# COMPARISON OF EDIT HISTORY CLUSTERING TECHNIQUES FOR SPATIAL HYPERTEXT

A Thesis

by

## **BIKASH MANDAL**

Submitted to the Office of Graduate Studies of Texas A&M University in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

December 2005

Major Subject: Computer Science

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## Approved by:

Chair of Committee, Frank Shipman Committee Members, Richard Furuta

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#### **ABSTRACT**

Comparison of Edit History Clustering Techniques for
Spatial Hypertext. (December 2005)

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Chair of Advisory Committee: Dr. Frank Shipman

History mechanisms available in hypertext systems allow access to past user interactions with the system. This helps users evaluate past work and learn from past activity. It also allows systems identify usage patterns and potentially predict behaviors with the system. Thus, recording history is useful to both the system and the user.

Various tools and techniques have been developed to group and annotate history in Visual Knowledge Builder (VKB). But the problem with these tools is that the operations are performed manually. For a large VKB history growing over a long period of time, performing grouping operations using such tools is difficult and time consuming. This thesis examines various methods to analyze VKB history in order to automatically group/cluster all the user events in this history.

In this thesis, three different approaches are compared. The first approach is a pattern matching approach identifying repeated patterns of edit events in the history. The second approach is a rule-based approach that uses simple rules, such as "group all consecutive events on a single object". The third approach uses hierarchical agglomerative clustering (HAC) where edits are grouped based on a function of *edit time* and *edit location*.

The contributions of this thesis work are: (a) developing tools to automatically cluster large VKB history using these approaches, (b) analyzing performance of each approach

in order to determine their relative strengths and weaknesses, and (c) answering the question, "how well do the automatic clustering approaches perform" - by comparing the results obtained from this automatic tool with that obtained from the manual grouping performed by actual users on a same set of VKB history.

Results obtained from this thesis work show that the rule-based approach performs the best in that it best matches human-defined groups and generates the fewest number of groups. The hierarchic agglomerative clustering approach is in between the other two approaches with regards to identifying human-defined groups. The pattern-matching approach generates many potential groups but only a few matches with those generated by actual VKB users.

#### ACKNOWLEDGEMENTS

It is my great pleasure to offer my heart felt thanks and gratitude to a number of people without whose help and support this thesis work would never have been possible.

I am deeply grateful to Dr. Frank Shipman, my thesis supervisor, who led me in the right direction with thoughtful advice. From the very beginning he has always given me constant guidance and inspiration to make this thesis work successful. I would like to express my gratitude to Dr. Richard Furuta, Dr. Michael G Messina and Dr. Carroll Messer. Dr. Messer was my external advisor at the beginning of the thesis work. Their thoughtful comments and suggestions have made this thesis more consistent.

I had the opportunity to work with a number of very talented and knowledgeable people at the Center for the Study of Digital Libraries Laboratory (CSDL) at Texas A&M University. I would like to specially thank Dr. Haowei Hsieh. He has been tremendously helpful for a number of implementation issues during the development of this thesis work. I would also like to thank my fellow students and researchers in the CSDL Laboratory. They provided valuable suggestions and feedback during the discussions in CSDL group meetings.

Finally I thank all others who have directly and indirectly helped me in this thesis work in the department and outside the department.

# **TABLE OF CONTENTS**

		Page
A]	BSTRACT	iii
A	CKNOWLEDGEMENTS	V
T	ABLE OF CONTENTS	vi
LI	IST OF FIGURES	viii
LI	IST OF TABLES	ix
1	INTRODUCTION	1
2	SPATIAL HYPERTEXT	5
	2.1 Characteristics of spatial hypermedia systems	7 9
3	HYPERTEXT HISTORY	10
	3.1 Navigation history	11 13 15
4	HISTORY IN THE VISUAL KNOWLEDGE BUILDER	16
	4.1 The problem of long histories	19
5	AUTOMATICALLY CLUSTERING EDIT HISTORY	20
	5.1 Clustering approaches	20
6	CLUSTERING VKB HISTORY	25
	6.1 Pattern matching approach	25
	6.2 Rule-based approach	27
	6.3 Hierarchical agglomerative clustering (HAC)	30
7	COMPARISON OF CLUSTERING ANALYSIS	35
	7.1 Experimental data	35 39

	Page
<ul><li>7.3 Results and observations for the rule-based approach</li><li>7.4 Results and observations for the hierarchical clustering approach</li></ul>	
7.5 Comparing results from the three methods	
8 RESULTS AND DISCUSSION	51
6 RESULTS AND DISCUSSION	
9 CONCLUSION	57
REFERENCES	59
APPENDIX 1	65
APPENDIX 2	76
APPENDIX 3	80
VITA	97

# LIST OF FIGURES

FIGURE		Page
2.1	Types of relationships found in spatial hypertext	5
2.2	Relationship by activity-related areas	6
4.1	VKB history mechanisms	17
4.2	History sessions dialogue	18
5.1	Dendrogram showing the agglomeration of objects based on distance	24
6.1	Grouping events on single element	28
6.2	Grouping events in collection	29
6.3	Calculation of spatial distance among nodes	31
6.4	Non-threshold clustering process	32
6.5	Clustering process using threshold method	34
7.1	Event appearance -30 weeks	37
7.2	Event appearance during part of one day	37
7.3	Distribution of tokens among different segments	42
7.4	Time between events in the edit history	47
7.5	Distribution of time gap between subsequent edits	47
7.6	Spatial distance between events in the edit history	48
7.7	Distribution of spatial distances between subsequent events	49

