular with constant radius, R.

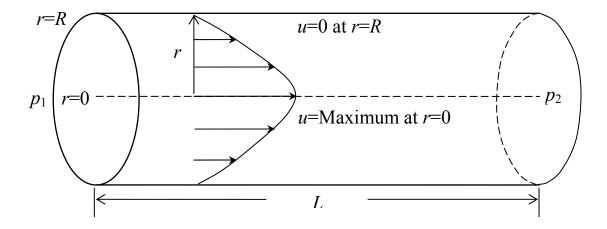


Figure 2-2. Fluid flow profile in a circular pipe

According to the definition of viscosity,  $\tau = F / A = \mu (\partial u / \partial y)$ , the drag forces (friction force) acting on a fluid layer at radius r as it moves ahead at a velocity of u(r). The drag force  $F_d$  acting on a cylinder of fluid at radius r and length L is

$$\frac{F_d}{A} = \mu \frac{du(r)}{dr}$$

where

 $F_d$  = The drag force on the surface of layer

r = Radius of the layer, measured from center of pipe

u(r) = Fluid velocity at radius of r

A =Surface area of the layer of fluid, which is equal to  $2\pi rL$ ,

L =Length of the pipe

 $\mu$  = Fluid viscosity

Substituting surface area into the definition of viscosity we have drag force

$$F_d = \mu 2\pi r L \frac{du(r)}{dr} \tag{2.1}$$

Basing on force balance, forces in the horizontal direction should be summed up to zero for steady-state flow, which can be expressed as

(Force resulting from  $p_1$ )=  $F_d$  + (Force resulting from  $p_2$ )

Expressing in pressure gives

$$p_1 \pi r^2 = F_d + p_2 \pi r^2$$

or

$$F_d = (p_1 - p_2)\pi r^2 (2.2)$$

where

 $p_1$  = Inlet pressure,

 $p_2$  = Outlet pressure,

 $\pi r^2$  = Cross-section area of the pipe.

Substituting Equation 2.1 into Equation 2.2 yields

$$\mu 2\pi r L \frac{du(r)}{dr} = (p_1 - p_2)\pi r^2$$
 (2.3)

Separating variables gives

$$du = -\frac{(p_1 - p_2)\pi r^2}{\mu 2\pi r L} dr = -\frac{(p_1 - p_2)r}{2\mu L} dr$$
 (2.4)

Integrating from the pipe wall to the center and applying boundary conditions

$$u(\mathbf{r}) = u$$

and

$$u(r=R)=0$$

we obtain

$$\int_{0}^{u} du = -\frac{(p_{1} - p_{2})}{2\mu L} \int_{R}^{r} r dr = -\frac{(p_{1} - p_{2})}{2\mu L} \left(\frac{r^{2}}{2} - \frac{R^{2}}{2}\right)$$
(2.5)

Therefore the velocity of the fluid can be expressed as a function of radius, r.

$$u = \frac{(p_1 - p_2)}{4\mu L} (R^2 - r^2)$$
 (2.6)

Using control element concept we can calculate the volumetric flow rate through the pipe q. Integrating the fluid velocity u over each element of cross-sectional area  $2\pi r dr$  (Figure 2-3).

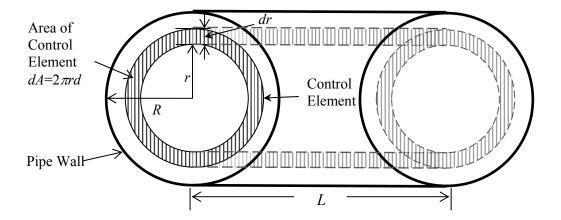


Figure 2-3. Cross section view of a circular pipe

Thus we come up with

$$q = \int_0^R \frac{(p_1 - p_2)}{4\mu L} (R^2 - r^2) 2\pi r dr = \frac{\pi (p_1 - p_2) R^4}{8\mu L}$$
 (2.7)

where

q = Volumetric flow rate,

Equation 2.7 is the famous Poiseville's equation. It should be kept in mind that Poiseville's equation is applies to incompressible fluids only. For gas, due to its high compressibility the Poiseville's equation cannot be employed directly. To derive similar equation for gas flow in the pipe we will combine real gas law and mass conservation. Now if we know the inlet pressure  $p_1$  and average velocity  $\overline{u}_1$ , the pressure p and velocity  $\overline{u}$  of any point at downstream can be calculated. Mass conservation indicates that mass flow rate is the same for every horizontal location in the pipe

$$\frac{dm_1}{dt} = \frac{dm}{dt} \tag{2.8}$$

where

m = Mass at downstream,

 $m_1$  = Mass at inlet,

t = Time,

Expressing in volume and density gives

$$\frac{d(V_1 \rho_1)}{dt} = \frac{d(V\rho)}{dt} \tag{2.9}$$

where

V = Volume at downstream,

 $V_1$  = Volume at inlet,

 $\rho$  = Density at downstream,

 $\rho_l$  = Density at inlet,

If we use the average velocity and cross section area to represent the volumetric flow rate, we have

$$\overline{u}_1 A \rho_1 = \overline{u} A \rho \tag{2.10}$$

where

 $\overline{u}$  = Average velocity at downstream,

 $\overline{u}_1$  = Average velocity at inlet,

A =Cross section area of pipe,

Cancelling out the cross section area yields

$$\overline{u}_1 \rho_1 = \overline{u} \rho \tag{2.11}$$

Real gas law gives

$$p_1 V_1 = z_1 n R_{oas} T_1 (2.12)$$

and

$$pV = znRT (2.13)$$

where

T = Temperature at downstream,

 $T_1$  = Temperature at inlet,

z = Compressibility at downstream,

 $z_1$  = Compressibility at inlet,

n = Mole of gas,

 $R_{gas}$  = Gas constant,

for inlet and downstream, respectively.

Multiplying molecular weight to both sides we have

$$p_1 V_1 M w = z_1 n R_{gas} T_1 M w (2.14)$$

and

$$pVMw = znR_{ogs}TMw (2.15)$$

where

Mw = Molecular weight,

Rearrangement gives

$$p_1 M w = \frac{z_1 R_{gas} T_1 n M w}{V_1} = z_1 R_{gas} T_1 \rho_1$$
 (2.16)

and

$$pMw = \frac{zR_{gas}TnMw}{V} = zR_{gas}T\rho \tag{2.17}$$

Substituting Equations 2.16 and 2.17 into Equation 2.11 we obtain

$$\overline{u}_1 \frac{p_1 M w}{z_1 R_{eas} T_1} = \overline{u} \frac{p M w}{z R_{eas} T}$$
(2.18)

Since temperature is constant,  $T_1 = T$ , cancelling out Mw,  $R_{gas}$ , and temperatures yields

$$\overline{u}_1 \frac{p_1}{z_1} = \overline{u} \frac{p}{z} \tag{2.19}$$

If the pressure drop in the pipe is small comparing with measuring pressure and pressure drop due to kinetic energy change is negligible, which is the case in this study, Equation 2.7 can be expressed in average velocity

$$q = \overline{u}A = \overline{u}\pi R^2 = \frac{\pi(p_1 - p_2)R^4}{8\mu L}$$

or

$$\overline{u} = \frac{(p_1 - p_2)R^2}{8uL} \tag{2.20}$$

Expressing in derivative is

$$\overline{u} = -\frac{dp}{dl} \frac{R^2}{8\mu} \tag{2.21}$$

Equation 2.19 can be cast to

$$\overline{u} = \overline{u}_1 \frac{zp_1}{z_1 p} \tag{2.22}$$

Substituting Equation 2.22 into Equation 2.21 we have

$$\overline{u}_{1} \frac{zp_{1}}{z_{1}p} = -\frac{dp}{dl} \frac{R^{2}}{8\mu}$$
 (2.23)

Separating variables yields

$$-\frac{z_1 p}{z p_1} dp = \frac{8\overline{u}_1 \mu}{R^2} dl \tag{2.24}$$

Integrating from inlet to outlet we have

$$\int_{p_1}^{p_2} -\frac{z_1 p}{z p_1} dp = \int_{0}^{L} \frac{8 \overline{u}_1 \mu}{R^2} dl$$
 (2.25)

Considering the facts that compressibility factor z and viscosity  $\mu$  are strong functions of pressure and the lack of rigorous expressions for these functions, there is no closed-form expression for integral in Equation 2.25. In case of very low pressure gradient, we employed  $z_{av}$  and  $\mu_{av}$  to denote the average compressibility and viscosity of gas in the pipe. In this study the pressure difference between inlet and outlet is 0-10 psi, which is very small comparing with 3000-25000 psig measuring pressure, thus the variation of viscosity and compressibility with pressure can be neglected. Equation 2.25 is replaced with

$$\int_{p_1}^{p_2} -\frac{z_1 p}{z_{av} p_1} dp = \int_{0}^{L} \frac{8 \overline{u}_1 \mu_{av}}{R^2} dl$$
 (2.26)

or

$$\frac{z_1}{2z_{av}p_1} \left( p_1^2 - p_2^2 \right) = \frac{8\overline{u}_1 \mu_{av} L}{R^2}$$
 (2.27)

Recasting Equation 2.27 gives

$$\frac{z_1}{2z_{ov}p_1} (p_1 - p_2)(p_1 + p_2) = \frac{8\overline{u}_1 \mu_{av} L}{R^2}$$
 (2.28)

or

$$\overline{u}_{1} = \frac{(p_{1} - p_{2})R^{2}}{8\mu_{av}L} \frac{z_{1}(p_{1} + p_{2})}{2z_{av}p_{1}}$$
(2.29)

Multiplying by cross section area,  $A = \pi R^2$  we have

$$\overline{u}_1 \pi R^2 = \frac{\pi (p_1 - p_2) R^4}{8 \mu_{\text{m}} L} \frac{z_1 (p_1 + p_2)}{2 z_{\text{m}} p_1}$$
(2.30)

Expressing in volumetric flow rate gives

$$q = \frac{\pi(p_1 - p_2)R^4}{8\mu_{av}L} \frac{z_1(p_1 + p_2)}{2z_{av}p_1}$$
 (2.31)

which has an addition term,  $\frac{z_1(p_1 + p_2)}{2z_{av}p_1}$ , accounting for compressible fluid flow.

Equation 2.31 is similar to Poiseville's equation. In case of incompressible fluids,  $\frac{z_1(p_1+p_2)}{2z_{av}p_1}$  will collapse to 1, and then Equation 2.31 will end up with Poiseville's equation.

### 2.1.1 Capillary Viscometers

Transpiration method is the base for capillary viscometer. Capillary viscometer is named after its key part, a cylindrical capillary tube. It also has another often used name, Rankine viscometer. In a capillary viscometer, fluid flows through a cylindrical capillary tube. Figure 2-4 shows a typical capillary viscometer in two positions: (a) is in horizontal position, and (b) is in vertical position. The measurement principle is the combination of Poiseville equation and real gas law. Viscosity is determined by measuring the flow rate of the fluid flowing through the capillary tube and the pressure differential between both ends of the capillary tube. This measurement method is based on the laws of physics; therefore, this is called the absolute measurement of viscosity.

The principle and structure of the capillary viscometer is simple, but accurate measurement is the key for success. The inside of the capillary viscometer must be kept very clean. Also, a thorough drying of the capillary tube is required before each measurement. Temperature control is essential because the capillary tube is susceptible to thermal expansion or contraction under the influence of temperature, especially in lower viscosity ranges. These thermal impacts might introduce errors to the measurement. In addition, capillary tube is hard to withstand high pressure. A constant tube diameter and regular geometric shape at HPHT are necessary to obtain good result. As a result, capillary viscometer is suitable for measurement at low-moderate pressure and temperature.

The measurement of gas viscosity using capillary viscometer is delineated as follow. 1) A drop of clean mercury is introduced into a sufficiently narrow cylindrical glass tube filled with gas, completely fills the cross-section of the tube and forms a practically perfect internal seal as between the spaces on either side of it; 2) changing the viscometer from horizontal to any inclination will cause the mercury pellet start to flow due to the gravity force or the density difference between mercury and gas; 3) mercury pellet quickly come into equilibrium with the proper difference of gas pressure established above and below; 4) actually the descending mercury pellet acts as a piston, forcing the gas through the capillary tube. Any alteration of inclination angle of the viscometer will change the descending velocity of the mercury pellet.

A typical capillary viscometer is a closed glass vessel consisting of two connected tubes as shown in Figure 2-5, one is a fine capillary tube and the other is tube with much larger inner-diameter compared with the former, yet sufficiently narrow for a pellet of mercury to remain intact in it. The governing equation to calculate gas viscosity from capillary viscometer is derived as follow (Rankine, 1910).

Let V be the volume unoccupied by mercury; the volume of the capillary tube is much less than V, therefore it is negligible. Let p denote the steady pressure of the gas in the tube when the viscometer is held horizontally and let  $\Delta p$  be the pressure difference caused by the mercury pellet when the apparatus is vertical. Let  $p_1$  be the pressure and  $V_1$  the volume at any time above the mercury, and  $p_2$ ,  $V_2$ , the corresponding quantities below the mercury. Then

$$V = V_1 + V_2$$
, and  $\Delta p = p_2 - p_1$  (2.32)

Now if we keep the temperature constant, then real gas law gives

$$pV = p_1 V_1 + p_2 V_2 (2.33)$$

Substituting Equation 2.32 into Equation 2.33 we obtain

$$pV = p_1 V_1 + (p_1 + \Delta p)V_2 = p_1 V + \Delta p V_2$$
 (2.34)

Since  $V_2 = V - V_1$ , Equation 2.34 can be rearranged into

$$pV = p_1 V + \Delta p (V - V_1)$$

or

$$p_1 = p - \Delta p + \Delta p \left(\frac{V_1}{V}\right) \tag{2.35}$$

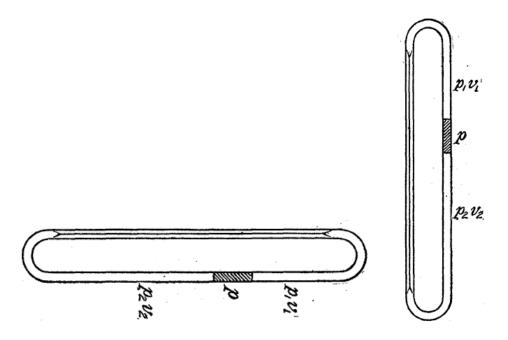
From Equation 2.35 we can see that the pressure above the mercury increases linearly with  $V_I$ , so does the pressure below the mercury, meanwhile the pressure difference remains constant (caused by the density difference between mercury and gas). Let  $dV_{elementary}$  be an elementary volume of gas emerging from the top end of the capillary. This will result in an increase of pressure  $dp_I$ , and also an increase  $dV_I$  in  $V_I$ . The relation between these quantities is

$$dV_{elementary} = dV_1 + V_1 \frac{dp_1}{p_1}$$
(2.36)

which can be expressed as

$$dV_{elementary} = \frac{V}{\Delta p} dp_1 + \frac{V}{\Delta p} (p_1 - p + \Delta p) \frac{dp_1}{p_1}$$





(a) Viscometer in horizontal position (b) Viscometer in vertical position Figure 2-4. Capillary viscometer in two positions, after Rankine (1910)

Recalling Meyer's (Meyer, 1866) formula for transpiration, and neglecting for the moment the slipping correction, we can write

$$dV_{elementary} = \frac{\pi R^4 (p_2^2 - p_1^2)}{8\mu l 2p_1} dt$$
 (2.38)

$$dV_{elementary} = \frac{(p_2 + p_1)(p_2 - p_1)\pi R^4}{16\mu p_1 l} dt$$

$$= \frac{\Delta p(2p_2 - \Delta p)\pi R^4}{16\mu p_1 l} dt$$
(2.39)

where

$$p_2 = p_1 + \Delta p$$

 $\Delta p$  = Pressure difference (Reading from gauge) measured in cms. of mercury at 0°C

 $\mu$  = Air viscosity

R =Radius of capillary tube

L = Length of the capillary tube

If we assume that  $p_1$  and  $p_2$  change sufficiently slowly for the steady state to be set up without appreciable lag; let  $\pi R^4 / 8\mu l = K$ , and substituting for  $p_2$  in Equation 2.39, we obtain

$$dV_{elementary} = K\Delta p \frac{(2p_2 - \Delta p)}{2p_1} dt$$
 (2.40)

By comparing right hand side of Equations 2.37 and 2.40 we note that they are equal.

$$\frac{V}{\Delta p}dp_1\frac{\left(2p_1-p+\Delta p\right)}{p_1} = K\Delta p\frac{\left(2p_2-\Delta p\right)}{2p_1}dt \tag{2.41}$$

Let  $x = 2p_1 + \Delta p$  and  $dx = 2dp_1$ , Equation 2.41 can be written as

$$\frac{V}{\Delta p}(x-p)dx = K\Delta pxdt \tag{2.42}$$

Integration of Equation 2.42 gives

$$\frac{V}{\Delta p} (x - p \log x) \Big|_{x1}^{x2} = K \Delta p dt \tag{2.43}$$

Recalling  $p_1 = p - \Delta p + \Delta p \left(\frac{V_1}{V}\right)$  from Equation 2.35, then

$$x = 2 \left[ p - \Delta p + \Delta p \left( \frac{v_1}{V} \right) \right] + \Delta p = 2p - \Delta p \left( 1 - \frac{2v_1}{V} \right)$$
 (2.44)

Suppose that t is the time taken for the upper volume to increase from  $V_I$  to  $V_I$ , the following is the equation giving the air viscosity.

$$\frac{V}{\Delta p} \left\{ \frac{2\Delta p \left(V_1' - V_1\right)}{V} - p \log \left[ \frac{2p - \Delta p \left(1 - \frac{2V_1'}{V}\right)}{2p - \Delta p \left(1 - \frac{2V_1}{V}\right)} \right] \right\} = K\Delta pt (2.45)$$

By substituting  $\pi R^4 / 8\mu l = K$  into Equation 2.45 we have

$$2(V_{1}' - V_{1}) - \frac{pV}{\Delta p} \log \left[ \frac{2p - \Delta p \left( 1 - \frac{2V_{1}'}{V} \right)}{2p - \Delta p \left( 1 - \frac{2V_{1}}{V} \right)} \right] = \frac{\pi R^{4} \Delta pt}{8\mu l}$$
 (2.46)

It should be noted that the capillary attraction in the wider limb makes the value of  $\Delta p$  not proportional to the length of the mercury pellet. If the pellet was undeformed by the downward movement, capillarity would produce no resultant effect, taking account of the symmetry of the ends. Actually, the upper surface is less curved than the lower one during the motion. This results in a diminution of the effective driving pressure.

A classic capillary viscometer used by Rankine (1923) to measure the viscosities of neon, xenon, and krypton is illustrated as Figure 2-5. Detail geometry of the apparatus can be obtained from Rankine (1910).

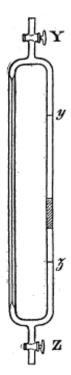


Figure 2-5. A classic capillary viscometer, after Rankine (1910)

## 2.1.2 Falling (or Rolling) Ball Viscometers

From its name we know that the falling (or rolling) ball viscometer measures viscosity by dropping a column- or sphere-shaped rigid body with known dimensions and density into a sample and measuring the time taken for it to fall a specific distance (Figure 2-6). Another type of device measures traveling time when horizontally transporting a rigid body, such as a piston or a needle, in a sample fluid at a constant speed by the force applied by the electromagnetic field. All falling-body viscometers measure fluid viscosity basing on Stokes' law.

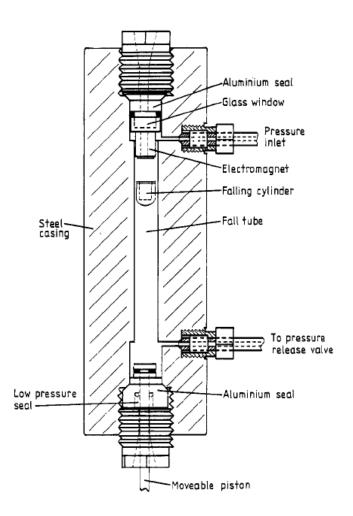


Figure 2-6. Cross section of falling cylinder viscometer body and ancillary components, after Chan and Jckson (1985)

Unlike the vibrating or rotational viscometers, the falling-ball viscometers shown Figure 2-6 cannot continuously measure viscosity. It is also impossible to continuously output digital signals of viscosity coefficient or to control data. In falling ball viscometer the fluid is stationary in a vertical glass tube. A sphere of known size and density is allowed to descend through the fluid. The time for the ball to fall from start point to the end point on the tube can be recorded and the length it travels can be measured. Electronic sensing can be used for timing. At the end of the tube there are two marks, the time for the ball passing these two marks are recorded so that the average velocity of the ball is calculated assuming the distance between these two marks is close enough. Knowing the terminal velocity, the size and density of the sphere, and the density of the liquid, Stokes' Law can be used to calculate the viscosity.

Besides the use of a sphere in falling ball viscometers, both cylinders and needles have been used by various researchers to measure the viscosity. Instruments are also available commercially using these types of geometry. Therefore, commonly used falling ball viscometer includes falling ball, falling cylinder, and falling needle viscometers. Figure 2-7 is the illustration of a falling ball viscometer. Typical falling cylinder viscometer can be referred to Figure 2-6 mentioned above. An example of falling needle viscometer can be seen in Figure 2-8.

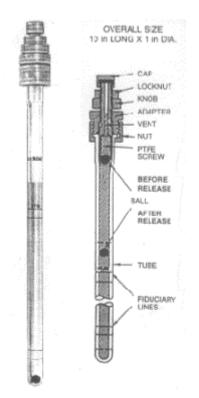


Figure 2-7. Cross section of a falling ball viscometer body, after Florida Atlantic University (2005)

There are some drawbacks when the viscosity is measure by the ball viscometer, these include that the motion of the ball during its descent in the viscometer tube exhibits random slip and spin (Herbert and Stoke, 1886). If we use a cylinder instead of a ball, the problem can be overcome easily. First, a cylinder equipped with stabilizing projections, shows little if any tendency toward dissipating energy in this fashion. Thus the error in measuring experimental fall times is reduced. Second, when ball viscometers are used for measuring low viscosities, the ball diameter must be nearly equal to the tube diameter, making the instrument extremely sensitive to the effects of nonuniform construction, poor reproducibility results. The cylinder however may be easily oriented in a consistent fashion so that any effect of nonuniform construction is constant (Dabir et al., 2007).

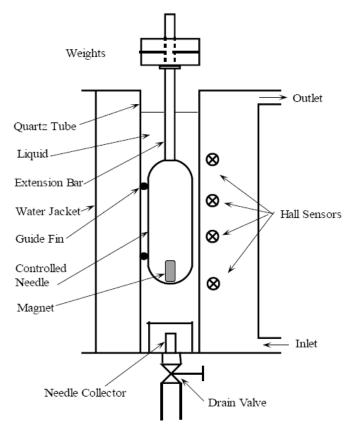


Figure 2-8. Cross section of a falling needle viscometer body, after Park (1994)

Rolling ball viscometers employ the same measuring method as falling ball viscometer except that the falling trajectory is slant instead of vertical. A classic rolling ball viscometer is shown in Figure 2-9.

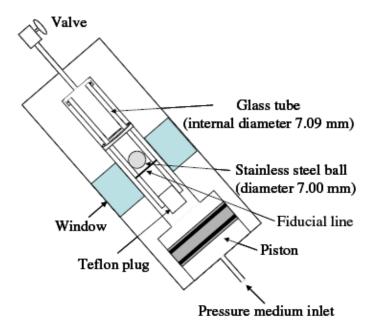


Figure 2-9. Rolling ball viscometer, after Tomida et al. (2005)

# 2.1.3 Vibrating viscometers

Vibrating viscometers can be dated back to the 1950s Bendix instrument, which is of a class that operates by measuring the damping of an oscillating electromechanical resonator immersed in a fluid whose viscosity is to be determined. The resonator generally oscillates in torsion or transversely as a cantilever beam or tuning fork. They are rugged industrial systems used to measure viscosity in many fields. The principle of vibrating viscometer is that it measures the damping of an oscillating electromechanical resonator immersed in the test liquid. The resonator may be a cantilever beam, oscillating sphere or tuning fork which oscillates in torsion or transversely in the fluid. The resonator's damping is measured by several methods:

- 1) Measuring the power input necessary to keep the oscillator vibrating at constant amplitude. The higher the viscosity, the more power is needed to maintain the amplitude of oscillation.
- 2) Measuring the decay time of the oscillation once the excitation is switched off. The higher the viscosity, the faster the signal decays.

3) Measuring the frequency of the resonator as a function of phase angle between excitation and response waveforms. The higher the viscosity, the larger the frequency changes for a given phase change.

The designation of vibrating viscometer usually uses three technologies. There are tuning fork, oscillating sphere, and vibrating rod (or wire) technologies. Each of these technologies is described as follow.

Tuning fork technology-vibrational viscometers designed based on tuning fork technology measure the viscosity by determining the bandwidth and frequency of the vibrating fork resonance; the bandwidth giving the viscosity measurement whilst the frequency giving the fluid density (Figure 2-10). A temperature sensor can be easily accommodated in the instrument for temperature measurement. In addition, other parameters such as viscosity gravity gradients and ignition indices for fuel oils can be calculated.

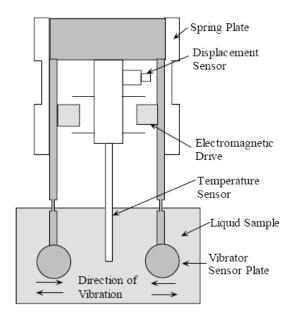


Figure 2-10. Vibrational viscometer employed tuning fork technology, after Paul N. Gardner Co. (2010)

Oscillating sphere technology - in this method a sphere oscillates (Figure 2-11) about its polar axis with precisely controlled amplitude (Steffe, 1992). The viscosity is calculated from the power required to maintain this predetermined amplitude of oscillation. While it is very simple in design, the oscillating sphere viscometer provides viscosity that is density dependent. Therefore, density of the test fluid should be determined independently if kinematic viscosity is required for process control. The principle of oscillating sphere viscometer had been studied by Stokes (1868) many years ago.

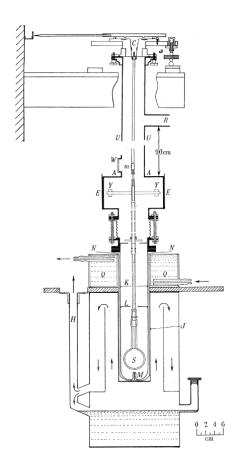


Figure 2-11. An oscillating sphere system for creating controlled amplitude in liquid, after Steffe (1992)

Vibrating rod (or wire) technology - in the viscometer the active part of the sensor is a vibrating rod (or wire). The vibration amplitude varies according to the viscosity of the fluid in which the rod is immersed (Figure 2-12).

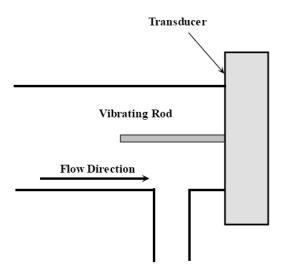


Figure 2-12. Vibrating rod system for measuring dynamic viscosity, after Steffe (1992)

Vibrating viscometers are best suited for many requirements in viscosity measurement. The important features of vibrating viscometers are small sample volume requirement, high sensitivity, ease of operation, continuous readings, wide range, optional internal reference, flow through of the test fluids and consequent easy clean out and prospect of construction with easily available materials. Contrasted to rotational viscometers, which require more maintenance and frequent calibration after intensive use, vibrating viscometers has no moving parts, no weak parts and the sensitive part is very small. Actually even the very basic or acid fluid can be measured by adding a special coating or by changing the material of the sensor. Currently, many industries around the world consider these viscometers as the most efficient system to measure viscosity of any fluid.

#### 2.2 Gas Viscosity Experimental Data

Common approach to estimate gas viscosity comprises direct experimental measurement and gas viscosity correlations. Direct measurement provides reliable and confident result so with the cost of high expense and time consuming and cost expensive. Furthermore, quantity of fluid sample and availability of appropriate measuring instrument that can handle experiment at reservoir condition limit its application. Given the aforementioned disadvantages most PVT lab reports provided gas viscosity estimated from correlations. Although gas viscosity correlation provides a simple and low cost method to predict gas viscosity, accuracy of calculated viscosity is depended on the database it based on. A good gas viscosity correlation needs accurate lab data as its solid base. We cannot evaluate the correlation before we know what kind of lab data is used. One thing for sure is that a correlation cannot guarantee its validity outside of the thermodynamic conditions of lab data. Thus, it is necessary to understand the limitation of available gas viscosities database. In this study a review of available pure nitrogen, methane, and natural gas viscosity is crucial to make our project sense considering high methane concentration in most HPHT gas reservoirs and high nonhydrocarbon concentration such as nitrogen in some HPHT gas reservoirs.

Earhart (1916) determined 10 natural gases viscosities using a capillary viscometer. Yen (1919) measured nitrogen viscosity at temperature of 23 °C and pressures of 14.7 psia using a capillary viscometer. Boyd (1930) applied the transpiration method, or same principle as capillary viscometer, on measuring nitrogen viscosity at temperatures of 30, 50, and 70 °C and pressures from 73 to 178.8 atms. Trautz and Zink (1930) measured methane and nitrogen viscosities at temperatures from 23 to 499 °C. Michels and Gibson (1931) designed an apparatus basing on capillary principle to measure nitrogen viscosity at temperatures of 25, 50, and 75 °C and pressures from 15.37 to 965.7 atms. Berwald and Johnson (1933) measured 25 natural gases viscosities at temperature of 60 °F and pressure of 29.4 psia with a capillary viscometer. Rudenko and Schubnikow (1934) measured nitrogen viscosities at temperature from 63 to 77 °K and pressure less than 8

psia with a capillary viscometer. Adzumi (1937) measured methane, ethane, propane, CH<sub>4</sub>-C<sub>2</sub>H<sub>2</sub>, C<sub>2</sub>H<sub>2</sub>-C<sub>3</sub>H<sub>6</sub>, and C<sub>3</sub>H<sub>6</sub>-C<sub>3</sub>H<sub>8</sub> mixtures viscosities at temperature from 0 to 100 °C and pressure of 14.7 psia with a capillary viscometer. Sage and Lacey (1938) measured methane and 2 natural gases viscosity at temperatures of 100, 160, and 220 °F and pressures up to 2600 psi. Johnston and McCloskey (1940) measured methane and nitrogen viscosity at temperatures from 90 to 200 °K and pressures up to 14.7 psia using an oscillating-disk viscometer. Smith and Brown (1943) measured pure ethane and propane viscosities at temperatures from 15 to 200 °C and pressures from 100 to 5000 psi utilizing a rolling-ball viscometer. They also developed a viscosity correlation basing on available data. Bicher and Katz (1943) measured pure methane and methane-propane mixture viscosities utilizing a rolling-ball inclined-tube viscometer. They ran experiments at temperatures of 77, 167, 257, 347, and 437 °F and pressures from 14.7 to 5000 psia. Comings et al. (Comings and Egly, 1940; Coming et al., 1944) used two Rankine viscometers (capillary viscometer) constructed of Pyrex glass to measure methane and natural gas viscosities at temperatures of 30, 50, 70, and 95 °C and pressures from 1 to 171 atms. Similar to Comings's study, Van Itterbeek et al. (1947) measured nitrogen viscosity at temperatures from -312 to 64 °F and low to ordinary pressures with an oscillating disc viscometer. Carr (1952) and Stewart (1952) used two Rankine viscometers (capillary viscometer) constructed of Pyrex glass to measure methane and three natural gas viscosities at temperatures from 70 to 200 °F and pressures from 14.7 to 10000 psia. Iwasaki (1954) measured pure nitrogen and nitrogenhydrogen mixture viscosities utilizing an oscillating disc viscometer at temperatures of 25, 100, and 150 °C and pressures up to 200 atms. Lambert et al. (1955) measured methane and ethane viscosities an oscillating viscometer at temperatures from 35 to 78 °C and low pressures. Ross and Brown (1957) used a capillary tube viscometer to measure pure nitrogen and methane viscosities at temperatures of 25, 0, -25, and -50 °C and pressures from 500 to 10000 psig. Ellis and Raw (1958) measured nitrogen viscosity at temperatures from 700 to 1000 °C and low pressures through a capillary tube viscometer. Baron et al. (1959) used Rankine viscometer (capillary viscometer) to

measure pure nitrogen and methane viscosities at temperatures of 125, 175, 225, and 275 °F and pressures from 100 to 8000 psig. To solve the problem of grass capillary viscometer broken at high pressure, he balanced the pressures between inside and outside of tube by charging the annulus around the tube. Kestin and Leidenfrost (1959) constructed an oscillating-disk viscometer to measure pure nitrogen viscosities at temperatures from 19 to 25 °C and pressures from 0.139 to 62.7 atms. Swift et al. (1959) measured methane viscosity at temperatures from -83 to -150 °C and pressures from 350 to 710 psia with a falling-body viscometer. Golubev (1959) used the capillary tube viscometer to measure pure nitrogen and methane viscosities at condition of temperatures range from -58.12 to 1292 °F and pressures range from 14.7 to 14700 psia. Golubev data shows a significant difference compared data from the other available database. Swift et al. (1960) extended his measurement on methane viscosity at temperatures from -82 to -140 °C and pressures from 85 to 675 psia with a fallingcylinder viscometer. Flynn et al. (1963) developed a capillary viscometer to measure nitrogen viscosity at temperatures of -78, -50, -25, 25, and 100 °C and pressures from 6.77 to 176 atms. Barua et al. (1964) measured methane viscosity at temperatures from -50 to 150 °C and pressures up to 200 atms using a capillary viscometer. Carmichael et al. (1965) measured methane viscosity at temperatures of 40, 100, 220, 340, and 400 °F and pressures from 14.7 to 5000 psia using a rotating-cylinder type viscometer. Lee (1965) presented viscosity values of pure methane basing on work done by Mario Gonzalez. Data were acquired at temperature from 100 to 340 °F and pressure from 200 to 8000 psia. Recommended methane viscosity values are presented in Table 2-1. Lee claimed that viscosity values corresponding to the region of this investigation are accurate within ±5% percent. Lee also collected pure hydrocarbons such as ethane, propane, n-butane, npentane, and n-decane and gas mixtures (methane-propane, methane-butane, and methane-decane) viscosities in order to derive gas viscosity correlation. He considered the following mole percentage: 10, 20, 30, 40, 50, 60, 70, 80, and 90 percent in binary mixtures. Giddings et al. (1965) developed a versatile absolute capillary-tube viscometer to measure methane viscosity at temperatures from 40 to 280 °F and pressures from 100

to 8000 psia. Wilson (1965) constructed a rolling ball viscometer to measure 10 natural gases viscosity at temperatures from 77 to 400 °F and pressures from 1000 to 10000 psia. Dipippo et al. (1966) constructed an oscillating disc viscometer to measure nitrogen viscosity at temperatures from 75 to 410 °F and pressures from 5.7 to 25 psia. Lee and Gonzalez et al. (Gonzalez et al., 1966; Gonzalez et al., 1970) measured the viscosities of eight natural gases using a capillary-tube viscometer to honor the true reservoirs, for all of the samples, the range of temperature is 100 to 340 °F and the range of pressure is from 14.7 to 8000 psia. Gonzalez et al. (1966) published his methane viscosity data covered temperatures from 100 to 340 °F and pressures from 200 to 8000 psia. Huang et al. (1966) measured methane viscosities at temperatures from -170 to 0 °C and pressure up to 5000 psia with a falling cylinder type viscometer. Van Itterbeek et al. (1966) provided nitrogen viscosities measured by a oscillating disk viscometer at temperatures of 70, 77.3, 83.9 and 90.1 °K and pressures from 0.5 to 98 atms. Boon et al. (1967) provided methane and nitrogen viscosities measured by a capillary viscometer at temperatures from 91 to 114 °K and the corresponding saturated vapor pressures. Kestin and Yata (1968) measured pure methane, nitrogen, and H<sub>2</sub>-N<sub>2</sub>, CH<sub>4</sub>-CO<sub>2</sub>, CH<sub>4</sub>-C<sub>4</sub>H<sub>10</sub> binary mixtures viscosities using an oscillating-disk viscometer at temperatures 20 and 30 °C and pressures from 1 to 25 atms. Grevendonk et al. (1970) measured liquid nitrogen viscosity using a torsionally vibrating piezoelectric crystal viscometer at temperatures from 66 to 124 °K and pressures from vapor pressure to 196 x 10<sup>5</sup> N/m<sup>2</sup>. Helleman et al. (Helleman et al., 1970; Helleman et, al. 1973) measured methane viscosities at temperatures from 96 to 187 °K and pressures up to 100 atms and nitrogen viscosities at temperatures from 77 to 203 °F and pressures of 14.7 psia using an oscillating-disk viscometer. Diehl et al. (1970) used Geopal viscometer (capillary tube viscometer) to determine the pure hydrocarbon and nitrogen gas viscosities. For all of the samples, the range of temperature is 32 to 302 °F and the range of pressure is from 14.7 to 7350 psia. Latto and Saunders (1972) measured nitrogen viscosity at temperatures from 90 to 400 °K and pressures from 1 to 150 atms using a capillary viscometer. Stephan and Lucas (1979) collected a large database of gas viscosities from

several investigators with different methods including torsional crystal, oscillating disk, rolling ball, rotating cylinder, capillary tube, and falling ball. The data includes gases such as pure hydrocarbons (methane to n-decane), nitrogen, and carbon dioxide. The range of temperatures and pressures differs from one component to another. In general the temperatures range is from 212 to 1832 °F and the pressures range is from 14.7 to 10290 psia. Diller (1980) measured the viscosity of compressed gases and liquid methane at temperatures between 100 and 300 °K and pressures up to 4350 psia with a torsionally oscillating quartz crystal viscometer. As a extension of his work in 1980, Diller (1983) used same viscometer to measure the viscosity of compressed gases and liquid nitrogen at temperatures between 90 and 300 °K and pressures up to 4350 psia. Hongo et al. (1988) used Maxwell type oscillating-disc viscometer to measure the viscosity of methane and methane-chlorodifluoromethane mixtures in the temperature range from 298.15 to 373.15 °K and at pressures up to 5MP. Van Der Gulik et al. (1988) used vibrating wire viscometer to measure the viscosity of methane at 25 °C and pressures from 1 to 10,000 bar. Vogel et al. (1999) used a vibrating wire viscometer to measure the viscosity of methane at temperature of 260, 280, 300, 320, 340, and 360 °K and pressures up to 20 MPa. Assael et al. (2001) employed a vibrating wire viscometer to measure the viscosity of methane at the temperature range from 313 to 455 °K at a pressure close to atmospheric and in the temperature range from 240 to 353 °K at pressures up to 15 MPa. Schley et al. (2004) used a vibrating-wire viscometer to measure methane viscosity at temperatures of 260, 280, 300, 320, 340, and 360 K and at pressures up to 29 MPa. Seibt et al. (2006) measured nitrogen viscosity with a vibratingwire viscometer. The measurements were performed along the six isotherms of 298.15, 323.15, 348.15, 373.15, 398.15, and 423.15  $^{o}K$  and at pressures up to a maximum of 35MPa. Tables 2-1 to 2-4 show experimental data of methane viscosity from some investigators. Table 2-5 depicts experimental data of nitrogen viscosity from some investigators.

Table 2-1. Methane viscosity collected by Lee (1965)

Pressure			Tei	mperature (	(°F)		
(psia)	100	160	220	280	340	400	460
14.70	0.01140	0.01250	0.01340	0.01440	0.01530	0.01660	0.01750
100.00	0.01190	0.01300	0.01400	0.01500	0.01600	0.01700	0.01790
200.00	0.01200	0.01300	0.01410	0.01510	0.01610	0.01710	0.01800
300.00	0.01210	0.01310	0.01410	0.01510	0.01620	0.01720	0.01800
400.00	0.01220	0.01320	0.01420	0.01520	0.01620	0.01730	0.01810
500.00	0.01240	0.01330	0.01430	0.01530	0.01630	0.01730	0.01820
600.00	0.01250	0.01350	0.01440	0.01540	0.01640	0.01740	0.01830
800.00	0.01280	0.01370	0.01460	0.01550	0.01650	0.01760	0.01840
1000.00	0.01320	0.01400	0.01480	0.01570	0.01670	0.01780	0.01860
1250.00	0.01370	0.01450	0.01520	0.01600	0.01700	0.01800	0.01880
1500.00	0.01440	0.01490	0.01560	0.01630	0.01720	0.01830	0.01910
1750.00	0.01520	0.01540	0.01600	0.01680	0.01750	0.01850	0.01930
2000.00	0.01600	0.01600	0.01640	0.01700	0.01780	0.01860	0.01950
2500.00	0.01770	0.01720	0.01740	0.01780	0.01850	0.01940	0.02010
3000.00	0.01950	0.01860	0.01860	0.01870	0.01930	0.02010	0.02070
3500.00	0.02120	0.02020	0.01970	0.01970	0.02010	0.02070	0.02130
4000.00	0.02310	0.02170	0.02090	0.02060	0.02090	0.02140	0.02190
4500.00	0.02490	0.02320	0.02200	0.02170	0.02180	0.02220	0.02250
5000.00	0.02660	0.02460	0.02330	0.02280	0.02260	0.02300	0.02320
6000.00	0.02990	0.02740	0.02570	0.02500	0.02440	0.02450	0.02460
7000.00	0.03280	0.02990	0.02810	0.02710	0.02620	0.02610	0.02600
8000.00	0.03550	0.03230	0.03000	0.02910	0.02810	0.02750	0.02730
9000.00	0.03800	0.03450	0.03220	0.03100	0.03000	0.02910	0.02860
10000.00	0.04060	0.03660	0.03420	0.03300	0.03180	0.03050	0.03000
Note: visco	sity in cp						

Table 2-2. Methane viscosity by Diehl et al. (1970)

Pressure			Ter	nperature (	(°F)		
(psia)	86	104	122	140	158	176	194
14.70	0.01116	0.01150	0.01183	0.01216	0.01248	0.01279	0.01310
220.50	0.01140	0.01170	0.01205	0.01235	0.01270	0.01300	0.01330
367.50	0.01155	0.01190	0.01220	0.01255	0.01285	0.01320	0.01350
735.00	0.01210	0.01240	0.01270	0.01300	0.01335	0.01365	0.01400
1102.50	0.01290	0.01315	0.01340	0.01365	0.01395	0.01425	0.01455
1470.00	0.01390	0.01410	0.01430	0.01450	0.01470	0.01490	0.01515
1837.50	0.01510	0.01520	0.01530	0.01545	0.01560	0.01575	0.01590
2205.00	0.01640	0.01640	0.01645	0.01650	0.01655	0.01665	0.01675
2940.00	0.01905	0.01895	0.01885	0.01875	0.01870	0.01865	0.01860
3675.00	0.02175	0.02150	0.02125	0.02105	0.02085	0.02070	0.02055
4410.00	0.02410	0.02380	0.02350	0.02320	0.02290	0.02265	0.02240
5145.00	0.02650	0.02610	0.02570	0.02530	0.02490	0.02455	0.02425
5880.00	0.02880	0.02830	0.02780	0.02730	0.02685	0.02640	0.02600
6615.00	0.03105	0.03045	0.02990	0.02930	0.02875	0.02825	0.02775
7350.00	0.03320	0.03250	0.03190	0.03125	0.03060	0.03000	0.02945
Note: viso	cosity in cp	)					

Table 2-2. Continued

Pressure		Temperature (°F)							
(psia)	212	230	248	266	280	302			
14.70	0.01341	0.01371	0.01400	0.01430	0.01459	0.01488			
220.50	0.01360	0.01395	0.01425	0.01455	0.01485	0.01515			
367.50	0.01380	0.01410	0.01440	0.01470	0.01500	0.01530			
735.00	0.01430	0.01460	0.01490	0.01515	0.01545	0.01575			
1102.50	0.01480	0.01505	0.01535	0.01560	0.01585	0.01610			
1470.00	0.01540	0.01565	0.01590	0.01615	0.01635	0.01655			
1837.50	0.01610	0.01630	0.01650	0.01670	0.01690	0.01710			
2205.00	0.01685	0.01700	0.01715	0.01730	0.01750	0.01770			
2940.00	0.01860	0.01865	0.01870	0.01880	0.01890	0.01900			
3675.00	0.02045	0.02040	0.02035	0.02030	0.02025	0.02025			
4410.00	0.02220	0.02205	0.02190	0.02180	0.02170	0.02160			
5145.00	0.02395	0.02370	0.02350	0.02330	0.02315	0.02300			
5880.00	0.02565	0.02535	0.02505	0.02475	0.02450	0.02430			
6615.00	0.02730	0.02690	0.02655	0.02620	0.02590	0.02565			
7350.00	0.02890	0.02845	0.02805	0.02765	0.02730	0.02700			
Note: vise	cosity in cp	)			•				

Table 2-3. Methane viscosity by Stephan and Lucas (1979)

Pressure			Temper	ature (°F)		
(psia)	80.33	116.3	152.3	188.3	224.3	260.3
14.70	0.01100	0.01170	0.01230	0.01300	0.01350	0.01420
294.00	0.01150	0.01210	0.01270	0.01340	0.01400	0.01460
441.00	0.01170	0.01230	0.01190	0.01360	0.01420	0.01480
588.00	0.01200	0.01260	0.01320	0.01380	0.01440	0.01500
677.67	0.01210	0.01270	0.01330	0.01390	0.01450	0.01510
808.50	0.01240	0.01300	0.01350	0.01410	0.01470	0.01530
882.00	0.01250	0.01310	0.01360	0.01420	0.01480	0.01540
1029.00	0.01290	0.01340	0.01390	0.01440	0.01500	0.01550
1176.00	0.01320	0.01370	0.01410	0.01460	0.01510	0.01570
1323.00	0.01360	0.01400	0.01440	0.01480	0.01530	0.01580
1470.00	0.01390	0.01430	0.01460	0.01500	0.01550	0.01600
1764.00	0.01490	0.01510	0.01530	0.01560	0.01600	0.01640
2058.00	0.01600	0.01590	0.01600	0.01620	0.01650	0.01690
2205.00	0.01650	0.01630	0.01640	0.01650	0.01680	0.01710
2940.00	0.01920	0.01870	0.01840	0.01830	0.01830	0.01850
4410.00	0.02450	0.02330	0.02250	0.02200	0.02160	0.02150
5880.00	0.03030	0.02850	0.02710	0.02610	0.02530	0.02470
7350.00	0.03490	0.03260	0.03090	0.02960	0.02860	0.02780
8820.00	0.03880	0.03620	0.03430	0.03290	0.03170	0.03070
10290.00	0.04260	0.03950	0.03730	0.03570	0.03450	0.03350
Note: visc	osity in cp					

Table 2-3. Continued

Pressure	Temperature (°F)									
(psia)	296.3	332.3	368.3	404.3	440.3	476.3				
14.70	0.01470	0.01540	0.01600	0.01660	0.01720	0.01770				
294.00	0.01530	0.01600	0.01660	0.01720	0.01780	0.01840				
441.00	0.01540	0.01610	0.01670	0.01730	0.01790	0.01850				
588.00	0.01560	0.01620	0.01680	0.01740	0.01800	0.01860				
677.67	0.01570	0.01630	0.01690	0.01750	0.01810	0.01870				
808.50	0.01580	0.01640	0.01700	0.01760	0.01820	0.01880				
882.00	0.01590	0.01640	0.01700	0.01760	0.01820	0.01880				
1029.00	0.01600	0.01660	0.01720	0.01780	0.01830	0.01890				
1176.00	0.01620	0.01670	0.01730	0.01790	0.01850	0.01910				
1323.00	0.01630	0.01690	0.01750	0.01810	0.01860	0.01920				
1470.00	0.01650	0.01700	0.01760	0.01820	0.01870	0.01930				
1764.00	0.01690	0.01740	0.01800	0.01850	0.01900	0.01960				
2058.00	0.01730	0.01780	0.01830	0.01880	0.01930	0.01990				
2205.00	0.01750	0.01800	0.01850	0.01900	0.01950	0.02010				
2940.00	0.01870	0.01900	0.01950	0.01990	0.02040	0.02090				
4410.00	0.02140	0.02150	0.02170	0.02190	0.02220	0.02250				
5880.00	0.02440	0.02410	0.02410	0.02410	0.02430	0.02450				
7350.00	0.02730	0.02680	0.02660	0.02640	0.02630	0.02630				
8820.00	0.03000	0.02940	0.02890	0.02860	0.02830	0.02820				
10290.00	0.03260	0.03180	0.03130	0.03070	0.03030	0.03000				
Note: visc	osity in cp									

Table 2-4. Methane viscosity by Golubev (1959)

Pressure			Temperature (°F)							
(psia)	77	122	167	212	302	392	482			
14.70	0.01108	0.01182	0.01260	0.01331	0.01471	0.01603	0.01725			
146.96	0.01120	0.01193	0.01270	0.01340	0.01477	0.01611	0.01728			
293.92	0.01137	0.01210	0.01280	0.01350	0.01483	0.01617	0.01733			
587.84	0.01180	0.01247	0.01312	0.01377	0.01512	0.01634	0.01745			
881.76	0.01237	0.01295	0.01350	0.01416	0.01530	0.01653	0.01765			
1175.68	0.01310	0.01352	0.01392	0.01452	0.01556	0.01675	0.01785			
1469.59	0.01395	0.01417	0.01445	0.01497	0.01580	0.01700	0.01809			
2204.39	0.01652	0.01610	0.01600	0.01627	0.01685	0.01775	0.01872			
2939.19	0.01930	0.01830	0.01787	0.01787	0.01807	0.01867	0.01947			
3673.99	0.02187	0.02062	0.02002	0.01965	0.01942	0.01975	0.02030			
4408.78	0.02455	0.02300	0.02205	0.02142	0.02085	0.02075	0.02120			
5143.58	0.02705	0.02530	0.02401	0.02320	0.02230	0.02182	0.02205			
5878.38	0.02942	0.02745	0.02593	0.02486	0.02370	0.02290	0.02295			
7347.97	0.03365	0.03145	0.02955	0.02815	0.02635	0.02500	0.02470			
8817.57	0.03740	0.03485	0.03277	0.03120	0.02887	0.02705	0.02645			
10287.16	0.04087	0.03820	0.03545	0.03395	0.03130	0.02910	0.02820			
11756.76	0.04410	0.04095	0.03855	0.03655	0.03367	0.03107	0.02995			
Note: visco	osity in cp									

Table 2-5. Nitrogen viscosity collected by Stephan and Lucas (1979)

Temperature			Pressu	re (psi)		
°F	14.504	145	290	435	580	725
-343	0.2633	0.2677	0.2728	0.2777	0.2826	0.2876
-334	0.2113	0.2154	0.2197	0.2244	0.229	0.2336
-325	0.1677	0.1713	0.1753	0.1793	0.1832	0.1875
-316	0.00552	0.1366	0.14	0.1433	0.1467	0.1501
-307	0.00586	0.1111	0.1136	0.1164	0.1192	0.1219
-298	0.0062	0.09326	0.09528	0.09737	0.09951	0.1018
-289	0.00654	0.08093	0.08266	0.08429	0.08602	0.08777
-280	0.00688	0.0713	0.07297	0.07459	0.07616	0.07772
-271	0.00722	0.00783	0.06397	0.06584	0.0676	0.06929
-262	0.00756	0.00811	0.05517	0.05728	0.05925	0.06112
-253	0.00789	0.0084	0.04626	0.04902	0.0514	0.05354
-244	0.00821	0.00868	0.00953	0.03974	0.04335	0.04612
-235	0.00852	0.00896	0.00968	0.01155	0.03369	0.0381
-226	0.00883	0.00925	0.00988	0.01107	0.01805	0.02945
-217	0.00914	0.00954	0.0101	0.01103	0.01314	0.01998
-208	0.00945	0.00983	0.01028	0.01112	0.0125	0.01551
-190	0.01006	0.01041	0.01085	0.01145	0.01232	0.01365
-172	0.01066	0.01098	0.01138	0.01186	0.01252	0.0134
-154	0.01124	0.01154	0.01189	0.01232	0.01286	0.01353
-136	0.01181	0.01209	0.01241	0.01279	0.01325	0.0138
-118	0.01237	0.01263	0.01293	0.01327	0.01367	0.01415
-100	0.01292	0.01316	0.01344	0.01376	0.01411	0.01452
-82	0.01346	0.01369	0.01395	0.01424	0.01456	0.01493
-64	0.01399	0.01421	0.01445	0.01472	0.01502	0.01535
-46	0.0145	0.01471	0.01494	0.01519	0.01546	0.01577
-28	0.015	0.0152	0.01542	0.01566	0.01591	0.01619
-10	0.01549	0.01568	0.01589	0.01612	0.01635	0.01661
Note: viscosit	y in cp					

Table 2-5. Continued

Temperature			Pressu	re (psi)		
°F	14.504	145	290	435	580	725
8	0.01597	0.01615	0.01635	0.01657	0.01679	0.01703
26	0.01644	0.01662	0.0168	0.01701	0.01722	0.01745
44	0.01691	0.01708	0.01726	0.01745	0.01765	0.01787
62	0.01737	0.01753	0.01771	0.01789	0.01808	0.01829
80	0.01782	0.01797	0.01815	0.01832	0.0185	0.0187
98	0.01826	0.01841	0.01858	0.01874	0.01892	0.0191
116	0.0187	0.01885	0.019	0.01916	0.01934	0.01951
134	0.01913	0.01928	0.01942	0.01958	0.01975	0.01991
152	0.01956	0.01971	0.01985	0.02	0.02015	0.02032
170	0.02	0.02014	0.02028	0.02042	0.02056	0.02073
260	0.02204	0.02216	0.02228	0.0224	0.02253	0.02267
350	0.02396	0.02406	0.02417	0.02428	0.02439	0.02451
440	0.02577	0.02586	0.02596	0.02606	0.02615	0.02626
530	0.02747	0.02756	0.02764	0.02774	0.02782	0.02791
620	0.02908	0.02916	0.02924	0.02932	0.0294	0.02948
710	0.03062	0.03069	0.03077	0.03084	0.03091	0.03099
800	0.0321	0.03217	0.03224	0.0323	0.03237	0.03244
980	0.03491	0.03497	0.03503	0.03509	0.03514	0.03521
1160	0.03753	0.03758	0.03763	0.03769	0.03774	0.03779
1340	0.03999	0.04004	0.04008	0.04013	0.04018	0.04023
1520	0.04232	0.04236	0.0424	0.04245	0.04249	0.04253
1700	0.04453	0.04457	0.04461	0.04465	0.04469	0.04473
1880	0.04662	0.04666	0.04669	0.04673	0.04677	0.0468
Note: viscosit	y in cp					

Table 2-5. Continued

Temperature			Pressu	re (psi)		
°F	870	1015	1160	1305	1450	1813
-343	0.2927	0.2978	0.3027	-	-	-
-334	0.2383	0.2429	0.2475	0.2523	0.2568	0.2687
-325	0.1914	0.1957	0.1998	0.2041	0.2084	0.2191
-316	0.1537	0.1573	0.1609	0.1645	0.1682	0.1777
-307	0.1248	0.1278	0.1308	0.1338	0.1369	0.1448
-298	0.104	0.1063	0.1087	0.1111	0.1136	0.12
-289	0.08951	0.09135	0.09319	0.09507	0.097	0.102
-280	0.07922	0.08076	0.08229	0.08386	0.08542	0.08949
-271	0.07089	0.07242	0.07392	0.07539	0.07681	0.08034
-262	0.06294	0.06469	0.06636	0.06794	0.06948	0.07308
-253	0.05553	0.05737	0.0591	0.06078	0.06243	0.06636
-244	0.04849	0.05041	0.05255	0.05437	0.05608	0.06005
-235	0.04135	0.04407	0.04633	0.04836	0.05023	0.05445
-226	0.03424	0.03763	0.04033	0.0427	0.04479	0.04931
-217	0.02686	0.03131	0.03462	0.0373	0.0397	0.04427
-208	0.02068	0.02544	0.02923	0.03229	0.03487	0.04012
-190	0.0157	0.01847	0.02147	0.02434	0.02696	0.03248
-172	0.0146	0.01614	0.018	0.02004	0.02211	0.02698
-154	0.01437	0.01542	0.01666	0.01805	0.01958	0.02347
-136	0.01446	0.01525	0.01616	0.01719	0.01832	0.02139
-118	0.01469	0.01532	0.01604	0.01685	0.01774	0.0202
-100	0.01499	0.01553	0.01612	0.01678	0.0175	0.01951
-82	0.01534	0.0158	0.01632	0.01688	0.01748	0.01918
-64	0.01572	0.01613	0.01657	0.01758	0.01799	0.01912
-46	0.01611	0.01647	0.01687	0.0173	0.01776	0.01903
-28	0.0165	0.01683	0.01719	0.01758	0.01799	0.01912
-10	0.01689	0.0172	0.01753	0.01788	0.01825	0.01927
Note: viscosity	in cp					

Table 2-5. Continued

Temperature			Pressur	re (psi)		
°F	870	1015	1160	1305	1450	1813
8	0.01729	0.01758	0.01788	0.01819	0.01854	0.01946
26	0.0177	0.01796	0.01824	0.01852	0.01884	0.01969
44	0.0181	0.01835	0.01861	0.01887	0.01917	0.01995
62	0.0185	0.01874	0.01898	0.01923	0.0195	0.02023
80	0.0189	0.01912	0.01935	0.01959	0.01984	0.02052
98	0.0193	0.0195	0.01972	0.01995	0.02018	0.02082
116	0.0197	0.01989	0.0201	0.02032	0.02053	0.02113
134	0.02009	0.02028	0.02047	0.02068	0.02089	0.02145
152	0.02048	0.02067	0.02085	0.02105	0.02126	0.02178
170	0.02087	0.02106	0.02124	0.02142	0.02162	0.02212
260	0.0228	0.02294	0.02308	0.02324	0.02339	0.0238
350	0.02463	0.02474	0.02487	0.02499	0.02513	0.02546
440	0.02636	0.02647	0.02658	0.02669	0.0268	0.02709
530	0.028	0.0281	0.02819	0.02829	0.02839	0.02864
620	0.02957	0.02965	0.02974	0.02982	0.02991	0.03014
710	0.03107	0.03114	0.03122	0.0313	0.03138	0.03159
800	0.03251	0.03258	0.03266	0.03273	0.03281	0.03299
980	0.03527	0.03533	0.03539	0.03546	0.03552	0.03568
1160	0.03785	0.0379	0.03795	0.03801	0.03807	0.03821
1340	0.04027	0.04032	0.04037	0.04042	0.04047	0.0406
1520	0.04258	0.04262	0.04267	0.04271	0.04276	0.04287
1700	0.04476	0.04481	0.04485	0.04489	0.04493	0.04503
1880	0.04684	0.04687	0.04691	0.04695	0.04699	0.04708
Note: viscosit	y in cp					

Table 2-5. Continued

Temperature			Pressu	re (psi)		
°F	2176	2538	2901	3626	4351	5802
-343	-	-	-	-	-	-
-334	0.2808	0.2927	0.3047	0.3288	0.3533	1
-325	0.2301	0.2411	0.2523	0.2747	0.2979	0.3445
-316	0.1872	0.1971	0.2071	0.2279	0.2491	0.2928
-307	0.153	0.1614	0.1702	0.1884	0.2075	0.2475
-298	0.1267	0.1338	0.1412	0.1568	0.1733	0.2092
-289	0.1075	0.1131	0.1191	0.1321	0.1462	0.1774
-280	0.09376	0.09825	0.103	0.1135	0.1253	0.152
-271	0.08395	0.08763	0.0915	0.09992	0.1094	0.1317
-262	0.07644	0.07972	0.08305	0.09002	0.0977	0.1161
-253	0.06993	0.07325	0.0764	0.08255	0.08902	0.1041
-244	0.06376	0.0673	0.07056	0.07655	0.08232	0.09503
-235	0.05821	0.06167	0.06507	0.07127	0.07686	0.088
-226	0.05323	0.05677	0.06007	0.06631	0.07204	0.08241
-217	0.04863	0.05229	0.05563	0.06172	0.06748	0.0775
-208	0.04438	0.04811	0.05154	0.05765	0.06325	0.07311
-190	0.03694	0.04082	0.04425	0.05032	0.05576	0.06544
-172	0.03126	0.03503	0.03836	0.04427	0.04959	0.05895
-154	0.02719	0.03066	0.03382	0.03946	0.0445	0.05354
-136	0.02454	0.02755	0.03045	0.03573	0.04049	0.04903
-118	0.02281	0.02543	0.02797	0.0328	0.03757	0.03529
-100	0.02173	0.02397	0.02624	0.0306	0.0347	0.04227
-82	0.02105	0.02301	0.025	0.02391	0.03268	0.03975
-64	0.02038	0.02173	0.02413	0.02767	0.03114	0.03773
-46	0.02045	0.02198	0.02354	0.02673	0.0299	0.03602
-28	0.02038	0.02173	0.02314	0.02604	0.02895	0.03464
-10	0.0204	0.02161	0.02288	0.02552	0.0282	0.03353
Note: viscosit	y in cp					

Table 2-5. Continued

Temperature		T	Pressur	re (psi)	T	
°F	2176	2538	2901	3626	4351	5802
8	0.02048	0.02159	0.02274	0.02517	0.02764	0.03259
26	0.02062	0.02163	0.02269	0.02492	0.02722	0.03182
44	0.02081	0.02174	0.02271	0.02477	0.02691	0.03121
62	0.02103	0.02188	0.02279	0.02372	0.02669	0.03073
80	0.02126	0.02206	0.02289	0.02466	0.02654	0.03035
98	0.02151	0.02226	0.02304	0.0247	0.02644	0.03004
116	0.02178	0.02248	0.02321	0.02477	0.02641	0.0298
134	0.02206	0.02271	0.02341	0.02487	0.02642	0.02963
152	0.02236	0.02297	0.02363	0.02501	0.02647	0.02952
170	0.02268	0.02326	0.02387	0.02518	0.02656	0.02947
260	0.02423	0.0247	0.02518	0.02616	0.0273	0.02961
350	0.02583	0.02621	0.02661	0.02744	0.02834	0.03025
440	0.0274	0.02773	0.02806	0.02877	0.02953	0.03115
530	0.02892	0.0292	0.02949	0.03011	0.03076	0.03216
620	0.03038	0.03064	0.03089	0.03144	0.03201	0.03323
710	0.0318	0.03203	0.03226	0.03274	0.03326	0.03435
800	0.03318	0.03339	0.0336	0.03404	0.0345	0.03548
980	0.03585	0.03602	0.03619	0.03656	0.03695	0.03776
1160	0.03835	0.0385	0.03965	0.03897	0.0393	0.03999
1340	0.04073	0.04085	0.04099	0.04127	0.04156	0.04216
1520	0.04299	0.0431	0.04322	0.04346	0.04372	0.04426
1700	0.04514	0.04524	0.04535	0.04557	0.0458	0.04628
1880	0.04718	0.04728	0.04737	0.04758	0.04778	0.04819
Note: viscosit	y in cp					

Table 2-5. Continued

Temperature	Pressure (psi)						
°F	6527	7252	8702	10153	11603	13053	14504
-325	0.3678	0.3914	-	-	-	-	-
-316	0.3151	0.3376	-	-	-	-	-
-307	0.2685	0.2896	-	-	-	-	-
-298	0.2283	0.2478	-	-	-	-	-
-289	0.1945	0.2121	-	-	-	-	-
-280	0.1668	0.1826	-	-	-	-	-
-271	0.1445	0.1581	-	-	-	-	-
-262	0.1268	0.1386	-	-	-	-	-
-253	0.1131	0.123	-	-	-	-	-
-244	0.1025	0.1108	-	-	-	-	-
-235	0.09427	0.1012	-	-	-	-	-
-226	0.08782	0.0937	-	-	-	-	-
-217	0.08264	0.08774	-	-	-	-	-
-208	0.07794	0.08267	-	-	-	-	-
-190	0.07	0.0743	0.08271	-	-	-	-
-172	0.06331	0.06749	0.0755	0.08316	-	-	-
-154	0.05761	0.06167	0.06936	0.07671	0.08374	-	-
-136	0.05292	0.05675	0.06401	0.07111	0.07789	0.08443	-
-118	0.04906	0.05263	0.05963	0.06227	0.07275	0.07905	0.08545
-100	0.04584	0.04926	0.05584	0.0665	0.06832	0.07435	0.0805
-82	0.04313	0.04638	0.0526	0.05867	0.06451	0.07026	0.07606
-64	0.04085	0.04396	0.04987	0.05562	0.06118	0.06671	0.07211
-46	0.03901	0.04188	0.0475	0.05295	0.05827	0.06356	0.06871
-28	0.03743	0.04015	0.04547	0.05064	0.0557	0.06074	0.06573
-10	0.0361	0.03869	0.04371	0.04865	0.05344	0.05823	0.06306
Note: viscosity in cp							

Table 2-5. Continued

Temperature	Pressure (psi)						
°F	6527	7252	8702	10153	11603	13053	14504
8	0.03501	0.03745	0.0422	0.04691	0.05148	0.05605	0.06067
26	0.03412	0.03641	0.04091	0.04539	0.04976	0.05414	0.05853
44	0.03337	0.03554	0.03982	0.04406	0.04825	0.05245	0.05661
62	0.03276	0.03481	0.03387	0.04291	0.0469	0.05093	0.05489
80	0.03226	0.0342	0.03805	0.0419	0.0457	0.04956	0.05336
98	0.03186	0.0337	0.03734	0.04101	0.04465	0.04834	0.052
116	0.03153	0.03328	0.03675	0.04024	0.04374	0.04725	0.05078
134	0.03127	0.03293	0.03625	0.03958	0.04295	0.04629	0.04969
152	0.03108	0.03266	0.03583	0.03901	0.04225	0.04546	0.04872
170	0.03095	0.03247	0.0355	0.03855	0.04163	0.04476	0.04785
260	0.03086	0.03209	0.0345	0.03701	0.03954	0.04212	0.04471
350	0.03125	0.03226	0.03433	0.03645	0.0386	0.04076	0.04301
440	0.03199	0.03286	0.03465	0.03645	0.03831	0.04019	0.04209
530	0.03289	0.03364	0.0352	0.03679	0.03842	0.04008	0.04176
620	0.03388	0.03455	0.0359	0.03733	0.03877	0.04026	0.0418
710	0.03493	0.03552	0.03674	0.03801	0.03931	0.04064	0.04208
800	0.036	0.03654	0.03762	0.03878	0.03997	0.04118	0.04241
980	0.03819	0.03863	0.03955	0.0405	0.04149	0.04252	0.04357
1160	0.04036	0.04073	0.04152	0.04233	0.04318	0.04405	0.04495
1340	0.04247	0.04281	0.04349	0.04419	0.04494	0.04569	0.04647
1520	0.04453	0.04482	0.04542	0.04605	0.0467	0.04737	0.04807
1700	0.04653	0.04679	0.04732	0.04788	0.04845	0.04906	0.04968
1880	0.04844	0.04867	0.04916	0.04966	0.05018	0.05072	0.05128
Note: viscosity in cp							

Literature review shows that although numerous researches on gas viscosity were undertaken, no data for the gas viscosities are available above the 14700 psia that the HPHT region beings, therefore the validities of correlations that based experimental data are doubted.

# 2.3 Available Gas Viscosity Correlations

Since good gas viscosity correlation provides a simple and low cost method to predict gas viscosity, we reviewed several well known correlations used to determine gas viscosity in industry. Here we discuss the most useful correlations such as Comings-Mayland-Egly (Comings and Egly, 1940; Comings et al., 1944) correlation, Smith-Brown (1943) correlation, Bicher-Katz (1943) correlation, Carr-Kobayashi-Burrrow (1954) correlation, Jossi-Stiel-Thodos (1962) correlation, and Lee-Gonzalez-Eakin (Gonzalez et al., 1970) correlation. In addition, the National Institute of Standard and Technology (NIST) (2000) has developed a computer program that predicts thermodynamic and transport properties of hydrocarbon fluids. Londono (2001) optimized existing gas viscosity and density correlations (or gas z-factor, then calculate gas density using EOS) and developed new gas viscosity and density correlations all basing on his collected database. Sutton (2005) optimized existing gas viscosity to developed new gas viscosity basing on a database containing thousands data points. Viswanathan (2007) modified Lee-Gonzalez-Eakin correlation using the NIST methane values. Discussing on these correlations and their databases gives an insight of current understanding of gas viscosity.

### 2.3.1 Comings-Mayland-Egly Correlation (1940, 1944)

Inspired by analogy to the approximate equality of the compressibility factors for a wide variety of compounds at equal reduced temperatures and pressures, Comings-Mayland-Egly correlation (Comings and Egly, 1940) proposed graphical correlation to estimate gas viscosity using Viscosity Ratio versus Reduced Pressure Charts (Figure 2-13). Viscosity ratio was defined as the ratio of viscosity at interested pressure temperature to

the viscosity at same temperature, but at pressure of one atmosphere. Essentially, the principle behind this analogy is the theory of corresponding states. Therefore it is not valid for most polar molecules. Data used in this correlation consists of viscosity of carbon dioxide, nitrogen, ammonia, water, methane, propane, and butane available from literatures.

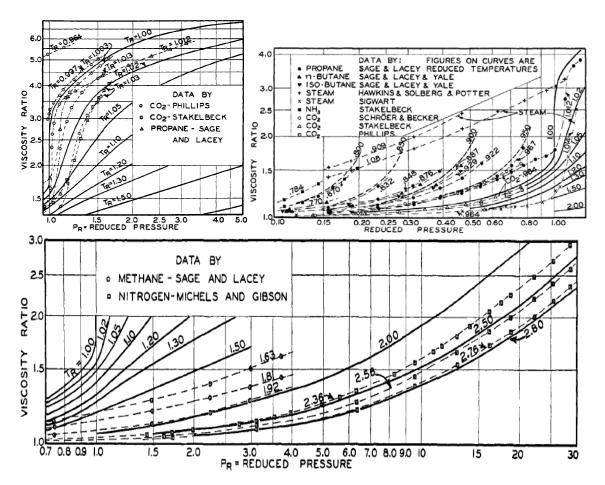


Figure 2-13. Viscosity ratio versus reduced pressure charts used to estimate gas viscosity, after Comings and Egly (1940)

In 1944 Comings et al. (1944) measured viscosity of N<sub>2</sub>, CO<sub>2</sub>, CH<sub>4</sub>, C<sub>2</sub>H<sub>6</sub>, and C<sub>3</sub>H<sub>8</sub> at pressure from 14.7 to 14196 psia and temperature from 14 to 374 °F. With these lab data and the data collected in 1940 (Table 3-6). Comings et al. (1944) improved this correlation by exploiting the analogy between viscosity and kinetic pressure. Both the

kinetic pressure and viscosity are the results of the transfer of momentum in that the kinetic pressure is normal to the wall and viscosity is parallel to the wall. Therefore viscosity should be proportional to kinetic pressure. In brief, this correlation bases on corresponding states theory. This approach applies four steps to get natural gas viscosity. Firstly we need to get the gas viscosity at interested temperature and pressure of one atmosphere,  $\mu_1$ , which can be obtained from the International Critical Table. Secondly the reduced pressure and reduced temperature are calculated. Thirdly go to Figures 2-14 or 2-15 to read the logarithm of the viscosity ratio,  $log(\mu/\mu_1)$ , or viscosity ratio,  $\mu/\mu_1$ . Finally with the viscosity ratio and viscosity at interested temperature and pressure of one atmosphere obtained in first step gas viscosity at interested condition can be calculated.

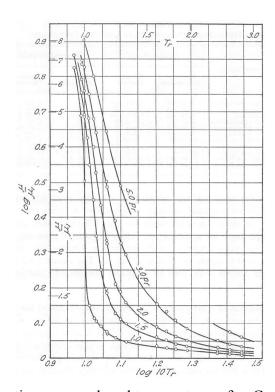


Figure 2-14. Viscosity ratio versus reduced temperature, after Comings et al. (1944)

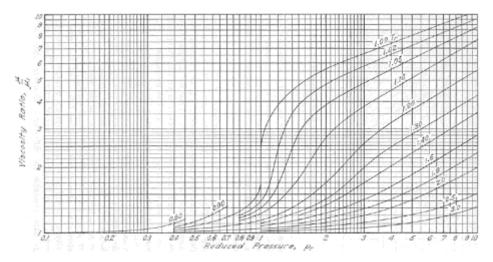


Figure 2-15. Viscosity ratio versus reduced pressure, after Comings et al. (1944)

Inevitably, Comings-Mayland-Egly correlation is good for pure gas. Its validity for natural gas is still questionable because there is no natural gas or gas mixtures viscosity in the database. The highest pressure and temperature for methane viscosity are 2514 psia 203 °F, respectively. As a result, no data at high pressure and temperature is available to support its validity for gas viscosity in HPHT reservoir. Comings also indicated that the correlation gives 10-12% error for ethane viscosity at reduced pressure higher than 2.0.

Table 2-6. Viscosity-temperature-pressure data used for Comings-Mayland-Egly (1940, 1944) correlation

Composition	Investigators	Pressure	Temperature
		psia	°F
CO <sub>2</sub>	Comings, Mayland, and Egly	65-2013	104
$CO_2$	Phillips	14.7-1646	68-104
$CO_2$	Schroer and Becker	14.7-860	86.5
$CO_2$	Stakelbeck	73-1763.5	14-104
C <sub>2</sub> H <sub>4</sub>	Comings, Mayland, and Egly	64.6-2013	104
C <sub>2</sub> H <sub>4</sub>	Comings, Mayland, and Egly	74.6-2513	86-203
CH <sub>4</sub>	Comings, Mayland, and Egly	64.6-2513	86-203
$N_2$	Michels and Gilbson	161-14196	77-167
C <sub>3</sub> H <sub>8</sub>	Comings, Mayland, and Egly	64.6-614.3	86-220
$C_3H_8$	Sage and Lacey	701-999	160-220
$C_3H_8$	Smith and Brown	999-4996.6	203-374
C <sub>2</sub> H <sub>6</sub>	Smith and Brown	749.5-4996.6	59-167
n-butane	Sage and Lacey	Vapor pressure- 2000	100-220
i-butane	Sage and Lacey	Vapor pressure- 2000	100-220
NH <sub>3</sub>	Stakelbeck	14.7-323	-4-176
Steam	Hawkins and Solberg	14.7-4000	640-761
Steam	Sigwart	14.74	714

### 2.3.2 Smith-Brown Correlation (1943)

Smith and Brown (1943) estimated fluid viscosity using theorem of corresponding states. The theory of corresponding states is based on the concept that the physics properties of different substances exhibit a similar behavior at the same values of reduced temperature and pressure. The theory is not rigorous, but it usually gives a good approximation with a minimum of effort. Smith and Brown believed theorem of corresponding states can provide a relationship between  $\eta/\sqrt{M}$  and reduced pressure

for paraffins, where  $\eta$  is viscosity and M is molecular weight. Since few experimental data is available, Smith and Brown built a rolling ball viscometer to determine the viscosities of ethane and propane in the range 100 to 5000 psia and 150 to 200 °C. Basing on viscosity of methane, ethane, propane, butane, pentane, hexane, octane, decane and bicomponent mixtures (Table 2-7), a graphical correlation as shown in Figure 2-16 was constructed.

Table 2-7. Viscosity-temperature-pressure data used for Smith-Brown (1943) correlation

Composition	Investigators	Pressure	Temperature °F	
		ps1a	F	
CH <sub>4</sub>	Sage and Lacey	701-999	160-220	
$C_2H_6$	Smith and Brown	749.5-4996.6	59-167	
$C_3H_8$	Smith and Brown	999-4996.6	203-374	
$C_3H_8$	Sage and Lacey	<2000	100-220	
n-Butane	Sage and Lacey	Vapor pressure- 2000	100-220	
i-Butane	Sage and Lacey	Vapor pressure- 2000	100-220	
n-Pentane	Hubbard and Brown	1000	77-482	
n-Pentane	Bridgman	<171000	86-167	
i-Butane	Bridgman	<171000	86-167	
n-Hexane	Bridgman	<171000	86-167	
n-Octane	Bridgman	<142000	86-167	
n-Decane	Dow	<85000	86-167	
n-Hexane-n- Decane mixtures	Dow	<57000	86-167	
$C_2H_6$ - $C_{12}H_{26}$	Evans	unknown	32-212	

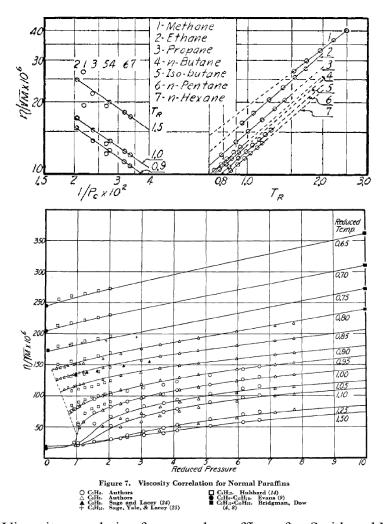


Figure 2-16. Viscosity correlation for normal paraffins, after Smith and Brown (1943)

Smith-Brown correlation is not applicable for methane as shown in Figure 2-16 (*top*). Smith verified that it is a very good approximation for ethane and higher paraffins viscosity. This correlation gives better estimation on liquids than gases.

# 2.3.3 Bicher-Katz Correlation (1943)

With a rolling ball viscometer Bicher-Katz (1943) correlation expanded Smith-Brown database through measuring methane, propane, and methane-propane mixture viscosity at pressure from 400-5000 psia and temperature from 77 to 437 °F, which covered a

larger temperature range comparing with Smith and Brown data. In their database they also included the viscosity of natural gas from Berwald and Johnson (1933) and Sage and Lacey (1938) (Table 2-8). For gas viscosity at high temperature Bicher and Katz inserted a coefficient K into  $\eta/\sqrt{M}$  to adjusted deviation from ideal gas behavior (Figure 2-17).

Table 2-8. Viscosity-temperature-pressure data used for Bicher-Katz (1943) correlation

Composition	Investigators	Pressure psia	Temperature °F	
CH <sub>4</sub>	Sage and Lacey	701-999	160-220	
$C_2H_6$	Smith and Brown	749.5-4996.6	59-167	
C <sub>3</sub> H <sub>8</sub>	Smith and Brown	999-4996.6	203-374	
$C_3H_8$	Sage and Lacey	<2000	100-220	
n-Butane	Sage and Lacey	Vapor pressure-2000	100-220	
i-Butane	Sage and Lacey	Vapor pressure-2000	100-220	
n-Pentane	Hubbard and Brown	1000	77-482	
n-Pentane	Bridgman	<171000	86-167	
i-Butane	Bridgman	<171000	86-167	
n-Hexane	Bridgman	<171000	86-167	
n-Octane	Bridgman	<142000	86-167	
n-Decane	Dow	<85000	86-167	
n-Hexane-n- Decane mixture	Dow	<57000	86-167	
2 natural gases	Sage and Lacey	<2600	100-220	
25 Natural gases	Berwald and Johnson	<500	60	
CH <sub>4</sub>	Bicher and Katz	400-5000	77-437	
C <sub>3</sub> H <sub>8</sub>	Bicher and Katz	400-5000	77-437	
Methane- Propane mixtures	Bicher and Katz	400-5000	77-437	

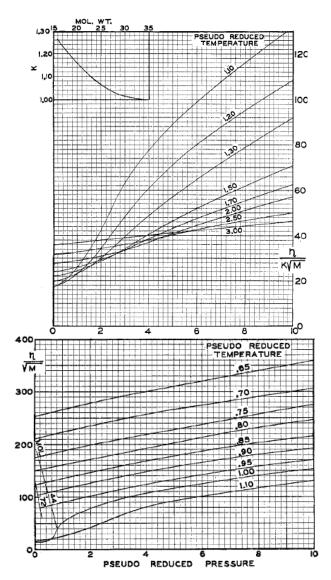


Figure 2-17. Viscosity of paraffin hydrocarbons at high-reduced temperatures (*top*) and at low-reduced temperatures (*bottom*), after Bicher and Katz (1943)

## 2.3.4 Carr-Kobayashi-Burrrow Correlation (1954)

Carr-Kobayashi-Burrrow (1954) correlation inherited the spirit of Comings-Mayland-Egly correlation. It is an upgraded version of Comings-Mayland-Egly correlation. It includes two steps to estimate natural gas viscosity. First we need to get the gas viscosity at atmospheric conditions. Equations 2.47 through 2.51 are used to calculate gas

viscosity at this condition. Once viscosity at atmospheric conditions is available, it is calibrated to reservoir conditions, or reservoir pressure and temperature conditions, by applying charts or correlation. Figures 2-18 and 2-19 are used to calibrate viscosity at atmospheric conditions to reservoir conditions. In the calibration, the concepts of pseudoreduced pressure and pseudoreduced temperature are applied. Gas viscosity ratio,  $\mu_g/\mu_{1\text{atm}}$ , is estimated from these curves. Using gas viscosity ratio and gas viscosity at atmospheric conditions, gas viscosity at reservoir conditions can be calculated.

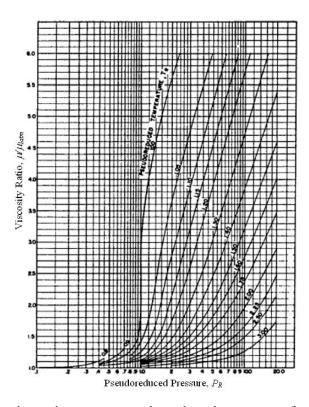


Figure 2-18. Viscosity ratio versus pseudo-reduced pressure, after Carr et al. (1954)

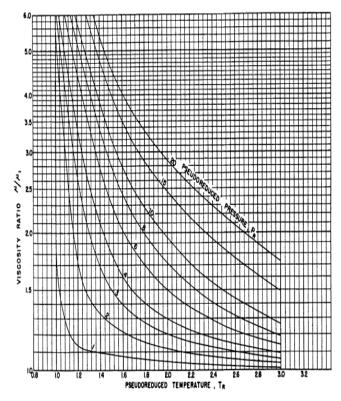


Figure 2-19. Viscosity ratio versus pseudo-reduced temperature, after Carr et al. (1954)

$$\mu_{1atm} = (\mu_{1atm} \text{ uncorrected}) + (N_2 \text{ correction}) 
+ (CO_2 \text{ correction}) + (H_2 S \text{ correction})$$
(2.47)

$$\mu_{1atm} \text{ uncorrected} = (1.709 \times 10^{-5} - 2.062 \times 10^{-6} \gamma_g) T + 8.188 \times 10^{-3} - 6.15 \times 10^{-3} \log \gamma_g$$
(2.48)

$$N_2 \text{ correction} = y_{N_2} \left[ (8.48 \times 10^{-3}) \log \gamma_g + 9.59 \times 10^{-3} \right]$$
 (2.49)

$$CO_2 \text{ correction} = y_{CO_2} \left[ (9.08 \times 10^{-3}) \log \gamma_g + 6.24 \times 10^{-3} \right] (2.50)$$

$$H_2 S$$
 correction =  $y_{H_2 S} \left[ (8.49 \times 10^{-3}) \log \gamma_g + 3.73 \times 10^{-3} \right]$ . (2.51)

where

 $\mu_{1atm}$  = Gas viscosity at 1 atm, cp

 $\gamma_g$  = Gas specific gravity (air=1)

 $y_{N_2,CO_2,H,S}$  = Mole fraction of the non-hydrocarbon component

 $T = \text{Temperature}, \, ^{\text{o}}\text{F}$ 

The advantage of Carr-Kobayashi-Burrrow correlation is that it could correct the effect of non-hydrocarbons, which affect the natural gas viscosity significantly. It also gives 1.50 percent absolute error for the gas viscosity according to Carr's report.

Carr-Kobayashi-Burrrow correlation based on the measurement of pure components such as nitrogen, carbon dioxide, methane, ethylene, propane, simulated mixture samples, and natural gas. Table 2-9 lists the fluid sample and measuring pressure temperature range of the experimental data used to develop this correlation. It is observed that this correlation based on limited pressure and temperature range. Therefore its application in HPHT is not yet to be proved by more extensive lab data at HPHT.

Table 2-9. Viscosity-temperature-pressure data used for Carr-Kobayashi-Burrrow (1954) correlation

Composition	Investigators	Pressure	Temperature	Memo			
		psia	°F				
CH <sub>4</sub>	Comings, Mayland, and Egly	64.6-2513	86-203				
CH <sub>4</sub>	Bicher and Katz	14.7-500	77-437				
CH <sub>4</sub>	Carr, Kobayashi, and Burrrow	14.7-8030	71-200				
N <sub>2</sub>	Michels and Gilbson	161-14196	77-167				
N <sub>2</sub> -0.6, CH <sub>4</sub> -73.4, C <sub>2</sub> H <sub>6</sub> -25.6, C <sub>3</sub> H <sub>6</sub> -0.2, C <sub>3</sub> H <sub>8</sub> -0.2	Carr, Kobayashi, and Burrrow	14.7-10030	77.7-150.2	Simulated high ethane content gas			
He-0.8, N <sub>2</sub> -15.8, CH <sub>4</sub> -73.1, C <sub>2</sub> H <sub>6</sub> -6.1, C <sub>3</sub> H <sub>8</sub> -3.4, i-C <sub>4</sub> H <sub>10</sub> -0.2, n-C <sub>4</sub> H <sub>10</sub> -0.6	Carr, Kobayashi, and Burrrow	14.7-9580	79.7-150.4	High nitrogen content natural gas			
N <sub>2</sub> -0.3, CH <sub>4</sub> -95.6, C <sub>2</sub> H <sub>6</sub> - 3.6, C <sub>3</sub> H <sub>8</sub> -0.5	Carr, Kobayashi, and Burrrow	14.7-8465	85.1-220	Simulated low ethane content gas			
C <sub>2</sub> H <sub>4</sub>	Comings, Mayland, and Egly	74.6-2513	86-203				
C <sub>2</sub> H <sub>4</sub>	Gonikberg	<2500	75-158				
CO <sub>2</sub>	Golubev	<2500	122-212				
CO <sub>2</sub>	Comings, Mayland, and Egly	65-2013	104				
CO <sub>2</sub>	Phillips	14.7-1764	68-104				
C <sub>3</sub> H <sub>8</sub>	Comings, Mayland, and Egly	64.6-614.3	86-220				
Note: Composition is in mole percent							

Another inconvenience of Carr et al. correlation comes from the use of chart to get gas viscosity at interested point. As the advance of computer and more accurate calculations can be achieved by computer program, correlations are more desirable since computer program will calculate the viscosity through correlation but not charts or figures. Dempsey (1965) developed following correlation to replace Figures 2-18 and 2-19.

$$\ln \left[ T_{pr} \left( \frac{\mu_g}{\mu_{1atm}} \right) \right] = a_0 + a_1 p_{pr} + a_2 p_{pr}^2 + a_3 p_{pr}^3 
+ T_{pr} \left( a_4 + a_5 p_{pr} + a_6 p_{pr}^2 + a_7 p_{pr}^3 \right) 
+ T_{pr}^2 \left( a_8 + a_9 p_{pr} + a_{10} p_{pr}^2 + a_{11} p_{pr}^3 \right) 
+ T_{pr}^3 \left( a_{12} + a_{13} p_{pr} + a_{14} p_{pr}^2 + a_{15} p_{pr}^3 \right)$$
(2.52)

where

 $T_{pr}$  = Pseudo-reduced temperature,

 $p_{pr}$  = Pseudo-reduced pressure,

 $a_0$ - $a_{15}$  = Coefficients of the equation, which are

$a_0 = -2.46211820$	$a_6 = 0.360373020$	$a_{11} = 0.00441015512$
$a_1 = 2.97054714$	$a_7 = -0.01044324$	$a_{12} = 0.0839387178$
$a_2 = -0.28626405$	$a_8 = -0.793385684$	$a_{13} = -0.186408848$
$a_3 = 0.008054205$	$a_9 = 1.39643306$	$a_{14} = 0.0203367881$
$a_4 = 2.80860949$	$a_{10} = -0.149144925$	$a_{15} = -0.000609579263$
$a_5 = -3.49803305$		

#### 2.3.5 Jossi-Stiel-Thodos Correlation (1962)

Basing upon the experimental data of pure components including argon, nitrogen, oxygen, carbon dioxide, sulfur dioxide, methane, ethane, propane, *i*-butane, *n*-butane, and *n*-pentane (Table 2-10), Jossi et al. (1962) developed a correlation for the viscosity of gas mixtures. The relationship between the residual viscosity modulus  $(\mu_g - \mu^*)\xi$  and reduced density  $\rho_r$  is the cornerstone for Jossi-Stiel-Thodos correlation. The critical properties of the gas such as critical pressure, temperature, and density, interested pressure temperature, and the molecular weight are as inputs. Jossi-Stiel-Thodos correlation for normally behaving substances is expressed as follow:

$$\left[ \left( \mu_g - \mu^* \right) \xi + 10^{-4} \right]^{\frac{1}{4}} = 0.1023 + 0.023364 \rho_r$$

$$+ 0.058533 \rho_r^2 - 0.0400758 \rho_r^3 + 0.009332 \rho_r^4$$
(2.53)

where

$$\rho_r = \frac{\rho_g}{\rho_c} \tag{2.54}$$

$$\xi = \frac{T_c \frac{1}{6}}{M_w^2 p_c^2 \frac{2}{3}} \tag{2.55}$$

$$\mu^* = \frac{3.40 \times 10^{-4} T_r^{0.94}}{\xi} \quad \text{for } T_r \le 1.50$$
 (2.56)

$$\mu^* = \frac{1.778 \times 10^{-4} \left(4.58T_r - 1.67\right)^{5/8}}{\xi} \text{ for } T_r > 1.50$$
 (2.57)

where

 $\rho_c$  = Critical density, g/cc

 $\rho_g$  = Gas density, g/cc

 $\rho_r$  = Reduced density

 $T_c$  = Critical temperature,  ${}^{\rm o}{\rm K}$ 

 $T_r$  = Reduced temperature,  ${}^{\circ}K$ 

 $p_c$  = Critical pressure, atm

 $M_w$  = Molecular weight

 $\mu_g$  = Gas viscosity, cp

 $\mu^*$  = Gas viscosity at low pressures (1.47-73.5 psia), cp

Figures 2-20 and 2-21 compared the correlation with the experimental data for both normal behaving substances and substances investigated by Jossi.