# LIST OF TABLES

TABLE		Page
3.1	Uses of authoring and navigation history by authors, readers, and the system [Akkapeddi 2003]	15
5.1	Dissimilarities and similarities for different hierarchical clustering techniques [Everitt 1981]	22
7.1	Distribution of events across the multi-year authoring process	36
7.2	VKB operation summary	38
7.3	Token with maximum length from pattern based method	40
7.4	Token with maximum frequency of appearance from pattern based method	41
7.5	Tokens of maximum length in rule based approach	43
7.6	Token with maximum frequency of appearance from rule based method	45
7.7	Events applied on same symbol	46
7.8	Common tokens obtained from all three methods	50
8.1	List of groups obtained from manual grouping	51
8.2	Detection of manual groups by different strategies	53
8.3	Statistics of detected groups by automatic strategies	56

#### 1. INTRODUCTION

Structuring and interacting with data in freeform systems is an active area of research [Chiu 1998], [Edmonds 1988]. In freeform systems, flexibility in the organization of data is important. Data should not be structured prematurely as, during the course of the activity, perceived structures may emerge in unexpected ways and they may be subjected to multiple interpretations. When the domain of application is known, a more robust system can be achieved by designing it to dynamically interpret an anticipated set of frequently used structures appropriate for that domain. Unfortunately, when freeform manipulation of content is enabled, the resulting interpretation can become ambiguous over time. One approach to addressing the communication issues that result is to store the history of the information space so that users can access earlier versions when trying to disambiguate expression.

With the continued decrease in the cost of persistent storage, more applications are storing user history for use beyond the individual session. There are a variety of uses of such history. Lee [Lee 1992] identifies seven basic uses of information in a user's history: reuse, inter-referential input/output, error recovery, navigation, reminding, user modeling, and user interface adaptation. Greenberg [Greenberg 1993a] distinguishes three kinds of reuse facilities: adaptive systems, programming by examples (PBE) and history mechanisms. *Adaptive systems* use dynamic models of previous inputs to predict subsequent ones, which are then made available to the user. *Programming by example* is concerned with the reuse and generalization of long input sequences. *History mechanisms* allow users to manipulate a temporally ordered list of their interactions.

This thesis follows the style and format of ACM Transactions on Information Systems.

User history over long periods of time can become huge and difficult to manage. One example of this, and the context of this thesis, is the Visual Knowledge Builder (VKB) [Shipman 2001] developed in the CSDL Laboratory of Texas A&M University. VKB is a spatial hypertext system and provides a visual workspace for collecting, organizing, and sharing information. It is based on prior work on support for information analysis in VIKI [Marshall 1994]. It uses two-dimensional *collections* that can contain other collections and visual *symbols* that represent information *objects*. Users modify visual attributes of *collections* and *symbols* to indicate their interpretation of the information. These features facilitate the development of task-specific visual languages and support collaborative knowledge-building tasks.

VKB has been under development since 1997 and in use since 1999. Some VKB workspaces have been in use for more than five years and include two to three thousand events. Prior work on VKB explored an interface for attaching user interpretations of history via grouping and annotating history events [Akkapeddi 2003]. Groups may include other groups to form a hierarchal view of edit history. Groups of edits can be assigned meaningful labels by the user. Annotations attached to user events or groups of events can take the form of a plain text statement or metadata, one or more attribute/value pairs. The grouping and annotations allow filtering of the history to locate past states of the VKB document. Unfortunately, the grouping and annotation of large edit histories requires significant human effort and is rarely used.

This thesis work explores the potential to automatically analyze the edit history to generate initial groupings of edit events to reduce required human effort. These groupings and patterns may be valuable for: (a) accessing desired segments of long edit histories (b) identifying portions of edit history with special or similar attributes, and (c) predicting future interaction during VKB authoring. This thesis implements and analyzes following three approaches to cluster VKB edit history:

Pattern matching approach: This approach attempts to recognize repeated event patterns via detailed analysis of the edit history. History event sequences of a specified length range are identified using a simple pattern matching algorithm [Capelle 2002]. This approach helps develop tools similar to those used in programming by demonstration (PBD).

Rule based approach: In this approach spatial relationship among objects determines the grouping of history events. The edit events/actions are grouped based on the object(s) being edited and the container of objects. The objective of this approach is to generate simple and logical groups based on *spatial* and *containing* relationships of VKB objects and containers.

Hierarchical agglomerative clustering (HAC) approach: In this approach, time and space in VKB workspace domain are used as two different dimensions during clustering. The time when sequential events occur and position of the objects/collections in the VKB workspace that are manipulated by those events are used to determine the "interdistance" between the two events. The inter-distance is calculated from a linear function of time and space. The objective of this approach is to find clusters of objects based on proximity in the VKB history space.