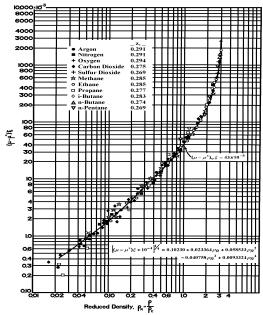


Figure 2-20. Relationship between the residual viscosity modulus  $(\mu_g - \mu^*)\xi$  and reduced density  $\rho_r$  for normally behaving substances, after Jossi et al. (1962)

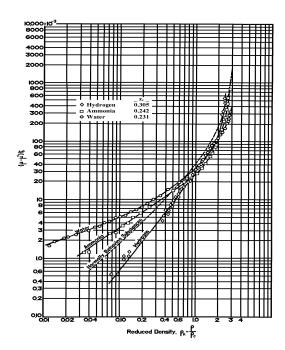


Figure 2-21. Relationship between the residual viscosity modulus  $(\mu_g - \mu^*)\xi$  and reduced density  $\rho_r$  for the substances investigated, after Jossi et al. (1962)

Jossi-Stiel-Thodos correlation relied on pure substances. It may not be suitable for gas mixture. Its database covered methane viscosity data from Comings et al. (1940 and 1944), Baron et al. (1959), Swift et al. (1959), and Kuss (1952), which are in low to moderate pressure and temperature. Jossi reported approximately 4 percent average absolute error and also stated that this correlation should only be applied for values of reduced density below 2.0. We cannot endorse this correlation for HPHT condition before we have data to proof it.

Table 2-10. Viscosity-temperature-pressure data used for Jossi-Stiel-Thodos (1962) correlation

Composition	Investigators	Pressure	Temperature
	_	psia	°F
Hydrogen	Gibson	323-1822	-330-(-321)
Hydrogen	Golubev	14.7-11760	-432-482
Hydrogen	Johns	14.7-1458	116-260
Hydrogen	Michels	294-44100	32-302
Hydrogen	Schaefer	<184875	-434-932
Hydrogen	van Itterbeek	220-12348	-343-(-298)
Argon	Iwasaki	14.7-735	68-86
Argon	Kiyama	14.7-1470	122-572
Argon	Michels	<29392	32-167
Argon	Rudenko	14.7	freezing point- boiling point
Nitrogen	Iwasaki	291-2770	76-301
Nitrogen	Michels	161-14196	77-167
Nitrogen	Rudenko	14.2-356	-333-(-297)
Nitrogen	Shubnikov	14.2-356	-333-(-297)
Oxygen	Galkov	17.7-356	-290-(-260)
Oxygen	Gibson	323-1822	-330-(-321)
Oxygen	Rudenko	14.2-356	-321-(-297)
Oxygen	van Itterbeek	4.2-356	-321-(-297)
Carbon Dioxide	Michels	<29392	32-167
Carbon Dioxide	Kiyama	14.7-1470	122-572
Carbon Dioxide	Michels	14.7-29400	32-167
Carbon Dioxide	Stakelbeck	14.7-294	-20-80

Table 2-10. Continued

Composition	Investigators	Pressure psia	Temperature °F	
Sulfur dioxide	Awberry	< vapor pressure	5-86	
Sulfur dioxide	Stakelbeck	14.7-294	<104	
Ammonia	Carmichael	17-5915	100-400	
Ammonia	Kiyama	14.7-1470	122-572	
Ammonia	Shimotake	250-5000	212-392	
Ammonia	Stakelbeck	14.7-294	-20-80	
Water	Hawkins	14.7-2800	550-850	
Water	Richter	normal pressure	<572	
Water	Schille	normal pressure	282-1000	
Water	Shugayev	normal pressure	282-1410	
Water	Sigwart	normal pressure	282-1000	
Water	Timroth	14.2-2845	482-842	
Methane	Baron	114.7-8014.7	125-275	
	Comings, Mayland,			
Methane	and Egly	64.6-2513	86-203	
Methane	Kuss	<8820	68-176	
Methane	Swift	85-675	-220-(-115.6)	
Ethane	Baron	114.7-8014.7	125-275	
Ethane	Smith and Brown	749.5-4996.6	59-167	
Ethane	Swift	25-716	-112-89.6	
Propane	Baron	114.7-8014.7	125-275	
_	Comings, Mayland,			
Propane	and Egly	64.6-614.3	86-220	
Propane	Lipkin	<140	-100-100	
Propane	Sage and Lacey	<2000	100-220	
Propane	Smith and Brown	999-4996.6	203-374	
Propane	Swift	50-620	-22-206	
i-Butane	Lipkin	<140	-100-100	
i-Butane	Sage and Lacey	<2000	100-220	
n-Butane	Lipkin	<140	-100-100	
n-Butane	Sage and Lacey	<2000	100-220	
n-Butane	Swift	45-250	68-212	
n-Pentane	Lohrenz	10000	253-286	
n-Pentane	Reamer and Sage	15.7-5000	100-280	

### 2.3.6 Lee-Gonzalez-Eakin Correlation (1970)

To honor natural gas in petroleum engineering and develop a gas viscosity correlation, Gonzalez et al. (1970) measured viscosities of eight natural gases for temperature from 100 to 340 oF and pressure from 14.7 to 8000 psia. Combining with some pure components such as methane, ethane, and propane (Table 2-11), Gonzalez et al. (1970) derived a correlation that is simpler than Carr-Kobayashi-Burrrow correlation to predict gas viscosity at reservoir conditions. The inputs required in Lee-Gonzalez-Eakin correlation are gas density, molecular weight of gas, and temperature. Equations 2.58 through 2.61 are used to get gas viscosity provided molecular and density at interested condition known.

$$\mu_g = 10^{-4} K \exp(X \rho_g^Y).$$
 (2.58)

$$K = \frac{(9.379 + 0.01607M_w)T^{1.5}}{209.2 + 19.26M_w + T}.$$
(2.59)

where

$$X = 3.448 + \left\lceil \frac{986.4}{T} \right\rceil + 0.01009 M_w. \tag{2.60}$$

$$Y = 2.447 - 0.2224X. (2.61)$$

where

 $\mu_g = \text{Gas viscosity, cp}$ 

 $\rho_g$  = Gas density, g/cc

 $M_W$ = Molecular weight

 $T = \text{Temperature}, {}^{\text{o}}\text{R}$ 

Table 2-11. Viscosity-temperature-pressure data used for Lee-Gonzalez-Eakin (1970) correlation

Composition	Investigators	Pressure psia	Temperature °F	Memo	
Methane	Gonzalez, Bukacek and Lee	200-8000	100-340		
Methane	Carr, Kobayashi, and Burrrow	14.7-8030	71-200		
Ethane	Eakin, Starling and Dolan	200-8000	77-340		
Propane	Starling, Eakin and Ellington	100-8000	77-280		
n-Butane	Dolan, Starling and Lee	1000-8000	100-340		
i-Butane	Gonzalez and Lee	100-8000	100-340		
n-Pentane	Lee and Ellington	2000-3000	100-340		
n-Decane	Lee and Ellington	200-8000	100-340		
2,2- Dimethylpropane	Gonzalez and Lee	100-8000	100-340		
Methane- propane mixtures	Gidding	14.7-8000	100-280		
Methane- <i>n</i> -Butane mixtures	Dolan, Ellington and Lee	200-8000	100-340		
Methane- <i>n</i> -Decane mixtures	Lee, Gonzalez and Eakin	Bubble point-7000	100-340		
N <sub>2</sub> -0.6, CH <sub>4</sub> - 73.4, C <sub>2</sub> H <sub>6</sub> -25.6, C <sub>3</sub> H <sub>6</sub> -0.2, C <sub>3</sub> H <sub>8</sub> - 0.2	Carr, Kobayashi, and Burrrow	14.7- 10030	77.7-150.2	Simulated high ethane content gas	
He-0.8, N <sub>2</sub> -15.8, CH <sub>4</sub> -73.1, C <sub>2</sub> H <sub>6</sub> - 6.1, C <sub>3</sub> H <sub>8</sub> -3.4, i-C <sub>4</sub> H <sub>10</sub> -0.2, n- C <sub>4</sub> H <sub>10</sub> -0.6	Carr, Kobayashi, and Burrrow	14.7-9580	79.7-150.4	High nitrogen content natural gas	
N <sub>2</sub> -0.3, CH <sub>4</sub> - 95.6, C <sub>2</sub> H <sub>6</sub> -3.6, C <sub>3</sub> H <sub>8</sub> -0.5	Carr, Kobayashi, and Burrrow	14.7-8465	85.1-220	Simulated low ethane content gas	
Eight natural gases			100-340	Compositions are in Table 2-12	

Table 2-12. Composition of eight natural gas samples (Gonzalez et al., 1970)

Sample No.	1	2	3	4	5	6	7	8
N2	0.21	5.2	0.55	0.04	-	0.67	4.8	1.4
CO2	0.23	0.19	1.7	2.04	3.2	0.64	0.9	1.4
Не	-	-	ı	-	-	0.05	0.03	0.03
C1	97.8	92.9	91.5	88.22	86.3	80.9	80.7	71.7
C2	0.95	0.94	3.1	5.08	6.8	9.9	8.7	14
C3	0.42	0.48	1.4	2.48	2.4	4.6	2.9	8.3
nC4	0.23	0.18	0.5	0.58	0.48	1.35	1.7	1.9
iC4	-	0.01	0.67	0.87	0.43	0.76	-	0.77
C5	0.09	0.06	0.28	0.41	0.22	0.6	0.13	0.39
C6	0.06	0.06	0.26	0.15	0.1	0.39	0.06	0.09
C7+	0.03	-	0.08	0.13	0.04	0.11	0.03	0.01
Total	100.0	100.0	100.0	100.0	100.0	100.0	100.0	100.0
Note: Composition is in mole percent								

In deriving this correlation, recommended viscosity values are based on smoothed plots of viscosity versus temperature, viscosity versus pressure. Lee-Gonzalez-Eakin correlation gives 2.0 percent average absolute error at low pressure and 4 percent at high pressure. It provides better result if gas specific gravity is less than 1.0. The correlation can be used to forecast gas viscosity at temperature from 100 to 340 °F and pressure from 100 to 8000 psi, according to Lee.

One of disadvantages of Lee-Gonzalez-Eakin correlation is that it uses density, molecular weight, and temperature as input variables to calculate natural gas viscosity. Petroleum engineers prefer pressure to density when they estimate gas viscosity in routine work because most of time pressure is easy to get instead of density.

Another disadvantage is this correlation does not consider natural gas that contains high percentage of non-hydrocarbon. We used nitrogen to test the validity of Lee-Gonzalez-Eakin correlation in predicting non-hydrocarbons viscosity. As our expected, it ended up with the conclusion that this correlation is unable to forecast non-hydrocarbons viscosity. Lab experiment in nitrogen viscosity illustrates that this correlation is

inappropriate for nitrogen. This will be shown in our result. In reality, non-hydrocarbons such as nitrogen, carbon dioxide, and hydrogen sulfide are often found in natural gas. As wells become deeper and deeper, more and more non-hydrocarbons are found in the gas reservoir, some reservoirs even have up to 50-60 percent of non-hydrocarbons. Gas reservoirs in South China Sea contain 55-60 volume percent of carbon dioxide and hydrogen sulfide. Sour gas reservoirs in East China Sea are discovered with 20-30 volume percent carbon dioxide. Development and production of sour gas require a correlation that can remove the effect of these non-hydrocarbons.

Lee-Gonzalez-Eakin correlation covers a relatively short pressure range. Its application in high pressure, i.e. greater than 10000 psi is still uncertain. Now more and more reservoirs discovered are deep and under high pressure and high temperature, and the major component of the reservoir fluids is methane. Therefore, a model that predicts methane viscosity at high pressure and temperature is desirable.

## 2.3.7 NIST Program

The National Institute of Standard and Technology (NIST) (2000) provides a program, NIST reference fluid thermodynamic and transport properties-REFPROP (Lemmon, 2007), version 8.0, through which thermodynamic and transport properties of hydrocarbon can be estimated. Not only pure components, but also mixtures containing up to 20 components can be input into the program to get their thermodynamic properties. The range of the pressure and temperature are up to 44100 psi and 1340 °F, respectively. In REFPROP, viscosity and is modeled with either an extended corresponding states method, or in some cases the friction theory method. Gas viscosity can be obtained from this program, but one thing needed to be aware is that the program predicts the fluid properties using correlation developed at low-moderate pressure and temperature. The correlations were based on the lab data collected from literatures. Comparing densities of methane and nitrogen from NIST program with lab data from

literatures (Boyd, 1930; Bicher and Katz, 1943; Carr, 1952; Iwasaki, 1954; Ellis and Raw, 1959; Golubev, 1959; Swift et al., 1959; Barua et al., 1964; Wilson, 1965; Dipippo et al., 1966; Lee et al., 1966; Gonzalez et al., 1966; Van Itterbeek et al., 1966; Helleman et al., 1970; Latto and Saunders, 1972; Stephan and Lucas, 1979; Diller, 1980; Diller, 1983; Straty and Diller, 1980; Setzmann and Wagner, 1991; Nowak et al., 1997a; Nowak et al., 1997b; Klimeck et al., 1998) indicates that differences are so small thus can be neglected (Figures 2-22 and 2-23). It is also noted that density data covers low to high pressure and temperature. Pressure range for methane and nitrogen densities are 3.6 to 72518 and 14.7 to 7350 psia, respectively. Temperature range for methane and nitrogen densities are 8.3 to 656.3 and 32 to 476.3 °F, respectively. As a result, these available density data can be used to derive our new gas viscosity correlation at low to high pressure and temperature. Comparing viscosities of methane and nitrogen from NIST program with lab data from literatures (Earhart, 1916; Boyd, 1930; Bicher and Katz, 1943; Comings et al., 1944; Van Itterbeek et al., 1947; Carr, 1952; Iwasaki, 1954; Ross and Brown, 1957; Ellis and Raw, 1959; Kestin and Leidenfrost, 1959; Swift et al., 1959; Golubev, 1959; Swift et al., 1959; Flynn et al., 1963; Barua et al., 1964; Wilson, 1965; Dipippo et al., 1966; Lee et al., 1966; Gonzalez et al., 1966; Van Itterbeek et al., 1966; Helleman et al., 1970; Diehl et al., 1970; Latto and Saunders, 1972; Stephan and Lucas, 1979; Diller, 1980; Diller, 1983) indicates differences are so small thus can be neglected (Figures 2-22 and 2-23). Pressure range for methane and nitrogen viscosities are 14.7 to 11757 and 14.5 to 14504 psia, respectively. Temperature range for methane and nitrogen viscosities are 77 to 482 and -342.7 to 1880 °F, respectively. As a result, these available density and viscosity data can be used to derive our new gas viscosity correlation. As more and more studies are conducted on gas viscosity at high pressure and high temperature, the validity of extrapolating correlations that are derived from low-moderate pressure and temperature condition to predict gas viscosity at high pressure and high temperature is doubted. NIST indicates that they will update their database as more data available.

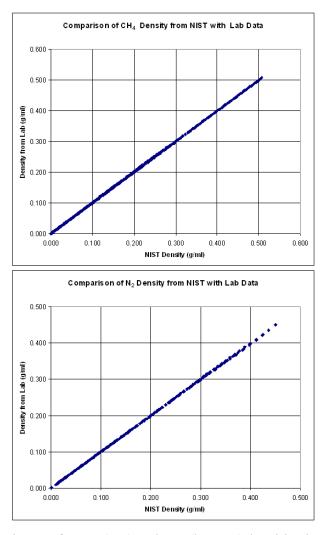


Figure 2-22. Comparisons of CH4 (top) and N2 (bottom) densities between NIST values and lab data

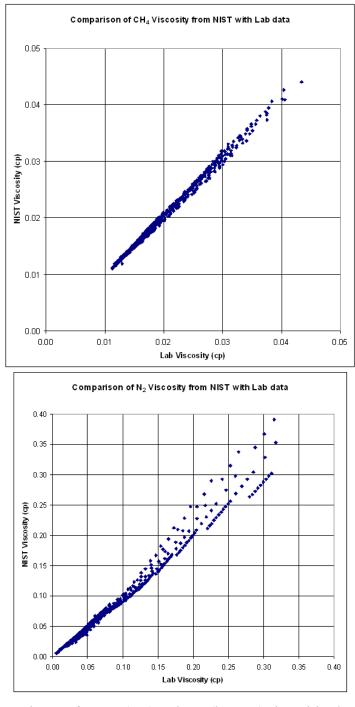


Figure 2-23. Comparisons of CH4 (top) and N2 (bottom) viscosities between NIST value and lab data

#### 2.3.8 Londono Correlations (2001)

Londono (2001) collected a total of 13656 data points from former investigators to optimize Jossi-Stiel-Thodos and Lee-Gonzalez-Eakin gas viscosity correlations and Dranchuk-Abou-Kassem and Nishimi-Saito gas density correlations. Londono indicated that these data points have properties such as composition, viscosity, density, temperature, pressure, pseudoreduced properties, and gas compressibility factor from hydrocarbon and non-hydrocarbon. He used this database to evaluate the applicability of the existing models to determine hydrocarbon gas viscosity and density (or gas z-factor, then calculate gas density using EOS). In addition, he developed new models/calculation approaches to determine hydrocarbon viscosity and provided an optimization of the existing equations-of-state (EOS) for the calculation of the gas z-factor. In brief, Londono modified existing correlations' coefficients or constants basing on his database with nonlinear least-square statistical method, while kept the original forms unchanged. The optimized Jossi-Stiel-Thodos correlation is

$$[(\mu_g - \mu^*)\xi + 10^{-4}]^{\frac{1}{4}} = 0.170018 + 0.990675\rho_r$$

$$-0.407490\rho_r^2 - 0.066959\rho_r^3 + 0.007359\rho_r^4$$
(2.62)

where

$$\rho_r = \frac{\rho_g}{\rho_c} \tag{2.63}$$

$$\xi = \frac{T_c^{4.76271}}{M_w^{3.83480} p_c^{2.72582}}$$
 (2.64)

where

 $\rho_c$  = Critical density, g/cc

 $\rho_g$  = Gas density, g/cc

 $\rho_r$  = Reduced density

 $T_c$  = Critical temperature,  ${}^{\rm o}{\rm K}$ 

 $p_c$  = Critical pressure, atm

 $M_w$  = Molecular weight

 $\mu_g$  = Gas viscosity, cp

 $\mu^*$  = Gas viscosity at low pressures (1.47-73.5 psia), cp

 $\xi$  = Viscosity parameter

The optimized Lee-Gonzalez-Eakin correlation is

$$\mu_{g} = 10^{-4} K \exp(X \rho_{g}^{Y}). \tag{2.65}$$

$$K = \frac{(19.9216 + 0.0326212M_w)T^{1.38392}}{210.076 + 18.5762M_w + T}.$$
 (2.66)

where

$$X = 3.84699 + \left\lceil \frac{991.303}{T} \right\rceil + 0.00924455 M_w. \tag{2.67}$$

$$Y = 2.11068 - 0.136279X. (2.68)$$

where

 $\mu_g = \text{Gas viscosity, cp}$ 

 $\rho_g$  = Gas density, g/cc

 $M_W$ = Molecular weight

 $T = \text{Temperature}, {}^{\circ}\text{R}$ 

It is obvious that Londono optimized existing gas viscosity and density correlations (or gas z-factor, then calculate gas density using EOS) and developed new gas viscosity and density correlations all basing on his collected database. He did not perform experiment by himself, thus no new data were added to the database. A review of his database showed that the highest pressures for hydrocarbons/natural gas and nonhydrocarbons (N<sub>2</sub>, CO<sub>2</sub>) viscosity data are 11760 and 14708 psia, respectively. It should be noted that correlation is only as good as experimental data it based on. Therefore, we can conclude that the uncertainty of Londono correlations at HPHT still exists.

#### 2.3.9 Sutton Correlation (2005)

Sutton (2005) collected 5881 data points of gas viscosity data done by Gonzalez et al. (1970), Knapstad et al. (1990), Canet et al. (2002), Audonnet and Padua (2004), and Elsharkawy (2004) to developed a correlation. His database consists of viscosity data for methane, propane, methane-propane, methane-butane, methane-n-decane and natural gas viscosity. The methane-decane binary mixtures also used to estimate the behavior of a gas condensate that has a large heptanes-plus component. The database in which the correlation is based upon does not include the pure methane viscosities data above 10,000 psi, therefore Sutton correlation is not proved to be suitable for HPHT gas reservoirs. Sutton correlation is as follow:

$$\mu_{gsc}\xi = 10^{-4} [0.807T_{pr}^{0.618} - 0.357 \exp(-0.449T_{pr}) + 0.340 \exp(-4.058T_{pr}) + 0.018]$$
(2.69)

$$\mu_{g} = \mu_{gsc} \exp\left(X\rho_{g}^{Y}\right). \tag{2.70}$$

where

$$\xi = 0.949 \left( \frac{T_{pc}}{Mw^3 p_{pc}^4} \right)^{\frac{1}{6}}.$$
 (2.71)

$$X = 3.47 + \left\lceil \frac{1.588}{T} \right\rceil + 0.0009 Mw. \tag{2.72}$$

$$Y = 1.66378 - 0.04679X. (2.73)$$

where

 $M_w = \text{Molecular weight}$ 

 $p_{pc}$  = Pseudocritical pressure, psia

 $T = \text{Temperature}, {}^{\text{o}}\text{R}$ 

 $T_{pc}$  = Pseudocritical temperature, °R

 $T_{pr}$  = Pseudoreduced temperature

 $\mu_{o}$  = Gas viscosity, cp

 $\mu_{gsc}$  = Low pressure gas viscosity, cp

 $\rho_g$  = Gas density, g/cc

 $\xi$  = Viscosity normalizing parameter

#### 2.3.10 Viswanathan Correlation (2007)

Viswanathan (2007) used a Cambridge Viscosity SPL440 viscometer to measure the viscosity of pure methane. He measured methane viscosity at temperature of 116, 152, 188, 224, and 260 °F and pressure from 4500 to 20000 psia. Using NIST values at temperatures of 100, 150, 200, 250, 300, 350, and 400 °F and pressure from 5000 to 30000 psia with interval of 1000 psia, Viswanathan modified Lee-Gonzalez-Eakin correlation as follows:

$$\mu_g = K \exp(X \rho_g^Y). \tag{2.74}$$

$$K = \frac{0.0001 * (5.0512 - 0.2888 M_w) T^{1.832}}{-443.8 + 12.9 M_w + T}.$$
 (2.75)

where

$$X = -6.1166 + \left\lceil \frac{3084.9437}{T} \right\rceil + 0.3938 M_w. \tag{2.76}$$

$$Y = 0.5893 - 0.1563X. (2.77)$$

where

 $\mu_g$  = Gas viscosity, cp

 $\rho_g$  = Gas density, g/cc

 $M_W$ = Molecular weight

 $T = \text{Temperature}, {}^{\text{o}}\text{R}$ 

Summary, no measured gas viscosity at high pressure and high temperature is available so far. Thus correlations derived from data obtaining at low-moderate pressure and temperature cannot be simply extrapolated to high pressure and high temperature

conditions. Experiments that measure gas viscosity at high pressure and high temperature must be conducted before we derived correlation that can predict gas viscosity accurately. As a result, a correlation covered both low and high pressure and temperature is highly recommended. But it needs measured data as its solid base.

#### **CHAPTER III**

### **OBJECTIVE**

Because a good correlation needs a wide range viscosity data as its cornerstone, the lack of methane and nitrogen viscosity at HPHT required we put enormous effort towards the viscosity of pure methane and nitrogen at HPHT. By adding methane and natural gas viscosity at high pressures and high temperatures, a new correlation can be derived to predict gas viscosity at HPHT.

Another fact needed to be addressed is that more nitrogen is found as we move to high pressure and high temperature reservoirs. High concentration nitrogen in natural gas affects not only the heat value of natural gas but also gas viscosity, which is critical to petroleum engineering. The importance of gas viscosity is seen in its contribution in the resistance to the flow of a fluid both in porous media and pipes during gas production and transportation. Nitrogen is also one of common inject gases in gas injection projects, thus an accurate estimation of its viscosity is vital to analyze reservoir performance. Due to lack of correlation for nitrogen viscosity and the fact that hydrocarbon viscosity correlation is inappropriate for nitrogen viscosity, a new correlation that is tailored for nitrogen viscosity will be derived based on our experimental data. It provides a good approach to get nitrogen viscosity at HPHT.

## **CHAPTER IV**

#### **METHODOLOGY**

## **4.1 Experiment Facility**

As mention before we need viscosity at HPHT to develop a new correlation through which accurate viscosity can be guaranteed. To fill the viscosity data we will put our effort in measuring gas viscosity at HPHT through appropriate facility. Falling-body principle is employed in setup our experimental facility. Dr. Teodoriu, Dr. McCain, Mr. Anup Viswanathan, and Mr. Frank Platt (Viswanathan, 2007; Viswanathan and McCain, 2005; Viswanathan et al., 2006) prepared and installed this delicate apparatus. The facility consists of gas source, gas booster system, temperature control system, measuring system, and data acquisition system. Figure 4-1 shows the setup of apparatus. Figure 4-2 illustrates the layout of facility. Following is a detail description of the facility.



Figure 4-1. The setup of apparatus for this study

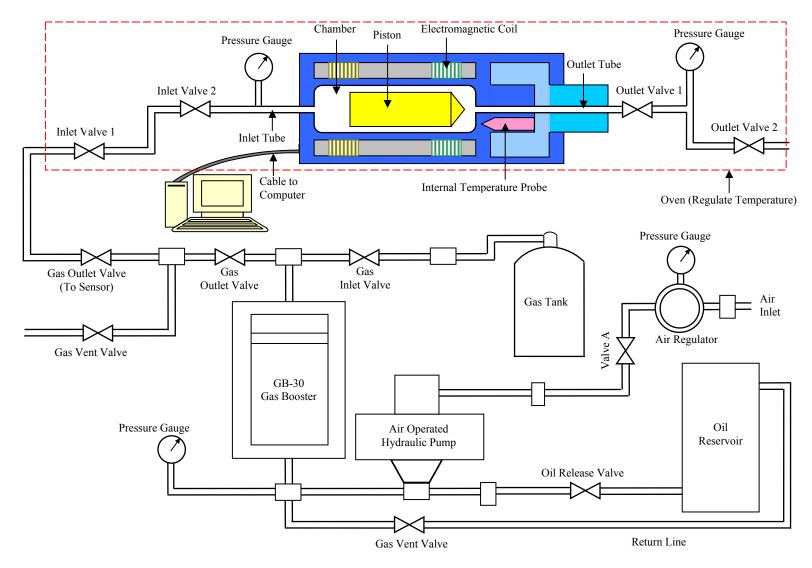


Figure 4-2. Schematic of experimental facility

#### 4.1.1 Gas Source

The gas we used for viscosity measurement is nitrogen, methane, and air. A gas tank that supplies low pressure gas is used as original source. Gas tank is connected to the inlet of gas booster system where gas is compressed to high pressure for measurement. Through gas booster system we can compress gas from 1000 psi to 25000 psi.

## **4.1.2** Gas Booster System

Since the gas tank cannot provide pressure required by experiment, a gas booster system was used to compress the gases to high pressures that match the requirement. The gas booster system is consisting of a hydraulic pump coupled with the gas booster cylinder to increase the pressure of a given gas sample. The gas booster system as used in this project was manufactured by High Pressure Equipment Company. It belongs to Model GBS-30 (Figure 4-3) which means it is rated for use up to 30,000 psi and has a one-to-one ratio. Displacement per stroke is 112 cubic inches (1835 ml). Model GBS-30 is complete and ready to operate. All that is required is an air supply for the pump and a commercially available container of compressed gas.



Figure 4-3. Gas booster system used to compress gas in this study

The gas booster system includes manual valves, air regulator, filter and lubricator, air gauge, high pressure gauge, reservoir, oil filter, pump, gas booster and related high pressure tubing and fittings. The two major parts are air operated hydraulic pump which uses house air at a pressure of 70 psia to pump hydraulic oil out of the oil reservoir and the gas booster cylinder which contains a piston to separate the oil and the gas.

Operation is by means of an air operated hydraulic pump which pressurizes one end of the gas booster which then compresses the gas in the opposite end of the booster. To accomplish this, the gas inlet valve is opened to permit gas to fill the gas end of the booster. Check valves are provided to permit gas flow in one direction only. With the gas outlet valve open, the hydraulic pump is operated in order to pressurize the hydraulic end of the booster. Thus, the gas is compressed in the booster. If required pressure is not reached by the end of the stroke, the gas booster can easily be recycled for additional strokes. Note the gauge on these systems is connected to the hydraulic side of the booster. On the Model GBS-30 which has a 1 to 1 ratio, there is a direct reading of the pressure in the gas end of the booster.

There are some drawbacks with the proto gas booster system. One of them is that the rate of release of high pressure gas from the system is hard to be regulated, whereas the gas outlet valve supplied is inadequate for this measure of control. Another difficulty is the rate of release of oil from the gas booster cylinder cannot be controlled accurately. An excessively rapid drop in pressure can cause the o-rings in the gas booster cylinder to disintegrate and this can have dangerous implications. In order to improve the system to be more efficient and safe, some changes were made to the gas booster system in the laboratory. An extra pressure transducer was attached to the gas line since the main pressure gauge on the gas booster system was connected to the oil line and this only approximately described the true gas pressure. A couple of micro-tip controlled valves were installed to help in carefully regulating the high pressure gas, and the vented oil.

Followings are the steps to operate the gas booster system:

- 1) All the valves are initially closed. The cylinder which contains the gas sample is connected to the inlet of the gas booster system and cranked open. The inlet valve in the gas booster system is also opened. All other valves are in the close position. Gas starts to fill in the gas booster cylinder pushing the piston down.
- 2) The oil vent valve is now opened to allow for any remaining hydraulic oil in the gas booster cylinder to trickle into the oil reservoir. This ensures that the cylinder is now completely filled with the gas sample alone. The gas inlet valve is now closed.
- 3) Valve A, the master valve for supplying air to the pump is opened and then the air regulator is slowly opened to the desired level. This sets the pump in motion and oil starts coming in from the bottom of the gas booster cylinder. The oil vent valve should now be closed to allow the oil to accumulate in the cylinder.
- 4) On opening the air regulator further, more and more oil passes into the gas booster cylinder from the oil reservoir. This causes a reduction of volume of the gas sample thus increasing the pressure.
- 5) When the desired pressure has been reached, both Valve A and the air regulator should be closed so that the pressure does not keep increasing.
- 6) The gas outlet valve can now be opened to supply high pressure gas as required.
- 7) When the experiments have ceased, the oil vent valve is now carefully opened to release the oil back into the reservoir. This causes an increase in volume of the gas and causes the pressure to go down.
- 8) The gas vent valve can now be opened to purge any remaining gas from the system.

The high pressure gas from the gas booster system is now available to be connected to the measurement sensor for the measurement of gas viscosity.

#### **4.1.3** Temperature Control System - Oven

The temperature of the measuring system is controlled by a mechanical convection oven, which was manufactured by Yamato Scientific America Inc. The measuring system was placed inside the oven. The oven mode is DKN400 (Figure 4-4) with electric capacity of 115V AC, 12A and temperature setting range from 0 to 320 °C. The overheat protection function incorporated into the oven prevents the damage to oven and measuring system in case of human error. With this oven we can manipulate the measuring temperature as we want. One drawback of this setup is that it usually takes 5 to 6 hours for temperature reaching constant when we change to a new temperature own to the fact that the convection medium used to transfer heat to measuring system is air.



Figure 4-4. The temperature control system in this study

#### 4.1.4 Measurement System - Cambridge Viscometer

Every type of viscometer has its advantages and disadvantages. In this research a modified falling body viscometer is used to measure gases viscosity at HPHT. The

viscometer we used is Cambridge Viscosity SPL440 viscometer. It is a piston-style viscometer designed by Cambridge Viscosity, Inc. exclusively for measuring viscosities of petroleum fluids, oils and gases. The measurable range of the gas viscosity is from 0.02 to 0.2 cp. The accuracy of the VISCOpvt is reported to be around 1% of full scale of range. Its operating pressure is up to 25000 psi, respectively. The viscometer schematic is shown in Figure 4-5. The Cambridge VISCOpvt works on the principle of a known piston traversing back and forth in a measuring chamber containing the fluid sample. The piston is driven magnetically by two coils located at opposite ends. The time taken by the piston to complete one motion is correlated to the viscosity of the fluid in the measuring chamber by a proprietary equation.



Figure 4-5. Schematic of the measurement system in this study

There are some disadvantages with the original SPL440 viscometer to measure gas viscosity. First, the viscometer was initially supplied in the oil measurement mode, where the measurement chamber is inclined at an angle of 45° from the horizontal. The time of travel becomes very short if the medium is gas. Thereby the accuracy of the travel time cannot be guaranteed. This problem is overcome by making the whole arrangement horizontal or nearly horizontal. Keeping it horizontal gives the added advantage of nullifying any gravity effects. Another disadvantage is that the prototype cannot work efficiently with only two valves used to control the flow of fluid with one at

the inlet tube and another at the outlet tube. These two valves are installed far away from the cell. Therefore it requires large volume of test sample. This installation also increases the time for gas to reach equilibrium considering the pressure difference between two ends of the cell caused by the movement of piston. Dr. Teodoriu modified the configuration of the original design by one pressure gauge at the inlet (very close to the cell), one more valve at the inlet, and one more valve at the outlet. This modification drastically reduces the time to reach equilibrium and cut down the required volume of test sample to 30-40 %. Pressure gauge close to the cell provides more accurate data than before.

The general procedures to operate the viscometer are:

- 1) After the installation of the whole experiment facility and gas in gas booster system had been compressed and ready to be used, connect the inlet end of the viscometer to the outlet line of the gas booster system.
- 2) Adjust the sensor's temperature to the desired temperature by regulating the oven temperature.
- 3) Open outlet valve of viscometer; open inlet valve of viscometer; open the outlet valves at the gas booster system. Let the gas from gas booster system purge the existing gas in the chamber and flow line for about one minute.
- 4) Now close the outlet valve of viscometer; keep inlet valve of viscometer open to fill the chamber with measured gas until the pressure reaches the desired value.
- 5) Close inlet valve of viscometer; wait for the temperature in the chamber becomes constant.
- 6) Adjust the pressure to the measured pressure; close the outlet valve of viscometer; close the inlet valve of viscometer.
- 7) Start to measure gas viscosity at certain pressure and temperature.
- 8) After finish one measurement, keep temperature constant and change pressure to other value to continue another measurement.

9) When the experiment finishes, close the outlet valves at the gas booster system; close the inlet valve of viscometer; open outlet valves to vent gas.

## 4.1.5 Data Acquisition System

The Cambridge viscometer was also supplied with RS-232 serial communication support, allowing the data measured by the viscometer to be synchronized with a desktop computer. We setup a new recording control panel through which the measurement is controlled (Figure 4-6). This gives the provision to save the data for later analysis. The software used to record the measured data is ViscoLab. Through data acquisition system we can output measured pressure, average temperature, average gas viscosity, current temperature, and current gas viscosity. The measured interval can be adjusted as requirement. With this system, manual recording of the experiment is not necessary and large storage of measurement data becomes feasible.

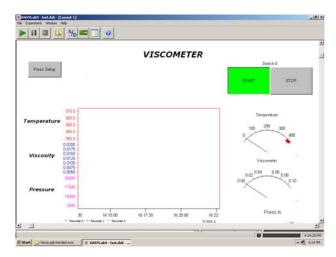


Figure 4-6. Recording control panel to control the experiment

#### **4.2 Experiment Procedure**

The measurement in this stage is limited to nitrogen and methane. We started experiment with measuring nitrogen viscosity considering safety and easy calibration. Constrained

by the viscometer measurement capacity of 0.02-0.2 cp and the viscometer rated pressure of 25000 psig, we selected 3000 psi as the minimum pressure and 25000 psig as the maximum for nitrogen. After finishing some experiments or particular time interval, the facility was disassembled and all components were cleaned. These were done because after particular period there are some contaminants trapped inside the chamber and piston (Figure 4-7) will introduce system error to the measurement. After the cleaning, all parts were assembled and ready to be used immediately. As we finished the experiment on nitrogen viscosity, we switched to methane viscosity. We selected 4000 psi as the minimum pressure and 25000 psig as the maximum for methane because the viscometer cannot provide accurate data at pressure less than 4000 psig.

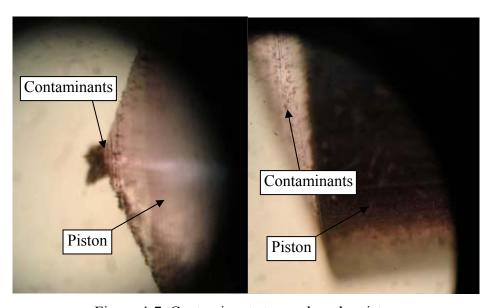


Figure 4-7. Contaminants trapped on the piston

We decide the measurement procedure according to 1) the time required reaching temperature equilibrium in measurement system is much longer than the time to reach pressure equilibrium in the system, while the time for pressure reaching equilibrium takes less than 10 seconds, 2) safety and data calibration requirements, 3) the viscometer rated pressure and temperature, and 4) enough measuring data point to develop viscosity

correlation. Therefore temperature will be the same and only the pressure is changed in an experiment. After completing one experiment, we change to another temperature.

The following steps are used to implement our experiments:

- 1) We start experiment on measuring nitrogen viscosity. The first experiment is at lowest temperature.
- 2) Set the temperature at the desired value and wait until temperature in the measuring system becomes constant. This may take 5-7 hours.
- 3) In an experiment, we begin the measurement from lowest pressure of 3000 psi and keep temperature constant. The measurement of viscosity at particular pressure and temperature usually lasts 15-30 minutes.
- 4) Increase the pressure by 500 psi while keep temperature stable, measure viscosity at this pressure and temperature for 15-30 minutes.
- 5) Continue the measurement by increasing the pressure until we reach the highest pressure, which is ≤ 25000 psig, and always keep temperature constant during this step, then measure viscosity at this pressure and temperature for 15-30 minutes.
- 6) Decrease the pressure by 500 psi and keep temperature constant at the same time, and then measure viscosity at this pressure and temperature for 15-30 minutes.
- 7) Keep reducing pressure until touching the lowest pressure and keep temperature constant at the same time, again measuring time for each pressure and temperature is 15-30 minutes. So far we finish one experiment.
- 8) Steps 3-7 are repeated several times to understand the repeatability of the measurement, i.e., we measure viscosity at same pressure and temperature several times.
- 9) Through Steps 3-8 we finish the measurement for one temperature. We change the temperature and wait 5-7 hours until it becomes constant, then repeat Steps 3-8 to get viscosity for this new temperature.

- 10) Continue to more temperatures until we finish measurement of nitrogen viscosity.
- 11) Upon completing nitrogen viscosity measurement we transfer to methane and repeat the same step we measure nitrogen viscosity.

The cleaning of the viscometer is dependent on the number of experiments or the viscometer running time. Repeated measurement provides abundant data for calibration in the data analysis.

# 4.3 Measurement Principle of Viscometer in This Study

The knowledge of geometry of measuring cell is important to understand the principle behind the measurement. The cell is a cylinder-shaped chamber with a piston inside (Figures 4-1 and 4-8). Table 4-1 lists the dimension of chamber and piston.

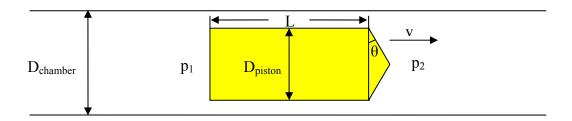


Figure 4-8. Piston moves inside of chamber of viscometer using in this study

Piston Overall Length of Piston (Include the cone) 0.9412 inches Length of piston flank(rectangle part, exclude height of cone) 0.87658 inches Outer diameter of Piston 0.312 inches Base angle of the cone  $(\theta)$ 22.5 degree Height of the cone 0.06462 inches Surface area of the cone(exclude base area) 0.07808 in<sup>2</sup> Surface area of the piston flank (exclude the base and cone) 5.50773 in<sup>2</sup> Weight of piston 4.807 g Chamber Inner diameter of chamber 0.314 inches Length of chamber 1.4 inches

Table 4-1. The dimension of chamber and piston (Malaguti and Suitter, 2010)

In our study, the viscometer is placed horizontally. Therefore the chamber and piston are in horizontal position. Figure 4-8 shows the cut away view of chamber inside which a piston is moving from left to right. The piston is driven by an electromagnetic force. For simplification, the following assumptions are made:

- 1) The time to accelerate is negligible or very short time for piston from static to reach constant speed. This is because the acceleration time is very small compared to the 2-way piston travel time. The flow in annulus is steady-state flow.
- 2) A known, constant electromagnetic force applied during one way travel.
- 3) Piston is moving in the center of chamber and does not touch the chamber wall.
- 4) Fourth assumption is that both piston and chamber built from same material and have same roughness.
- 5) The test fluid is Newtonian.
- 6) Gas viscosity is uniform throughout the chamber. Actually the pressure difference between two ends of piston is 0-10 psi, which is very small comparing with 3000-25000 psig measuring pressure, thus the variation of viscosity with pressure can be neglected. So does the density.

- 7) Pressure drop along the annulus between piston and chamber is mainly friction pressure drop, and the contribution from kinetic energy change is so small that it is negligible.
- 8) For the laminar flow there is no slip on the surfaces of chamber and piston.

  Assumption 7) can be proved by the first law of thermodynamics or the principal

Assumption 7) can be proved by the first law of thermodynamics or the principle of conservation of energy based on the uniform constructions of chamber and piston and the pressure difference in assumption 6).

Forces on piston can be analyzed in two dimensions, horizontal and vertical directions. For the purpose of this study, vertical forces are not considered. In horizontal direction, when the piston moves with a constant velocity, v, the pressure in front of the piston is higher than that behind the piston. In addition, the fluid flowing from the front of piston through the annulus between piston and chamber wall to back of piston results in the drag forces on the cone and flank of piston. Because the chamber and piston are in horizontal position, the potential energy change is zero. As a result the piston is subjected to five forces, the electromagnetic force, the drag force on the cone surface, the drag force on the flank of the piston, the fluid forces in front of and behind the piston. According to the force equilibrium, we have the following form.

$$F_{em} + F_{behind} = DF_{piston\ cone} + DF_{piston\ flank} + F_{front}$$
 (4.1)

where

 $F_{em}$  = Electromagnetic force,

 $DF_{viston\ cone}$  = Drag force on the cone surface,

 $DF_{piston flank}$  = Drag force on the flank of the piston,

 $F_{front}$  = Fluid force in front of the piston,

 $F_{behind}$  = Fluid force behind the piston.

The fluid force behind the piston is

$$F_{behind} = p_1 A_{piston \ base} = \pi \frac{D_{piston}^2}{4} p_1 \tag{4.2}$$

where

 $p_1$  = Pressure behind the piston,

 $A_{piston\ base}$  = Area of base of piston.

The fluid force in front of the piston is

$$F_{front} = p_2 A_{cone\ base} = p_2 A_{piston\ base} = \pi \frac{D_{piston}^2}{4} p_2 \tag{4.3}$$

where

 $p_2$ = Pressure in front of the piston,

 $A_{cone\ base}$  = Area of base of cone.

The drag force on the flank of the piston can be derived according to the flow regime of fluid flowing around the piston. The drag force will be analyzed in two cases. One is laminar flow and another is turbulent flow. When piston moves at a constant velocity the volume of the fluid displaced by the piston is equal to the volume flows through the annulus during a specific time interval,  $\Delta t$  we have

$$V_{displacing} = V_{displaced} \tag{4.4}$$

where

 $V_{displacing}$  = Displacing volume when piston moves ahead,

 $V_{\it displaced}$  = Displaced fluid volume that flows through annulus and back to the behind of piston.

The displacing and displaced volumes can be expressed by

$$L_{\textit{displacing}} A_{\textit{piston base}} = L_{\textit{fluid flow}} A_{\textit{annulus}} \tag{4.5}$$

in terms of travel distance and cross section area.

where

 $L_{\it displacing} = {
m Travel \ distance \ of \ piston \ during \ a \ specific \ time \ interval},$ 

 $L_{\it fluid flow}$  = Travel distance of fluid flow in annulus during a specific time interval,

 $A_{annulus}$  = Cross section area of annulus.

Replacing travel distance with velocity and time interval and knowing that annulus area is the difference between chamber cross section area and piston base area, we obtain

$$v_{piston} \Delta t A_{piston \ base} = \overline{v}_{fluid} \Delta t \left( A_{chamber} - A_{piston \ base} \right) \tag{4.6}$$

where

 $v_{piston}$  = Piston velocity,

 $\overline{v}_{fluid}$  = Mean fluid flow velocity,

Cancelling out the same term on both hand sides and expressing area in diameter results in

$$v_{piston} \frac{\pi}{4} D_{piston}^2 = \overline{v}_{fluid} \left( \frac{\pi}{4} D_{chamber}^2 - \frac{\pi}{4} D_{piston}^2 \right)$$
(4.7)

where

 $D_{piston}$  = Piston diameter,

 $D_{chamber}$  = Chamber diameter,

After several rearrangement of Equation 4.7 we come up with

$$\overline{v}_{fluid} = v_{piston} \frac{D_{piston}^2}{\left(D_{chamber}^2 - D_{piston}^2\right)} \tag{4.8}$$

It should be noted that fluid velocity in Equation 4.8 is average velocity in the annulus. In our case, the diameter of piston and chamber are 0.312 and 0.314 inches, respectively. Therefore the average fluid velocity is 77.75 times of piston velocity. For the case of laminar flow, we assume fluid velocities on piston and chamber walls are zero and reach maximum in the center of annulus. Bourgoyne et al. (1986) provide an analytical solution for the pressure drop along the annulus. Now we consider a control fluid volume in the annulus, which can be represented by rectangular slot flow as far as the ratio of piston diameter to chamber diameter exceeds 0.3. In our case the ratio is 0.312/0.314, which is much higher than 0.3. Now consider a rectangular slot with an area of A and height of h used to represent the annular flow in our apparatus (Figure 4-9). The area and height can be expressed in diameters, which are

$$A = Wh = \frac{\pi}{4} \left( D_{chamber}^2 - D_{piston}^2 \right)$$
 (4.9)

where

$$W = \frac{\pi}{2} \left( D_{chamber} + D_{piston} \right) \tag{4.10}$$

and

$$h = \frac{1}{2} \left( D_{chamber} - D_{piston} \right) \tag{4.11}$$

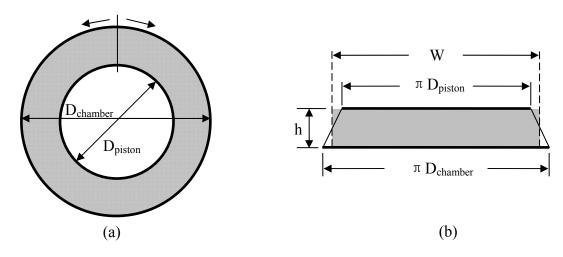


Figure 4-9. Representing the annulus as a slot: (a) annulus and (b) equivalent slot, after Bourgoyne et al. (1986)

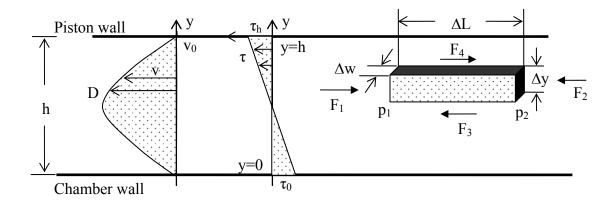


Figure 4-10. Free body diagram for controlled fluid volume in a slot, after Bourgoyne et al. (1986)

We deal with a controlled fluid volume (Figure 4-10) with width  $\Delta w$  and thickness  $\Delta y$ . According to Bourgoyne et al. (1986), Force equilibrium in horizontal direction gives

$$F_1 + F_4 = F_2 + F_3 \tag{4.12}$$

where

$$F_1 = p_1 \Delta w \Delta y \tag{4.13}$$

$$F_2 = p_2 \Delta w \Delta y = \left( p_1 + \frac{dp_f}{dL} \Delta L \right) \Delta w \Delta y \tag{4.14}$$

$$F_3 = \tau_v \Delta w \Delta L \tag{4.15}$$

and

$$F_4 = \tau_{y + \Delta y} \Delta w \Delta L = \left(\tau_y + \frac{d\tau}{dy} \Delta y\right) \Delta w \Delta L \tag{4.16}$$

where

 $\Delta L$  = Length of controlled fluid volume,

 $\tau$  = Shear stress,

 $\frac{dp_f}{dL}$  = Frictional pressure gradient in annulus,

 $\frac{d\tau}{dy}$  = Shear stress gradient in y direction,

Substituting Equations 4.13 through 4.16 into Equations 4.12 yields

$$p_{1}\Delta w \Delta y + \left(\tau_{y} + \frac{d\tau}{dy} \Delta y\right) \Delta w \Delta L = \left(p_{1} + \frac{dp_{f}}{dL} \Delta L\right) \Delta w \Delta y + \left(\tau_{y} \Delta w \Delta L\right) \Delta w \Delta L$$

$$+ \tau_{y} \Delta w \Delta L$$

$$(4.17)$$

Expanding and cancelling out the same terms on both sides gives

$$\frac{d\tau}{dy}\Delta y \Delta w \Delta L = \frac{dp_f}{dL}\Delta L \Delta w \Delta y \tag{4.18}$$

Dividing Equations 4.18 by  $\Delta y \Delta w \Delta L$ , we have

$$\frac{d\tau}{dy} = \frac{dp_f}{dL} \tag{4.19}$$

Because  $dp_f/dL$  is not a function of y, Equation 4.19 can be integrated with respect to y. Separating variables and integrating gives

$$\tau = y \frac{dp_f}{dL} + \tau_0 \tag{4.20}$$

where  $\tau_0$  is the constant of integration that corresponds to the shear stress at y=0. From the definition of shear rate,  $\dot{\gamma}$ , we obtain

$$\dot{\gamma} = -\frac{dv}{dy} \tag{4.21}$$

Combining Equations 4.21 with the definition of viscosity for Newtonian fluid gives

$$\tau = \mu \dot{\gamma} = -\mu \frac{dv}{dv} = y \frac{dp_f}{dL} + \tau_0 \tag{4.22}$$

where

 $\mu$  = Newtonian fluid viscosity,

v = Newtonian fluid velocity,

Again, separating variable and integrating yields

$$v = -\frac{y^2}{2\mu} \frac{dp_f}{dL} - \frac{\tau_0 y}{\mu} + v_0 \tag{4.23}$$

where  $v_0$  is the second constant of integration that corresponds to the fluid velocity at y=0. Applying the boundary condition

$$v_0 = 0$$
 at  $y=0$ , (4.24)

we have

$$0 = -\frac{0^2}{2\mu} \frac{dp_f}{dL} - \frac{\tau_0 0}{\mu} + v_0 \tag{4.25}$$

Similarly applying the boundary condition

$$v_0 = 0$$
 at  $y = h$ , (4.26)

we have

$$0 = -\frac{h^2}{2\mu} \frac{dp_f}{dL} - \frac{\tau_0 h}{\mu} + v_0 \tag{4.27}$$

Therefore, the constants of integration  $v_0$  and  $\tau_0$  are

$$v_0 = 0 \tag{4.28}$$

and

$$\tau_0 = -\frac{h}{2} \frac{dp_f}{dL}.\tag{4.29}$$

Substituting Equations 4.28 and 4.29 into 4.23 gives

$$v = \frac{1}{2\mu} \frac{dp_f}{dL} \left( hy - y^2 \right) \tag{4.30}$$

The flow rate q is the product of velocity v and area A. Integrating the controlled volume flow rate throughout the interval 0 to h and recalling Equation 4.30 we obtain total flow rate

$$q = \int_{0}^{h} v dA = \int_{0}^{h} v W dy = \frac{W}{2\mu} \frac{dp_{f}}{dL} \int_{0}^{h} (hy - y^{2}) dy$$
 (4.31)

Integrating Equations 4.31 yields

$$q = \frac{Wh^3}{12\,\mu} \frac{dp_f}{dL} \tag{4.32}$$

Substituting Equations 4.10 and 4.11 into 4.32, we obtain

$$q = \frac{\pi}{192 \,\mu} \frac{dp_f}{dL} \left( D_{chamber}^2 - D_{piston}^2 \right) \left( D_{chamber} - D_{piston} \right)^2 \tag{4.33}$$

Expressing the flow rate in terms of the mean flow velocity and solving for the frictional pressure gradient gives

$$\overline{v}_{\mathit{fluid}} = \frac{q}{A} = \frac{\frac{\pi}{192 \, \mu} \, \frac{dp_{\mathit{f}}}{dL} \Big( D_{\mathit{chamber}}^2 - D_{\mathit{piston}}^2 \Big) \Big( D_{\mathit{chamber}} - D_{\mathit{piston}} \Big)^2}{\frac{\pi}{A} \Big( D_{\mathit{chamber}}^2 - D_{\mathit{piston}}^2 \Big)}$$

or

$$\frac{dp_f}{dL} = \frac{q}{A} = \frac{48\mu \overline{v}_{fluid}}{\left(D_{chamber} - D_{piston}\right)^2}.$$
(4.34)

Integrating Equation 4.34 and recalling  $\bar{v}_{fluid} = v_{piston} \frac{D_{piston}^2}{\left(D_{chamber}^2 - D_{piston}^2\right)}$  we have friction pressure drop along the annulus

$$p_{2} - p_{1} = \int_{0}^{L_{piston flank}} \frac{dp_{f}}{dL} dL = \frac{48\mu \bar{v}_{fluid} L_{piston flank}}{\left(D_{chamber} - D_{piston}\right)^{2}}$$

$$= \frac{48\mu \left[v_{piston} \frac{D_{piston}^{2}}{\left(D_{chamber}^{2} - D_{piston}^{2}\right)}\right] L_{piston flank}}{\left(D_{chamber} - D_{piston}\right)^{2}}$$

$$= \frac{48\mu v_{piston} D_{piston}^{2} L_{piston flank}}{\left(D_{chamber} - D_{piston}\right)^{3} \left(D_{chamber} + D_{piston}\right)}$$

$$(4.35)$$

Substituting Equations 4.11 and 4.34 into 4.29 we have shear stress on piston wall, which is opposite to the shear stress on fluid.

$$-\tau_{0} = -\left(-\frac{h}{2}\frac{dp_{f}}{dL}\right) = \frac{D_{chamber} - D_{piston}}{4} \frac{48\mu \bar{v}_{fluid}}{\left(D_{chamber} - D_{piston}\right)^{2}}$$

$$= \frac{12\mu \bar{v}_{fluid}}{D_{chamber} - D_{piston}}$$

$$(4.36)$$

Thus the drag force on the flank of the piston,  $DF_{piston flank}$ , is

$$DF_{piston flank} = A_{piston flank} \left(-\tau_0\right) = \frac{12\pi D_{piston} L_{piston flank} \mu \overline{\nu}_{fluid}}{D_{chamber} - D_{piston}}$$
(4.37)

for laminar flow.

where

 $L_{piston flank}$  = Length of piston flank.

If flow in the annulus is turbulence, the drag force on the flank of the piston can be analyzed by employing Reynolds number and friction factor.

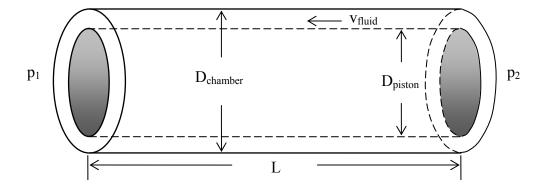


Figure 4-11. Schematic of fluid flow through an annulus between piston and chamber

For Figure 4-11, force balance requires that

$$(p_2 - p_1)A_{annulus} = DF_{chamber} + DF_{piston flank}$$

$$= \tau_{piston} \pi D_{piston} L_{piston flank} + \tau_{chamber} \pi D_{chamber} L_{piston flank}$$

$$(4.38)$$

Since piston diameter is very close to chamber diameter and basing on symmetrical geometry, we have following observations

$$\tau_{chamber} = \tau_{piston}, \tag{4.39}$$

and

$$D_{chamber} \cong D_{piston}$$
. (4.40)

Therefore, we obtain

$$DF_{chamber} \cong DF_{piston flank}$$
 (4.41)

and

$$(p_2 - p_1)\frac{\pi}{4}(D_{chamber}^2 - D_{piston}^2) = \pi \tau_{piston} L_{piston flank}(D_{piston} + D_{chamber}) (4.42)$$

or

$$\frac{\left(p_2 - p_1\right)}{L_{piston flank}} = \frac{4\tau_{piston}}{\left(D_{chamber} - D_{piston}\right)} \tag{4.43}$$

Introducing the definition of the Fanning friction factor (Wikipedia, 2009), *f*, which is the ratio of the shear stress on the tubular wall applied by unit volume of fluid to its kinetic energy.

$$f = \frac{shear\ stress\ on\ the\ wall/volume\ fluid}{kinetic\ energy/volume\ fluid} \tag{4.44}$$

or

$$f = \frac{\tau_{piston} + \tau_{chamber}}{\frac{1}{2} \rho_f \overline{v}_{fluid}^2} \,. \tag{4.45}$$

where

 $\rho_f$  = Fluid density.

Recalling  $\tau_{piston} = \tau_{chamber}$ , we have

$$\tau_{piston} = \frac{1}{4} f \rho_f \bar{v}_{fluid}^2 \tag{4.46}$$

The fanning friction factor for smooth pipe, which is as in our case, and a Reynolds number range of 2,100 to 100,000, can be approximated by the following form (Blasius, 1913):

$$f = \frac{0.0791}{N_{\text{Re}}^{0.25}} \tag{4.47}$$

where  $N_{Re}$  is the Reynolds number, which is expressed as:

$$N_{\rm Re} = \frac{D_e \overline{v}_{fluid} \rho_f}{u} \tag{4.48}$$

where

 $D_e$  = Equivalent circular diameter,

The equivalent circular diameter  $D_e$  is equal to four times the hydraulic radius  $r_H$ .

$$D_{\rho} = 4r_{H} \tag{4.49}$$

and the hydraulic radius is defined as the ratio of the cross-sectional area to the wetted perimeter of the flow channel. In our case it is

$$r_{H} = \frac{\frac{\pi}{4} \left( D_{chamber}^{2} - D_{piston}^{2} \right)}{\pi \left( D_{piston} + D_{chamber} \right)} = \frac{D_{chamber} - D_{piston}}{4}$$
(4.50)

Substituting Equation 4.50 into 4.49, we have

$$D_e = 4 \frac{\left(D_{chamber} - D_{piston}\right)}{4} = D_{chamber} - D_{piston} \quad (4.51)$$

Substituting Equation 4.51 into 4.48, we have

$$N_{\text{Re}} = \frac{\left(D_{chamber} - D_{piston}\right) \overline{v}_{fluid} \rho_f}{\mu} \tag{4.52}$$

Substituting Equation 4.52 into 4.47, we have

$$f = \frac{0.0791}{\left\lceil \frac{\left(D_{chamber} - D_{piston}\right)\overline{v}_{fluid}\rho_{f}}{\mu} \right\rceil^{0.25}}$$
(4.53)

Substituting Equation 4.53 into 4.46, we have

$$\tau_{piston} = \frac{1}{4} \left\{ \frac{0.0791}{\left[ \frac{\left( D_{chamber} - D_{piston} \right) \overline{v}_{fluid} \rho_{f}}{\mu} \right]^{0.25}} \right\} \rho_{f} \overline{v}_{fluid}^{2}$$
(4.54)

Simplifying Equation 4.54 yields

$$\tau_{piston} = \frac{0.0198 \rho_f^{0.75} \mu^{0.25} \overline{v}_{fluid}^{1.75}}{\left(D_{chamber} - D_{piston}\right)^{0.25}}$$
(4.55)

Thus the drag force on the flank of the piston,  $DF_{piston flank}$ , is expressed as

$$DF_{piston flank} = \tau_{piston} A_{piston flank} = \frac{0.0198\pi D_{piston} L_{piston flank} \rho_f^{0.75} \mu^{0.25} \overline{v}_{fluid}^{1.75}}{\left(D_{chamber} - D_{piston}\right)^{0.25}} (4.56)$$

for turbulent flow in annulus.

The drag force on the cone surface,  $DF_{piston\ cone}$ , can be estimated by applying Stokes' law (Castleman, 1926). Figure 4-8 illustrates a piston traveling through a homogeneous fluid. If the motion of the sphere is sufficiently slow, the inertia terms become negligible. Under this condition the cone of the piston experience a drag force resulting from the viscous fluid flow around the cone surface. The magnitude of drag force is dependent on the flow regime, laminar or turbulent flow.

For laminar flow, the drag force is calculated from Stokes law. Stokes law has shown that for creeping flow (Castleman, 1926) (i.e., the streamlines of fluid movement pass smoothly about the particle and there is no eddying downstream of it) the drag force is related to the piston velocity through the fluid by:

$$DF_{piston cone} = 3\pi D_{piston} \mu v_{piston}. \tag{4.57}$$

This equation is found to give acceptable accuracy for Reynolds numbers below 0.1. For Reynolds numbers greater than 0.1, empirically determined friction factors must be used.

In case of turbulent flow, the concept of friction factor is introduced to estimate drag force. It is defined by:

$$f = \frac{DF_{piston cone}}{AE_{\nu}}. (4.58)$$

Then the drag force can be expressed as:

$$DF_{piston\,cone} = f A E_k \tag{4.59}$$

where

A =Characteristic area of the cone,

 $E_k$  = Kinetic energy per unit volume.

The characteristic area of the cone in our case is given by:

$$A = \frac{1}{4} \pi D_{piston}^2 \,. \tag{4.60}$$

The kinetic energy per unit volume is given by:

$$E_k = \frac{\rho_f v_{piston}^2}{2} \,. \tag{4.61}$$

The friction factor f is a function of the Reynolds number and, in the case of non-spherical shapes, a term called the sphericity. Sphericity,  $\psi$ , is defined as the surface area of a sphere containing the same volume as the particle divided by the surface area of the particle. In our case the particle is a cone with following geometry:

Base diameter =
$$D_{piston}$$
,

Angle between base and flank = 22.5 degree, thus height of the cone is

Height of the cone=
$$\frac{D_{piston}}{2} \tan(22.5^{\circ})$$
. (4.62)

Therefore the volume and surface area of the cone are

$$A_{cone} = \pi \left(\frac{D_{piston}}{2}\right) \left\{ \left(\frac{D_{piston}}{2}\right)^2 + \left(\frac{D_{piston}}{2} \tan(22.5^\circ)\right)^2 \right\}^{0.5} + \pi \left(\frac{D_{piston}}{2}\right)^2 (4.63)$$

$$V_{cone} = \frac{1}{3}\pi \left(\frac{D_{piston}}{2}\right)^{2} \left(\frac{D_{piston}}{2} \tan(22.5^{\circ})\right) = \frac{1}{3}\pi \left(0.051777D_{piston}^{3}\right)$$
(4.64)

The ball that has equivalent volume to the cone will have an equivalent diameter of

$$\frac{4}{3}\pi \left(\frac{D_{equivalent}}{2}\right)^3 = \frac{1}{3}\pi \left(0.051777D_{piston}^3\right)$$

or

$$D_{equivalent} = \sqrt[3]{0.103554} D_{piston} \tag{4.65}$$

where

 $D_{equivalent}$  = Equivalent ball diameter,

Then the surface area of the equivalent ball is

$$A_{equivalent} = 4\pi \left(\frac{\sqrt[3]{0.103554}D_{piston}}{2}\right)^2 = \pi \left(0.220517D_{piston}^2\right)(4.66)$$

Sphericity of the cone according to the definition is

$$\psi = \frac{A_{equivalent}}{A_{cone}} = \frac{\pi \left(0.220517 D_{piston}^{2}\right)}{\pi \left(\frac{D_{piston}}{2}\right)^{2} + \left(\frac{D_{piston}}{2} \tan(22.5^{o})\right)^{2}} + \pi \left(\frac{D_{piston}}{2}\right)^{2} (4.67)$$

$$= 0.424$$

Bourgoyne et al. (1986) developed a graphical correlation to estimate the friction-factor from given Reynolds-number and sphericity. A directed read of friction factor can be accomplished using Figure 4-12.

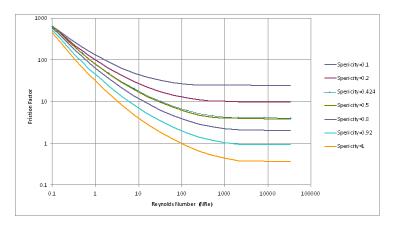


Figure 4-12. Friction factor vs. particle Reynolds number for particles of different sphericities, after Bourgoyne et al. (1986)

Reynolds number is expressed as

$$N_{\rm Re} = \frac{\rho_f v_{piston} D_{piston}}{\mu} \,. \tag{4.68}$$

For the piston in our study, whose sphericity is 0.424, the relationship between friction factor and Reynolds number can be expressed as

$$f = 10^{1.9068 - 0.78036 \log(N_{\text{Re}}) + 0.117434 \left[\log(N_{\text{Re}})\right]^{2}}$$

$$= 10^{1.9068 - 0.78036 \log\left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log\left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2}}$$

$$(4.69)$$

Therefore the drag force on the cone surface is

$$DF_{\textit{piston cone}} = \left(\frac{\pi \rho_f v_{\textit{piston}}^2 D_{\textit{piston}}^2}{8}\right) 10^{1.9068 - 0.78036 \log \left(\frac{\rho_f v_{\textit{piston}} D_{\textit{piston}}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_f v_{\textit{piston}} D_{\textit{piston}}}{\mu}\right)\right]^2} (4.70)$$

Including these forces into force balance Equation 4.1, we have

$$F_{em} + \pi \frac{D_{piston}^2}{4} p_1 = 3\pi D_{piston} \mu v_{piston} + \frac{12\pi D_{piston} L_{piston} f_{lank} \mu \overline{v}_{fluid}}{D_{chamber} - D_{piston}} + \pi \frac{D_{piston}^2}{4} p_2$$

or

$$F_{em} = 3\pi D_{piston} \mu v_{piston} + \frac{12\pi D_{piston} L_{piston flank} \mu \bar{v}_{fluid}}{D_{chamber} - D_{piston}} + \pi \frac{D_{piston}^2}{4} (p_2 - p_1) (4.71)$$

for laminar flow, and

$$\begin{split} F_{em} + \pi \frac{D_{piston}^{2}}{4} p_{1} \\ = & \left( \frac{\pi \rho_{f} v_{piston}^{2} D_{piston}^{2}}{8} \right) 10^{\frac{1.9068 - 0.78036 \log \left( \frac{\rho_{f} v_{piston} D_{piston}}{\mu} \right) + 0.117434 \left[ \log \left( \frac{\rho_{f} v_{piston} D_{piston}}{\mu} \right) \right]^{2}}{\left( D_{chamber} - D_{piston} \right)^{0.25} \overline{v}_{fluid}^{1.75}} + \pi \frac{D_{piston}^{2}}{4} p_{2} \end{split}$$

or

$$F_{em} = \left(\frac{\pi \rho_{f} v_{piston}^{2} D_{piston}^{2}}{8}\right) 10^{1.9068 - 0.78036 \log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2}} + \frac{0.0198\pi D_{piston} L_{piston flank} \rho_{f}^{0.75} \mu^{0.25} \overline{v}_{fluid}^{1.75}}{\left(D_{chamber} - D_{piston}\right)^{0.25}} + \pi \frac{D_{piston}^{2}}{4} \left(p_{2} - p_{1}\right)$$

$$(4.72)$$

for turbulent flow.

Substituting Equation 4.8 into Equations 4.71 and 4.72 we obtain

$$F_{em} = 3\pi D_{piston} \mu v_{piston} + \frac{12\pi D_{piston} L_{piston flank} \mu v_{piston} \frac{D_{piston}^{2}}{\left(D_{chamber}^{2} - D_{piston}^{2}\right)}}{D_{chamber} - D_{piston}} + \frac{D_{piston}^{2}}{D_{chamber}^{2} - D_{piston}}$$

$$+ \pi \frac{D_{piston}^{2}}{A} \left(p_{2} - p_{1}\right)$$

$$(4.73)$$

for laminar flow, and

$$F_{em} = \left(\frac{\pi \rho_{f} v_{piston}^{2} D_{piston}^{2}}{8}\right) 10^{1.9068 - 0.78036 \log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2}}$$

$$- 0.0198\pi D_{piston} L_{piston} f_{lank} \rho_{f}^{0.75} \mu^{0.25} \left[v_{piston} \frac{D_{piston}^{2}}{\left(D_{chamber}^{2} - D_{piston}^{2}\right)}\right]^{1.75}$$

$$+ \frac{\left(D_{chamber}^{2} - D_{piston}^{2}\right)^{0.25}}{\left(D_{chamber} - D_{piston}^{2}\right)^{0.25}}$$

$$+ \pi \frac{D_{piston}^{2}}{4} \left(p_{2} - p_{1}\right)$$

$$(4.74)$$

for turbulent flow.

Again substituting Equation 4.35 into Equation 4.73 we obtain

$$\begin{split} F_{em} &= 3\pi D_{piston} \mu v_{piston} + \frac{12\pi D_{piston} L_{piston} f_{lank} \mu v_{piston} D_{piston}^2}{\left(D_{chamber} - D_{piston}\right)^2 \left(D_{chamber} + D_{piston}\right)} \\ &+ \pi \frac{D_{piston}^2}{4} \frac{48\mu v_{piston} D_{piston}^2 L_{piston} f_{lank}}{\left(D_{chamber} - D_{piston}\right)^3 \left(D_{chamber} + D_{piston}\right)} \end{split}$$

or

$$F_{em} = 3\pi D_{piston} \mu v_{piston} + \frac{12\pi L_{piston flank} \mu v_{piston} D_{piston}^3 D_{chamber}}{\left(D_{chamber} - D_{piston}\right)^3 \left(D_{chamber} + D_{piston}\right)}$$
(4.75)

for laminar flow.

Recalling 
$$\frac{\left(p_2-p_1\right)}{L_{\textit{piston flank}}} = \frac{4\tau_{\textit{piston}}}{\left(D_{\textit{chamber}}-D_{\textit{piston}}\right)}$$
 and  $\tau_{\textit{piston}} = \frac{1}{4}f\rho_f\overline{v}_{\textit{fluid}}^2$ , we have

$$\frac{\left(p_{2} - p_{1}\right)}{L_{piston flank}} = \frac{4\left(\frac{1}{4}f\rho_{f}\overline{v}_{fluid}^{2}\right)}{\left(D_{chamber} - D_{piston}\right)}$$

$$= \frac{10^{1.9068-0.78036 \log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2} \rho_{f} \left[v_{piston} \frac{D_{piston}^{2}}{\left(D_{chamber}^{2} - D_{piston}^{2}\right)}\right]^{2}}{\left(D_{chamber} - D_{piston}\right)}$$

or

$$p_{2} - p_{1} = \frac{10^{1.9068 - 0.78036 \log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2} \rho_{f} v_{piston}^{2} D_{piston}^{4} L_{piston flank}}{\left(D_{chamber} - D_{piston}\right)^{3} \left(D_{chamber} + D_{piston}\right)^{2}}$$
(4.76)

Again substituting Equation 4.76 into Equation 4.74 we obtain

$$F_{em} = \left(\frac{\pi \rho_{f} v_{piston}^{2} D_{piston}^{2}}{8}\right) 10^{1.9068 - 0.78036 \log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2}}$$

$$+ \frac{0.0198\pi D_{piston} L_{piston} f_{lank} \rho_{f}^{0.75} \mu^{0.25} \left[v_{piston} \frac{D_{piston}^{2}}{\left(D_{chamber}^{2} - D_{piston}^{2}\right)}\right]^{1.75}}{\left(D_{chamber} - D_{piston}\right)^{0.25}}$$

$$+ \frac{D_{piston}^{2}}{4} \left(\frac{1.9068 - 0.78036 \log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} v_{piston} D_{piston}}{\mu}\right)\right]^{2} \rho_{f} v_{piston}^{2} D_{piston}^{4} L_{piston} f_{lank}}{\left(D_{chamber} - D_{piston}\right)^{3} \left(D_{chamber} + D_{piston}\right)^{2}}\right)$$

for turbulent flow.

Equations 4.75 and 4.77 are the governing equations for viscosity measurement in laminar and turbulent flow. Now we consider the laminar flow case. Extracting  $\mu v_{piston}$  from terms on the right-hand side of Equation 4.75 yields

$$F_{em} = \mu v_{piston} \left[ 3\pi D_{piston} + \frac{12\pi L_{piston flank} D_{piston}^3 D_{chamber}}{\left( D_{chamber} - D_{piston} \right)^3 \left( D_{chamber} + D_{piston} \right)} \right] (4.78)$$

Piston velocity can be expressed as

$$v_{piston} = \frac{L_{chamber}}{t} \tag{4.79}$$

where

 $L_{chamber}$  = Chamber length,

t = Piston travel time from one end of chamber length to the other,

Substituting Equation 4.79 into Equation 4.78 and recasting gives

$$\mu = \frac{F_{em}t}{L_{chamber} \left[ 3\pi D_{piston} + \frac{12\pi L_{piston flank} D_{piston}^{3} D_{chamber}}{\left( D_{chamber} - D_{piston} \right)^{3} \left( D_{chamber} + D_{piston} \right)} \right]}$$
(4.80)

Equation 4.80 indicates that under laminar flow condition fluid viscosity can be estimated by recording the travel time, assuming the geometry of piston and chamber, and electromagnetic force are given. After a thorough review of "viscous drag" paper (Cambridge Viscosity Inc., 2010) provided by the manufacturer-Cambridge we found that Cambridge derived an equation that is similar to Equation 4.80 for laminar flow. It should be noted that the derivation in the "viscous drag" paper is not completely shown. Therefore we cannot check its validity.

For turbulent flow, substituting Equation 4.79 into Equation 4.77 we have

$$F_{em} = \left(\frac{\pi \rho_{f} L_{chamber}^{2} D_{piston}^{2}}{8t^{2}}\right) 10^{1.9068-0.78036 \log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right)\right]^{2}}$$

$$+ \frac{0.0198 \pi D_{piston} L_{piston} \int_{lank} \rho_{f}^{0.75} \mu^{0.25} \left[\frac{D_{piston}^{2} L_{chamber}}{t \left(D_{chamber}^{2} - D_{piston}^{2}\right)}\right]^{1.75}}{\left(D_{chamber} - D_{piston}\right)^{0.25}}$$

$$+ \frac{D_{piston}^{2}}{4} \left(\frac{1.9068-0.78036 \log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right)\right]^{2}}{\left(D_{chamber} - D_{piston}\right)^{3} \left(D_{chamber} + D_{piston}\right)^{2} t^{2}}\right)$$

or

$$F_{em} = \left(\frac{\pi \rho_{f} L_{chamber}^{2} D_{piston}^{2}}{8t^{2}}\right) 10^{1.9068-0.78036 \log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right) + 0.117434 \left[\log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right)\right]^{2}} \\ + \frac{0.0198 \pi \rho_{f}^{0.75} \mu^{0.25} D_{piston}^{4.5} L_{chamber}^{1.75} L_{piston flank}}{(D_{chamber} - D_{piston})^{2} (D_{chamber} + D_{piston})^{1.75} t^{1.75}} \\ + \frac{\pi 10}{4 (D_{chamber} - D_{piston})^{2} (D_{chamber} D_{piston}) + 0.117434 \left[\log \left(\frac{\rho_{f} L_{chamber} D_{piston}}{\mu l}\right)\right]^{2} \rho_{f} D_{piston}^{6} L_{chamber}^{2} L_{piston flank}}{4 (D_{chamber} - D_{piston})^{3} (D_{chamber} + D_{piston})^{2} t^{2}}$$

Since the viscosity,  $\mu$ , cannot be separated from time, t, in Equation 4.81, the estimation of viscosity can only be done by solving Equation 4.81 implicitly. A trial and error method would be used to build a relationship between viscosity and travel time. After the relationship is constructed viscosity can be measured by recording the one-way travel time. Another difficulty for turbulent flow is that fluid density at interested condition must be known. Therefore the measurement of fluid density need to be run simultaneously, otherwise density will be calculated through an equation-of-states, which requires the composition of fluid. To eliminate the complexity turbulent flow should be avoided during the experiment. The manufacturer did not provided information about the application of viscometer under the turbulent flow condition.

## 4.4 Calibration of Experimental Data

#### 4.4.1 Raw data and the Manufacturer's Converted Equation

Apparently the raw data from experiment is not true gas viscosity if we note the big difference between raw viscosity data and NIST values in both methane and nitrogen viscosity at different pressures and temperatures in Figures 4-13 through 4-16. The manufacturer did not provide the proprietary equation that leads to the raw data. Therefore we do not know the relationship between piston traveling time and raw viscosity data in this black box. Since the raw measured viscosity reading directly from the viscometer is not the true gas viscosity, the manufacturer of Cambridge viscometer provided an equation to convert the raw data to what they believe is true gas viscosity. The equation to correct the pressure effect is

$$\eta_{c,p} = \eta_M * ((A + 4.61E - 05 * P) / A)^{2.875}.$$
 (4.82)

where

p = Pressure, psia

 $\eta_M$  = Measured viscosity, cp

 $\eta_{c,p}$  =P-corrected viscosity, cp

A = Annulus (measurement chamber diameter-piston diameter) in thousandths of an inch.

For the viscometer we used, the measurement chamber diameter is 0.314 inches, piston diameter is 0.312 inches. Therefore, A is

$$A = (0.314 - 0.312)*1000 = 2 (4.83)$$

As a result, the equation used to convert measured viscosity to corrected viscosity becomes

$$\eta_{c,p} = \eta_M * ((2 + 4.61E - 05 * P)/2)^{2.875}.$$
 (4.84)

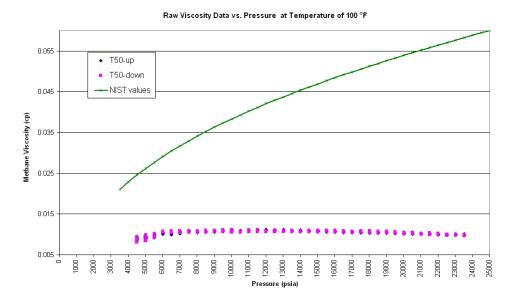


Figure 4-13. Comparison of raw viscosity data with NIST values for methane at temperature of  $100\,^{\circ}\text{F}$ 

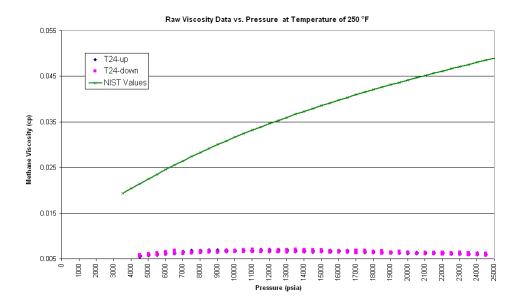


Figure 4-14. Comparison of raw viscosity data with NIST values for methane at temperature of 250  $^{\rm o}{\rm F}$ 

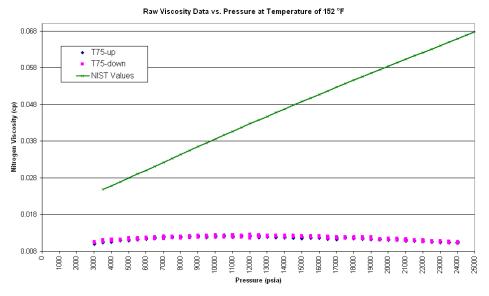


Figure 4-15. Comparison of raw viscosity data with NIST values for nitrogen at temperature of 152  $^{\rm o}{\rm F}$ 

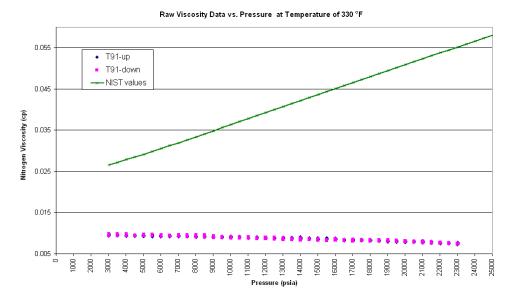


Figure 4-16. Comparison of raw viscosity data with NIST values for nitrogen at temperature of 330 °F

## 4.4.2 New Converted Equation to Convert Raw Data to True Viscosity

A close look at this equation indicates that it only considers the effect of pressure, and omits temperature. Thus the validity of this equation is needed to be checked with the available viscosity data. Comparing these converted data with NIST values for methane viscosity at temperatures of 100 and 250 °F and nitrogen viscosity at temperatures of 152 and 330 °F indicated that these converted data are not true gas viscosities (Figures 4-17 through 4-20). It is noted that the converted viscosities deviate from NIST values for both methane and nitrogen.

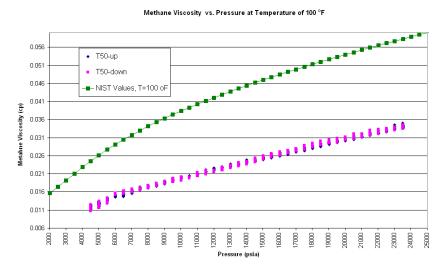


Figure 4-17. Comparison of pressure-converted methane viscosity with NIST values at temperature of 100  $^{\rm o}{\rm F}$ 

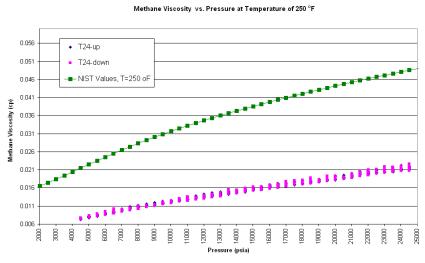


Figure 4-18. Comparison of pressure-converted methane viscosity with NIST values at temperature of 250  $^{\rm o}{\rm F}$ 

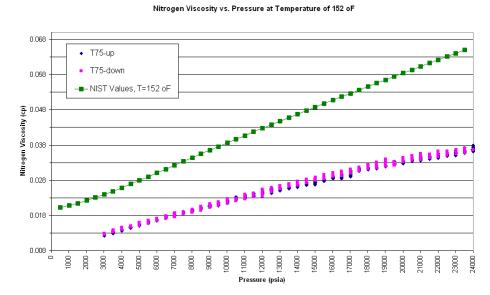


Figure 4-19. Comparison of pressure-converted nitrogen viscosity with NIST values at temperature of 152  $^{\rm o}{\rm F}$ 

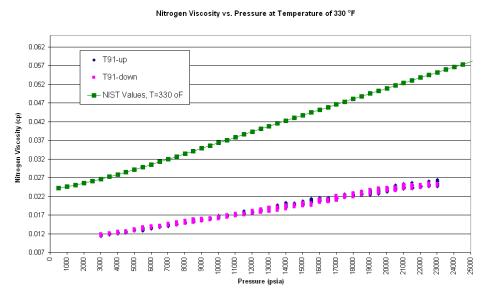


Figure 4-20. Comparison of pressure-converted nitrogen viscosity with NIST values at temperature of 330  $^{\rm o}{\rm F}$ 

Since the equation provided by manufacturer cannot convert raw data into true viscosity, a new calibration equation is necessary and vital. To be convenient, we denoted the viscosity calculated from manufacturer's equation as pressure-converted viscosity since it only consists pressure correction. The viscosity calculated from the new calibration equation we are going to develop is denoted as pressure-temperature-converted viscosity because both pressure and temperature corrections are incorporated. To develop the new equation we respect two facts: 1) obviously temperature plays a vital role. Its effect on gas viscosity cannot be neglected. So it must be included into the converted equation as pressure. 2) To honor gas viscosity at low-moderate pressure provided by former investigators, we used their data as our calibration goal since these data are agree with each other thus are accepted by most researchers. Since nitrogen and methane viscosity at moderate pressure range, 3000 to 8000 psig, had been studied thoroughly and accepted by people, we calibrated our data to the existing viscosity data at the range of 3000 to 8000 psig using pressure and temperature as variables in the calibrating equation.

The development of new equation is shown in the following steps:

# 1) Candidate database for constructing new calibration equation

As mentioned above, nitrogen and methane viscosity at moderate pressure range, 3000 to 8000 psig, had been studied thoroughly and accepted by people, we calibrated raw data to the existing viscosity data at those conditions using pressure and temperature as variables in the calibrating equation.

## 2) Raw data pre-process

For the sake of high quality data acquisition, same temperature pressure experiments are repeated. Two to seven experiments were run to check the repeatability of the viscometer. Experiments with high repeatability are chosen as the database to develop new calibration equation. Data recorded at unstable pressure and temperature are removed. Outliers are excluded. After this pre-

process, only data with good quality are input into the database for generating the new calibration equation.

## 3) Converting raw data using manufacturer's equation

Although how manufacturer came up with Equation 4.82 is a black box to us. In this work we kept Equation 4.82 to honor that manufacturer had corrected the pressure effect on viscosity. But since they omitted the temperature effect, we will implement what had left behind. Comparing pressure-converted viscosity with NIST values at pressure range of 3000 to 8000 psi as shown in Figures 4-17 through 4-20 we found that there is a gap between pressure-converted viscosity and true viscosity. So we need to find out a correlation that can convert the pressure-converted viscosity to true viscosity. This can be done by rotating the pressure-converted viscosity to the position that is parallel to true viscosity, and then apply a vertical shift to make it overlap with the true viscosity at pressure range of 3000 to 8000 psi.

## 4) Converting the pressure-converted viscosity to true viscosity

As said in step 3), the conversion requires a rotation and a vertical shift. Mathematically a non-linear regression method is applied to get the correlation due to two facts. a) the relation between slope of pressure-converted viscosity and slope of NIST values is not a simple linear-relationship, and b) The vertical shift is a function of temperature. The pressure-converted viscosities at different pressure temperature are collected (Tables 4-2 and 4-4). NIST viscosity at corresponding pressure temperature is also collected (Tables 4-3 and 4-5). A statistical analysis gave that the following term

$$\left[\frac{C_1 * Ln(T)}{T} + C_2 * Ln(T) + C_3\right] * (p - 3014.7)$$

where

p = Pressure, psia

 $T = \text{Temperature}, \, ^{\text{o}}\text{F}$ 

 $C_1$ ,  $C_2$ , and  $C_3$  = Coefficients

can rotate the pressure-converted viscosity to the position that is parallel to NIST viscosity. But the rotation still cannot match the converted viscosity with true viscosity, as a result, a vertical shift term

$$C_4 * T + C_5$$

where

 $C_4$  and  $C_5$  = Coefficients

is required so that two viscosity can overlap.