This thesis work is carried out by implementing following 3 steps:

- (a) Automatic clustering tools and techniques are developed to do the clustering of a large VKB history file using three approaches mentioned above;
- (b) Performance of each clustering technique is analyzed to determine their relative strengths and weaknesses and finally;
- (c) Answering the question, "how well do these automatic clustering tools perform" by comparing the results obtained from these automatic tools with that obtained from the manual grouping by actual VKB users on a same history.

This thesis will provide an understanding of the automatic grouping techniques with advantages and disadvantages of the three different approaches implemented. This result informs the design of history clustering for other applications that store edit history. These results will also facilitate development of further enhancements to VKB's functionality and user interface.

The next section provides an overview of spatial hypertext. Section 3 enumerates many of the potential roles of user history in hypertext systems. Section 4 describes the history-related functionality provided in the current version of VKB and the need to automatically cluster VKB edit history. Section 5 presents an overview of clustering techniques and Section 6 describes three clustering approaches applied to VKB histories. Section 7 compares the performance of the three approaches. Section 8 discusses these results and Section 9 presents conclusions from this thesis project as a whole.

#### 2. SPATIAL HYPERTEXT

Spatial hypertexts evolved from traditional navigational and node-link based hypertext systems like Xerox NoteCards [Halasz 1987] and the Virtual Notebook System [Shipman 1989]. Such systems provided views of the node and link graph structure of the hypertext to provide users with greater context about how one page of content fit within the overall hypertext. The success of such views led to map-based hypertexts that used graphical views of network as the primary interface, including Aquanet [Marshall 1991] and gIBIS [Conklin 1988]. When such tools were used for authoring, users often avoided creating explicit links between information objects and instead used spatial position and visual similarity to express relations.

Spatial hypermedia systems like VIKI [Marshall 1994] were designed to provide visual means to develop task-based interpretations of information using proximity, alignment, repeated patterns, and visual attributes of information chunks. This expression is used to indicate information object similarity, to cluster information objects into groups, and to identify relationships between information objects.

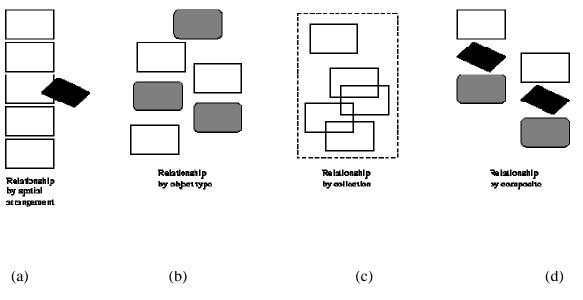


Figure 2.1: Types of relationships found in spatial hypertext

Figure 2.1 provides examples of four forms of spatial expression found in spatial hypertext systems.

Relationship by spatial arrangement: This relationship is expressed by proximity between objects [Figure 2.1(a)]. It can be horizontal lists, vertical lists, matrices, stacks etc., each of which requires a certain alignment and visual uniformity of objects to express ordered groupings.

• Relationship by object type: As shown in Figure 2.1(b), it is expressed by visual similarities between objects. Object type relationships can express category membership that cross-cuts spatial positioning. Visual similarities can be expressed with color, font, extent, shape, border-width etc.

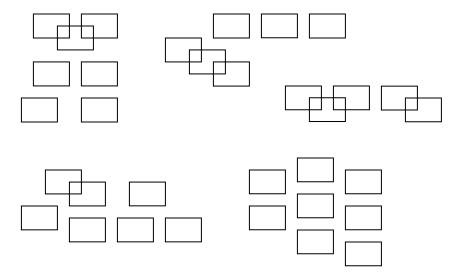


Figure 2.2: Relationship by activity-related areas

- Relationship by collection: This relationship is categorizes a set of objects according to some criteria [Figure 2.1(c)]. A spatial hypertext collection is a separate space containing the set of objects that are related by their membership in that collection. Subspaces can express hierarchical ordering of collections.
- Relationship by composite: Composites provide users with the ability to express relationships between different types of objects [Figure 2.1(d)]. They can reveal themselves as recurring patterns of objects, where the immediate constituents of the composites can be of arbitrary type.

In addition to the forms of expression shown in Figure 2.1, people group objects into activity related areas, as shown in Figure 2.2.

Relationship by activity-related areas: As shown in Figure 2.2, a space is said to
be organised into activity-related areas when objects are clustered (by spatial
proximity) in such a way that objects in the same cluster relate to the same task.
Only the clear spatial separation of objects into clusters is significant, not
structure within the clusters.

#### 2.1 CHARACTERISTICS OF SPATIAL HYPERMEDIA SYSTEMS

The following is a description of properties of the spatial hypermedia systems:

- (1) Structure creation: In spatial hypermedia, the focus is on active creation of structure rather than reading and traversing structure [Marshall 1994].
- (2) Emerging structure: Spatial hypermedia allows structure creation even when users only have a fuzzy idea about what kind of structure to create. It allows the user to create collections before naming and typing them. Thus it supports explorative development of

informal emerging structure. In [Marshall 1997], it is mentioned that "people's organisational strategies change over the duration of a task as they become more familiar with the material to be organised. This stresses the need for emerging structure in tasks involving structuring."