5) Determination of coefficients

The coefficients are determined by obtaining minimum variance from converted viscosity and NIST viscosity, which are

$$C_1$$
= 1.35379E-05  $C_2$ = 2.26139E-07  $C_3$ = -6.1948E-07  $C_4$ = 9.363238E-06  $C_5$ = 1.023E-03

6) Summing up all terms to get new calibration equation

Summing up pressure-corrected viscosity, rotation term, and vertical shift term we come up with the pressure-temperature-corrected viscosity, or true viscosity, which is expressed as

$$\eta_t = \eta_{c,p} + Rotation term + Vertical shift term$$

or

$$\eta_{t} = \eta_{M} * ((2 + 4.61E - 05 * P) / 2)^{2.875} 
+ \left[ \frac{1.35379E - 05 * Ln(T)}{T} + 2.26139E - 07 * Ln(T) - 6.1948E - 07 \right] 
* (p - 3014.7) + 9.363238E - 06 * T + 0.01023$$
(4.85)

where

p = Pressure, psia

 $T = \text{Temperature}, \, ^{\text{o}}\text{F}$ 

 $\eta_M$  = Raw data or measured viscosity, cp

 $\eta_t$  = True viscosity, cp

Table 4-2. Pressure-corrected nitrogen viscosity

Pressure		Temperature (°F)							
(psia)	116	134	152	170	200	250			
3014.7	0.01336	0.01324	0.01292	0.01271	0.01247	0.01212			
3514.7	0.01425	0.01384	0.01368	0.01312	0.01299	0.01252			
4014.7	0.01520	0.01443	0.01433	0.01410	0.01355	0.01312			
4514.7	0.01597	0.01527	0.01516	0.01465	0.01400	0.01359			
5014.7	0.01659	0.01581	0.01572	0.01540	0.01455	0.01409			
5514.7	0.01749	0.01659	0.01655	0.01618	0.01514	0.01460			
6014.7	0.01817	0.01722	0.01720	0.01683	0.01586	0.01507			
6514.7	0.01888	0.01790	0.01804	0.01743	0.01639	0.01537			
7014.7	0.01959	0.01861	0.01867	0.01792	0.01707	0.01576			
7514.7	0.02038	0.01936	0.01923	0.01854	0.01764	0.01635			
8014.7	0.02118	0.02015	0.01984	0.01912	0.01825	0.01694			

Table 4-2. Continued

Pressure	Temperature (°F)								
(psia)	260	280	300	330	350				
3014.7	0.012035	0.011923	0.011835	0.01129	0.010814				
3514.7	0.012456	0.012348	0.012175	0.011813	0.01123				
4014.7	0.012892	0.012733	0.012485	0.011997	0.011939				
4514.7	0.013247	0.012951	0.012718	0.012282	0.01228				
5014.7	0.013565	0.013411	0.013201	0.012656	0.012453				
5514.7	0.013873	0.013844	0.013507	0.013007	0.012727				
6014.7	0.014261	0.014277	0.013856	0.013354	0.012908				
6514.7	0.01466	0.014692	0.014293	0.013703	0.013301				
7014.7	0.015177	0.01512	0.01471	0.013952	0.013624				
7514.7	0.01569	0.01553	0.015247	0.01438	0.014048				
8014.7	0.016218	0.015946	0.015544	0.014636	0.014334				

Table 4-3. Nitrogen viscosity from NIST

Pressure	Temperature (°F)							
(psia)	116	134	152	170	200	250		
3014.7	0.02353	0.023724	0.023938	0.024169	0.024583	0.025333		
3514.7	0.024604	0.024731	0.024886	0.025065	0.025403	0.02605		
4014.7	0.025723	0.025783	0.025878	0.026002	0.02626	0.026799		
4514.7	0.026874	0.026867	0.026901	0.02697	0.027147	0.027576		
5014.7	0.028047	0.027974	0.027948	0.027961	0.028058	0.028375		
5514.7	0.029231	0.029094	0.029009	0.02897	0.028986	0.029191		
6014.7	0.030421	0.030222	0.030081	0.029989	0.029927	0.030021		
6514.7	0.031611	0.031353	0.031157	0.031014	0.030875	0.030862		
7014.7	0.032798	0.032483	0.032234	0.032042	0.031829	0.031709		
7514.7	0.033978	0.03361	0.03331	0.033071	0.032786	0.032562		
8014.7	0.035152	0.034731	0.034383	0.034098	0.033743	0.033418		

Table 4-3. Continued

Pressure	Temperature (°F)							
(psia)	260	280	300	330	350			
3014.7	0.025489	0.025806	0.026129	0.02662	0.026952			
3514.7	0.026188	0.026473	0.026765	0.027216	0.027523			
4014.7	0.026919	0.027169	0.02743	0.027838	0.02812			
4514.7	0.027677	0.027891	0.028119	0.028483	0.028738			
5014.7	0.028456	0.028634	0.028828	0.029147	0.029375			
5514.7	0.029253	0.029394	0.029555	0.029828	0.030028			
6014.7	0.030064	0.030168	0.030295	0.030522	0.030694			
6514.7	0.030885	0.030953	0.031047	0.031228	0.031372			
7014.7	0.031714	0.031746	0.031806	0.031942	0.032058			
7514.7	0.032548	0.032545	0.032573	0.032663	0.032752			
8014.7	0.033386	0.033348	0.033344	0.03339	0.033451			

Table 4-4. Pressure-corrected methane viscosity

Pressure	Temperature (°F)								
(psia)	100	120	140	160	180	188	200		
4514.7	0.01180	0.01091	0.01008	0.00949	0.00892	0.00872	0.00844		
5014.7	0.01304	0.01195	0.01098	0.01034	0.00995	0.00950	0.00894		
5514.7	0.01394	0.01289	0.01149	0.01104	0.01062	0.01026	0.00959		
6014.7	0.01547	0.01354	0.01231	0.01168	0.01124	0.01107	0.01046		
6514.7	0.01591	0.01400	0.01341	0.01238	0.01184	0.01156	0.01102		
7014.7	0.01622	0.01459	0.01415	0.01298	0.01236	0.01201	0.01163		
7514.7	0.01711	0.01521	0.01500	0.01364	0.01283	0.01254	0.01218		
8014.7	0.01774	0.01587	0.01558	0.01375	0.01354	0.01301	0.01269		

Table 4-4. Continued

Pressure	Temperature (°F)							
(psia)	220	225	230	250	260	280		
4514.7	0.00802	0.007977	0.007837	0.007502	0.007343	0.007072		
5014.7	0.008687	0.008627	0.0085	0.007961	0.007856	0.007505		
5514.7	0.009226	0.009111	0.008954	0.008435	0.008353	0.00798		
6014.7	0.009758	0.009669	0.009475	0.008902	0.008819	0.008413		
6514.7	0.010405	0.010208	0.009997	0.009339	0.009286	0.008892		
7014.7	0.010717	0.010633	0.010504	0.00983	0.009647	0.009296		
7514.7	0.011451	0.011093	0.010897	0.010291	0.010079	0.009679		
8014.7	0.011816	0.011747	0.011352	0.010727	0.010605	0.010097		

Table 4-4. Continued

Pressure	Temperature (°F)							
(psia)	300	320	340	360	380	415		
4514.7	0.006833	0.006619	0.00615	0.006281	0.006134	0.005942		
5014.7	0.007186	0.006821	0.006531	0.006593	0.00639	0.006176		
5514.7	0.007579	0.007169	0.00709	0.006909	0.006657	0.006376		
6014.7	0.00794	0.007546	0.007484	0.00726	0.007018	0.006591		
6514.7	0.008369	0.007955	0.007757	0.007485	0.007176	0.006885		
7014.7	0.008705	0.008299	0.007987	0.007671	0.007413	0.007084		
7514.7	0.009026	0.008634	0.008245	0.007983	0.007652	0.007294		
8014.7	0.009376	0.008916	0.008583	0.008143	0.0079	0.007536		

Table 4-5. Methane viscosity from NIST

Pressure	Temperature (°F)								
(psia)	100	120	140	160	180	188	200		
4514.7	0.02454	0.02377	0.02315	0.02265	0.02226	0.02212	0.02195		
5014.7	0.02615	0.02529	0.02459	0.02401	0.02353	0.02337	0.02315		
5514.7	0.02766	0.02674	0.02596	0.02531	0.02477	0.02458	0.02433		
6014.7	0.02909	0.02811	0.02728	0.02657	0.02597	0.02576	0.02546		
6514.7	0.03045	0.02941	0.02853	0.02777	0.02712	0.02688	0.02656		
7014.7	0.03173	0.03065	0.02972	0.02892	0.02822	0.02797	0.02763		
7514.7	0.03296	0.03184	0.03086	0.03002	0.02928	0.02902	0.02865		
8014.7	0.03412	0.03297	0.03196	0.03108	0.03031	0.03003	0.02963		

Table 4-5. Continued

Pressure	Temperature (°F)							
(psia)	220	225	230	250	260	280		
4514.7	0.021708	0.021658	0.021612	0.02146	0.021401	0.021315		
5014.7	0.022844	0.022778	0.022716	0.022503	0.022416	0.022277		
5514.7	0.023958	0.023877	0.0238	0.023533	0.02342	0.023231		
6014.7	0.025042	0.024949	0.024859	0.024541	0.024405	0.02417		
6514.7	0.026095	0.025989	0.025888	0.025526	0.025367	0.025091		
7014.7	0.027113	0.026997	0.026886	0.026483	0.026305	0.025991		
7514.7	0.028098	0.027972	0.027852	0.027412	0.027217	0.026868		
8014.7	0.029049	0.028916	0.028786	0.028314	0.028102	0.027722		

Table 4-5. Continued

Pressure		Temperature (°F)							
(psia)	300	320	340	360	380	415			
4514.7	0.021266	0.021246	0.021253	0.021282	0.021331	0.021456			
5014.7	0.022178	0.022113	0.022078	0.022069	0.022082	0.022151			
5514.7	0.023085	0.022978	0.022904	0.022858	0.022837	0.022851			
6014.7	0.023983	0.023835	0.023724	0.023643	0.023589	0.023551			
6514.7	0.024864	0.02468	0.024534	0.02442	0.024336	0.024248			
7014.7	0.025728	0.02551	0.025331	0.025187	0.025073	0.024939			
7514.7	0.026572	0.026322	0.026113	0.02594	0.0258	0.025622			
8014.7	0.027395	0.027116	0.026879	0.02668	0.026514	0.026294			

The new calibration equation is applied to converted measured viscosity (or raw data) to pressure-temperature-corrected viscosity for the measurement at condition of pressure from 3000 to 25000 psig and temperature from 98 to 415 °F. Figures 4-21 through 4-24 illustrate the comparisons of converted gas viscosity using the new correlation with NIST values for methane viscosity at temperatures of 100 and 250 °F and nitrogen at temperatures of 152 and 330 °F. These comparisons indicate that converted viscosities are close to NIST values at pressure range of 3000 to 8000 psig for both methane and nitrogen as expected. Thus raw data are converted to gas viscosity using the new converted equation obtained from our analysis. It should be borne in mind that Equation 4.85 can only be valid for this specific viscometer used in this investigation.

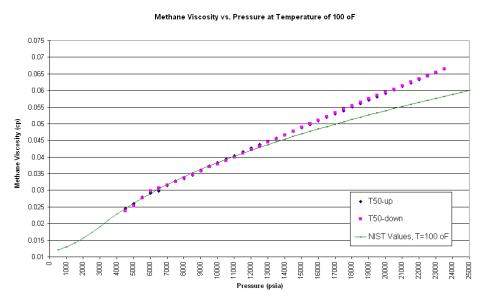


Figure 4-21. Comparison of pressure-temperature-converted methane viscosity with NIST values at temperature of 100 °F

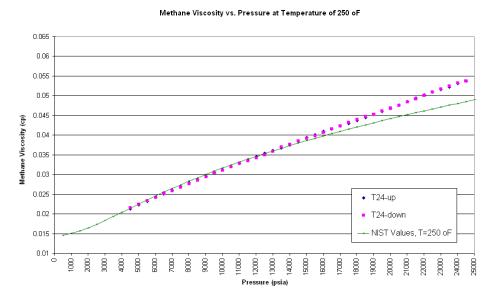


Figure 4-22. Comparison of pressure-temperature-converted methane viscosity with NIST values at temperature of 250  $^{\rm o}{\rm F}$ 

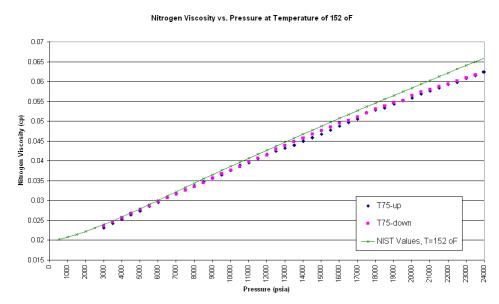


Figure 4-23. Comparison of pressure-temperature-converted nitrogen viscosity with NIST values at temperature of 152  $^{\rm o}{\rm F}$ 

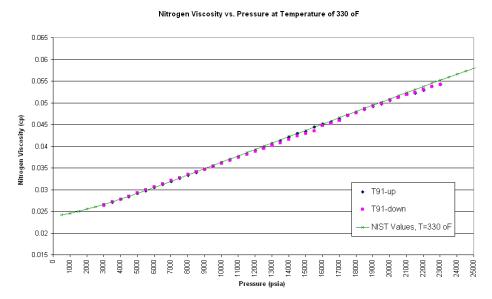


Figure 4-24. Comparison of pressure-temperature-converted nitrogen viscosity with NIST values at temperature of 330  $^{\rm o}{\rm F}$ 

#### **CHAPTER V**

## **EXPERIMENTAL RESULTS**

## **5.1 Nitrogen Viscosity Measurement**

The nitrogen is prepared by ACETYLENE OXYGEN Co.. The mole fraction of nitrogen is 99.95%. Initial pressure in the gas tank is 1500 psig. Lots of efforts were investigated on nitrogen viscosity. There are totally 91 tests on nitrogen viscosity. Measuring condition is at pressures range from 3000 to 24500 psig with interval of 500 psi and at temperatures of 99, 105, 109, 111, 116, 134, 152, 165, 170, 174, 187, 200, 250, 260, 280, 300, 330, and 350 °F. Table 5-1 lists the experiments we had done on measuring nitrogen viscosity. Experiment data are used to develop the new converted equation. The more experiments we did on nitrogen, the more confident we are on the new converted equation. These experimental data are also used to develop a new gas viscosity correlation that is specified for nitrogen viscosity.

Table 5-1. Statistic of nitrogen viscosity experiment in this study

Composition	Temperature	Pressure	No. of Experiment
	°F	psia	
$N_2$	99	3014.7-13514.7	4
$N_2$	105	3014.7-14014.7	3
$N_2$	109	3014.7-13514.7	3
$N_2$	111	3014.7-14014.7	3
$N_2$	116	3014.7-23014.7	7
$N_2$	134	3014.7-22014.7	14
$N_2$	151	3014.7-13514.7	3
$N_2$	152	3014.7-24014.7	10
$N_2$	165	3014.7-15514.7	3
$N_2$	170	3014.7-23514.7	11
$N_2$	174	3014.7-15014.7	4
$N_2$	187	3014.7-17014.7	2
$N_2$	200	3014.7-24514.7	6
$N_2$	250	3014.7-22514.7	4
$N_2$	260	3014.7-24514.7	6
$N_2$	280	3014.7-24514.7	2
$N_2$	300	3014.7-24514.7	2
N <sub>2</sub>	330	3014.7-23514.7	2
$N_2$	350	3014.7-24514.7	2

#### **5.2 Nitrogen Viscosity Analysis**

Comparing lab data from this study with NIST values and data from other investigators illuminated that extrapolating correlation based on low-moderate pressure/temperature to HPHT yields unacceptable result. For all experiments on nitrogen viscosity, lab data deviated from NIST value at high pressure at temperature of 116 °F (Figures 5-1 to 5-4). Similar result can be observed for temperature of 134, 152, 170, 200, 250, 260, 280, 300, 330, and 350 °F as show in Figures A-1 to A-27 in Appendix *A*. The deviation of NIST values from experimental data can be as high as 4.91% at pressure higher than 25014.7 psia. At high pressure nitrogen viscosities from lab are lower than NIST values. The difference between lab data and NIST values increases as pressure increases. This

difference at high pressure indicates that existing correlation cannot provide accurate viscosity to optimize the production of gas reservoirs with moderate-high nitrogen concentration at HPHT.

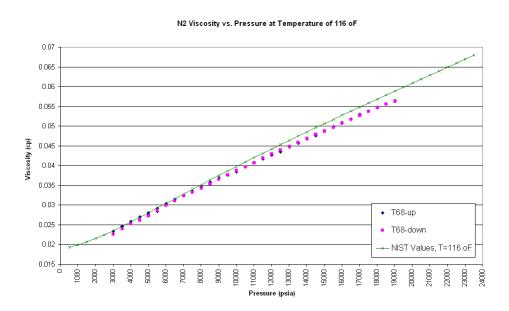


Figure 5-1. Nitrogen viscosity vs. pressure at 116 °F (Test 68)

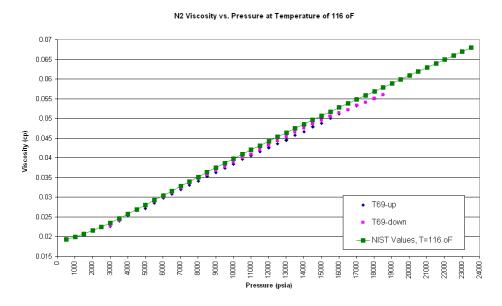


Figure 5-2. Nitrogen viscosity vs. pressure at 116 °F (Test 69)

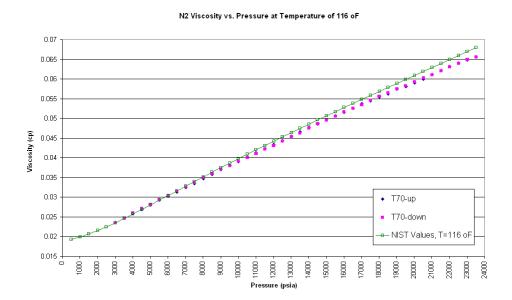


Figure 5-3. Nitrogen viscosity vs. pressure at 116 °F (Test 70)

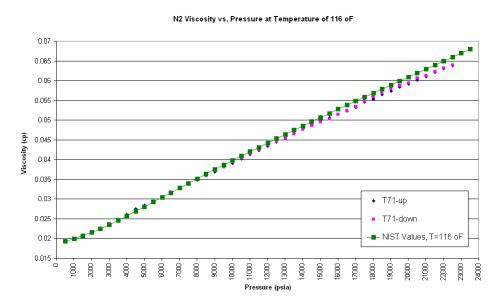


Figure 5-4. Nitrogen viscosity vs. pressure at 116 °F (Test 71)

Nitrogen, as a non-hydrocarbon, shows different thermodynamics properties from normal paraffins. Its viscosity varying with pressure and temperature does not follow the theorem of corresponding state as we see in hydrocarbon. So far no correlation is available to estimate nitrogen viscosity. A correlation that is particular for nitrogen viscosity is highly desirable and urgent as we encounter more and more high nitrogen HPHT gas reservoir. To develop this correlation we consider the both convenience and popularity. Since Lee-Gonzalez-Eakin correlation is one of the most common used viscosity correlations in petroleum engineering and easy to be coded into a program, we employed the same form as Lee-Gonzalez-Eakin correlation and changed the coefficients so that the new correlation can be used for nitrogen viscosity only. Database used to develop correlation consists of both literature experimental data and our lab data. A non-linear regression method was applied in preparing the correlation. Therefore, the nitrogen viscosity correlation gives a very convenient way to determine nitrogen viscosity at a large range of pressure temperature condition.

To illustrate the importance of our lab data and correlation, Nitrogen viscosities from new correlation are compared with Lee-Gonzalez-Eakin correlation and NIST values. In the comparison, viscosity at temperatures of 116, 200, 300, and 350 °F and pressure from 3514.7 to 25014.7 psia are selected to investigate the effect of pressure and temperature. Considering the observation that Lee-Gonzalez-Eakin correlation shows exponential increase of nitrogen viscosity as pressure increases, which deviates radically from both lab data and NIST value (Figures 5-5 through 5-8), we concluded that Lee-Gonzalez-Eakin correlation is inappropriate for nitrogen viscosity. As a result we switched to the comparison between our data with NIST values. Two observations were made basing on the comparison:

- 1) Our nitrogen viscosity is lower than NIST values at high pressure region
- 2) For same temperature, the nitrogen viscosity difference becomes larger as pressure increases

Error analysis in Table 5-2 indicates that even the absolute error is low, the relative error can be as high as 4.91% at temperature of 200 °F and pressure of 23514.7 psia. It should be noted that data in this study are used as base for both absolute error and relative error. Figures 5-9 through 5-12 show the comparisons between new correlation and NIST values.

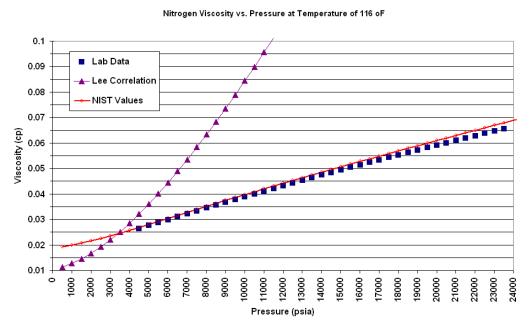


Figure 5-5. Lee-Gonzalez-Eakin correlation is inappropriate for nitrogen viscosity at temperature of 116  $^{\rm o}{\rm F}$ 

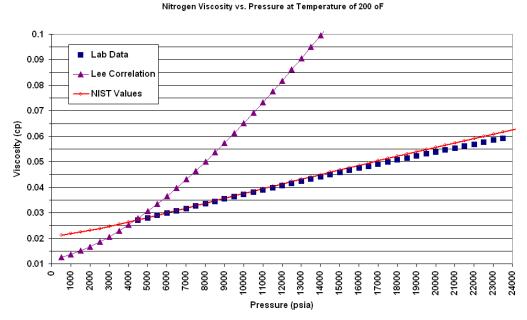


Figure 5-6. Lee-Gonzalez-Eakin correlation is inappropriate for nitrogen viscosity at temperature of 220  $^{\rm o}{\rm F}$ 

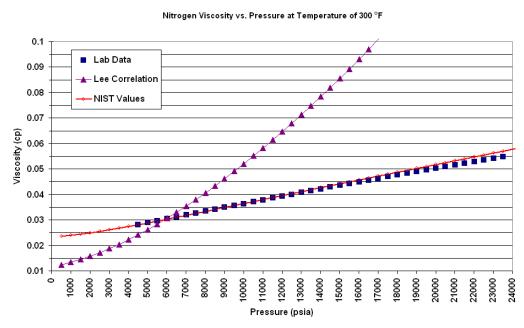


Figure 5-7. Lee-Gonzalez-Eakin correlation is inappropriate for nitrogen viscosity at temperature of 300  $^{\rm o}{\rm F}$ 

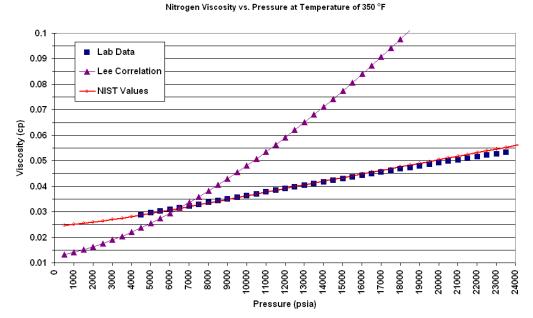


Figure 5-8. Lee-Gonzalez-Eakin correlation is inappropriate for nitrogen viscosity at temperature of 350  $^{\rm o}{\rm F}$ 

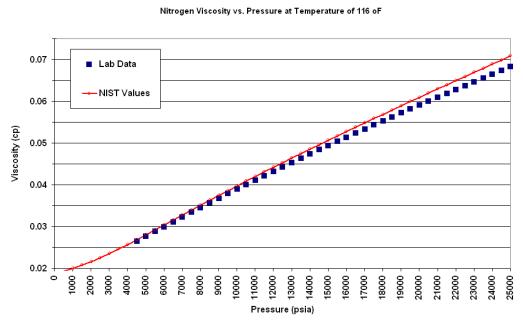


Figure 5-9. Comparison between new correlation and NIST values at temperature of 116  $^{\rm o}{
m F}$ 

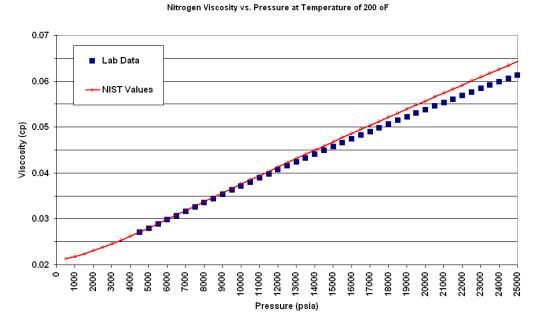


Figure 5-10. Comparison between new correlation and NIST values at temperature of  $200\,^{\circ}\text{F}$ 

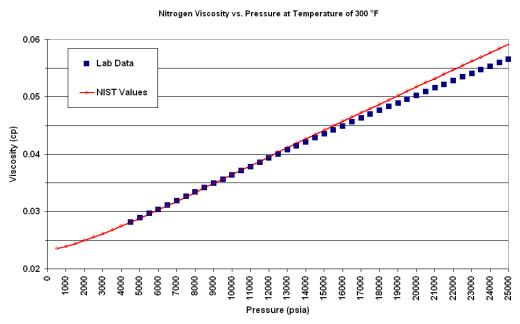


Figure 5-11. Comparison between new correlation and NIST values at temperature of 300  $^{\rm o}{\rm F}$ 

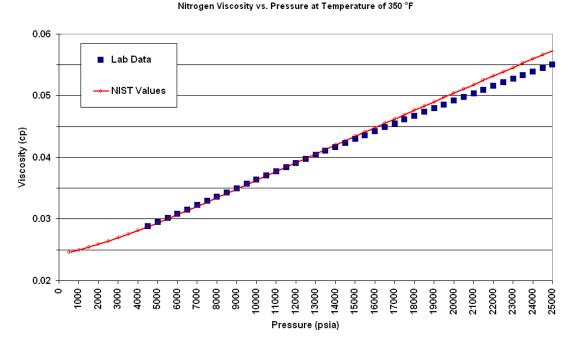


Figure 5-12. Comparison between new correlation and NIST values at temperature of 350 °F

Temperature	Abso	olute Error	(cp)	Relative Error (%)			
(°F)	Pre	essure (psi	a)	Pre	ssure (ps	ia)	
	10015	10015 20015 23515			20015	23515	
		NIST					
116	0.00082	0.00188	0.00263	2.0962	3.1841	3.8554	
200	0.00044	0.00193	0.00301	1.1927	3.5843	4.9099	
300	0.00008	0.00150	0.00262	0.2158	2.9869	4.6299	
350	-0.00005	0.00126	0.00234	-0.1332	2.5626	4.2463	

Table 5-2. Error analysis for nitrogen viscosity from NIST program

# 5.3 Methane Viscosity Measurement

Methane used in the experiment is provided by MATHESON TRIGAS Inc.. The mole fraction of methane is 99.98%. Initial pressure in the gas tank is 1500 psig. Measurement had been done at pressure range from 4500 to 25000 psig and temperature of 100, 120,

140, 160, 180, 188, 200, 220, 225, 230, 250, 260, 280, 300, 320, 340, 360, 380, and 415 °F. Again, Table 5-3 lists the experiments we had done on measuring methane viscosity. Totally 50 experiments had been run in order to prepare an abundant dataset for our gas viscosity correlation.

Table 5-3. Statistic of methane viscosity experiment in this study

Composition	Temperature	Pressure	No. of Experiment
_	°F	psia	-
CH <sub>4</sub>	100	4514.7-25014.7	2
CH <sub>4</sub>	111	4014.7-24014.7	2
CH <sub>4</sub>	120	4514.7-24514.7	2
CH <sub>4</sub>	131	4514.7-23514.7	2
CH <sub>4</sub>	140	4514.7-25014.7	2
CH <sub>4</sub>	151	4514.7-24514.7	4
CH <sub>4</sub>	160	4514.7-25014.7	2
CH <sub>4</sub>	171	4514.7-24514.7	3
CH <sub>4</sub>	180	4514.7-25014.7	2
CH <sub>4</sub>	188	4514.7-24514.7	3
CH <sub>4</sub>	200	4014.7-24514.7	3
CH <sub>4</sub>	220	5014.7-25014.7	3
CH <sub>4</sub>	225	4514.7-25014.7	1
CH <sub>4</sub>	230	4514.7-24514.7	1
CH <sub>4</sub>	250	4514.7-24514.7	2
CH <sub>4</sub>	260	4514.7-25014.7	2
CH <sub>4</sub>	280	4514.7-25014.7	2
CH <sub>4</sub>	300	4514.7-24514.7	2
CH <sub>4</sub>	320	4514.7-25014.7	2
CH <sub>4</sub>	340	4514.7-25014.7	2
CH <sub>4</sub>	360	4514.7-24514.7	2
CH <sub>4</sub>	380	4514.7-25014.7	2
CH <sub>4</sub>	415	4514.7-24514.7	2

### **5.4 Methane Viscosity Analysis**

Same as the procedure to analyze nitrogen, lab data are compared with NIST values and data (low-moderate pressure/temperature) from other investigators. Through the comparison, we found that lab data match with NIST values at low-moderate pressure, but at high pressure methane viscosities from lab are higher than NIST values for the experiments at temperature of 100 °F (Figures 5-13 to 5-14). Similar result can be observed for temperature of 120, 140, 160, 180, 188, 200, 220, 225, 230, 250, 260, 280, 300, 320, 340, 360, 380, and 415 °F as show in Figures B-1 to B-37 in Appendix B. The difference between lab data and NIST values decreases as temperature increases; this difference increases as pressure increases.

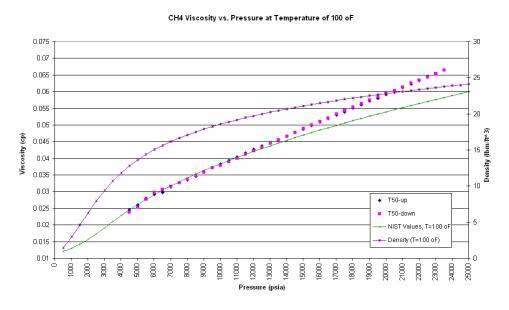


Figure 5-13. Methane viscosity vs. pressure at 100 °F (Test 50)

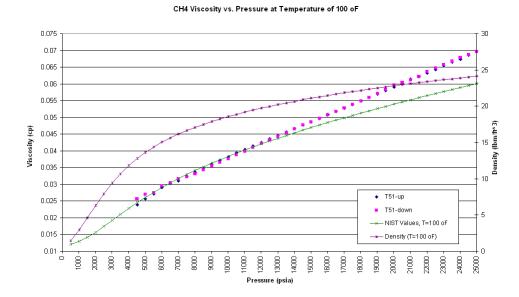


Figure 5-14. Methane viscosity vs. pressure at 100 °F (Test 51)

As we mentioned before, we developed our new correlation in the same form as Lee-Gonzalez-Eakin correlation. Lee-Gonzalez-Eakin correlation is based on low-moderate pressure experimental data and proved to be not accurate enough at HPHT by our experiment results. Again, easy to be used and coded into computer program are our top priority in constructing new correlation. Basing on our experiment result and existing viscosity data at low pressure, a modified Lee-Gonzalez-Eakin gas viscosity correlation was constructed using non-linear regression method. This correlation covers larger pressure and temperature range than available correlations. Therefore, it gives more confidence on estimating gas viscosity.

The significance of this correlation is testified by the comparison our viscosity with Lee-Gonzalez-Eakin correlation, NIST values, and Viswanathan correlation. In the comparison, viscosity at temperatures of 100, 200, 300, and 415 °F are selected to investigate the effect of pressure and temperature. These comparisons indicate that at high pressure, new correlation gives higher methane viscosity than Lee-Gonzalez-Eakin correlation, NIST values, and Viswanathan correlation. The difference becomes smaller

as temperature increases, while as pressure increases, the difference increases. The relative error at low temperature such as 100 °F can be up to -10.12%, -11.03%, and -16.13% for Lee-Gonzalez-Eakin correlation, NIST, and Viswanathan, respectively. At high temperature such as 415 °F the relative error can be as high as -2.47%, -9.12%, and -11.01% for Lee-Gonzalez-Eakin correlation, NIST, and Viswanathan, respectively. Table 5-4 shows the results of error analysis. It should be noted that data in this study are used as base for both absolute error and relative error. Figures 5-15 through 5-18 show the comparisons methane viscosity in this study with existing correlations.

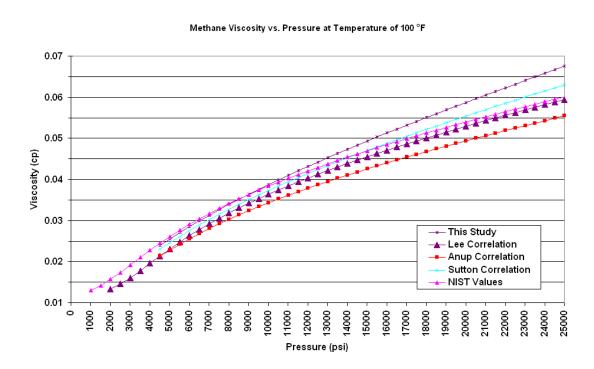


Figure 5-15. Comparison this study with existing correlations at temperature of 100 °F

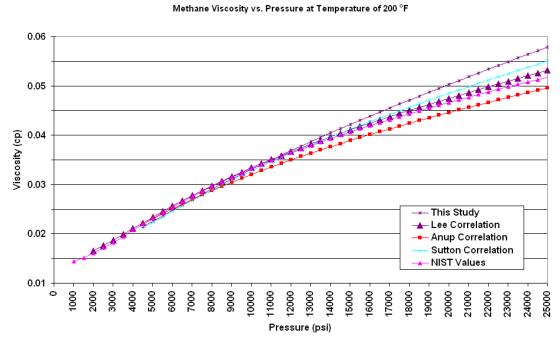


Figure 5-16. Comparison this study with existing correlations at temperature of 200 °F

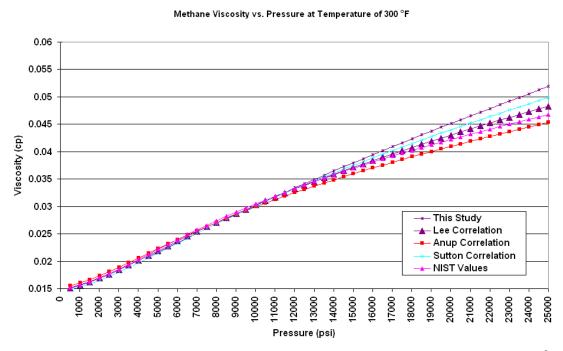


Figure 5-17. Comparison this study with existing correlations at temperature of 300  $^{\rm o}{\rm F}$ 

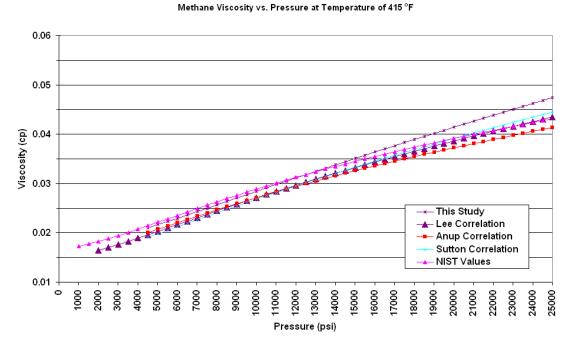


Figure 5-18. Comparison this study with existing correlations at temperature of 415 °F

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Table 5-4.	Error anai	IVSIS 10	r metnane	VISCOSILV	irom	amerent	correlations

Temperature		solute Error (			ative Error	· /
(°F)	F	Pressure (psia	.)	P	ressure (psi	a)
	10015	20015	25015	10015	20015	25015
		Lee-(	Gonzalez-Eal	kin Correlat	ion	
100	-0.00032	-0.00444	-0.00683	-0.82	-7.56	-10.12
200	0.00028	-0.00281	-0.00472	0.85	-5.59	-8.16
300	0.00095	-0.00131	-0.00282	3.16	-2.89	-5.44
415	0.00161	0.00002	-0.00118	4.63	0.04	-2.47
			NIST Pro	gram		
100	-0.00038	-0.00479	-0.00744	-0.98	-8.15	-11.03
200	0.00013	-0.00366	-0.00611	0.38	-7.27	-10.55
300	0.00031	-0.00291	-0.00514	1.04	-6.45	-9.91
415	0.00042	-0.00234	-0.00437	1.46	-5.60	-9.12
		V	'iswanathan <b>(</b>	Correlation		
100	-0.00261	-0.00810	-0.01089	-6.74	-13.79	-16.13
200	-0.00107	-0.00572	-0.00829	-3.23	-11.36	-14.31
300	-0.00024	-0.00418	-0.00655	-0.78	-9.26	-12.63
415	0.00027	-0.00307	-0.00527	0.94	-7.36	-11.01

#### **CHAPTER VI**

## **NEW GAS VISCOSITY CORRELATIONS**

#### 6.1 Nitrogen Viscosity Correlation

The aforementioned differences for both nitrogen and methane at high pressure indicate that available correlations give unacceptable result at HPHT. Two gas viscosity correlations were developed upon the completed experiments on methane and nitrogen viscosity. One is specified for methane viscosity to honor the importance of methane in HPHT gas reservoirs; another is tailored for nitrogen considering the fact that some HPHT reservoirs contain significant amount of nitrogen.

Due to the lack of nitrogen viscosity data at HPHT and correlation that is suitable for nitrogen viscosity, a correlation that provides accurate nitrogen viscosity is preferred. Since Lee-Gonzalez-Eakin correlation is one of the most common used viscosity correlations in petroleum engineering and can be coded into computer program easily, we developed a correlation that has the same form as Lee-Gonzalez-Eakin correlation. The coefficients in the correlation were updated using NIST values and lab data from our experiment. Due to the fact that we do not have viscosity data at pressure from 500 to 2999 psi in our experiment, NIST values at this pressure range were used. As we already showed in Chapter II, NIST values match with lab data very well at pressure from 500 to 2999 psi. Combining NIST values at pressure from 514.7 to 2514.7 psia with our lab data at pressure from 3014.7 to 24514.7 psia the coefficients were determined, and then the final form of correlation was developed. This correlation is tailored for nitrogen viscosity. It is expressed as:

$$\mu_g = K \exp(X \rho_g^Y). \tag{6.1}$$

$$K = \frac{0.0001 * (9.206483 + 3.550036M_w) T^{1.217156}}{208.9852 + 18.70586M_w + T}.$$
 (6.2)

where

$$X = -3.41179 + \left\lceil \frac{999.9949}{T} \right\rceil + 0.14457226 M_w. \tag{6.3}$$

$$Y = 1.293365 + 0.11245X. (6.4)$$

where

 $\mu_g$  = Gas viscosity, cp

 $\rho_g$  = Gas density, g/cc

 $M_W$  = Molecular weight

T = Temperature, R

New correlation that based on lab data and NIST values (Table 6-1) covers larger pressure and temperature. It eliminated the embarrassment fact of lacking correlation to calculate nitrogen viscosity. Thus it provided an easy but reliable approach to determine nitrogen viscosity when petroleum engineers deal with high nitrogen HPHT reservoir.

Table 6-1. Data used to develop nitrogen viscosity correlation

Pressure		Temperature (oF)					
(psia)	116	134	152	170	200	250	
514.7	0.019345	0.019771	0.020193	0.02061	0.021296	0.022414	
1014.7	0.01999	0.020387	0.020783	0.021177	0.021828	0.022897	
1514.7	0.020736	0.021096	0.021457	0.02182	0.022426	0.023433	
2014.7	0.021582	0.021894	0.022213	0.022537	0.023088	0.02402	
2514.7	0.022518	0.022773	0.023043	0.023323	0.023809	0.024654	
3014.7	0.023344	0.02364	0.023728	0.023941	0.024386	0.025195	
3514.7	0.024604	0.024595	0.024851	0.024699	0.025257	0.025939	
4014.7	0.025919	0.025547	0.025853	0.026036	0.026169	0.026888	
4514.7	0.027063	0.02675	0.027038	0.026937	0.026972	0.027711	
5014.7	0.028055	0.027653	0.027954	0.028042	0.027872	0.028558	
5514.7	0.029326	0.0288	0.029148	0.029168	0.028804	0.029416	
6014.7	0.030382	0.029793	0.030153	0.030173	0.02988	0.030239	
6514.7	0.031464	0.030834	0.031353	0.031124	0.030758	0.030883	
7014.7	0.032543	0.031905	0.032339	0.031971	0.031789	0.03162	
7514.7	0.033704	0.033018	0.033251	0.032947	0.032705	0.032555	
8014.7	0.034875	0.034169	0.034219	0.033878	0.033667	0.033494	
8514.7	0.035969	0.035258	0.035219	0.034711	0.034534	0.034212	
9014.7	0.037071	0.036345	0.036191	0.035596	0.035564	0.035015	
9514.7	0.038043	0.037568	0.037012	0.036507	0.036531	0.035661	
10014.7	0.039160	0.037993	0.038116	0.037269	0.037403	0.0364	
10514.7	0.040056	0.039071	0.039339	0.038284	0.038248	0.037461	
11014.7	0.041098	0.040124	0.039978	0.039276	0.039071	0.038295	
11514.7	0.042163	0.041445	0.041031	0.040181	0.039937	0.039196	
12014.7	0.043098	0.042464	0.042063	0.041123	0.04076	0.040078	
12514.7	0.044248	0.043453	0.042871	0.041906	0.04162	0.040866	
13014.7	0.045402	0.044475	0.043651	0.042836	0.042424	0.041651	
13514.7	0.046322	0.045475	0.044413	0.043746	0.043342	0.042484	
14014.7	0.047623	0.0464	0.045371	0.04461	0.044206	0.043	
14514.7	0.048683	0.047166	0.046265	0.045549	0.044919	0.043715	
15014.7	0.049568	0.048247	0.047084	0.046079	0.045791	0.044493	
Note: viscosit	ty in cp						

Table 6-1. Continued.

Pressure			Temperat	ture (°F)				
(psia)	116	134	152	170	200	250		
15514.7	0.050592	0.049266	0.048075	0.047023	0.046517	0.045475		
16014.7	0.051764	0.050264	0.049088	0.047862	0.047192	0.046351		
16514.7	0.052672	0.051207	0.049954	0.048649	0.048031	0.047241		
17014.7	0.053605	0.05222	0.050862	0.049491	0.048815	0.048091		
17514.7	0.054731	0.053216	0.052445	0.050268	0.049518	0.048763		
18014.7	0.055697	0.054021	0.053098	0.051093	0.050487	0.049704		
18514.7	0.056688	0.054946	0.053637	0.051915	0.051173	0.050559		
19014.7	0.057709	0.055809	0.054551	0.052777	0.051948	0.05102		
19514.7	0.058486	0.056899	0.055435	0.053651	0.053018	0.051942		
20014.7	0.059449	0.057801	0.056138	0.054433	0.053677	0.052681		
20514.7	0.060453	0.058634	0.057104	0.055233	0.054713	0.053849		
21014.7	0.061207	0.059407	0.057874	0.05592	0.055375	0.054375		
21514.7	0.062227	0.060503	0.058565	0.056644	0.05594	0.055036		
22014.7	0.063335	0.061437	0.059415	0.057361	0.056725	0.05572		
22514.7	0.064221	-	0.060009	0.057992	0.057472	0.056405		
23014.7	0.065187	-	0.060928	0.058939	0.058197	0.057207		
23514.7	0.065890	-	0.061715	0.059527	0.058906	0.057812		
24014.7	-	-	0.062615	0.060454	0.059759	-		
24514.7	-	-		-	0.060374	-		
Note: viscos	Note: viscosity in cp							

Table 6-1. Continued

Pressure		Temperature (°F)						
(psia)	260	280	300	330	350			
514.7	0.022634	0.023071	0.023502	0.024142	0.024562			
1014.7	0.023108	0.023528	0.023945	0.024563	0.024971			
1514.7	0.023633	0.024033	0.024431	0.025023	0.025416			
2014.7	0.024207	0.024583	0.024958	0.025521	0.025895			
2514.7	0.024827	0.025175	0.025525	0.026054	0.026408			
3014.7	0.025341	0.025691	0.0260644	0.026213	0.026199			
3514.7	0.02611	0.026465	0.0267543	0.027087	0.026968			
4014.7	0.026895	0.027199	0.0274147	0.027623	0.02803			
4514.7	0.027598	0.027766	0.0279982	0.028261	0.028724			
5014.7	0.028265	0.028575	0.0288316	0.028986	0.029251			
5514.7	0.028922	0.029357	0.0294874	0.029689	0.029879			
6014.7	0.029657	0.03014	0.0301861	0.030388	0.030412			
6514.7	0.030405	0.030904	0.0309738	0.031089	0.031159			
7014.7	0.03127	0.031681	0.0317405	0.03169	0.031836			
7514.7	0.032132	0.03244	0.0326275	0.032471	0.032612			
8014.7	0.033008	0.033206	0.0332753	0.033078	0.033252			
8514.7	0.033814	0.034034	0.0340652	0.033856	0.033951			
9014.7	0.034548	0.034817	0.0348356	0.034723	0.034644			
9514.7	0.035435	0.03552	0.0355664	0.035516	0.035391			
10014.7	0.036164	0.036352	0.0362704	0.036222	0.03619			
10514.7	0.036966	0.037109	0.037045	0.03689	0.036907			
11014.7	0.03794	0.037968	0.0377955	0.037683	0.037543			
11514.7	0.038501	0.038726	0.0385455	0.038204	0.038125			
12014.7	0.039358	0.03951	0.0392036	0.039061	0.038825			
12514.7	0.040237	0.040282	0.0399718	0.039725	0.039535			
13014.7	0.041008	0.041068	0.0406165	0.040374	0.040161			
13514.7	0.041758	0.041772	0.0412419	0.041066	0.040862			
14014.7	0.04249	0.042391	0.0420897	0.041731	0.041482			
14514.7	0.043394	0.04311	0.0427644	0.042345	0.042209			
15014.7	0.044105	0.043879	0.0434234	0.043255	0.042845			
Note: vise	cosity in cp							

Table 6-1. Continued

Pressure		Те	emperature (°	(F)	
(psia)	260	280	300	330	350
15514.7	0.04482	0.044519	0.0440919	0.043831	0.043588
16014.7	0.04556	0.045284	0.0447748	0.044429	0.044109
16514.7	0.046467	0.046077	0.0455216	0.045059	0.044793
17014.7	0.047162	0.046819	0.0460829	0.04561	0.045602
17514.7	0.047831	0.047445	0.0468567	0.046205	0.046173
18014.7	0.048523	0.048267	0.0473977	0.047103	0.046742
18514.7	0.049305	0.048955	0.0483329	0.047899	0.047433
19014.7	0.050202	0.049607	0.0489835	0.048599	0.047751
19514.7	0.051041	0.050233	0.0495366	0.049106	0.048567
20014.7	0.051797	0.050873	0.0505066	0.049923	0.048764
20514.7	0.05261	0.051545	0.0508617	0.050343	0.049353
21014.7	0.053359	0.052255	0.0515341	0.050965	0.049894
21514.7	0.05414	0.053122	0.0520189	0.051458	0.050773
22014.7	0.054842	0.05386	0.0529056	0.052154	0.051344
22514.7	0.055556	0.054358	0.0536604	0.052833	0.052074
23014.7	0.056203	0.054914	0.0539155	0.053437	0.052615
23514.7	0.056774	0.055518	0.0545946	0.053902	0.053167
24014.7	0.057433	0.055971	0.0550585	-	0.053758
24514.7	0.058238	0.056712	0.055598	-	0.054709
Note: vise	cosity in cp				

To a certain level, the differences between lab data and values from correlation reflect the quality of the experiment. We also want to know the accuracy of new nitrogen viscosity correlation. The evaluation can be accomplished by comparing the calculated viscosity from correlation with lab data. Therefore error analysis gives us a confident interval of the new correlation. It should be noted that lab data are used as base for both absolute error and relative error. Tables 6-2 and 6-3 show the absolute error and relative error. Average absolute error is -4.31E-06 cp. Average relative error is -0.0247%.

Table 6-2. Absolute error by comparing nitrogen viscosity data with values from correlation

Pressure			Tempera	iture (°F)		
(psia)	116	134	152	170	200	250
			Absolute	Error (cp)		
514.7	-6.65E-05	-4.27E-05	-2.21E-05	-3.39E-06	2.17E-05	4.86E-05
1014.7	-2.02E-04	-1.69E-04	-1.41E-04	-1.17E-04	-8.29E-05	-4.39E-05
1514.7	-2.70E-04	-2.32E-04	-1.98E-04	-1.69E-04	-1.28E-04	-8.03E-05
2014.7	-3.06E-04	-2.62E-04	-2.23E-04	-1.88E-04	-1.41E-04	-8.57E-05
2514.7	-3.29E-04	-2.77E-04	-2.33E-04	-1.93E-04	-1.39E-04	-7.40E-05
3014.7	-1.61E-04	-2.05E-04	-2.76E-05	3.47E-05	6.72E-05	8.03E-05
3514.7	-3.68E-04	-1.65E-04	-2.08E-04	1.73E-04	2.29E-05	7.20E-05
4014.7	-5.87E-04	-8.15E-05	-2.29E-04	-2.31E-04	-2.73E-05	-1.12E-04
4514.7	-6.06E-04	-2.22E-04	-4.06E-04	-1.74E-04	5.62E-05	-1.47E-04
5014.7	-4.55E-04	-4.28E-05	-2.94E-04	-3.02E-04	6.07E-05	-1.90E-04
5514.7	-5.74E-04	-9.76E-05	-4.51E-04	-4.40E-04	4.39E-05	-2.32E-04
6014.7	-4.75E-04	5.81E-06	-4.12E-04	-4.49E-04	-1.08E-04	-2.31E-04
6514.7	-4.02E-04	6.23E-05	-5.67E-04	-4.03E-04	-6.04E-05	-4.57E-05
7014.7	-3.31E-04	8.53E-05	-5.11E-04	-2.53E-04	-1.64E-04	4.67E-05
7514.7	-3.48E-04	6.17E-05	-3.83E-04	-2.36E-04	-1.55E-04	-5.76E-05
8014.7	-3.84E-04	-7.65E-06	-3.18E-04	-1.79E-04	-1.95E-04	-1.67E-04
8514.7	-3.51E-04	-2.33E-05	-2.91E-04	-2.91E-05	-1.44E-04	-6.06E-05
9014.7	-3.37E-04	-4.30E-05	-2.44E-04	6.24E-05	-2.62E-04	-4.08E-05
9514.7	-2.02E-04	-2.09E-04	-5.37E-05	1.20E-04	-3.22E-04	1.32E-04
10014.7	-2.23E-04	4.13E-04	-1.56E-04	3.20E-04	-2.94E-04	2.05E-04
10514.7	-3.32E-05	3.73E-04	-3.85E-04	2.58E-04	-2.46E-04	-4.71E-05
11014.7	8.42E-07	3.48E-04	-3.83E-05	2.13E-04	-1.82E-04	-7.88E-05
11514.7	3.33E-06	4.61E-05	-1.15E-04	2.45E-04	-1.69E-04	-1.83E-04
12014.7	1.25E-04	3.90E-05	-1.78E-04	2.33E-04	-1.20E-04	-2.73E-04
12514.7	2.10E-05	5.10E-05	-2.48E-05	3.73E-04	-1.14E-04	-2.76E-04
13014.7	-9.31E-05	2.19E-05	1.47E-04	3.58E-04	-6.04E-05	-2.82E-04
13514.7	1.60E-05	7.20E-06	3.30E-04	3.56E-04	-1.25E-04	-3.40E-04
14014.7	-2.64E-04	6.10E-05	3.08E-04	3.90E-04	-1.44E-04	-8.77E-05

Table 6-2. Continued

Pressure	Temperature (°F)						
(psia)	116	134	152	170	200	250	
			Absolute l	Error (cp)			
14514.7	-3.11E-04	2.64E-04	3.45E-04	3.46E-04	-1.79E-05	-4.10E-05	
15014.7	-1.91E-04	1.46E-04	4.48E-04	7.03E-04	-5.72E-05	-6.18E-05	
15514.7	-2.17E-04	8.17E-05	3.73E-04	6.39E-04	4.28E-05	-2.91E-04	
16014.7	-3.96E-04	3.08E-05	2.68E-04	6.73E-04	1.89E-04	-4.21E-04	
16514.7	-3.20E-04	2.95E-05	3.06E-04	7.53E-04	1.65E-04	-5.69E-04	
17014.7	-2.75E-04	-4.91E-05	2.95E-04	7.73E-04	1.89E-04	-6.83E-04	
17514.7	-4.30E-04	-1.14E-04	-3.97E-04	8.52E-04	2.91E-04	-6.24E-04	
18014.7	-4.30E-04	4.33E-06	-1.65E-04	8.77E-04	1.20E-04	-8.39E-04	
18514.7	-4.63E-04	-3.54E-06	1.75E-04	9.00E-04	2.28E-04	-9.71E-04	
19014.7	-5.29E-04	4.60E-05	1.37E-04	8.79E-04	2.42E-04	-7.14E-04	
19514.7	-3.58E-04	-1.37E-04	1.20E-04	8.40E-04	-4.37E-05	-9.24E-04	
20014.7	-3.77E-04	-1.37E-04	2.81E-04	8.88E-04	7.57E-05	-9.53E-04	
20514.7	-4.41E-04	-7.32E-05	1.76E-04	9.13E-04	-1.85E-04	-1.42E-03	
21014.7	-2.61E-04	4.73E-05	2.61E-04	1.05E-03	-7.74E-05	-1.24E-03	
21514.7	-3.50E-04	-1.61E-04	4.21E-04	1.14E-03	1.24E-04	-1.21E-03	
22014.7	-5.32E-04	-2.10E-04	4.20E-04	1.23E-03	1.01E-04	-1.20E-03	
22514.7	-4.98E-04	-	6.68E-04	1.41E-03	1.15E-04	-1.19E-03	
23014.7	-5.44E-04	-	5.85E-04	1.27E-03	1.45E-04	-1.31E-03	
23514.7	-3.35E-04	-	6.34E-04	1.48E-03	1.86E-04	-1.23E-03	
24014.7	-	-	5.66E-04	1.35E-03	8.08E-05	-	
24514.7	-	-	-	-	2.10E-04	-	

Table 6-2. Continued

Pressure		Temperature (°F)						
(psia)	260	260 280 300 330 35						
	Absolute Error (cp)							
514.7	5.18E-05	5.56E-05	5.81E-05	5.50E-05	5.10E-05			
1014.7	-3.84E-05	-3.01E-05	-2.54E-05	-2.27E-05	-2.47E-05			
1514.7	-7.32E-05	-6.26E-05	-5.53E-05	-4.92E-05	-5.00E-05			
2014.7	-7.72E-05	-6.46E-05	-5.44E-05	-4.68E-05	-4.54E-05			
2514.7	-6.50E-05	-4.97E-05	-3.78E-05	-2.78E-05	-2.54E-05			
3014.7	1.02E-04	8.78E-05	5.03E-05	4.06E-04	7.56E-04			
3514.7	5.22E-05	2.48E-06	2.25E-05	1.57E-04	5.89E-04			
4014.7	1.53E-05	-1.40E-05	5.08E-05	2.71E-04	1.53E-04			
4514.7	8.31E-05	1.58E-04	1.77E-04	3.03E-04	1.05E-04			
5014.7	2.03E-04	1.03E-04	6.78E-05	2.62E-04	2.38E-04			
5514.7	3.45E-04	8.72E-05	1.48E-04	2.55E-04	2.82E-04			
6014.7	4.17E-04	7.86E-05	1.94E-04	2.58E-04	4.26E-04			
6514.7	4.79E-04	9.38E-05	1.55E-04	2.66E-04	3.63E-04			
7014.7	4.28E-04	9.69E-05	1.40E-04	3.77E-04	3.74E-04			
7514.7	3.79E-04	1.21E-04	6.04E-06	3.09E-04	2.86E-04			
8014.7	3.15E-04	1.37E-04	1.11E-04	4.15E-04	3.36E-04			
8514.7	3.20E-04	8.76E-05	7.18E-05	3.50E-04	3.25E-04			
9014.7	3.93E-04	8.07E-05	5.01E-05	1.93E-04	3.20E-04			
9514.7	3.08E-04	1.51E-04	6.48E-05	1.08E-04	2.58E-04			
10014.7	3.77E-04	8.77E-05	1.03E-04	1.08E-04	1.41E-04			
10514.7	3.68E-04	9.53E-05	6.62E-05	1.41E-04	1.04E-04			
11014.7	1.82E-04	-4.29E-06	4.96E-05	4.61E-05	1.43E-04			
11514.7	4.02E-04	-7.61E-06	2.85E-05	2.18E-04	2.34E-04			
12014.7	3.23E-04	-4.13E-05	9.47E-05	5.03E-05	2.02E-04			
12514.7	2.15E-04	-6.93E-05	4.66E-05	7.18E-05	1.57E-04			
13014.7	2.10E-04	-1.16E-04	1.16E-04	1.03E-04	1.90E-04			
13514.7	2.20E-04	-8.61E-05	2.01E-04	8.80E-05	1.45E-04			
14014.7	2.42E-04	2.45E-05	5.78E-05	9.47E-05	1.76E-04			

Table 6-2. Continued

Pressure		Te	mperature (°	°F)	
(psia)	260	280	300	330	350
		Abs	solute Error	(cp)	
14514.7	8.73E-05	2.80E-05	8.25E-05	1.49E-04	9.62E-05
15014.7	1.20E-04	-2.18E-05	1.19E-04	-9.90E-05	1.04E-04
15514.7	1.44E-04	5.20E-05	1.40E-04	-1.60E-05	9.00E-07
16014.7	1.37E-04	-5.29E-06	1.43E-04	4.03E-05	1.15E-04
16514.7	-4.12E-05	-9.39E-05	7.78E-05	5.94E-05	6.04E-05
17014.7	-1.30E-05	-1.36E-04	1.94E-04	1.55E-04	-1.22E-04
17514.7	3.67E-05	-6.81E-05	9.16E-05	2.01E-04	-7.03E-05
18014.7	5.84E-05	-2.01E-04	2.18E-04	-5.90E-05	-1.86E-05
18514.7	-1.44E-05	-2.02E-04	-5.40E-05	-2.22E-04	-9.57E-05
19014.7	-2.06E-04	-1.74E-04	-4.42E-05	-2.93E-04	1.97E-04
19514.7	-3.45E-04	-1.21E-04	5.75E-05	-1.74E-04	-1.12E-05
20014.7	-4.04E-04	-8.78E-05	-2.60E-04	-3.68E-04	3.98E-04
20514.7	-5.25E-04	-9.14E-05	3.31E-05	-1.70E-04	4.08E-04
21014.7	-5.84E-04	-1.35E-04	5.23E-06	-1.76E-04	4.65E-04
21514.7	-6.80E-04	-3.40E-04	1.60E-04	-5.86E-05	1.79E-04
22014.7	-7.02E-04	-4.20E-04	-9.02E-05	-1.45E-04	1.98E-04
22514.7	-7.39E-04	-2.64E-04	-2.11E-04	-2.21E-04	5.59E-05
23014.7	-7.12E-04	-1.69E-04	1.65E-04	-2.22E-04	9.97E-05
23514.7	-6.13E-04	-1.26E-04	1.13E-04	-8.95E-05	1.30E-04
24014.7	-6.05E-04	6.56E-05	2.71E-04	-	1.17E-04
24514.7	-7.44E-04	-3.27E-05	3.54E-04	-	-2.60E-04

Table 6-3. Relative error by comparing nitrogen viscosity data with values from correlation

Pressure	Temperature (°F)						
(psia)	116   134   152   170   200   250						
		I	Relative	Error (%	)		
514.7	-0.344	-0.216	-0.109	-0.016	0.102	0.217	
1014.7	-1.008	-0.830	-0.681	-0.553	-0.380	-0.192	
1514.7	-1.301	-1.101	-0.923	-0.773	-0.571	-0.343	
2014.7	-1.419	-1.198	-1.004	-0.834	-0.612	-0.357	
2514.7	-1.459	-1.216	-1.009	-0.828	-0.582	-0.300	
3014.7	-0.689	-0.867	-0.116	0.145	0.276	0.319	
3514.7	-1.495	-0.672	-0.837	0.701	0.091	0.278	
4014.7	-2.263	-0.319	-0.887	-0.888	-0.104	-0.415	
4514.7	-2.238	-0.829	-1.500	-0.646	0.208	-0.530	
5014.7	-1.623	-0.155	-1.053	-1.077	0.218	-0.666	
5514.7	-1.959	-0.339	-1.548	-1.507	0.153	-0.789	
6014.7	-1.563	0.020	-1.367	-1.489	-0.362	-0.762	
6514.7	-1.278	0.202	-1.810	-1.294	-0.196	-0.148	
7014.7	-1.017	0.268	-1.581	-0.793	-0.516	0.148	
7514.7	-1.032	0.187	-1.152	-0.717	-0.475	-0.177	
8014.7	-1.102	-0.022	-0.930	-0.527	-0.580	-0.500	
8514.7	-0.975	-0.066	-0.827	-0.084	-0.417	-0.177	
9014.7	-0.910	-0.118	-0.675	0.175	-0.737	-0.116	
9514.7	-0.532	-0.557	-0.145	0.329	-0.882	0.369	
10014.7	-0.568	1.087	-0.409	0.859	-0.787	0.564	
10514.7	-0.083	0.955	-0.977	0.674	-0.643	-0.126	
11014.7	0.002	0.867	-0.096	0.543	-0.466	-0.206	
11514.7	0.008	0.111	-0.279	0.610	-0.424	-0.466	
12014.7	0.290	0.092	-0.424	0.566	-0.294	-0.681	
12514.7	0.047	0.117	-0.058	0.890	-0.274	-0.677	
13014.7	-0.205	0.049	0.337	0.836	-0.142	-0.677	
13514.7	0.035	0.016	0.742	0.814	-0.289	-0.800	
14014.7	-0.554	0.131	0.680	0.875	-0.325	-0.204	

Table 6-3. Continued

Pressure	Temperature (°F)						
(psia)	116	134	152	170	200	250	
		R	Relative I	Error (%	5)		
14514.7	-0.640	0.561	0.746	0.759	-0.040	-0.094	
15014.7	-0.385	0.303	0.951	1.525	-0.125	-0.139	
15514.7	-0.428	0.166	0.776	1.358	0.092	-0.640	
16014.7	-0.766	0.061	0.546	1.406	0.401	-0.909	
16514.7	-0.607	0.058	0.612	1.549	0.344	-1.205	
17014.7	-0.513	-0.094	0.580	1.563	0.387	-1.421	
17514.7	-0.785	-0.214	-0.757	1.695	0.588	-1.280	
18014.7	-0.772	0.008	-0.311	1.717	0.238	-1.687	
18514.7	-0.816	-0.006	0.326	1.734	0.446	-1.921	
19014.7	-0.916	0.082	0.251	1.666	0.465	-1.399	
19514.7	-0.612	-0.242	0.217	1.566	-0.082	-1.779	
20014.7	-0.634	-0.236	0.501	1.631	0.141	-1.809	
20514.7	-0.730	-0.125	0.308	1.653	-0.338	-2.631	
21014.7	-0.427	0.080	0.450	1.874	-0.140	-2.283	
21514.7	-0.563	-0.266	0.720	2.010	0.221	-2.190	
22014.7	-0.840	-0.341	0.706	2.152	0.178	-2.146	
22514.7	-0.775	_	1.113	2.436	0.200	-2.113	
23014.7	-0.834	-	0.961	2.156	0.249	-2.287	
23514.7	-0.509	-	1.027	2.489	0.316	-2.129	
24014.7	-	-	0.904	2.238	0.135	-	
24514.7	-	-	-	-	0.347	-	

Table 6-3. Continued

Pressure		Tem	perature	(°F)			
(psia)	260	280	300	330	350		
		Relative Error (%)					
514.7	0.229	0.241	0.247	0.228	0.208		
1014.7	-0.166	-0.128	-0.106	-0.092	-0.099		
1514.7	-0.310	-0.261	-0.226	-0.196	-0.197		
2014.7	-0.319	-0.263	-0.218	-0.184	-0.175		
2514.7	-0.262	-0.197	-0.148	-0.107	-0.096		
3014.7	0.404	0.342	0.193	1.551	2.886		
3514.7	0.200	0.009	0.084	0.578	2.185		
4014.7	0.057	-0.051	0.185	0.981	0.547		
4514.7	0.301	0.568	0.631	1.073	0.367		
5014.7	0.719	0.361	0.235	0.902	0.813		
5514.7	1.194	0.297	0.503	0.857	0.942		
6014.7	1.404	0.261	0.642	0.850	1.400		
6514.7	1.577	0.304	0.501	0.857	1.165		
7014.7	1.367	0.306	0.441	1.191	1.174		
7514.7	1.180	0.373	0.019	0.952	0.878		
8014.7	0.955	0.412	0.333	1.255	1.009		
8514.7	0.948	0.257	0.211	1.033	0.958		
9014.7	1.136	0.232	0.144	0.556	0.923		
9514.7	0.869	0.425	0.182	0.304	0.730		
10014.7	1.042	0.241	0.284	0.297	0.391		
10514.7	0.995	0.257	0.179	0.382	0.281		
11014.7	0.479	-0.011	0.131	0.122	0.381		
11514.7	1.045	-0.020	0.074	0.571	0.615		
12014.7	0.822	-0.104	0.242	0.129	0.519		
12514.7	0.535	-0.172	0.117	0.181	0.396		
13014.7	0.512	-0.282	0.285	0.256	0.474		
13514.7	0.526	-0.206	0.487	0.214	0.356		
14014.7	0.570	0.058	0.137	0.227	0.424		

Table 6-3. Continued

Pressure		Temperature (°F)					
(psia)	260	280	300	330	350		
		Relat	tive Erro	r (%)			
14514.7	0.201	0.065	0.193	0.352	0.228		
15014.7	0.272	-0.050	0.273	-0.229	0.242		
15514.7	0.321	0.117	0.317	-0.037	0.002		
16014.7	0.301	-0.012	0.320	0.091	0.260		
16514.7	-0.089	-0.204	0.171	0.132	0.135		
17014.7	-0.028	-0.291	0.420	0.340	-0.266		
17514.7	0.077	-0.144	0.196	0.435	-0.152		
18014.7	0.120	-0.416	0.460	-0.125	-0.040		
18514.7	-0.029	-0.413	-0.112	-0.464	-0.202		
19014.7	-0.410	-0.350	-0.090	-0.603	0.412		
19514.7	-0.676	-0.241	0.116	-0.353	-0.023		
20014.7	-0.780	-0.173	-0.515	-0.737	0.815		
20514.7	-0.997	-0.177	0.065	-0.338	0.827		
21014.7	-1.095	-0.259	0.010	-0.346	0.933		
21514.7	-1.256	-0.641	0.308	-0.114	0.352		
22014.7	-1.280	-0.781	-0.170	-0.279	0.385		
22514.7	-1.329	-0.485	-0.393	-0.417	0.107		
23014.7	-1.267	-0.307	0.307	-0.416	0.190		
23514.7	-1.079	-0.227	0.206	-0.166	0.244		
24014.7	-1.053	0.117	0.493	-	0.218		
24514.7	-1.278	-0.058	0.637	-	-0.476		

#### **6.2 Methane Viscosity Correlation**

Since Lee-Gonzalez-Eakin correlation is one of the most common used viscosity correlations in petroleum engineering and can be coded into computer program easily, we developed a correlation that has the same form as Lee-Gonzalez-Eakin correlation. The coefficients in the correlation were updated using NIST values and lab data from our experiment. Due to the fact that we do not have viscosity data at pressure from 500 to 4500 psi in our experiment, NIST values at this pressure range were used. As we already showed in Chapter II, NIST values match with lab data very well at pressure from 500 to 4500 psi. Combining NIST values at pressure from 514.7 to 4014.7 psia with our lab data at pressure from 4514.7 to 24514.7 psia the coefficients were determined. A non-linear

regression approach is applied in determining the coefficients. As a result, the final form of correlation was developed. New gas viscosity correlation is as follows:

$$\mu_g = K \exp(X \rho_g^Y). \tag{6.5}$$

where

$$K = \frac{0.0001 * (9.18999 + 3.0893 M_w) T^{1.2288}}{208.99 + 18.83933 M_w + T}.$$
 (6.6)

$$X = 3.56014 + \left\lceil \frac{1000.01}{T} \right\rceil + 0.124465 M_w. \tag{6.7}$$

$$Y = 2.47862 - 0.12294X. (6.8)$$

where

 $\mu_g$  = Gas viscosity, cp

 $\rho_g$  = Gas density, g/cc

 $M_W$  = Molecular weight

T = Temperature, R

New correlation that based on lab data and NIST values (Table 6-3) covers larger pressure and temperature range than original Lee-Gonzalez-Eakin correlation. It covers both low and high pressure and temperature and gives more confidence on gas viscosity estimation when petroleum engineers deal with HPHT reservoir.

Table 6-4. Data used to develop new methane viscosity correlation

Pressure	Temperature (oF)						
(psia)	100	120	140	160	180		
514.7	0.01216	0.01248	0.01280	0.01312	0.01343		
1014.7	0.01303	0.01328	0.01355	0.01382	0.01409		
1514.7	0.01420	0.01436	0.01453	0.01473	0.01494		
2014.7	0.01568	0.01568	0.01573	0.01583	0.01595		
2514.7	0.01739	0.01720	0.01711	0.01708	0.01709		
3014.7	0.01921	0.01884	0.01859	0.01843	0.01834		
3514.7	0.02105	0.02052	0.02013	0.01984	0.01964		
4014.7	0.02284	0.02218	0.02166	0.02126	0.02095		
4514.7	0.02454	0.02377	0.02309	0.02265	0.02226		
5014.7	0.02630	0.02531	0.02447	0.02399	0.02376		
5514.7	0.02772	0.02675	0.02547	0.02517	0.02490		
6014.7	0.02977	0.02790	0.02678	0.02628	0.02599		
6514.7	0.03082	0.02886	0.02836	0.02746	0.02707		
7014.7	0.03156	0.02995	0.02959	0.02854	0.02806		
7514.7	0.03298	0.03108	0.03093	0.02968	0.02900		
8014.7	0.03413	0.03224	0.03200	0.03027	0.03018		
8514.7	0.03529	0.03344	0.03314	0.03124	0.03110		
9014.7	0.03656	0.03470	0.03421	0.03232	0.03195		
9514.7	0.03772	0.03585	0.03523	0.03349	0.03279		
10014.7	0.03879	0.03700	0.03620	0.03446	0.03376		
10514.7	0.03989	0.03807	0.03726	0.03548	0.03484		
11014.7	0.04101	0.03915	0.03813	0.03647	0.03552		
11514.7	0.04205	0.04020	0.03896	0.03739	0.03643		
12014.7	0.04305	0.04118	0.03986	0.03837	0.03732		
12514.7	0.04401	0.04218	0.04079	0.03931	0.03825		
13014.7	0.04505	0.04311	0.04182	0.04022	0.03916		
13514.7	0.04609	0.04412	0.04270	0.04113	0.04005		
14014.7	0.04714	0.04512	0.04369	0.04210	0.04088		
14514.7	0.04822	0.04614	0.04461	0.04304	0.04179		
15014.7	0.04915	0.04709	0.04558	0.04388	0.04272		
15514.7	0.05020	0.04812	0.04654	0.04467	0.04361		
16014.7	0.05126	0.04901	0.04743	0.04586	0.04443		
16514.7	0.05220	0.05004	0.04834	0.04690	0.04530		
17014.7	0.05323	0.05106	0.04926	0.04776	0.04612		
17514.7	0.05428	0.05204	0.05015	0.04856	0.04708		
18014.7	0.05533	0.05303	0.05112	0.04955	0.04799		

Table 6-4. Continued

Pressure		Temperature (oF)						
(psia)	100	120	140	160	180			
18514.7	0.05636	0.05393	0.05204	0.05047	0.04881			
19014.7	0.05743	0.05490	0.05284	0.05123	0.04966			
19514.7	0.05836	0.05588	0.05378	0.05217	0.05056			
20014.7	0.05937	0.05693	0.05474	0.05302	0.05138			
20514.7	0.06041	0.05789	0.05556	0.05391	0.05220			
21014.7	0.06187	0.05888	0.05657	0.05479	0.05306			
21514.7	0.06257	0.05993	0.05744	0.05567	0.05391			
22014.7	0.06355	0.06096	0.05839	0.05656	0.05481			
22514.7	0.06461	0.06220	0.05931	0.05753	0.05566			
23014.7	0.06575	0.06277	0.06017	0.05837	0.05650			
23514.7	0.06683	0.06402	0.06116	0.05914	0.05719			
24014.7	0.06777	0.06505	0.06209	0.05975	0.05819			
24514.7	0.06893	0.06603	0.06301	0.06064	0.05915			
25014.7	0.07002	-	0.06389	0.06173	0.06007			

Table 6-4. Continued

Pressure	Temperature (°F)						
(psia)	188	200	220	225	230		
514.7	0.01355	0.01374	0.01405	0.01413	0.01420		
1014.7	0.01420	0.01437	0.01464	0.01471	0.01478		
1514.7	0.01502	0.01516	0.01538	0.01544	0.01550		
2014.7	0.01600	0.01609	0.01626	0.01630	0.01634		
2514.7	0.01711	0.01715	0.01724	0.01726	0.01729		
3014.7	0.01832	0.01830	0.01830	0.01831	0.01832		
3514.7	0.01957	0.01950	0.01942	0.01940	0.01939		
4014.7	0.02085	0.02072	0.02056	0.02053	0.02050		
4514.7	0.02212	0.02195	0.02171	0.02171	0.02162		
5014.7	0.02337	0.02292	0.02284	0.02283	0.02275		
5514.7	0.02460	0.02403	0.02385	0.02378	0.02366		
6014.7	0.02589	0.02538	0.02484	0.02480	0.02465		
6514.7	0.02684	0.02640	0.02596	0.02580	0.02564		
7014.7	0.02776	0.02748	0.02674	0.02670	0.02661		
7514.7	0.02877	0.02850	0.02794	0.02762	0.02747		
8014.7	0.02971	0.02948	0.02877	0.02874	0.02839		
8514.7	0.03064	0.03050	0.02954	0.02968	0.02934		
9014.7	0.03149	0.03146	0.03031	0.03051	0.03023		
9514.7	0.03242	0.03238	0.03115	0.03133	0.03108		
10014.7	0.03334	0.03332	0.03201	0.03216	0.03189		
10514.7	0.03410	0.03425	0.03291	0.03287	0.03263		
11014.7	0.03504	0.03514	0.03371	0.03372	0.03348		
11514.7	0.03594	0.03596	0.03453	0.03445	0.03419		
12014.7	0.03677	0.03680	0.03535	0.03526	0.03501		
12514.7	0.03759	0.03770	0.03620	0.03607	0.03589		
13014.7	0.03848	0.03840	0.03689	0.03690	0.03658		
13514.7	0.03932	0.03912	0.03776	0.03753	0.03733		
14014.7	0.04026	0.04003	0.03856	0.03862	0.03804		
14514.7	0.04117	0.04092	0.03947	0.03943	0.03892		
15014.7	0.04216	0.04172	0.04031	0.04041	0.03989		
15514.7	0.04307	0.04246	0.04113	0.04106	0.04068		
16014.7	0.04396	0.04323	0.04193	0.04184	0.04139		
16514.7	0.04486	0.04398	0.04270	0.04250	0.04211		
17014.7	0.04570	0.04480	0.04363	0.04331	0.04306		
17514.7	0.04647	0.04568	0.04432	0.04406	0.04382		
18014.7	0.04734	0.04667	0.04517	0.04471	0.04463		

Table 6-4. Continued

Pressure	Temperature (°F)						
(psia)	188	200	220	225	230		
18514.7	0.04821	0.04773	0.04586	0.04561	0.04537		
19014.7	0.04907	0.04840	0.04661	0.04642	0.04619		
19514.7	0.04995	0.04919	0.04725	0.04724	0.04691		
20014.7	0.05088	0.05013	0.04789	0.04804	0.04773		
20514.7	0.05136	0.05092	0.04872	0.04879	0.04858		
21014.7	0.05210	0.05188	0.04949	0.04951	0.04935		
21514.7	0.05296	0.05270	0.05039	0.05036	0.05010		
22014.7	0.05377	0.05347	0.05116	0.05115	0.05086		
22514.7	0.05460	0.05418	0.05199	0.05191	0.05166		
23014.7	0.05550	0.05503	0.05282	0.05280	0.05243		
23514.7	0.05637	0.05584	0.05369	0.05365	0.05321		
24014.7	0.05726	0.05650	0.05416	0.05442	0.05394		
24514.7	0.05795	0.05731	0.05494	0.05522	0.05454		
25014.7	-	-	0.05587	0.05608	_		

Table 6-4. Continued

Pressure	Temperature (°F)						
(psia)	250	260	280	300	320		
514.7	0.01451	0.01466	0.01496	0.01526	0.01555		
1014.7	0.01506	0.01519	0.01547	0.01574	0.01602		
1514.7	0.01573	0.01585	0.01609	0.01634	0.01658		
2014.7	0.01652	0.01662	0.01682	0.01702	0.01723		
2514.7	0.01741	0.01748	0.01762	0.01778	0.01795		
3014.7	0.01837	0.01840	0.01849	0.01860	0.01872		
3514.7	0.01938	0.01938	0.01941	0.01947	0.01954		
4014.7	0.02041	0.02039	0.02036	0.02036	0.02039		
4514.7	0.02147	0.02140	0.02132	0.02126	0.02124		
5014.7	0.02239	0.02238	0.02221	0.02208	0.02191		
5514.7	0.02333	0.02334	0.02315	0.02294	0.02272		
6014.7	0.02426	0.02427	0.02405	0.02376	0.02356		
6514.7	0.02516	0.02520	0.02499	0.02466	0.02443		
7014.7	0.02611	0.02602	0.02586	0.02546	0.02524		
7514.7	0.02704	0.02692	0.02670	0.02624	0.02604		
8014.7	0.02794	0.02791	0.02758	0.02705	0.02679		
8514.7	0.02882	0.02873	0.02844	0.02776	0.02754		
9014.7	0.02959	0.02961	0.02928	0.02866	0.02834		
9514.7	0.03046	0.03041	0.03002	0.02943	0.02908		
10014.7	0.03126	0.03118	0.03083	0.03022	0.02982		
10514.7	0.03205	0.03194	0.03157	0.03094	0.03065		
11014.7	0.03287	0.03269	0.03237	0.03165	0.03141		
11514.7	0.03375	0.03338	0.03320	0.03241	0.03212		
12014.7	0.03455	0.03429	0.03399	0.03353	0.03283		
12514.7	0.03537	0.03504	0.03479	0.03438	0.03354		
13014.7	0.03614	0.03586	0.03556	0.03508	0.03425		
13514.7	0.03676	0.03666	0.03632	0.03584	0.03501		
14014.7	0.03752	0.03739	0.03714	0.03659	0.03575		
14514.7	0.03835	0.03827	0.03792	0.03725	0.03651		
15014.7	0.03932	0.03906	0.03885	0.03805	0.03727		
15514.7	0.03998	0.03988	0.03949	0.03882	0.03810		
16014.7	0.04084	0.04051	0.04035	0.03961	0.03885		
16514.7	0.04148	0.04127	0.04105	0.04048	0.03964		
17014.7	0.04222	0.04194	0.04193	0.04115	0.04048		
17514.7	0.04294	0.04281	0.04259	0.04196	0.04115		
18014.7	0.04365	0.04357	0.04336	0.04275	0.04189		

Table 6-4. Continued

Pressure	Temperature (°F)						
(psia)	250	260	280	300	320		
18514.7	0.04437	0.04445	0.04407	0.04336	0.04282		
19014.7	0.04514	0.04521	0.04480	0.04414	0.04350		
19514.7	0.04593	0.04609	0.04559	0.04491	0.04408		
20014.7	0.04665	0.04681	0.04622	0.04564	0.04476		
20514.7	0.04757	0.04759	0.04702	0.04646	0.04544		
21014.7	0.04842	0.04847	0.04786	0.04708	0.04606		
21514.7	0.04932	0.04915	0.04849	0.04791	0.04686		
22014.7	0.05008	0.04996	0.04915	0.04868	0.04759		
22514.7	0.05083	0.05080	0.04987	0.04928	0.04836		
23014.7	0.05141	0.05165	0.05060	0.05005	0.04894		
23514.7	0.05204	0.05226	0.05132	0.05071	0.04976		
24014.7	0.05294	0.05263	0.05195	0.05156	0.05083		
24514.7	0.05357	0.05335	0.05263	0.05200	0.05155		
25014.7	-	0.05407	0.05337	-	0.05228		

Table 6-4. Continued

Pressure	Temperature (°F)							
(psia)	340	360	380	415				
514.7	0.01584	0.01613	0.01642	0.01691				
1014.7	0.01629	0.01656	0.01683	0.01730				
1514.7	0.01683	0.01708	0.01732	0.01776				
2014.7	0.01745	0.01766	0.01789	0.01828				
2514.7	0.01813	0.01831	0.01850	0.01885				
3014.7	0.01886	0.01901	0.01917	0.01946				
3514.7	0.01964	0.01974	0.01987	0.02010				
4014.7	0.02044	0.02050	0.02059	0.02077				
4514.7	0.02096	0.02128	0.02133	0.02147				
5014.7	0.02181	0.02206	0.02205	0.02217				
5514.7	0.02283	0.02284	0.02278	0.02284				
6014.7	0.02369	0.02366	0.02361	0.02353				
6514.7	0.02443	0.02435	0.02424	0.02429				
7014.7	0.02512	0.02500	0.02494	0.02496				
7514.7	0.02585	0.02578	0.02565	0.02564				
8014.7	0.02665	0.02641	0.02637	0.02635				
8514.7	0.02748	0.02740	0.02714	0.02697				
9014.7	0.02841	0.02817	0.02786	0.02764				
9514.7	0.02908	0.02886	0.02859	0.02827				
10014.7	0.02980	0.02954	0.02922	0.02892				
10514.7	0.03058	0.03032	0.02995	0.02957				
11014.7	0.03133	0.03110	0.03054	0.03028				
11514.7	0.03202	0.03178	0.03123	0.03083				
12014.7	0.03279	0.03243	0.03194	0.03145				
12514.7	0.03356	0.03306	0.03261	0.03214				
13014.7	0.03432	0.03378	0.03333	0.03280				
13514.7	0.03501	0.03437	0.03400	0.03346				
14014.7	0.03577	0.03503	0.03467	0.03411				
14514.7	0.03650	0.03568	0.03530	0.03472				
15014.7	0.03720	0.03639	0.03599	0.03531				
15514.7	0.03804	0.03708	0.03661	0.03577				
16014.7	0.03912	0.03780	0.03730	0.03642				
16514.7	0.03971	0.03849	0.03797	0.03698				
17014.7	0.04039	0.03918	0.03866	0.03767				
17514.7	0.04099	0.03986	0.03934	0.03830				
18014.7	0.04203	0.04057	0.04000	0.03915				

Table 6-4. Continued

Pressure		Temperature (°F)							
(psia)	340	360	380	415					
18514.7	0.04272	0.04138	0.04068	0.03965					
19014.7	0.04339	0.04184	0.04132	0.04041					
19514.7	0.04404	0.04255	0.04194	0.04088					
20014.7	0.04458	0.04325	0.04254	0.04145					
20514.7	0.04526	0.04391	0.04323	0.04214					
21014.7	0.04588	0.04420	0.04380	0.04257					
21514.7	0.04658	0.04486	0.04431	0.04303					
22014.7	0.04711	0.04544	0.04502	0.04380					
22514.7	0.04788	0.04599	0.04570	0.04420					
23014.7	0.04836	0.04653	0.04628	0.04465					
23514.7	0.04891	0.04717	0.04677	0.04531					
24014.7	0.04939	0.04778	0.04740	0.04559					
24514.7	0.05011	0.04895	0.04796	0.04620					
25014.7	0.05071	-	0.04866	-					

The accuracy of the new methane correlation is vital for future viscosity estimation. As well as error analysis for nitrogen viscosity we compared the calculated viscosity from correlation with lab data. In analysis lab data are used as base for both absolute error and relative error. Tables 6-5 and 6-6 show the absolute error and relative error. Average absolute error is 7.06E-06 cp. Average relative error is 0.1068%.