- (3) Flexibility: Spatial hypermedia allows users to express a variety of interpretations of material by arranging material in multiple ways. The flexibility of spatial arrangment makes it easy to express relationships such as similar-to or different-from [Marshall 1995]. Along with spatial properties, the ability to change color, border, shape, font, etc., enables the expression of independent categorizations and information characteristics. For instance, one could express more relevance of an object by thicker borders, and less relevance by thinner borders.
- (4) Common understanding: Spatial hypermedia allows people in a group setting to discuss appropriate structures and, by moving objects around in a space, suggesting new structures. In this way communication surrounding a set of information can be grounded in the visual representation, providing for a common understanding of structure to be developed, over time. Though spatial structure is one's personal reflections, that understanding and interpretation of a collection of information can be communicated to others via visual expression [Marshall 1997].
- (5) Handling large structures: Spatial hypermedia allows people to structure large amounts of data in a comprehensive way. Some methods to show overview of structure fail when information sets grow large. For example, graph structures and networks indicating relationships and interdependencies get confusing when there are many links between nodes [Feiner 1988].
- (6) Spatial parsing: Some spatial hypertext systems include spatial parsers that attempt to recognize the perceptual structures being created in the visual workspace. These recognized structures are used by the system to facilitate the selection and manipulation of the structures and to aid in formalizing the implicit representation of relationships into

an explicit structure. The spatial parsers also provide feedback to the users about what the system has understood and provide some indication as to the comprehensibility of the information space for others.

#### 2.2 OTHER SPATIAL HYPERTEXT SYSTEMS

The use of spatial expression had been part of a number of earlier systems, such as Boxer's use of space in a programming environment [diSessa 1986]. Among hypertext systems, Storyspace used the concept of a writing space [Joyce 1991] for arranging the contents of a hypertext while authoring the links that are the structure of the resulting hypertext. There are now a large number of spatial hypertext systems or systems that have been motivated by spatial hypertext systems. Web Squirrel used the ease of spatial expression to make it easy to keep track of large numbers of URLs [Simpson 2001]. Hot Sauce is a graphical browser presenting labelled nodes in multiple colors in a three dimensional space [Guha 2005]. Nodes can link to external resources, like web pages, gopher files, ftp files, desktop files, email and database structure. A node can also hide/reveal other nodes to which it links to; thus capable of expressing hierarchical relationships. Hot Sauce presents content in a view where objects are floating freely in space.

#### 3. HYPERTEXT HISTORY

A very common phenomenon in our everyday life is "repetition". It has impact over computing and non-computing activities. In non-computing activities, people replay their favorite music; favor a subset of recipes and tools, and follow similar procedures to accomplish routine office tasks [Greenberg 1993b]. Hanson, Kraut, and Farber [Hanson 1984], and Greenberg and Witten [Greenberg 1988] report that, in computing environment, "a few commands issued during a user session comprise a large percentage of the total commands used". According to Lee [Lee 1992], recurrent activities arise for several reasons. Some tasks are routine and frequent or inherently repetitive. Given that many computer-based tasks involve repetition, there is an opportunity to collect a record of user's interactions—called a user history—and make it available for future use.

Lee also identifies seven basic uses of the information in a user's history: reuse, interreferential input/output, error recovery, navigation, reminding, user modeling, and user
interface adaptation. Greenberg [Greenberg 1993a] distinguishes between three kinds of
reuse facilities: adaptive systems, programming by example, and history mechanisms.

Adaptive systems use dynamic models of previous inputs to predict subsequent ones,
which are then made available to the user. Programming by example is concerned with
the reuse and generalization of long input sequences. History mechanisms allow users to
manipulate a temporally ordered list of their interactions.

There are two major types of history mechanisms in hypertext systems. The first type of history mechanism records navigation events, such as the traversal of links from page to page, and is appropriately called *navigation history*. The second type of history mechanism records the edit events that make up the authoring process, and is called *authoring history*. In navigation history, the movement of a reader through a hypertext is

recorded. This recording can be used in a number of applications like backtracking, already visited clues, generating personalized list of nodes and paths etc. Navigation history and some of the features it makes possible are included in most Web browsers. In the authoring history, events that edit the hypertext are recorded. Authoring history, at least at the session level, is found in editors like MS Word. They allow revisiting prior versions of a document and undo/redo edits.

Histories, whether of navigation or authoring, can either be linear or branching. In a linear history, returning to a prior state (e.g. using the "back" button in the browser to go to a previously visited page) and then making an alternate choice clears the forward history from the point of change. Branching history provides more information as each navigational path or editing sequence is recorded as a branch with one being indicated as being that for the current state of the hypertext. This type of history mechanisms has been proposed by Cockburn and Jones [Cockburn 1996].

## 3.1 NAVIGATION HISTORY

The primary uses of navigation history found in Web browsers are backtracking, history lists, and already-visited cues. Additional applications of navigation history include paths and guided tours, visualizations of and reflections on navigation, and the recognition of access patterns.

Backtracking and history lists enable the user to go back to a previously visited page. Backtracking reduces the disorientation problem, also known as the "getting lost in hyperspace" problem [Conklin 1987], by allowing the user to go back over the course of link traversal. There are a number of alternatives to single step backtracking. One approach is a structure-oriented backtracking [Nielsen 1990], where systems provide a

direct backtrack jumps based on their knowledge about the structure of the hypertext, to locations where the user is likely to want to return.