Table 6-5. Absolute error by comparing methane viscosity data with values from correlation

Pressure			Ten	nperature (	°F)				
(psia)	100	120	140	160	180	188	200		
	Absolute Error (cp)								
514.7	1.17E-03	1.15E-03	1.13E-03	1.11E-03	1.09E-03	1.08E-03	1.06E-03		
1014.7	8.66E-04	8.62E-04	8.55E-04	8.46E-04	8.32E-04	8.26E-04	8.16E-04		
1514.7	5.58E-04	5.70E-04	5.78E-04	5.81E-04	5.79E-04	5.78E-04	5.74E-04		
2014.7	2.54E-04	2.82E-04	3.05E-04	3.21E-04	3.33E-04	3.36E-04	3.39E-04		
2514.7	-2.69E-05	1.34E-05	4.80E-05	7.67E-05	1.00E-04	1.07E-04	1.17E-04		
3014.7	-2.62E-04	-2.19E-04	-1.79E-04	-1.42E-04	-1.11E-04	-9.95E-05	-8.44E-05		
3514.7	-4.42E-04	-4.03E-04	-3.65E-04	-3.26E-04	-2.91E-04	-2.78E-04	-2.60E-04		
4014.7	-5.62E-04	-5.39E-04	-5.05E-04	-4.71E-04	-4.35E-04	-4.23E-04	-4.03E-04		
4514.7	-6.27E-04	-6.24E-04	-5.40E-04	-5.75E-04	-5.44E-04	-5.34E-04	-5.14E-04		
5014.7	-8.10E-04	-6.85E-04	-5.44E-04	-6.22E-04	-8.46E-04	-6.09E-04	-3.66E-04		
5514.7	-6.97E-04	-6.82E-04	-1.87E-04	-5.27E-04	-7.87E-04	-6.72E-04	-3.54E-04		
6014.7	-1.28E-03	-4.42E-04	-1.78E-04	-3.95E-04	-7.00E-04	-8.03E-04	-5.77E-04		
6514.7	-9.14E-04	-4.59E-05	-4.71E-04	-3.49E-04	-6.15E-04	-6.20E-04	-4.99E-04		
7014.7	-2.79E-04	1.76E-04	-4.49E-04	-2.31E-04	-4.63E-04	-4.23E-04	-4.92E-04		
7514.7	-3.70E-04	3.26E-04	-5.63E-04	-2.04E-04	-2.91E-04	-3.35E-04	-4.43E-04		
8014.7	-2.28E-04	4.04E-04	-4.48E-04	3.48E-04	-3.77E-04	-1.90E-04	-3.68E-04		
8514.7	-1.34E-04	4.14E-04	-4.22E-04	4.93E-04	-2.20E-04	-6.91E-05	-3.61E-04		
9014.7	-1.78E-04	3.28E-04	-3.58E-04	5.09E-04	-1.32E-05	1.19E-04	-3.10E-04		
9514.7	-1.48E-04	3.30E-04	-2.67E-04	4.11E-04	1.78E-04	2.06E-04	-2.34E-04		
10014.7	-5.87E-05	2.98E-04	-1.54E-04	4.83E-04	2.18E-04	2.90E-04	-1.90E-04		
10514.7	-2.04E-05	3.29E-04	-1.42E-04	4.98E-04	1.38E-04	5.06E-04	-1.56E-04		
11014.7	-1.16E-05	3.36E-04	3.36E-05	5.17E-04	4.33E-04	5.40E-04	-9.99E-05		
11514.7	4.35E-05	3.46E-04	2.23E-04	5.99E-04	4.85E-04	5.93E-04	1.73E-05		
12014.7	1.15E-04	4.12E-04	3.33E-04	5.99E-04	5.54E-04	6.94E-04	1.00E-04		
12514.7	2.21E-04	4.37E-04	4.01E-04	6.18E-04	5.57E-04	8.02E-04	1.06E-04		
13014.7	2.26E-04	5.25E-04	3.57E-04	6.57E-04	5.69E-04	8.24E-04	3.03E-04		
13514.7	2.24E-04	5.15E-04	4.44E-04	6.86E-04	5.96E-04	8.80E-04	4.64E-04		
14014.7	1.83E-04	4.96E-04	4.14E-04	6.47E-04	6.55E-04	8.35E-04	4.31E-04		

Table 6-5. Continued

Pressure			Tem	perature (°	F)		
(psia)	100	120	140	160	180	188	200
			Abso	lute Error (	(cp)		
14514.7	1.16E-04	4.51E-04	4.30E-04	6.19E-04	6.36E-04	7.99E-04	4.09E-04
15014.7	1.70E-04	4.57E-04	3.99E-04	6.85E-04	5.85E-04	6.77E-04	4.61E-04
15514.7	1.10E-04	3.83E-04	3.58E-04	7.98E-04	5.66E-04	6.33E-04	5.67E-04
16014.7	1.95E-05	4.29E-04	3.82E-04	4.90E-04	6.13E-04	5.96E-04	6.29E-04
16514.7	4.19E-05	3.26E-04	3.70E-04	3.26E-04	5.90E-04	5.40E-04	7.09E-04
17014.7	-4.41E-05	2.39E-04	3.49E-04	3.31E-04	6.11E-04	5.29E-04	7.09E-04
17514.7	-1.49E-04	1.60E-04	3.42E-04	3.88E-04	4.88E-04	5.94E-04	6.47E-04
18014.7	-2.71E-04	8.15E-05	2.50E-04	2.58E-04	4.12E-04	5.41E-04	4.62E-04
18514.7	-3.76E-04	8.14E-05	2.02E-04	1.82E-04	4.14E-04	4.86E-04	2.02E-04
19014.7	-5.18E-04	3.78E-06	2.68E-04	2.66E-04	3.84E-04	4.39E-04	3.28E-04
19514.7	-5.39E-04	-9.61E-05	1.83E-04	1.58E-04	2.92E-04	3.52E-04	3.30E-04
20014.7	-6.42E-04	-2.67E-04	7.26E-05	1.37E-04	2.75E-04	2.20E-04	1.74E-04
20514.7	-7.86E-04	-3.61E-04	1.05E-04	6.20E-05	2.60E-04	5.35E-04	1.65E-04
21014.7	-1.34E-03	-4.86E-04	-7.12E-05	1.78E-06	1.87E-04	5.76E-04	-2.98E-05
21514.7	-1.16E-03	-6.64E-04	-9.99E-05	-7.26E-05	1.31E-04	5.06E-04	-7.47E-05
22014.7	-1.26E-03	-8.45E-04	-2.25E-04	-1.48E-04	1.26E-05	4.63E-04	-7.71E-05
22514.7	-1.44E-03	-1.23E-03	-3.19E-04	-3.18E-04	-5.20E-05	4.07E-04	-3.23E-05
23014.7	-1.71E-03	-9.58E-04	-3.64E-04	-3.60E-04	-1.14E-04	2.76E-04	-1.22E-04
23514.7	-1.92E-03	-1.37E-03	-5.35E-04	-3.36E-04	-3.81E-05	1.63E-04	-1.78E-04
24014.7	-1.99E-03	-1.56E-03	-6.48E-04	-1.53E-04	-2.66E-04	3.45E-05	-1.00E-04
24514.7	-2.29E-03	-1.70E-03	-7.66E-04	-2.64E-04	-4.68E-04	9.71E-05	-1.63E-04
25014.7	-2.53E-03	-	-8.40E-04	-5.70E-04	-6.23E-04	-	-

Table 6-5. Continued

Pressure			Tempera	iture (°F)					
(psia)	220	225	230	250	260	280			
	Absolute Error (cp)								
514.7	1.04E-03	1.03E-03	1.02E-03	9.91E-04	9.74E-04	9.40E-04			
1014.7	7.97E-04	7.92E-04	7.87E-04	7.64E-04	7.51E-04	7.25E-04			
1514.7	5.65E-04	5.63E-04	5.60E-04	5.45E-04	5.37E-04	5.18E-04			
2014.7	3.41E-04	3.41E-04	3.40E-04	3.37E-04	3.32E-04	3.22E-04			
2514.7	1.29E-04	1.32E-04	1.34E-04	1.39E-04	1.40E-04	1.39E-04			
3014.7	-6.32E-05	-5.93E-05	-5.57E-05	-4.20E-05	-3.72E-05	-3.14E-05			
3514.7	-2.33E-04	-2.27E-04	-2.22E-04	-2.02E-04	-1.95E-04	-1.83E-04			
4014.7	-3.74E-04	-3.68E-04	-3.62E-04	-3.39E-04	-3.29E-04	-3.13E-04			
4514.7	-4.87E-04	-5.33E-04	-4.78E-04	-4.55E-04	-4.37E-04	-4.20E-04			
5014.7	-5.66E-04	-6.11E-04	-5.87E-04	-4.21E-04	-4.84E-04	-4.40E-04			
5514.7	-5.13E-04	-5.19E-04	-4.77E-04	-3.88E-04	-5.02E-04	-4.87E-04			
6014.7	-4.54E-04	-4.99E-04	-4.36E-04	-3.45E-04	-4.83E-04	-4.84E-04			
6514.7	-5.19E-04	-4.69E-04	-4.01E-04	-2.75E-04	-4.67E-04	-5.24E-04			
7014.7	-2.61E-04	-3.35E-04	-3.62E-04	-2.64E-04	-3.48E-04	-4.91E-04			
7514.7	-4.38E-04	-2.50E-04	-2.18E-04	-2.33E-04	-3.08E-04	-4.42E-04			
8014.7	-2.61E-04	-3.72E-04	-1.53E-04	-1.87E-04	-3.71E-04	-4.33E-04			
8514.7	-4.19E-05	-3.28E-04	-1.31E-04	-1.36E-04	-2.73E-04	-4.09E-04			
9014.7	1.61E-04	-1.98E-04	-6.06E-05	2.32E-05	-2.46E-04	-3.76E-04			
9514.7	2.80E-04	-5.63E-05	3.43E-05	5.85E-05	-1.53E-04	-2.46E-04			
10014.7	3.69E-04	4.99E-05	1.45E-04	1.61E-04	-4.19E-05	-2.07E-04			
10514.7	4.00E-04	2.66E-04	3.27E-04	2.56E-04	6.40E-05	-9.99E-05			
11014.7	5.16E-04	3.19E-04	3.83E-04	3.09E-04	1.79E-04	-6.89E-05			
11514.7	6.09E-04	4.87E-04	5.63E-04	2.99E-04	3.43E-04	-7.75E-05			
12014.7	6.81E-04	5.65E-04	6.26E-04	3.49E-04	2.70E-04	-5.01E-05			
12514.7	7.06E-04	6.35E-04	6.08E-04	3.66E-04	3.49E-04	-4.29E-05			
13014.7	8.88E-04	6.64E-04	7.76E-04	4.31E-04	3.53E-04	-1.16E-05			
13514.7	8.84E-04	8.88E-04	8.74E-04	6.39E-04	3.65E-04	1.52E-05			
14014.7	9.26E-04	6.35E-04	1.01E-03	6.94E-04	4.39E-04	-1.95E-05			

Table 6-5. Continued

Pressure			Temper	ature (°F)		
(psia)	220	225	230	250	260	280
			Absolute	Error (cp)		
14514.7	8.59E-04	6.62E-04	9.50E-04	6.68E-04	3.60E-04	-2.23E-05
15014.7	8.51E-04	5.13E-04	8.02E-04	5.01E-04	3.51E-04	-1.89E-04
15514.7	8.50E-04	6.79E-04	8.21E-04	6.34E-04	3.16E-04	-6.35E-05
16014.7	8.63E-04	7.10E-04	9.18E-04	5.46E-04	4.54E-04	-1.73E-04
16514.7	9.07E-04	8.54E-04	9.91E-04	6.88E-04	4.65E-04	-1.27E-04
17014.7	7.78E-04	8.41E-04	8.34E-04	7.22E-04	5.51E-04	-2.62E-04
17514.7	8.85E-04	8.75E-04	8.58E-04	7.61E-04	4.36E-04	-1.87E-04
18014.7	8.15E-04	1.00E-03	8.26E-04	8.11E-04	4.23E-04	-2.30E-04
18514.7	9.02E-04	8.84E-04	8.54E-04	8.43E-04	2.93E-04	-2.11E-04
19014.7	9.27E-04	8.45E-04	7.97E-04	8.21E-04	2.67E-04	-2.19E-04
19514.7	1.06E-03	7.93E-04	8.32E-04	7.69E-04	1.25E-04	-2.98E-04
20014.7	1.19E-03	7.49E-04	7.75E-04	7.87E-04	1.29E-04	-2.17E-04
20514.7	1.12E-03	7.57E-04	6.78E-04	5.98E-04	7.28E-05	-3.11E-04
21014.7	1.10E-03	7.81E-04	6.50E-04	4.77E-04	-9.07E-05	-4.48E-04
21514.7	9.46E-04	6.72E-04	6.34E-04	2.94E-04	-6.26E-05	-3.77E-04
22014.7	9.25E-04	6.25E-04	6.16E-04	2.52E-04	-1.62E-04	-3.48E-04
22514.7	8.33E-04	6.03E-04	5.48E-04	2.19E-04	-2.84E-04	-3.77E-04
23014.7	7.37E-04	4.44E-04	5.11E-04	3.50E-04	-4.36E-04	-4.12E-04
23514.7	6.04E-04	3.28E-04	4.47E-04	4.26E-04	-3.50E-04	-4.52E-04
24014.7	8.64E-04	2.81E-04	4.35E-04	2.37E-04	-2.48E-05	-3.99E-04
24514.7	8.12E-04	1.96E-04	5.57E-04	3.07E-04	-5.45E-05	-4.13E-04
25014.7	6.06E-04	5.50E-05	-	-	-7.62E-05	-4.74E-04

Table 6-5. Continued

Pressure			Tempera	iture (°F)					
(psia)	300	320	340	360	380	415			
	Absolute Error (cp)								
514.7	9.05E-04	8.67E-04	8.27E-04	7.87E-04	7.45E-04	6.67E-04			
1014.7	6.95E-04	6.65E-04	6.32E-04	5.97E-04	5.59E-04	4.90E-04			
1514.7	4.97E-04	4.74E-04	4.46E-04	4.18E-04	3.86E-04	3.27E-04			
2014.7	3.09E-04	2.92E-04	2.73E-04	2.51E-04	2.25E-04	1.75E-04			
2514.7	1.32E-04	1.23E-04	1.10E-04	9.36E-05	7.49E-05	3.42E-05			
3014.7	-3.01E-05	-3.22E-05	-3.92E-05	-4.97E-05	-6.35E-05	-9.42E-05			
3514.7	-1.75E-04	-1.73E-04	-1.74E-04	-1.78E-04	-1.88E-04	-2.10E-04			
4014.7	-3.02E-04	-2.94E-04	-2.91E-04	-2.92E-04	-2.96E-04	-3.14E-04			
4514.7	-4.05E-04	-3.90E-04	-9.76E-05	-3.88E-04	-3.84E-04	-4.14E-04			
5014.7	-3.94E-04	-2.72E-04	-1.99E-04	-4.58E-04	-4.33E-04	-4.96E-04			
5514.7	-4.05E-04	-2.82E-04	-4.60E-04	-5.14E-04	-4.74E-04	-5.25E-04			
6014.7	-3.76E-04	-3.09E-04	-5.44E-04	-5.90E-04	-5.95E-04	-5.52E-04			
6514.7	-4.07E-04	-3.61E-04	-4.98E-04	-5.32E-04	-5.02E-04	-6.47E-04			
7014.7	-3.46E-04	-3.48E-04	-4.04E-04	-4.27E-04	-4.81E-04	-6.40E-04			
7514.7	-2.72E-04	-3.23E-04	-3.38E-04	-4.47E-04	-4.59E-04	-6.38E-04			
8014.7	-2.33E-04	-2.48E-04	-3.52E-04	-3.13E-04	-4.43E-04	-6.64E-04			
8514.7	-9.35E-05	-1.86E-04	-3.90E-04	-5.51E-04	-4.81E-04	-5.95E-04			
9014.7	-1.52E-04	-1.73E-04	-5.41E-04	-5.58E-04	-4.72E-04	-5.75E-04			
9514.7	-8.49E-05	-1.10E-04	-4.34E-04	-4.96E-04	-4.79E-04	-5.17E-04			
10014.7	-5.39E-05	-5.03E-05	-3.86E-04	-4.31E-04	-3.82E-04	-4.79E-04			
10514.7	4.16E-05	-8.72E-05	-3.92E-04	-4.65E-04	-3.95E-04	-4.49E-04			
11014.7	1.43E-04	-6.43E-05	-3.86E-04	-5.12E-04	-2.71E-04	-4.76E-04			
11514.7	1.87E-04	-2.73E-06	-3.24E-04	-4.60E-04	-2.49E-04	-3.49E-04			
12014.7	-1.47E-04	6.27E-05	-3.50E-04	-3.88E-04	-2.54E-04	-3.03E-04			
12514.7	-2.06E-04	1.16E-04	-3.76E-04	-2.91E-04	-2.19E-04	-3.21E-04			
13014.7	-1.26E-04	1.60E-04	-3.95E-04	-2.94E-04	-2.39E-04	-3.13E-04			
13514.7	-1.23E-04	1.48E-04	-3.58E-04	-1.79E-04	-2.21E-04	-3.14E-04			
14014.7	-1.09E-04	1.50E-04	-3.97E-04	-1.28E-04	-2.02E-04	-3.10E-04			

Table 6-5. Continued

Pressure			Tempera	ture (°F)					
(psia)	300	320	340	360	380	415			
	Absolute Error (cp)								
14514.7	-1.35E-05	1.27E-04	-4.05E-04	-8.63E-05	-1.48E-04	-2.60E-04			
15014.7	-6.55E-05	8.91E-05	-4.02E-04	-1.03E-04	-1.67E-04	-2.06E-04			
15514.7	-9.48E-05	-1.09E-05	-5.28E-04	-9.83E-05	-1.18E-04	-1.22E-05			
16014.7	-1.52E-04	-4.39E-05	-9.12E-04	-1.32E-04	-1.31E-04	-2.88E-05			
16514.7	-2.85E-04	-1.24E-04	-8.11E-04	-1.43E-04	-1.40E-04	4.87E-05			
17014.7	-2.40E-04	-2.52E-04	-7.97E-04	-1.68E-04	-1.69E-04	-1.56E-06			
17514.7	-3.28E-04	-2.25E-04	-7.11E-04	-1.75E-04	-1.97E-04	-5.35E-06			
18014.7	-4.07E-04	-2.67E-04	-1.07E-03	-2.19E-04	-2.03E-04	-2.22E-04			
18514.7	-3.06E-04	-5.10E-04	-1.09E-03	-3.61E-04	-2.40E-04	-9.72E-05			
19014.7	-3.79E-04	-5.01E-04	-1.08E-03	-1.63E-04	-2.35E-04	-2.37E-04			
19514.7	-4.51E-04	-3.95E-04	-1.06E-03	-2.27E-04	-2.09E-04	-9.44E-05			
20014.7	-4.90E-04	-3.95E-04	-9.32E-04	-2.76E-04	-1.75E-04	-4.77E-05			
20514.7	-6.20E-04	-3.98E-04	-9.59E-04	-2.82E-04	-2.28E-04	-1.27E-04			
21014.7	-5.59E-04	-3.44E-04	-9.16E-04	6.45E-05	-1.72E-04	5.55E-05			
21514.7	-6.98E-04	-4.86E-04	-9.61E-04	4.53E-05	-5.01E-05	1.96E-04			
22014.7	-7.93E-04	-5.44E-04	-8.45E-04	1.02E-04	-1.42E-04	2.49E-05			
22514.7	-7.20E-04	-6.55E-04	-9.70E-04	1.90E-04	-2.03E-04	2.26E-04			
23014.7	-8.15E-04	-5.77E-04	-8.05E-04	2.74E-04	-1.65E-04	3.75E-04			
23514.7	-8.11E-04	-7.48E-04	-7.15E-04	2.73E-04	-3.66E-05	3.07E-04			
24014.7	-9.96E-04	-1.17E-03	-5.63E-04	2.77E-04	-4.78E-05	6.22E-04			
24514.7	-4.16E-04	-1.23E-03	-6.38E-04	-2.66E-04	-1.02E-05	6.06E-04			
25014.7	-	-1.32E-03	-6.12E-04	-	-9.98E-05	-			

Table 6-6. Relative error analysis by comparing methane viscosity data with values from correlation

Pressure	Temperature (°F)								
(psia)	100	120	140	160	180	188	200		
	Relative Error (%)								
514.7	9.584	9.217	8.847	8.482	8.112	7.964	7.746		
1014.7	6.645	6.492	6.311	6.121	5.906	5.815	5.677		
1514.7	3.932	3.971	3.975	3.943	3.877	3.848	3.787		
2014.7	1.623	1.801	1.937	2.028	2.085	2.102	2.107		
2514.7	-0.155	0.078	0.280	0.449	0.585	0.626	0.683		
3014.7	-1.365	-1.162	-0.963	-0.769	-0.605	-0.543	-0.461		
3514.7	-2.098	-1.966	-1.812	-1.641	-1.481	-1.418	-1.332		
4014.7	-2.462	-2.429	-2.333	-2.214	-2.078	-2.026	-1.945		
4514.7	-2.557	-2.626	-2.340	-2.537	-2.446	-2.413	-2.343		
5014.7	-3.079	-2.707	-2.225	-2.595	-3.563	-2.604	-1.597		
5514.7	-2.514	-2.549	-0.733	-2.094	-3.160	-2.730	-1.471		
6014.7	-4.303	-1.584	-0.665	-1.501	-2.692	-3.102	-2.274		
6514.7	-2.965	-0.159	-1.662	-1.272	-2.270	-2.310	-1.890		
7014.7	-0.885	0.588	-1.516	-0.810	-1.650	-1.523	-1.791		
7514.7	-1.121	1.049	-1.821	-0.687	-1.003	-1.163	-1.554		
8014.7	-0.667	1.252	-1.399	1.150	-1.250	-0.641	-1.247		
8514.7	-0.379	1.237	-1.273	1.577	-0.708	-0.226	-1.183		
9014.7	-0.486	0.944	-1.048	1.574	-0.041	0.377	-0.985		
9514.7	-0.391	0.920	-0.758	1.228	0.542	0.636	-0.723		
10014.7	-0.151	0.804	-0.426	1.402	0.647	0.871	-0.569		
10514.7	-0.051	0.865	-0.382	1.404	0.397	1.484	-0.455		
11014.7	-0.028	0.858	0.088	1.418	1.220	1.542	-0.284		
11514.7	0.104	0.860	0.573	1.603	1.331	1.652	0.048		
12014.7	0.267	1.001	0.836	1.562	1.486	1.888	0.272		
12514.7	0.501	1.035	0.984	1.571	1.457	2.133	0.280		
13014.7	0.501	1.219	0.854	1.632	1.452	2.142	0.790		
13514.7	0.487	1.169	1.040	1.668	1.489	2.238	1.185		
14014.7	0.388	1.100	0.948	1.536	1.603	2.074	1.076		

Table 6-6. Continued

Pressure			Tem	perature	(°F)		
(psia)	100	120	140	160	180	188	200
			Relat	ive Erroi	(%)		
14514.7	0.240	0.977	0.963	1.439	1.523	1.939	0.999
15014.7	0.347	0.970	0.875	1.562	1.370	1.605	1.105
15514.7	0.219	0.796	0.769	1.787	1.299	1.471	1.337
16014.7	0.038	0.875	0.805	1.068	1.380	1.356	1.456
16514.7	0.080	0.652	0.766	0.695	1.303	1.204	1.611
17014.7	-0.083	0.469	0.708	0.693	1.325	1.158	1.583
17514.7	-0.275	0.307	0.682	0.800	1.036	1.278	1.417
18014.7	-0.490	0.154	0.488	0.522	0.858	1.143	0.990
18514.7	-0.667	0.151	0.387	0.361	0.847	1.009	0.424
19014.7	-0.902	0.007	0.507	0.520	0.773	0.895	0.677
19514.7	-0.923	-0.172	0.340	0.302	0.578	0.704	0.671
20014.7	-1.082	-0.470	0.133	0.259	0.535	0.433	0.347
20514.7	-1.302	-0.623	0.190	0.115	0.498	1.043	0.325
21014.7	-2.167	-0.826	-0.126	0.003	0.353	1.106	-0.057
21514.7	-1.847	-1.108	-0.174	-0.130	0.243	0.956	-0.142
22014.7	-1.979	-1.386	-0.385	-0.262	0.023	0.862	-0.144
22514.7	-2.228	-1.977	-0.537	-0.552	-0.094	0.746	-0.060
23014.7	-2.601	-1.526	-0.605	-0.616	-0.201	0.497	-0.222
23514.7	-2.869	-2.139	-0.876	-0.569	-0.067	0.289	-0.318
24014.7	-2.941	-2.405	-1.044	-0.257	-0.458	0.060	-0.177
24514.7	-3.322	-2.579	-1.216	-0.436	-0.792	0.168	-0.284
25014.7	-3.607	-	-1.315	-0.923	-1.037	-	-

Table 6-6. Continued

Pressure	Temperature (°F)							
(psia)	220	220   225   230   250   260   280						
	Relative Error (%)							
514.7	7.376	7.282	7.194	6.833	6.645	6.285		
1014.7	5.444	5.384	5.322	5.071	4.943	4.685		
1514.7	3.672	3.645	3.612	3.465	3.389	3.221		
2014.7	2.097	2.091	2.081	2.037	2.000	1.917		
2514.7	0.749	0.765	0.775	0.797	0.799	0.786		
3014.7	-0.346	-0.324	-0.304	-0.229	-0.202	-0.170		
3514.7	-1.198	-1.169	-1.143	-1.044	-1.004	-0.942		
4014.7	-1.820	-1.791	-1.767	-1.662	-1.616	-1.540		
4514.7	-2.243	-2.455	-2.210	-2.122	-2.041	-1.972		
5014.7	-2.480	-2.678	-2.580	-1.879	-2.161	-1.983		
5514.7	-2.151	-2.182	-2.015	-1.664	-2.149	-2.102		
6014.7	-1.827	-2.011	-1.771	-1.421	-1.990	-2.013		
6514.7	-2.001	-1.819	-1.566	-1.093	-1.854	-2.098		
7014.7	-0.975	-1.254	-1.360	-1.010	-1.337	-1.899		
7514.7	-1.566	-0.906	-0.794	-0.861	-1.143	-1.654		
8014.7	-0.908	-1.296	-0.537	-0.669	-1.330	-1.569		
8514.7	-0.142	-1.105	-0.445	-0.472	-0.951	-1.437		
9014.7	0.530	-0.648	-0.201	0.079	-0.832	-1.285		
9514.7	0.899	-0.180	0.110	0.192	-0.504	-0.819		
10014.7	1.154	0.155	0.455	0.515	-0.134	-0.671		
10514.7	1.214	0.808	1.001	0.798	0.200	-0.317		
11014.7	1.531	0.945	1.143	0.940	0.546	-0.213		
11514.7	1.765	1.414	1.647	0.886	1.028	-0.233		
12014.7	1.927	1.602	1.788	1.011	0.787	-0.147		
12514.7	1.950	1.762	1.695	1.034	0.995	-0.123		
13014.7	2.407	1.800	2.120	1.191	0.984	-0.032		
13514.7	2.342	2.366	2.340	1.739	0.995	0.042		
14014.7	2.400	1.645	2.644	1.849	1.173	-0.052		

Table 6-6. Continued

Pressure			Temper	ature (°	F)			
(psia)	220	225	230	250	260	280		
	Relative Error (%)							
14514.7	2.177	1.678	2.441	1.742	0.940	-0.059		
15014.7	2.112	1.270	2.010	1.274	0.899	-0.487		
15514.7	2.068	1.654	2.018	1.585	0.793	-0.161		
16014.7	2.059	1.697	2.218	1.338	1.121	-0.428		
16514.7	2.125	2.009	2.352	1.658	1.128	-0.309		
17014.7	1.784	1.942	1.938	1.711	1.313	-0.626		
17514.7	1.996	1.986	1.959	1.773	1.020	-0.438		
18014.7	1.803	2.244	1.851	1.857	0.971	-0.530		
18514.7	1.967	1.937	1.883	1.900	0.658	-0.478		
19014.7	1.989	1.820	1.724	1.820	0.590	-0.490		
19514.7	2.252	1.679	1.774	1.675	0.271	-0.654		
20014.7	2.480	1.560	1.624	1.687	0.276	-0.469		
20514.7	2.290	1.551	1.396	1.258	0.153	-0.662		
21014.7	2.224	1.576	1.317	0.986	-0.187	-0.936		
21514.7	1.878	1.335	1.266	0.596	-0.127	-0.778		
22014.7	1.808	1.221	1.210	0.504	-0.324	-0.708		
22514.7	1.602	1.162	1.060	0.430	-0.560	-0.757		
23014.7	1.396	0.841	0.974	0.681	-0.844	-0.815		
23514.7	1.124	0.611	0.840	0.818	-0.669	-0.882		
24014.7	1.596	0.517	0.806	0.447	-0.047	-0.769		
24514.7	1.479	0.355	1.022	0.572	-0.102	-0.785		
25014.7	1.084	0.098	-	-	-0.141	-0.888		

Table 6-6. Continued

Pressure	Temperature (°F)								
(psia)	300	320	340	360	380	415			
	Relative Error (%)								
514.7	5.929	5.578	5.224	4.881	4.537	3.944			
1014.7	4.416	4.150	3.879	3.603	3.322	2.833			
1514.7	3.044	2.856	2.652	2.446	2.229	1.843			
2014.7	1.816	1.696	1.565	1.419	1.256	0.957			
2514.7	0.744	0.683	0.608	0.511	0.405	0.181			
3014.7	-0.162	-0.172	-0.208	-0.262	-0.331	-0.484			
3514.7	-0.901	-0.883	-0.886	-0.903	-0.945	-1.047			
4014.7	-1.484	-1.441	-1.422	-1.422	-1.438	-1.510			
4514.7	-1.903	-1.834	-0.466	-1.821	-1.800	-1.929			
5014.7	-1.785	-1.240	-0.914	-2.077	-1.965	-2.238			
5514.7	-1.768	-1.241	-2.016	-2.248	-2.083	-2.297			
6014.7	-1.580	-1.310	-2.296	-2.493	-2.520	-2.348			
6514.7	-1.652	-1.478	-2.038	-2.183	-2.072	-2.665			
7014.7	-1.360	-1.377	-1.607	-1.710	-1.927	-2.562			
7514.7	-1.038	-1.239	-1.310	-1.732	-1.788	-2.490			
8014.7	-0.861	-0.927	-1.323	-1.187	-1.680	-2.520			
8514.7	-0.337	-0.677	-1.421	-2.010	-1.774	-2.206			
9014.7	-0.530	-0.610	-1.903	-1.981	-1.696	-2.080			
9514.7	-0.288	-0.378	-1.493	-1.718	-1.676	-1.829			
10014.7	-0.178	-0.169	-1.295	-1.461	-1.308	-1.657			
10514.7	0.135	-0.285	-1.281	-1.534	-1.318	-1.517			
11014.7	0.451	-0.205	-1.233	-1.645	-0.887	-1.573			
11514.7	0.576	-0.008	-1.011	-1.447	-0.798	-1.134			
12014.7	-0.439	0.191	-1.066	-1.196	-0.794	-0.964			
12514.7	-0.599	0.346	-1.120	-0.881	-0.670	-0.999			
13014.7	-0.360	0.467	-1.150	-0.871	-0.717	-0.956			
13514.7	-0.344	0.422	-1.022	-0.521	-0.649	-0.938			
14014.7	-0.297	0.421	-1.110	-0.366	-0.582	-0.909			

Table 6-6. Continued

Pressure	Temperature (°F)							
(psia)	300	320	340	360	380	415		
	Relative Error (%)							
14514.7	-0.036	0.347	-1.111	-0.242	-0.420	-0.750		
15014.7	-0.172	0.239	-1.082	-0.283	-0.463	-0.583		
15514.7	-0.244	-0.029	-1.388	-0.265	-0.322	-0.034		
16014.7	-0.384	-0.113	-2.331	-0.349	-0.352	-0.079		
16514.7	-0.705	-0.312	-2.043	-0.371	-0.370	0.132		
17014.7	-0.583	-0.623	-1.973	-0.428	-0.438	-0.004		
17514.7	-0.782	-0.547	-1.735	-0.439	-0.501	-0.014		
18014.7	-0.952	-0.637	-2.536	-0.540	-0.507	-0.568		
18514.7	-0.705	-1.192	-2.541	-0.873	-0.590	-0.245		
19014.7	-0.860	-1.151	-2.491	-0.390	-0.568	-0.586		
19514.7	-1.004	-0.896	-2.402	-0.533	-0.499	-0.231		
20014.7	-1.073	-0.882	-2.091	-0.639	-0.410	-0.115		
20514.7	-1.334	-0.877	-2.118	-0.642	-0.528	-0.302		
21014.7	-1.187	-0.748	-1.998	0.146	-0.393	0.131		
21514.7	-1.458	-1.038	-2.064	0.101	-0.113	0.456		
22014.7	-1.629	-1.143	-1.794	0.224	-0.316	0.057		
22514.7	-1.462	-1.355	-2.026	0.413	-0.444	0.511		
23014.7	-1.629	-1.179	-1.665	0.589	-0.356	0.841		
23514.7	-1.599	-1.502	-1.462	0.579	-0.078	0.678		
24014.7	-1.932	-2.299	-1.139	0.580	-0.101	1.364		
24514.7	-0.806	-2.384	-1.272	-0.544	-0.021	1.311		
25014.7	-	-2.516	-1.206	-	-0.205	-		

### **CHAPTER VII**

## CONCLUSIONS AND RECOMMENDATIONS

#### 7.1 Conclusions

Upon the study we finished, following conclusions were made:

- I. At high pressure, nitrogen viscosities from lab are lower than NIST values. The difference between lab data and NIST values increases as pressure increases.
- II. At high pressure, methane viscosities from lab are higher than NIST values. The difference between lab data and NIST values increases as temperature decreases; this difference also increases as pressure increases.
- III. New gas viscosity correlations derived in this study can be used to predict gas viscosity at HPHT confidently considering very high methane concentration in HPHT gas reservoirs.
- IV. Existing gas viscosity correlations is inappropriate for gas with moderate to high nonhydrocarbon concentration.
- V. A new nitrogen viscosity correlation based on our lab data was developed and can be used in HPHT reservoirs containing significant amount of nitrogen.

### 7.2 Recommendations

Further study should focus on

- I. Measuring carbon dioxide viscosity at HPHT,
- II. Measuring bi-component and tri-component mixtures viscosity,
- III. Measuring viscosity of natural gas sampled from HPHT reservoirs,
- IV. Deriving a new correlation basing on lab data covering low to high pressure and temperature.

## **NOMENCLATURE**

Symbol Description

atm atmosphere

atms atmospheres, pressure unit

A area

A a layer in fluid flow between two plates

AA constant in friction factor equation

bar pressure unit, 1 bar = 0.987 atms

B buoyant force

B a layer in fluid flow between two plates (higher velocity than layer A)

BB constant in friction factor equation

cm centimeter

cp centipoise

CC constant in friction factor equation

CO<sub>2</sub> carbon dioxide

°C Celsius temperature

d difference

*d*<sub>b</sub> ball diameter

D drag force

 $D_{y}$  drag force in y dimension, or vertical direction

 $E_k$  kinetic energy per unit volume

f friction factor

 $f_d$  driving force

Symbol Description

 $f_f$  friction force

ft foot or feet

F force

<sup>o</sup>F degree Fahrenheit

g gravity acceleration factor

g gram

g gas

 $g_c$  gravity constant

H<sub>2</sub>S hydrogen sulfide

HPHT high pressure high temperature

*in* inch

kg kilogram

K constant for viscosity from capillary viscometer

K constant for viscosity correlation

Kpa thousand Pascal

<sup>o</sup>K Kelvin temperature

*l* length, distance

*m* mass

*m* meter

 $m_b$  mass of ball or sphere

Mpa million Pascal

 $M_w$  molecular weight

*n* number of moles

Newton, force unit

Symbol Description

N<sub>2</sub> nitrogen

 $N_{Re}$  Reynolds number

*p* pressure

 $\Delta p$  pressure change

 $p_1$  pressure at inlet of pipe or tube

 $p_2$  pressure at outlet of pipe or tube

 $p_i$  initial pressure

 $p_c$  critical pressure

 $p_{pc}$  pseudocritical pressure

psi gauge pressure

psia absolute pressure

psig gauge pressure

P poise

Pa Pascal

 $p_{pr}$  pseudoreduced pressure

 $p_r$  reduced pressure

r distance from center of circle, tube, or pipe

*R* radius of circle, tube, or pipe

R universal gas constant

 $R_{gas}$  universal gas constant

s second

sec second

SC standard condition

t time

Symbol Description

*T* temperature

 $T_c$  critical temperature

 $T_{pc}$  pseudocritical temperature

 $T_{pr}$  pseudoreduced temperature

 $T_r$  reduced temperature

*u* velocity

 $u_x$  velocity in x direction

 $u_y$  velocity in y direction

v velocity

 $v_{slip}$  slip velocity

V volume

 $V_1$  volume above mercury in capillary tube

 $V_2$  volume below mercury in capillary tube

 $V_b$  volume of ball or sphere

 $V_{elementary}$  elementary volume

weight weight

x direction or dimension

x constant for viscosity correlation

y direction or dimension

 $y_{CO_2}$  mole fraction of carbon dioxide in vapor

 $y_{H,S}$  mole fraction of hydrogen sulfide in vapor

 $y_{N_2}$  mole fraction of nitrogen in vapor

 $y_{N_5, CO_5, H_5S}$  mole fraction of the non-hydrocarbon component

Y constant for viscosity correlation

z z-factor

#### Greek

<u>Symbol</u> <u>Description</u>

 $\gamma$  shear rate

 $\gamma_g$  gas specific gravity

 $\mu$  viscosity

 $\mu_{1atm}$  gas viscosity at 1 atmosphere

 $\mu_g$  gas viscosity

 $\mu_{\rm gSC}$  gas viscosity at standard condition

υ kinetic viscosity

 $\xi$  constant for viscosity correlation

 $\pi$  a mathematical constant whose value is the ratio of any circle's

circumference to its diameter

 $\rho$  density

 $\rho_b$  ball or sphere density

 $\rho_f$  fluid density

 $\rho_g$  gas density

 $\rho_r$  reduced density

au shear stress

 $\psi$  sphericity

 $\Delta$  indicates difference

## **Subscripts**

Symbol Description

1 inlet of the tube or pipe

1 above the mercury in capillary tube viscometer

1atm 1 atmosphere

Symbol **Description** 2 outlet of the tube or pipe 2 below the mercury in capillary tube viscometer Avg average  ${\rm CO_2}$ carbon dioxide g gas  $H_2S$ hydrogen sulfide i initial

N<sub>2</sub> nitrogen

SC low pressure condition

gSC gas at low pressure condition

x direction or dimension

y direction or dimension

### REFERENCES

Adzumi, H. 1937. Studies on the Flow of Gaseous Mixtures through Capillaries. I The Viscosity of Binary Gaseous Mixtures. *Bulletin of the Chemical Society of Japan.* **12**, (5): 199-226.

Assael, M.J. Dalaouti, N.K. and Vesovic, V. 2001. Viscosity of Natural-Gas Mixtures: Measurements and Prediction. *International Journal of Thermophysics*. **22**, (1): 61-71.

Audonnet, F. and Padua, A.A.H. 2004. Viscosity and Density of Mixtures of Methane and n-Decane from 298 to 393 K and up to 75 MPa. *Fluid Phase Equilibria*. **216**: 235-244.

Baron J.D. Roof, J.G. and Well, F.W. 1959. Viscosity of Nitrogen, Methane, Ethane, and Propane at Elevated Temperature. *Journal of Chemical and Engineering Data*. **4**: 283-288.

Barua, A.K. Afzal, M. Flynn, G.P. and Ross, J. 1964. Viscosities of Hydrogen, Deuterium, Methane, and Carbon Monoxide from -50° to 150 °C below 200 Atmospheres. *The Journal of Chemical Physics*. **41**: 374-378.

Berwald, W.B. and Johnson, T.W. 1933. *Viscosity of Natural Gases*. U.S. Department of Commerce, Bureau of Mines, Technical Paper, 555.

Bicher, L.B. and Katz, D.L. 1943. Viscosity of Methane-Propane System. *Ind. Eng. Chem.* **35**: 754-761.

Blasius, H. 1913. Das Aehnlichkeitsgesetz bei Reibungsvorgängen in Flüssigkeiten. *Mitteilungen über Forschungsarbeiten auf dem Gebiete des Ingenieurwesens*. **131**: VDI-Verlag Berlin.

Boon, J.P. Legros, J.C. and Thomaes, G. 1967. On the Principle of Corresponding State for the Viscosity of Simple Liquids. *Physica*. **33**: 547-557.

Bourgoyne, T.A. Chenevert, E.M. Millhein, K.K. and Young, S.F. 1986. *Applied Drilling Engineering*. Richardson, Texas: Textbook Series, SPE.

Boyd, J. 1930. The Viscosity of Compressed Gases. *Physica Review*. **35**: 1284-1297.

Cambridge Viscosity Inc. 2010. Unpublished Paper. Viscous Drag in the Oscillating Piston Viscometer, Medford, Maryland: Cambridge Viscosity, Inc.

Canet, X. Baylaucq, A. and Boned, C. 2002. High-Pressure (up to 140 MPa) Dynamic Viscosity of the Methane+Decane System. *International Journal of Thermophysics*, **23**: 1469-1486.

Carmichael, L.T. Virginia, B. and Sage, B.H. 1965. Viscosities of Hydrocarbons. Methane. *Journal of Chemical and Engineering Data*. **10**: 57-61.

Carr, N.L. 1952. *The Viscosity of Gas Mixtures at High Pressures*. PhD thesis, Chicago, Illinois: Illinois Institute of Technology.

Carr, N.L. Kobayashi, R. and Burrows, D.B. 1954. Viscosity of Hydrocarbon Gases under Pressure. *Trans.* AIME. **201**: 264-272.

Castleman, R.A. 1926. The Resistance to the Steady Motion of Small Spheres in Fluids. National Advisory Committee for Aeronautics, Technical Note No. 231, Washington D.C., February.

Chan, R.K.Y. and Jackson, D.A. 1985. An Automated Falling-Cylinder High Pressure Laser-Doppler Viscometer. *J. Phys. E: Sci. Instrum.* **18**: 510-515.

Comings, E.W. and Egly, R.S. 1940. Viscosity of Gases and Vapors at High Pressures. *Industrial and Engineering Chemistry.* **32**: 714-718.

Comings, E.W. Mayland, B.J. and Egly, R.S. 1944. *The Viscosity of Gases at High Pressures*. Chicago, Illinois: University of Illinois Engineering Experiment Station Bulletin Series No. 354.

Dabir S.V. Tushar K. Ghosh D. Prasad, H.L. Nidamartyv. K. D. and Kalipatnapu Y.R. 2007. *Viscosity of Liquids-Theory, Estimation, Experiment, and Data*. Columbia, Missouri: University of Missouri.

Dempsey, J.R. 1965. Computer Routine Treats Gas Viscosity as a Variable. *Oil and Gas Journal*. 141-143, August 16.

Diehl, J. Gondouin, M. Houpeurt, A. Neoschil, J. Thelliez, M. Verrien, J.P. and Zurawsky, R. 1970. *Viscosity and Density of Light Paraffins, Nitrogen and Carbon Dioxide*. Technip, Paris, CREPS/Geopetrole.

Diller, D. E. 1980. Measurements of the Viscosity of Compressed Gases and Liquid Methane. *Physica*. **104A**: 417-426.

Diller, D. E. 1983. Measurements of the Viscosity of Compressed Gases and Liquid Nitrogen. *Physica*. **119A**: 92-100.

Dipippo R. Kestin, J. and Whitelaw, J.H. 1966. A High-Temperature Oscillating-Disk Viscometer. *Physica*. **32**: 2064-2080.

Earhart, R. F. 1916. The Ratio of Specific Heats and the Coefficient of Viscosity of Natural Gas from Typical Fields. *Trans. Am. Soc. Mech. Eng.* **38**: 983-994.

Ellis, C.P. and Raw, J.R. 1959. High Temperature Gas Viscosities. II. Nitrogen, Nitric Oxide, Boron Trifluoride, Silicon Tetrafluoride, and Sulfur Hexafluoride. *The Journal of Chemical Physics*. **30**(2): 574-576.

Elsharkawy, A.M. 2004. Efficient Methods for Calculations of Compressibility, Density, and Viscosity of Natural Gases, *Fluid Phase Equilibria*. **218**:1-13.

Florida Atlantic University. 2005. Falling Ball Viscometer. http://wise.fau.edu/~blarkin/Viscometer.html.

Flynn, G.P. Hanks, R.V. and Lemaire, N.A. 1963. Viscosities of Nitrogen, Helium, Neon, and Argon from -78.5° to 100 °C below 200 Atmospheres. *The Journal of Chemical Physics*. **38**: 154-162.

Giddings, J.G. James, T.F. and Riki, K. 1966. Development of a High-Pressure Capillary-Tube Viscometer and Its Application to Methane, Propane, and Their Mixtures in the Gases and Liquid Regions. *The Journal of Chemical Physics*. **45**: 578-586.

Golubev, I.F. 1959. *Viscosity of Gases and Gas Mixtures, a Handbook*. This book is a translation from Russian by the National Technical Information Service. Alexandria, Virginia.

Gonzalez, M.H. Eakin, B.E. and Lee, A.L. 1970. *Viscosity of Natural Gases*. New York: Institute of Gas Technology (Chicago) Monograph on API Research Project 65.

Gonzalez, M.H. Richard, F.B. and Lee, A.L. 1966. The Viscosity of Methane. Paper SPE 1483 presented at the Annual Fall Meeting, Dallas, 2-5 Oct.

Grevendonk, W. Herreman, W. and De Bock, A. 1970. Measurements on the Viscosity of Liquid Nitrogen. *Physica*. **46**: 600-604.

Helleman, J.M. Kestin, J. and Ro, S.T. 1973. The Viscosity of Oxygen and Some of Its Mixtures with Other Gases, *Physica*. **65**: 362-375.

- Helleman, J.M. Zink, H. and Van Paemel, O. 1970. The Viscosity of Liquid Argon and Liquid Methane along Isotherms as a Function of Pressure. *Physica*. **46**: 395-410.
- Herbert, T. and Stokes, G.G. 1886. The Coefficient of Viscosity of Air. *Philosophical Transactions of the Royal Society of London*. **177**: 767-799.
- Hongo, M. Yokoyama, C. and Takahashi, D. 1988. Viscosity of Methane-Chlorodifluoromethane (R22) Gaseous Mixtures in the Temperature Range from 298.15 to 373.15 °K and at pressures up to 5MP. *Journal of Chemical Engineering of Japan*. **21**: 632-639.
- Huang, E.T.S. Swift, G.W. and Fred, K. 1966. Viscosities of Methane and Propane at Low Temperatures and High Pressure. *AIChE Journal*. **12**: 932-936.
- Iwasaki, H. 1954. Measurement of Viscosity of Gases at High Pressure. II Viscosities of Nitrogen and Mixture of Nitrogen and Hydrogen. *The Chemical Research Institute of Non-Aqueous Solution*. 296-307.
- Johnston, H.L. and McCloskey, K.E. 1940. Viscosities of Several Common Gases between 90°K and Room Temperature. *The Journal of Physical Chemistry*. **44**(9): 1038-1058.
- Jossi, J.A. Stiel, L.I. and Thodos G. 1962. The Viscosity of Pure Substances in the Dense Gaseous and Liquid Phases. *AIChE Journal*. **8**(1): 59-62.
- Kestin, J. and Leidenfrost, W. 1959. An Absolute Determination of the Viscosity of Eleven Gases over a Range of Pressures. *Physica*. **25**: 1033-1062.
- Kestin, J. and Yata, J. 1968. Viscosity and Diffusion Coefficient of Six Binary Mixtures. *The Journal of Chemical Physics*. **49**: 4780-4791.
- Klimeck, J. Kleinrahm, R. and Wagner, W. 1998. An Accurate Single-Sinker Densimeter and Measurement of the  $(p, \rho, T)$  Relation of Argon and Nitrogen in the Temperature Range from (235 to 520) K at Pressures up to 30 Mpa. *J. Chem. Thermodynamics.* **30**: 1571-1588.
- Knapstad, B. Skjolsvik, P.A. and Oye, H.A. 1990. Viscosity of the n-Decane Methane System in the Liquid Phase. *Ber. Bunsenges Phys. Chem.* **94**: 1156-1165.
- Kuss, E. 1952. High pressure research II: the viscosity of compressed gases (in German). *Z. Angew. Phys.* **4**(6): 203-207.
- Lambert, J.D. Cotton, K.J. Pailthorpe, M.W. Robinson, A.M. Scrivins, J. Vale, W.R.F. and Young, R.M. 1955. Transport Properties of Gaseous Hydrocarbons. *Proceedings of*

the Royal Society of London. Series A, Mathematical and Physical Sciences. **231**(1185): 280-290.

Latto, B., and Saunders, M.W. 1972. Viscosity of Nitrogen Gas at Low Temperatures Up to High Pressures: A New Appraisal. *Physica*. **46**: 600-604.

Lee, A.L. 1965. *Viscosity of Light Hydrocarbons*. New York: American Petroleum Institute, Monograph on API Research Project 65.

Lee, A.L. Gonzalez, M.H. and Eakin, B.E. 1966. The Viscosity of Natural Gases. Paper SPE 1340 presented at the 1966 Annual Technical Conference and Exhibition held in Shreveport, Louisiana, 11-12 November.

Lemmon, E.W. Huber, M.L. and McLinden, M.O. 2007. *NIST Reference Fluid Thermodynamic and Transport Properties—REFPROP Version 8.0, User's Guide*. Physical and Chemical Properties Division, National Institute of Standards and Technology, Boulder, Colorado.

Londono. F. 2001. New Correlations for Hydrocarbon Gas Viscosity and Gas Density. MS thesis, College Station, Texas: Texas A&M University,

Malaguti, D. and Suitter, R. 2010. Communication between Author and Cambridge Engineers. March.

Marsh, J. Zvandasara, T. Macgill, A. and Jenny, K. 2010. Material Selection for HP/HT Developments. Paper SPE 130716-MS presented at SPE International Conference on Oilfield Corrosion held in Aberdeen, United Kingdom, 24-25 May.

Meyer, O.E. 1866. Viskositiit Der Kolloide. Pogg. Ann. 127: 263.

Michels A. and Gibson R.O. 1931. The Measurement of the Viscosity of Gases at High Pressures: The Viscosity of Nitrogen to 1000 Atms. *Proc. R. Soc. Lond. A.* **134**: 288-307.

National Institute of Science and Technology (NIST). 2010. Web-Book of Thermodynamic Properties of Fluids. http://webbook.nist.gov,chemisty/fluid.