History lists tend to take one of two forms. The first representation is a sequential text-based list of the titles of nodes visited. Nielsen [Nielsen 1990] implemented the later method in a HyperCard-based hypertext system. The Symbolics Lisp [Walker 1987] environment contains a window-based hypertext system called the *Document Examiner*. This was designed for its extensive online manual. It provides two types of historical lists, a *command* history and a history of *topics* examined. The second representation is a "cache" of graphical miniatures of the most recently visited nodes. The National Museum of Denmark museum used a visual "cache" approach in their information system [Nielsen 1990]. The screen in the information system includes a graphic of a museum artifact. It is displayed horizontally along the bottom of the screen to provide the user with a quick method for returning to the eight most recently visited nodes.

Visual indicators such as checkmarks, asterisks, or the plus sign serve as "footprints" in overview diagrams and help users to avoid returning to nodes that have been recently visited [Wexelblat 1998]. Bernstein's Hypergate system displays a small marker called a "breadcrumb" next to hyperlinks. This leads to material the reader has already seen. A checkmark next to nodes that have been visited within the overview map is placed in Nielsen's HyperCard-based hypertext system [Nielsen 1990].

A persistent form of navigation history is Vannevar Bush's path [Bush 1945]. In today's hypertext systems, *paths* are typically associated with the idea of a guided tour, where author determines an appropriate order of presentation for a given audience. It may even include annotations explaining the items on the path. Trigg [Trigg 1986] extended this concept to NoteCards and called *stops* along the tour *tabletops*.

Similar to paths, "Footprints" [Wexelblat 1998] uses information from web server logs to figure out where users have gone and then processes that information into displays. It also provides a navigable scrollable list of titles for pages visited by the user. Thuring et al. [Thuring 1995] refers to a presentation interface that shows the history of a hyperspace reading session. It shows by chronologically listing nodes visited during the session. It also shows reader's current position within that hierarchy.

Paths do not have to be shared. Kashihara, et al. [Kashihara 2000], encourage users to reflect on their "*interactive history*", providing users with a view of their exploration process. It allows users to view and annotate the exploration history in order to rethink the exploration process they have carried out so far.

Another area of use of navigation history is identifying *access patterns* and thus prefetching data that may be accessed by the user in the near future. Navigation history can also be used to generate models of *users' interests* in order to make navigation suggestions to readers. The access metrics and access patterns available from server-side navigational history (server logs) can identify what information readers desire most and can help locate confusing links or common "wrong turns".

#### 3.2 AUTHORING HISTORY

Authoring or edit history can be very informative to both authors and readers. Authoring history is perhaps most valuable to authors as it allows them to undo and redo actions, to return to prior versions of their hypertexts, and to review edits made by collaborating authors. Edit history information helps readers interpret ambiguous materials by providing access to the context of an edit. Reviewing a sequence of edits provides insight into the thought processes and intentions of the author. Authoring history provides readers with a notion of the document's constructive time [Akkapeddi 2003].

A variety of hypertext systems have included some form of edit history. CoVer [Haake 1993] represents various versions of the same object through multi-state objects (mobs). The "derivation history" generates an unconnected graph structure over all versions of documents. The application can explore historical development according to a number of attributes like creation date of versions, specific author and comprehensible view over the version.

Writing Environment is an environment that can be used to create both electronic and printed documents [Smith 1987]. It has an "online tracker" to capture users' interactions. The captured information is represented as a sequence of symbols with attributes that constitute the history of the session. It also has a replay function that replays all the events that occurred during the session.

Hayashi and Sekuima [Hayashi 1993] in their "Nelumbo" system, implemented a mechanism that records users access histories in tree forms. Its WYSIWYG editor, displays not only the final version of the document but also the snapshot of various versions of the same document.

Additional forms of support based on authoring history can be provided by the system. Visual cues can be added to frequently modified portions of content [Edit wear]. Also, the system may use authoring history to identify common patterns of edits. These patterns can be the basis for macros, or where the system offering to complete menial tasks for the author. More ambitious generalizations of such patterns can be the basis for programming by demonstration (PBD) techniques. In such scenarios the system learns new behavior by analyzing the edits made by users working in the system over a period of time.

## 3.3 HISTORY APPLICATIONS

As mentioned in this section, there are a variety of applications of history data in hypertexts. Table 3.1 summarizes the above discussion by identifying applications of authoring and navigation history for readers, authors, and the system.

Table 3.1: Uses of authoring and navigation history by authors, readers, and the system [Akkapeddi 2003]

	Hypertext Author	Hypertext Reader	System
Authoring History	Undo/Redo, Return	Provides context for	Visualization of
	to prior document	interpreting the	edit patterns,
	states, Replaying	hypertext content	Macro
	edits of co-authors		generation,
			Programming
			by
			demonstration
Navigation History	Information about	Backtracking,	Pre-fetching,
	reader preferences	"Already visited"	Suggestions
	and confusion	cues, Paths	based
			on models of
			reader
			interest

#### 4. HISTORY IN THE VISUAL KNOWLEDGE BUILDER

The potential value of capturing edit history in spatial hypertext became apparent during use of VIKI [Marshall 1994], as users in collaborative spaces would leave notes to one another to explain the changes they had made. As such, the design of the Visual Knowledge Builder (VKB) included the ability to record the edits to the space and make this history persistent across sessions.