Nowak, P. Kleinrahm, R. and Wagner, W. 1997a. Measurement and Correlation of the  $(p, \rho, T)$  Relation of Nitrogen I. The Homogeneous Gas and Liquid Regions in the Temperature Range from 55 K to 239 K at Pressures up to 12 MPa. *J. Chem. Thermodynamics*. **29**: 1137-1156.

Nowak, P. Kleinrahm, R. and Wagner, W. 1997b. Measurement and Correlation of the  $(p, \rho, T)$  Relation of Nitrogen II. Saturated Liquid and Saturated Vapor Densities and

Vapor Pressures along the Entire Coexistence Curve. *J. Chem. Thermodynamics*. **29**: 1157-1174.

Park, N.A. 1994. Apparatus and Method for Viscosity Measurements Using a Controlled Needle Viscometer. http://www.patentstorm.us/patents/5327778/claims.html.

Paul N. Gardner Company, Inc. 2010. Vibrational Viscometer Based on Tuning Fork Technology. http://www.gardco.com/pages/viscosity/viscometers/sv\_10\_100.html.

Rankine, A.O. 1910. On a Method of Determining the Viscosity of Gases, Especially Those Available only in Small Quantities. *Proc. Roy. Soc.* **83A**: 265-276.

Rankine, A.O. 1923. A Simple Viscometer for Gases. J. Sci. Instr. 1: 105-111

Rudenko, N.S. and Schubnikow, L.W. 1934. The Viscosity of Liquid Nitrogen, Carbon Monoxide, Argon and Oxygen as a Function of Temperature. *Physikalische Zeitschrift Sowjetunion*. **6**: 470-477.

Ross, J. and Brown, G. 1957. Viscosity of Gases at High Pressures. *Ind. Eng. Chem.* **49**: 2026-2033.

Sage, B.H. and Lacey, W.N. 1938. Effect of Pressure upon Viscosity of Methane and Two Natural Gases. *Trans. Am. Inst. Mining Met. Engrs.* **127**: 118-134.

Schley, P. Jaeschke, M. Kuchenmeister, C. and Vogel E. 2004. Viscosity Measurements and Predictions for Natural Gas. *International Journal of Thermophysics*. **25**: 1623-1652.

Seibt, D. Vogel, E. Bich, E. Buttig, D. and Hassel, E. 2006. Viscosity Measurements on Nitrogen. *J. Chem. Eng. Data.* **51**: 526-533.

Setzmann, U. and Wagner, W. 1991. A New Equation of State and Tables of Thermodynamic Properties for Methane Covering the Range from the Melting Line to 625 K at Pressures up to 1000 MPa. *J. Phys. Chem. Ref. Data.* **20**(6): 1061-1155.

Smith, A.S. and Brown, G.G. 1943. Correlating Fluid Viscosity. *Ind. Eng. Chem.* **35**: 705-711.

Steffe, J.F. 1992. An Oscillating Sphere System for Creating Controlled Amplitude in Liquid, Rheological Methods in Food Process Engineering. Michigan, Illinois: Freeman Press.

Stephan, K. and Lucas, K. 1979. *Viscosity of Dense Fluids*. West Lafayette, Indiana: The Purdue Research Foundation.

Stewart, J.R. 1952. The Viscosity of Natural Gas Components at High Pressure. Master thesis, Chicago, Illinois: Illinois Institute of Technology.

Stokes, G.G. 1868. On the Communication of Vibration from a Vibrating Body to a Surrounding Gas. *Philosophical Transactions of the Royal Society of London*. **158**: 447-463.

Straty, G.C. and Diller, D.E. 1980. PVT of Saturated and Compressed Fluid Nitrogen. *J. Chem. Thermodynamics*. **12**: 927-936.

Sutton, R.P. 2005. Fundamental PVT Calculations for Associated and Gas/Condensate Natural-Gas Systems. Paper SPE 97099 presented at the SPE Annual Technical Conference and Exhibition, Dallas, Texas, 9–12 October.

Swift, G.W. Christy, J.A. and Kurata, F. 1959. Liquid Viscosities of Methane and Propane. *AIChE Journal*. **5**: 98-102.

Swift, G.W. Lorenz J. and Kurata, F. 1960. Liquid Viscosities above the Normal Boiling Point for Methane, Ethane, Propane, and n-Butane. *AIChE Journal*. **6**: 415-419.

Tomida, D. Kumagai, A. and Yokoyama, C. 2005. Viscosity Measurements and Correlation of the Squalane + CO2 Mixture. *International Journal of Thermophysics*, **28**(1): 133-145.

Trautz, M. and Zink, R. 1930. The Viscosity, Thermal Conductivity and Diffusion in Gas Mixtures. XII. Gas Viscosity at High Temperatures (in German). *Ann. Phys.* (*Leipzig*). **7**: 427-452.

Van Der Gulik, P. S. Mostert, R. and Van Den Berg, H. R. 1988. The Viscosity of Methane at 25 °C up to 10 kbar. *Physica*. **151A**: 153-166.

Van Itterbeek, A. Hellemans, J. Zink, H. and Van Cauteren, M. 1966. Viscosity of Liquefied Gases at Pressures between 1 and 100 Atmosphere. *Physica*. **32**: 2171-2172.

Van Itterbeek A. Van Paemel, O. and Van Lierde, J. 1947. Measurements on the Viscosity of Gas Mixtures. *Physica XIII*. **1-3**: 88-96.

Viswanathan, A. 2007. Viscosities of Natural Gases at High Pressures and High Temperatures. Master thesis, College Station, Texas: Texas A&M University.

Viswanathan, A. and McCain Jr., W.D. 2005. Crisman Institute for Petroleum Research Monthly Report, April 2005. Department of Petroleum Engineering, College Station: Texas A&M University.

Viswanathan, A. McCain Jr. W.D., and Teodoriu, C. 2006. Crisman Institute for Petroleum Research Monthly Report, March to December 2006. Department of Petroleum Engineering, College Station: Texas A&M University.

Vogel, E. Wilhelm, J. Cornelia, K. and Manfred, J. 1999. High-Precision Viscosity Measurements on Methane. Presented at the 15<sup>th</sup> European Conference on Thermophysical Properties, Wurzburg, Germany, 5-9 September.

Wikipedia. 2009. Definition of Fanning Friction Factor. http://en.wikipedia.org/wiki/Fanning friction factor.

Wikipedia. 2010. Viscosity. http://en.wikipedia.org/wiki/Viscosity.

Wilson, J. 1965. A Method of Predicting the Viscosities of Natural Gases for a Wide Range of Pressures and Temperatures. PhD dissertation, College Station, Texas: Texas A&M University.

Yen, K. 1919. LVIII. An Absolute Determination of the Coefficients of Viscosity of Hydrogen, Nitrogen, and Oxygen. *Philosophical Magazine Series 6*. Vol. **28**, Issue 227, Page 582-596.

Zhang, Zh. Fu, J. Lin, Y. Fan, H. Xia, B. and Zhang, J. 2010. The Mechanism of Pressure Control Problem in High H<sub>2</sub>S/CO<sub>2</sub> Gas Wells. Paper SPE 130143-MS presented at CPS/SPE International Oil & Gas Conference and Exhibition in China held in Beijing, China, 8-10 June.

# APPENDIX A

## Comparison of Nitrogen Viscosity from This Study with NIST Values

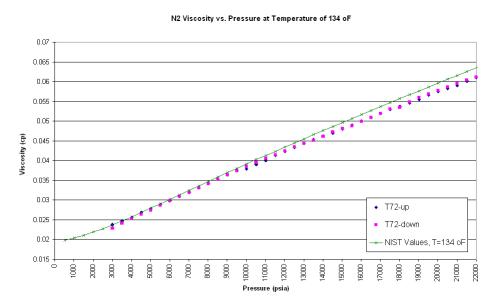


Figure A - 1. Nitrogen viscosity vs. pressure at 134 °F (Test 72)

## N2 Viscosity vs. Pressure at Temperature of 134 oF 0.07 0.065 0.06 0.055 0.05 Viscosity (cp) 0.045 0.04 0.035 0.03 • T73-up 0.025 NIST Values, T=134 oF 0.015 9

Figure A - 2. Nitrogen viscosity vs. pressure at 134 °F (Test 73)

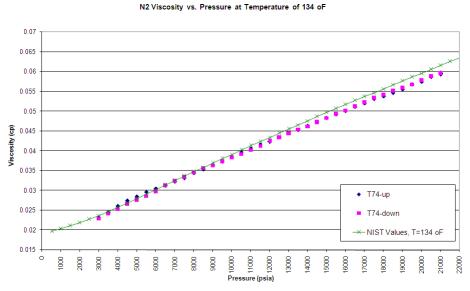


Figure A - 3. Nitrogen viscosity vs. pressure at 134 °F (Test74)

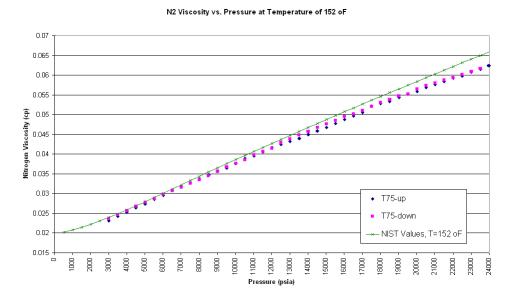


Figure A - 4. Nitrogen viscosity vs. pressure at 152 °F (Test 75)

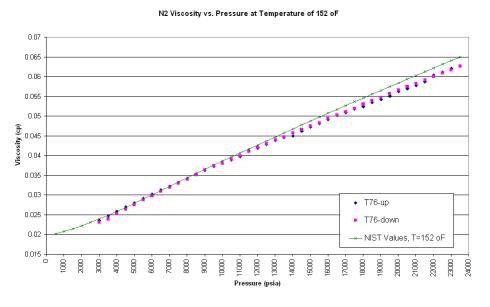


Figure A - 5. Nitrogen viscosity vs. pressure at 152 °F (Test 76)

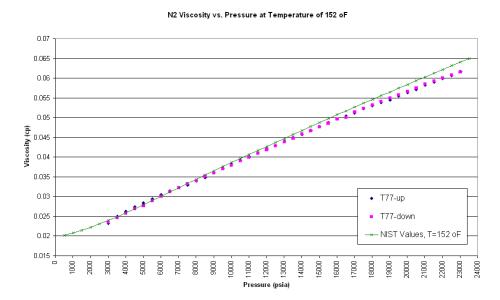


Figure A - 6. Nitrogen viscosity vs. pressure at 152 °F (Test 77)

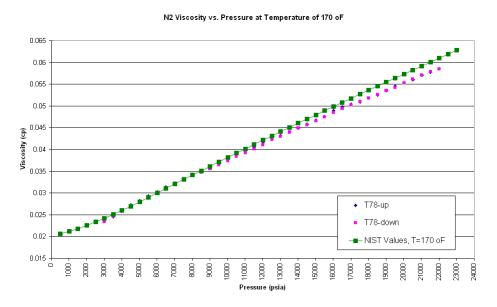


Figure A - 7. Nitrogen viscosity vs. pressure at 170 °F (Test 78)

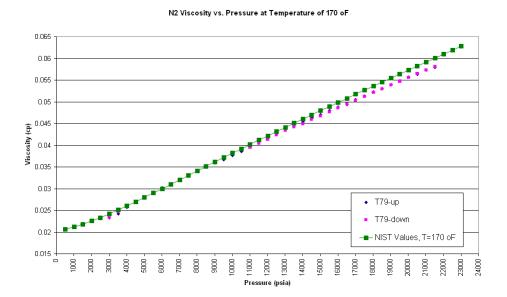


Figure A - 8. Nitrogen viscosity vs. pressure at 170 °F (Test 79)

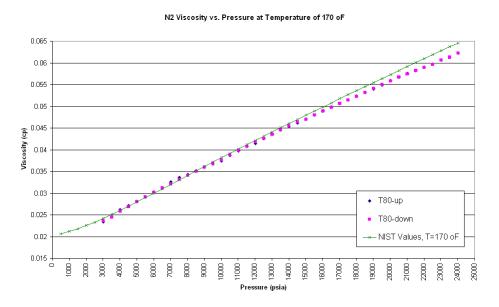


Figure A - 9. Nitrogen viscosity vs. pressure at 170 °F (Test 80)

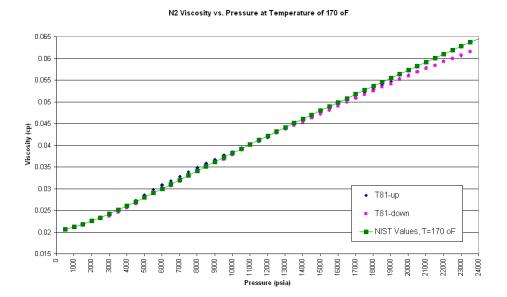


Figure A - 10. Nitrogen viscosity vs. pressure at 170 °F (Test 81)

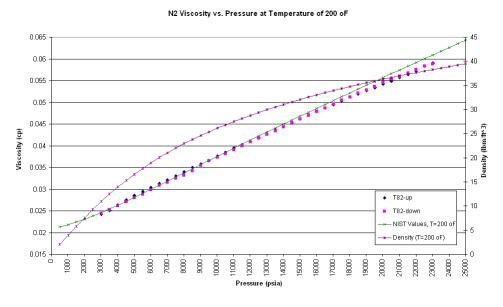


Figure A - 11. Nitrogen viscosity vs. pressure at 200 °F (Test 82)

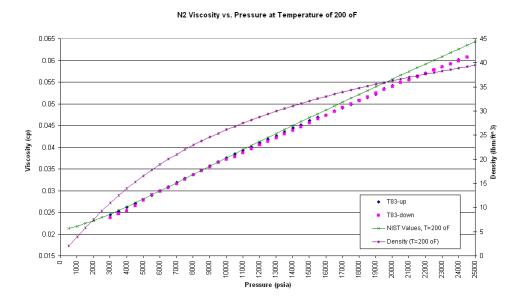


Figure A - 12. Nitrogen viscosity vs. pressure at 200 °F (Test 83)

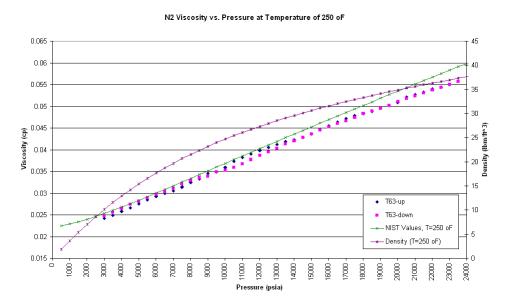


Figure A - 13. Nitrogen viscosity vs. pressure at 250 °F (Test 63)

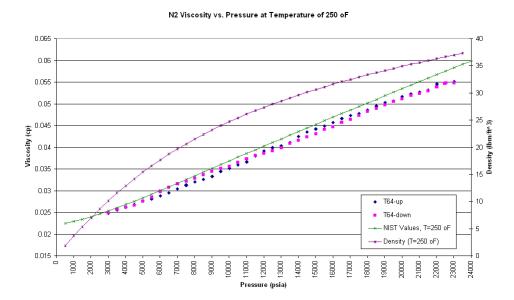


Figure A - 14. Nitrogen viscosity vs. pressure at 250 °F (Test 64)

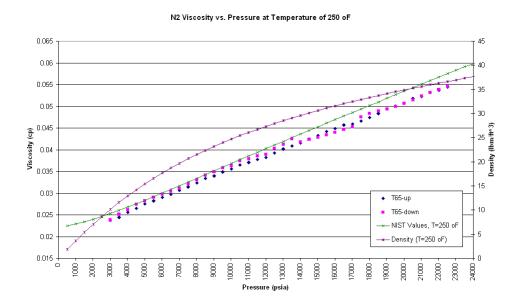


Figure A - 15. Nitrogen viscosity vs. pressure at 250 °F (Test 65)

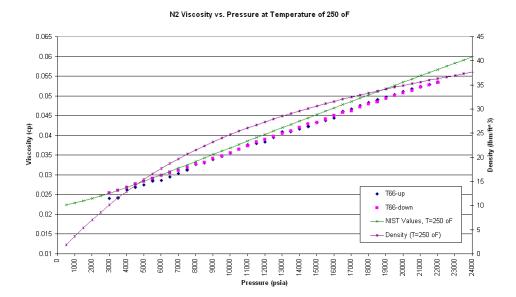


Figure A - 16. Nitrogen viscosity vs. pressure at 250 °F (Test 66)

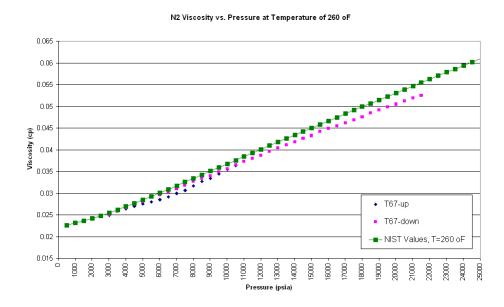


Figure A - 17. Nitrogen viscosity vs. pressure at 260 °F (Test 67)

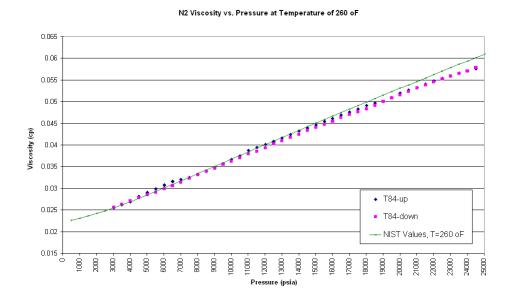


Figure A - 18. Nitrogen viscosity vs. pressure at 260 °F (Test 84)

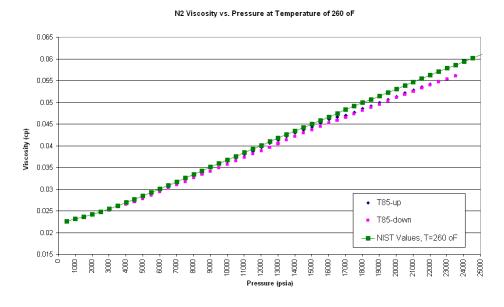


Figure A - 19. Nitrogen viscosity vs. pressure at 260 °F (Test 85)

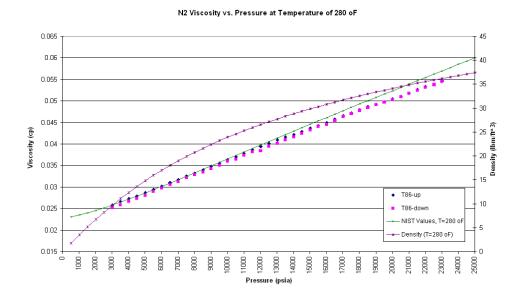


Figure A - 20. Nitrogen viscosity vs. pressure at 280 °F (Test 86)

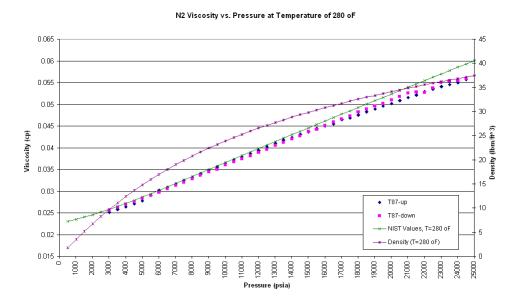


Figure A - 21. Nitrogen viscosity vs. pressure at 280 °F (Test 87)

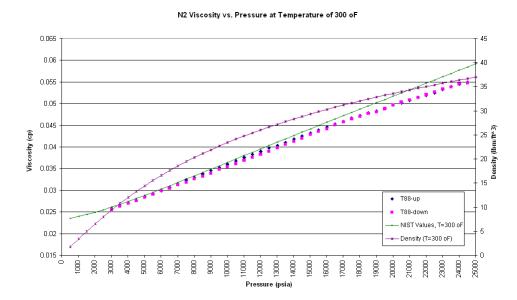


Figure A - 22. Nitrogen viscosity vs. pressure at 300 °F (Test 88)

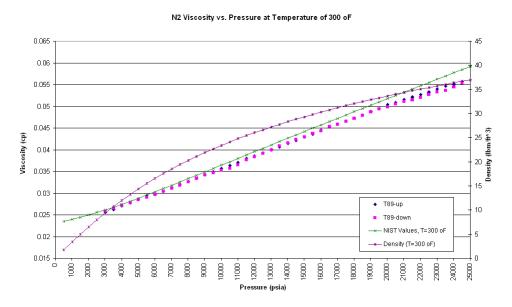


Figure A - 23. Nitrogen viscosity vs. pressure at 300 °F (Test 89)

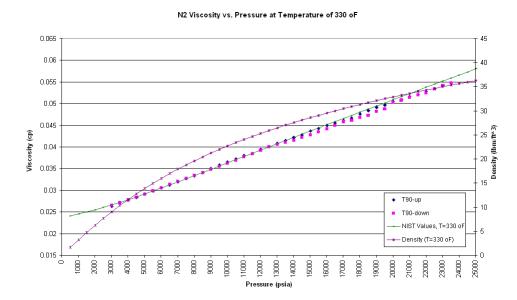


Figure A - 24. Nitrogen viscosity vs. pressure at 330 °F (Test 90)

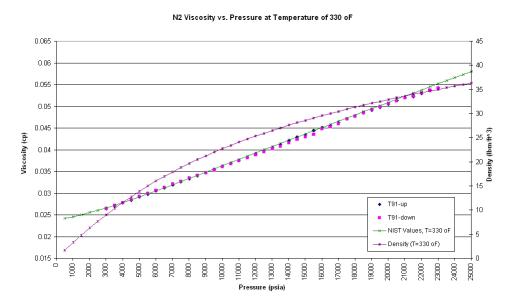


Figure A - 25. Nitrogen viscosity vs. pressure at 330 °F (Test 91)

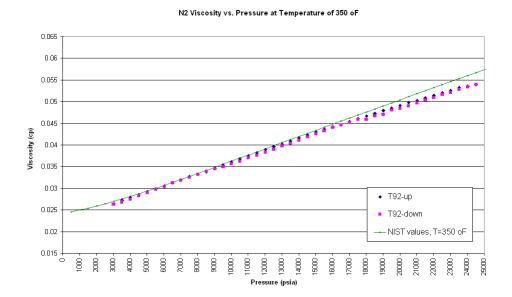


Figure A - 26. Nitrogen viscosity vs. pressure at 350 °F (Test 92)

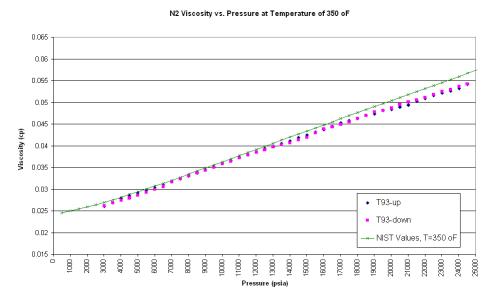


Figure A - 27. Nitrogen viscosity vs. pressure at 350 °F (Test 93)

## APPENDIX B

## Comparison of Methane Viscosity from This Study with NIST Value

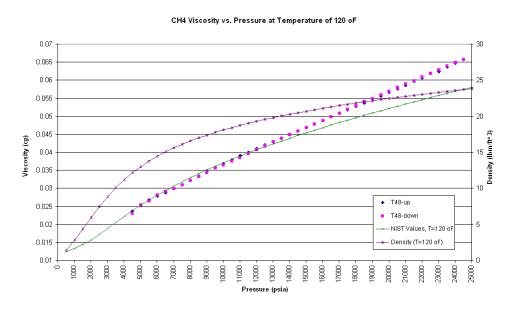


Figure B - 1. Methane viscosity vs. pressure at 120 °F (Test 48)

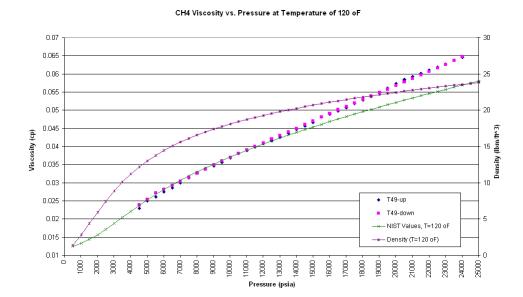


Figure B - 2. Methane viscosity vs. pressure at 120 °F (Test 49)

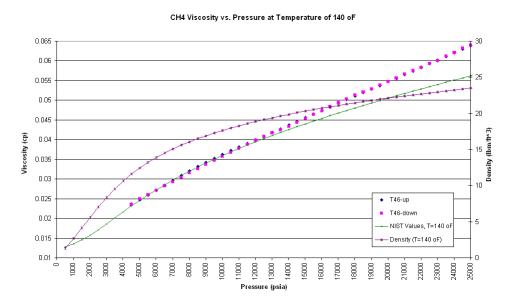


Figure B - 3. Methane viscosity vs. pressure at 140 °F (Test 46)

## CH4 Viscosity vs. Pressure at Temperature of 140 oF 0.065 0.055 0.05 0.045 Viscosity (cp) 0.04 0.035 0.03 0.025 T47-up 0.02 NIST Values, T=140 oF 0.015 Density (T=140 oF) 0.01 12000

Figure B - 4. Methane viscosity vs. pressure at 140 °F (Test 47)

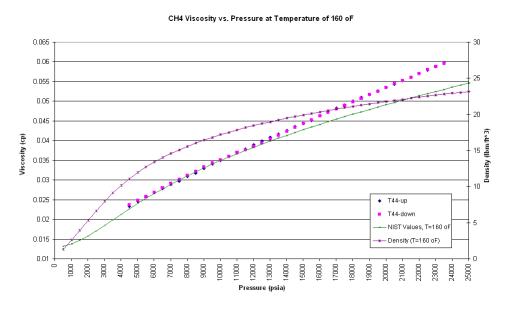


Figure B - 5. Methane viscosity vs. pressure at 160 °F (Test 44)

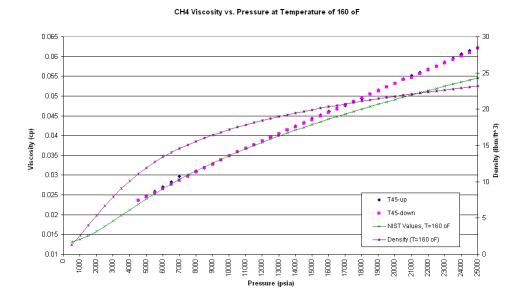


Figure B - 6. Methane viscosity vs. pressure at 160 °F (Test 45)

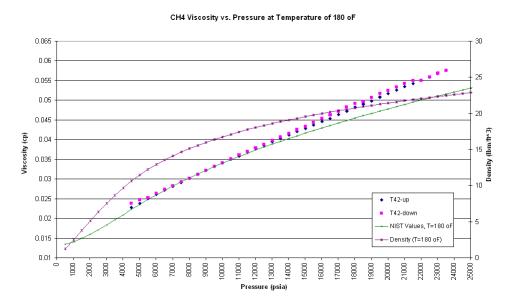


Figure B - 7. Methane viscosity vs. pressure at 180 °F (Test 42)

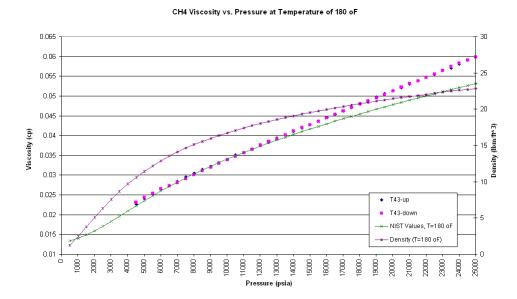


Figure B - 8. Methane viscosity vs. pressure at 180 °F (Test 43)

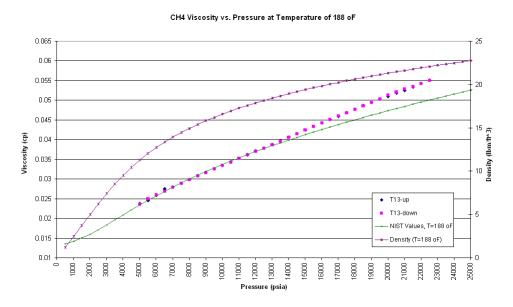


Figure B - 9. Methane viscosity vs. pressure at 188 °F (Test 13)

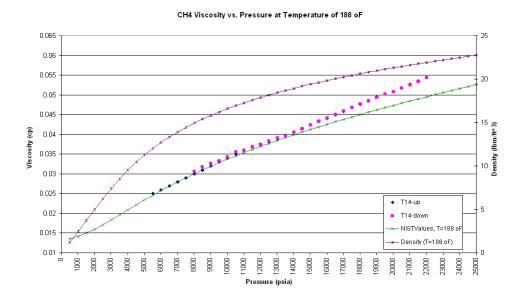


Figure B - 10. Methane viscosity vs. pressure at 188 °F (Test 14)

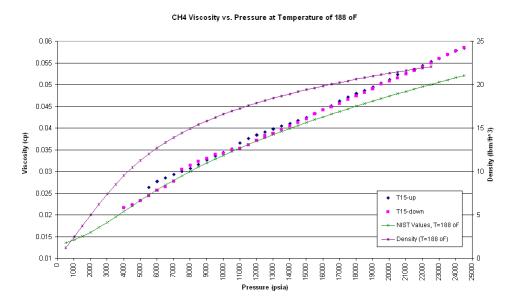


Figure B - 11. Methane viscosity vs. pressure at 188 °F (Test 15)

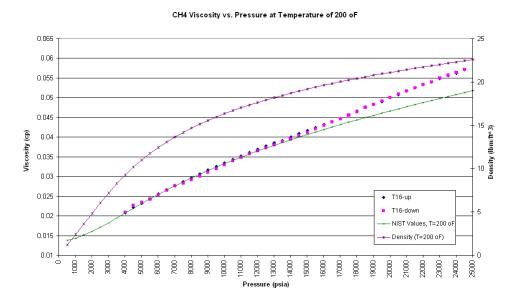


Figure B - 12. Methane viscosity vs. pressure at 200 °F (Test 16)

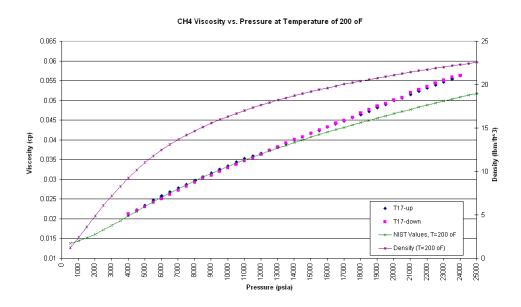


Figure B - 13. Methane viscosity vs. pressure at 200  $^{\rm o}$ F (Test 17)

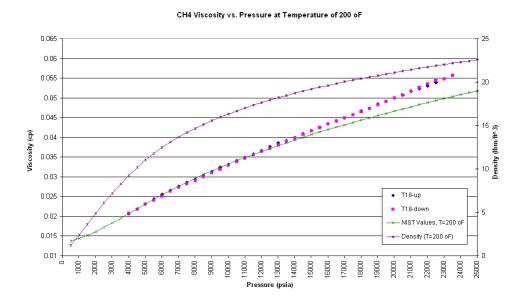


Figure B - 14. Methane viscosity vs. pressure at 200 °F (Test 18)

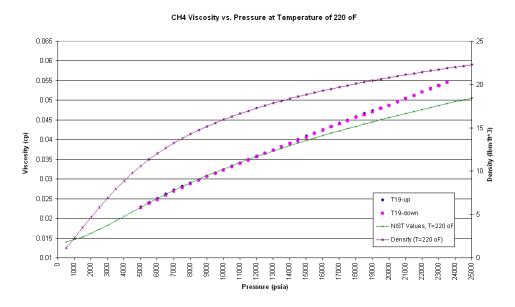


Figure B - 15. Methane viscosity vs. pressure at 220 °F (Test 19)

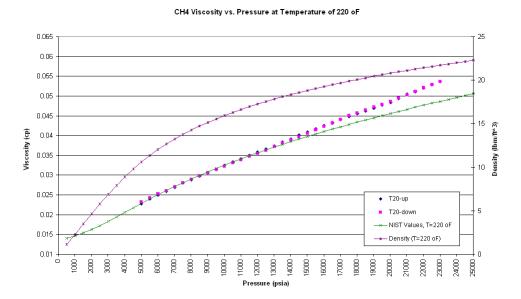


Figure B - 16. Methane viscosity vs. pressure at 220 °F (Test 20)

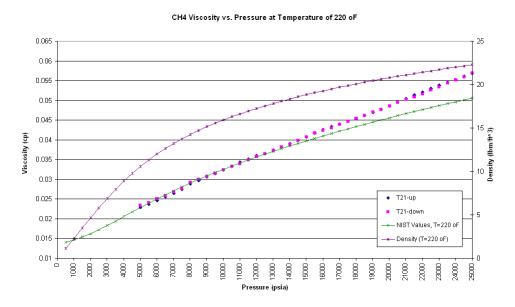


Figure B - 17. Methane viscosity vs. pressure at 220 °F (Test 21)

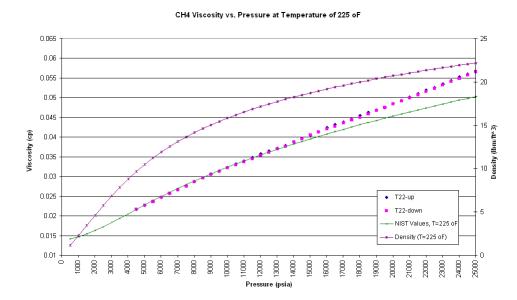


Figure B - 18. Methane viscosity vs. pressure at 225 °F (Test 22)

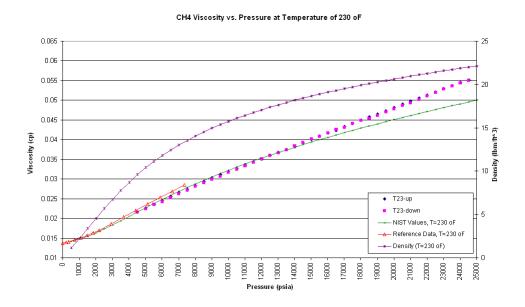


Figure B - 19. Methane viscosity vs. pressure at 230 °F (Test 23)

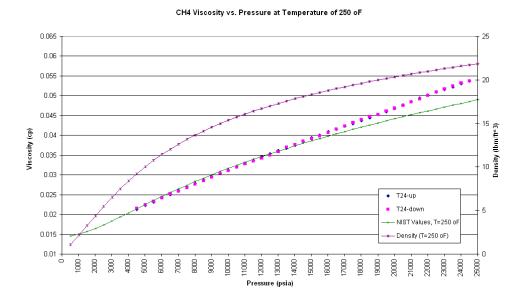


Figure B - 20. Methane viscosity vs. pressure at 250 °F (Test 24)

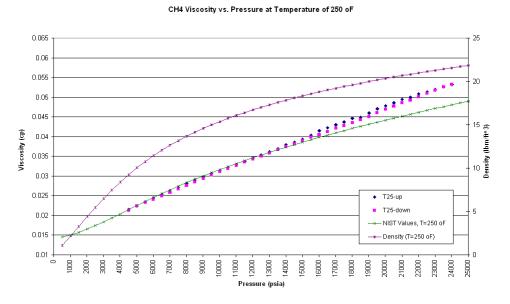


Figure B - 21. Methane viscosity vs. pressure at 250  $^{\rm o}$ F (Test 25)

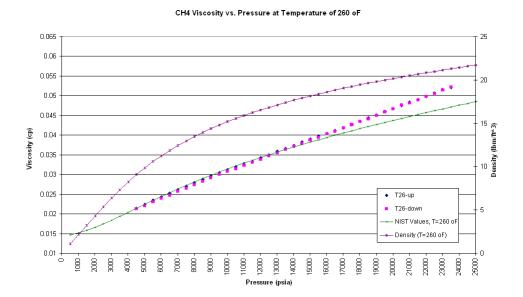


Figure B - 22. Methane viscosity vs. pressure at 260 °F (Test 26)

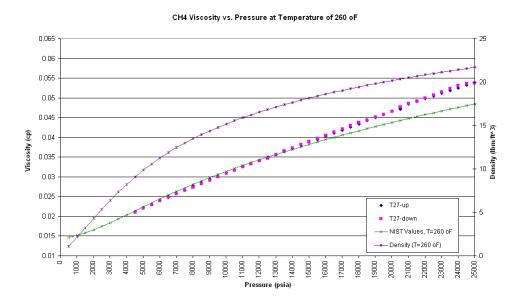


Figure B - 23. Methane viscosity vs. pressure at 260 °F (Test 27)

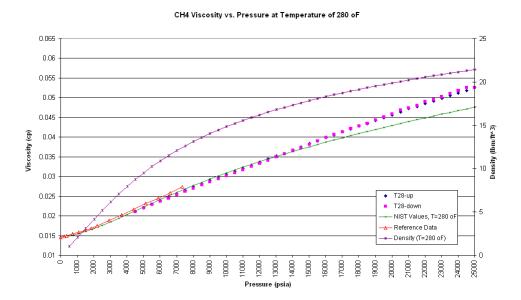


Figure B - 24. Methane viscosity vs. pressure at 280 °F (Test 28)

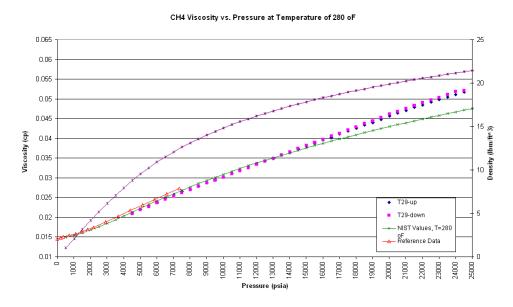


Figure B - 25. Methane viscosity vs. pressure at 280 °F (Test 29)

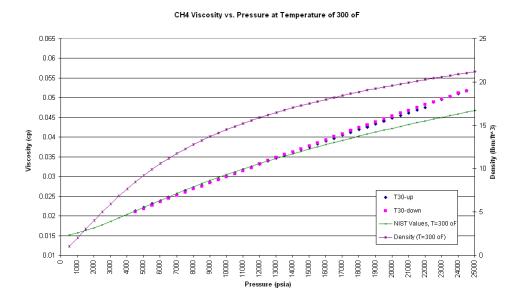


Figure B - 26. Methane viscosity vs. pressure at 300 °F (Test 30)

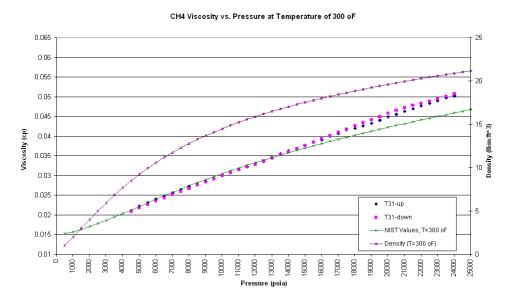


Figure B - 27. Methane viscosity vs. pressure at 300 °F (Test 31)

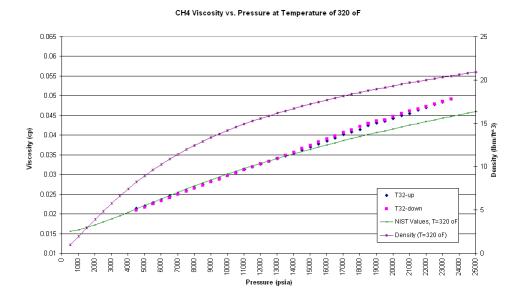


Figure B - 28. Methane viscosity vs. pressure at 320 °F (Test 32)

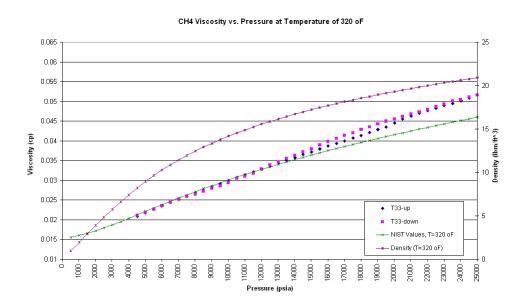


Figure B - 29. Methane viscosity vs. pressure at 320 °F (Test 33)

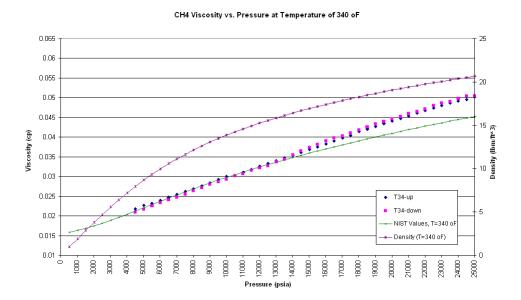


Figure B - 30. Methane viscosity vs. pressure at 340 °F (Test 34)

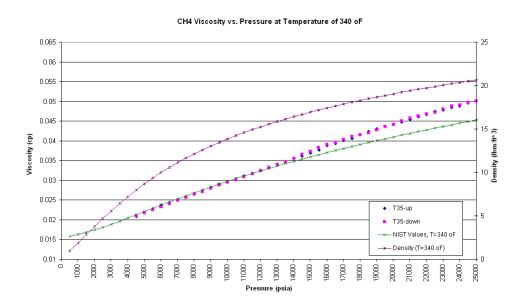


Figure B - 31. Methane viscosity vs. pressure at 340 °F (Test 35)

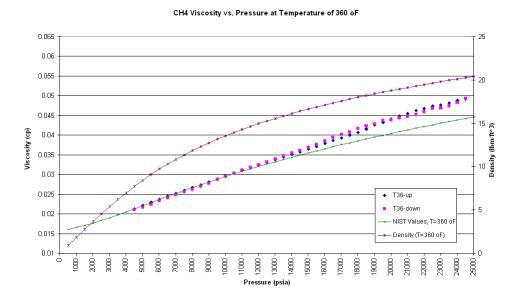


Figure B - 32. Methane viscosity vs. pressure at 360 °F (Test 36)

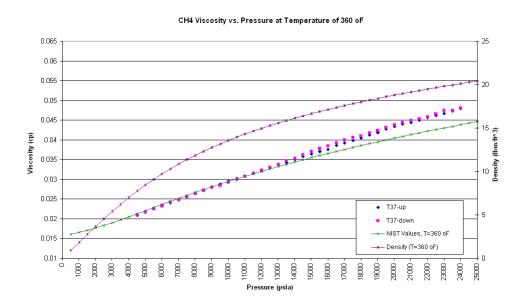


Figure B - 33. Methane viscosity vs. pressure at 360 °F (Test 37)

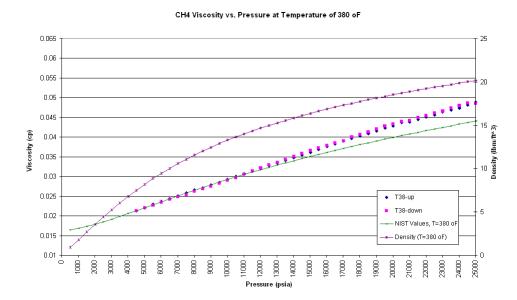


Figure B - 34. Methane viscosity vs. pressure at 380 °F (Test 38)

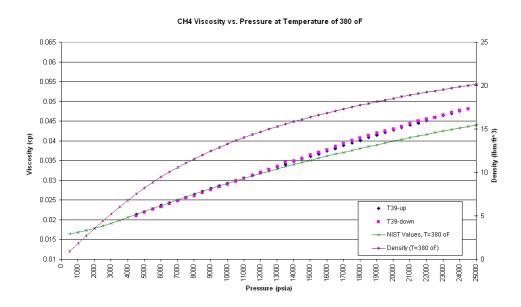


Figure B - 35. Methane viscosity vs. pressure at 380 °F (Test 39)

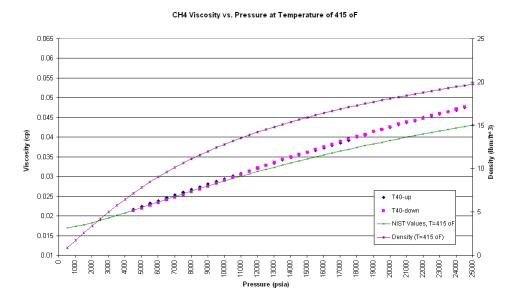


Figure B - 36. Methane viscosity vs. pressure at 415 °F (Test 40)

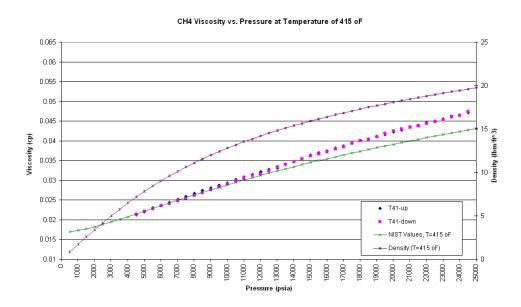


Figure B - 37. Methane viscosity vs. pressure at 415 °F (Test 41)

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