VKB provides four access mechanisms whereby users can return to prior states of or replay edits to the spatial hypertext [Shipman 2001]. The first is via play forward and backward buttons on the left side of the history toolbar (shown in Figure 4.1). Using these buttons, the user can step forward and backward one edit at a time or play through edits continuously in either direction. A control is provided for modifying the speed at which continuous playback occurs. The second access mechanism is a slider on the same toolbar that indicates the number of edits in the overall history and position of the state currently being displayed within that history. Users can drag the slider back and forth to get to prior or later periods of activity. As the user drags the slider, or as the slider changes position due to the displayed state changing based on one of the other history access mechanisms, the time indicator on the right side of the history toolbar changes to indicate the time of the edit currently indicated by the slider.

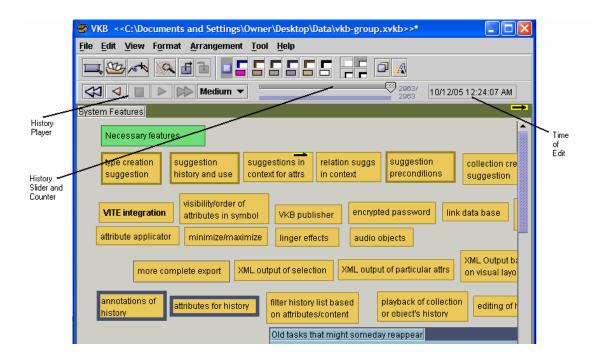


Figure 4.1: VKB history mechanisms

The two other history access mechanisms provided are selecting the start of a particular editing session in the History Sessions Dialogue (see Figure 4.2) and returning to a specific edit event on a particular object via a popup menu in the workspace. Together, the record of history and the variety of access mechanisms provide readers with a view of the writers', or constructive, time [Shipman 2001]. This supports learning and interpreting authors' work practices, recognizing patterns of activity in information space, and disambiguating specific actions and context.

Gaps between time stamps of the various events in the history provide a sense of the length and frequency for authoring and editing sessions. VKB uses gaps in the history to automatically recognize the editing sessions presented in the History Sessions Dialogue. This Dialogue also allows users to express interpretations related to the edit history by selectively grouping edit events together into meaningful clumps and annotating these groupings [Akkapeddi 2003].

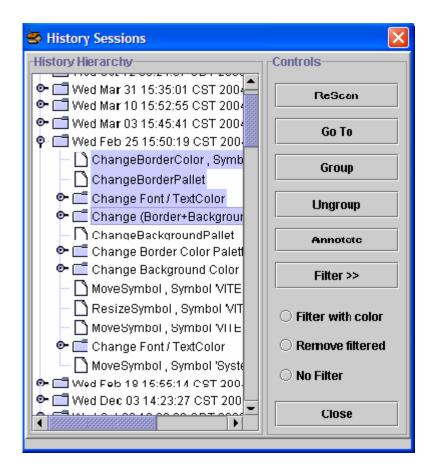


Figure 4.2: History sessions dialogue

Groups may include other groups to form a hierarchal view of edit history. Groups of edits can be assigned meaningful labels by the user. Annotations attached to user events or groups of events can take the form of a plain text statement or metadata, e.g., one or more attribute/value pairs. The grouping and annotations allow filtering of the history to locate past states of the VKB document. Unfortunately, the grouping and annotation of edit histories requires significant human effort and is rarely used.

#### 4.1 THE PROBLEM OF LONG HISTORIES

VKB has been under development since 1997 and in use since 1999. Some VKB workspaces have been in use for more than five years and include two to three thousand events. Manipulating the edit history in these cases becomes difficult. Having meaningful groupings within the edit history can help in accessing desired segments of long edit histories, identifying portions of edit history with special or similar attributes, and predicting future interaction during VKB authoring sessions. For a large VKB history, the current interface and support for grouping edit events is too difficult and time consuming.

The problem is two-fold. The first issue is that the level of detail of user activity captured in edit event is too low level for humans to evaluate and care about. The second issue is that it is only once the history becomes large that users start to perceive value to grouping and annotating the user history. By then, the history is too long for the current author-centric mechanisms to be used.

The rest of this thesis describes the exploration of techniques for automatically clustering VKB edit history to solve this problem. The next section provides an overview of clustering methods. This is followed by a description of the three methods implemented and evaluated with VKB history data.

#### 5. AUTOMATICALLY CLUSTERING EDIT HISTORY

The thesis has three major objectives. The first objective is developing tools to automatically cluster large VKB history. The second objective is analyzing the results of different clustering approaches to determine their relative strengths and weaknesses. The third objective is evaluating what roles the clustering approaches can fill in VKB by determining how well they match the manual grouping by VKB users.

#### 5.1 CLUSTERING APPROACHES

Clustering is an unsupervised learning method. In a clustering process there is no specific target value to be predicted. The objective of the clustering process is to find common patterns or groups of similar examples. There are a number of models and algorithms available for clustering. They can be classified and compared according to following dimensions:

- (a) Conceptual (model-based) vs. partitioning clustering
- (b) Exclusive vs. overlapping clustering
- (c) Hierarchical vs. flat clustering
- (d) Incremental vs. batch clustering

Conceptual clustering groups elements based on a preexisting model while partitioning clustering groups elements without using a preexisting model (e.g. based on their similarity to one another). If each element is placed in at most one cluster then it is exclusive while an element can be simultaneously placed in multiple clusters when using an overlapping approach. Clustering algorithms that produce clusters of clusters are hierarchical while those that do not are considered flat. Finally, if a clustering approach requires all the elements to be clustered prior to execution then it is a batch approach

while those that can cluster new elements without revisiting previously clustered elements are *incremental*.

There are many different approaches for clustering data. Some frequently used approaches are: (a) Cluster/2, (b) K-Means partitioning, (c) probability-based partitioning, (d) hierarchical agglomerative clustering, and (e) hierarchical divisive clustering [Everitt 1981]. Due to the goal of generating a hierarchy groups in edit history, this thesis will focus on hierarchical approaches.

Hierarchical clustering techniques build clusters step by step. There are two main approaches in hierarchical clustering: the Hierarchical Divisive Clustering technique and the Hierarchical Agglomerative Clustering (HAC) technique [Everitt 1981].

Divisive methods start with the assumption that all objects are part of a single cluster. The algorithm splits this large cluster step by step until each object is a separate cluster. On the other hand, agglomerative methods start inversely. Initially each object forms a separate cluster. The clusters are combined step by step. In each step, the two clusters with the highest similarity or the smallest dissimilarity are merged. Iteration continues until all objects are in one single cluster. Thus, hierarchical agglomerative clustering methods are based on a similarity or dissimilarity matrix of objects. Different methods differ in the way similarities or dissimilarities are calculated after two clusters are joined. Table 5.1 summarizes different calculations of similarity or dissimilarity used. This table uses the following notations:

 $d_{(p+q),i}^{new} = \text{dissimilarity between the new cluster } (p+q) \text{ with cluster } i$ 

 $d_{pi}$  = dissimilarity between the cluster p and cluster i

 $S_{(p+q),i}^{new} = \text{similarity between the new cluster } (p+q) \text{ with cluster } i$ 

 $s_{pi}$  = similarity between the cluster p and cluster i

Table 5.1: Dissimilarities and similarities for different hierarchical clustering techniques [Everitt 1981]

Method	Calculation of dissimilarities and similarities
Complete linkage	$d_{(p+q),i}^{new} = \max(d_{pi}, d_{qi}) \text{ res. } s_{(p+q),i}^{new} = \min(s_{pi}, s_{qi})$
Single linkage	$d_{(p+q),i}^{new} = \min(d_{pi}, d_{qi}) \ res. \ s_{(p+q),i}^{new} = \max(s_{pi}, s_{qi})$
Average linkage	$d_{(p+q),i}^{new} = (d_{pi} + d_{qi})/2$
Weighted average linkage	$d_{(p+q),i}^{new} = \left(n_p \cdot d_{pi} + n_q \cdot d_{qi}\right) / \left(n_p + n_q\right)$
Within average linkage	$d_{(p+q),i}^{new} = \left(n_p \cdot d_{pi} + n_q \cdot d_{qi}\right) / \left(n_p + n_q\right)$
	$d_{(p+q),(p+q)}^{new} = \frac{\left(\frac{2}{n_p \cdot (n_p-1)} \cdot d_{pp} + \frac{2}{n_q \cdot (n_q-1)} \cdot d_{qq} + n_p \cdot n_q \cdot d_{pq}\right)}{\left(n_p + n_q\right) \cdot \left(n_p + n_q - 1\right) / 2}$
Median linkage	$d_{(p+q),i}^{new} = \frac{1}{2} \cdot d_{pi} + \frac{1}{2} \cdot d_{qi} - \frac{1}{4} \cdot d_{pq}$
Centroid linkage	$d_{(p+q),i}^{new} = \frac{n_p}{n_p + n_q} \cdot d_{pi} + \frac{n_q}{n_p + n_q} \cdot d_{qi} - \frac{n_p \cdot n_q}{(n_p + n_q)^2} \cdot d_{pq}$

The following is a characteristic description of different methods:

Complete Linkage uses a max function and results in a strong definition of the homogeneity of clusters: "The largest dissimilarity between all objects of one cluster should be less than a certain value". The farthest neighbor of each object should have a distance less than a certain value. In contrast to complete linkage, *single linkage* only requires that the nearest neighbor is located within a certain distance. Thus, the method is called nearest neighbor. Both single and complete linkage methods can be used for similarity or dissimilarity measures.

The advantage of single and complete linkage is their invariance against monotonic transformation of the dissimilarities or similarities. If the dissimilarities or similarities

are squared or log-ed, the results do not change. A disadvantage of single linkage is the potential for *chaining*, which causes too few large and heterogeneous clusters. In contrast, complete linkage may produce too many small clusters.

The large heterogeneous clusters resulting from using single linkage and the many small clusters produced using complete linkage resulted in average linkage approaches. Average linkage, weighted average linkage, and within average linkage try to avoid these effects by using an average of the distances rather than a minimum or maximum function. The remaining methods characterize the cluster by selecting an existing object as a median or centroid, or generating a new object that then represents the cluster in further calculations.

Agglomeration can be visualized by "dendrogram", as shown in Figure 5.1. The dendrogram shows which objects are combined in which step. Objects  $O_1$  and  $O_2$  are combined in the first step. In the second step  $O_3$  is merged into the cluster built by  $O_1$  and  $O_2$ . In the third step  $O_4$  and  $O_5$  are combined. Finally all objects are combined into one cluster.

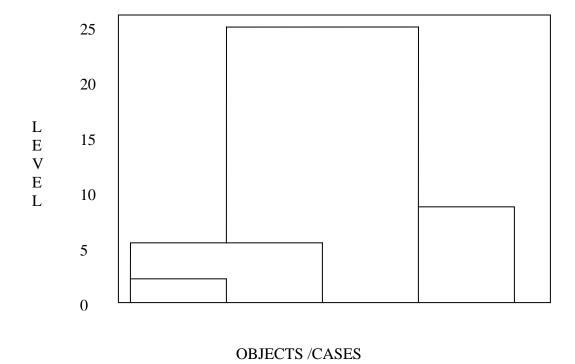


Figure 5.1: Dendrogram showing the agglomeration of objects based on distance

#### 6. CLUSTERING VKB HISTORY

Three different clustering algorithms were designed and implemented for grouping VKB edit history. The three implementations were developed independently and represent significantly different approaches. The first approach is a pattern matching approach that identifies repeated patterns of edit events in the history. The second approach is a rule-based approach that uses simple rules, such as "group all consecutive events on a single object" or "group all consecutive events within a collection". The third approach uses hierarchical agglomerative clustering (HAC) where edits are grouped based on a function of edit time and edit location.

The three different approaches used in this thesis are supported by the work of Ping-Herng Denny Lin [StatSoft 2005]. His comparison of data mining methods for classification purposes overlaps this efforts goal of grouping into meaningful edit sequences. Aggrawal & Yu's [Aggarwal 1998] survey of data mining techniques suggests a successful process for identifying meaningful co-occurrences that can combine association rules, clustering and then classification.

## 6.1 PATTERN MATCHING APPROACH

This approach finds repetitive patterns of events in the VKB edit history. It uses techniques similar to string matching [Capelle 2002, Garofalakis 1999] and to the pattern identification algorithms used for macro recognition in programming by demonstration (PBD). To identify patterns, each type of event is encoded as a unique element. An example is "ACRM" where A is an "Add Symbol" event, C is a "Change Symbol" event, R is for "Resize", and M is for "Move". In this approach, a sequence of events appearing consecutively, in the real chronological order of events, is termed a "token".

The *length* of this token is defined as the number of events in it. This approach searches for tokens between 4 and 20 elements in length that appear frequently within the event history. Considering patterns with length smaller than four will generate too many instances of repeated events, most of which will either have no meaning to users or represent an incomplete activity in the eyes of users. Considering patterns over length 20 is very unlikely to be useful in real applications. The objective of this approach is to find tokens of such a length that they conform to activities that users view as coherent.

In developing this approach, it was decided to identify patterns of events on *objects* and *collections*. This produces patterns of events that represent manipulations of objects, manipulations of collections and manipulations of combinations of objects and collections. An example is "after creating a new collection and changing its size and background color, the user creates two objects and modifies their textual content, shape and color". When such a pattern identification algorithm is applied to a long edit history, lots of repeated patterns can be found. Whether these patterns make sense to users depends on whether the groupings indicate a sequence of low-level actions that together instantiate a sub-task or sub-activity in the workspace (e.g. creating an new object or list of objects with certain content). To reduce this problem, user-defined constraints can be used to focus the mining task on interesting patterns [Capelle 2002].

A limitation of the current pattern matching implementation is that sequences of events must be identical in length and composition to be considered equivalent. The inclusion of wildcards or regular expressions would address this but makes the generation of potential patterns problematic. Then another algorithm must be designed to decide what to generalize and abstract into a wildcard or regular expression? Another limitation is that time gaps between edit events and the context of the event, e.g. the collection in which the event occurs, do not impact the grouping.

#### 6.2 RULE-BASED APPROACH

The rule-based approach groups VKB history events using rules based on observations of how users interact with VKB. This approach is somewhat similar to the rule-based approach to word clustering used by Hui, Han, et. al [Han 2003] in their text classification system. The implementation of this approach for this thesis is very simple and consists of two rules. The first rule groups contiguous events that modify the content, position or visual attributes of a particular object or collection in the workspace. This rule groups local actions on an entity in the workspace. The second rule groups all consecutive events that occur within a particular collection. This rule runs after the first rule and can generate groups that include groups generated by the first rule. The result of this process is groups of events in a particular subspace in the VKB workspace.

Figure 6.1 shows a scenario in VKB history, where  $C_i$  represents collection i,  $O_j$  represents object j, and '<>' is the top-level collection (or desktop) of a VKB workspace. The results of applying the first rule cause events  $e_2$ ,  $e_3$ ,  $e_4$ ,  $e_5$ , applied on object  $O_2$ , to be grouped together.  $O_2$  is in the top-level collection (shown as <>). Another 4-event grouping is  $e_7$ ,  $e_8$ ,  $e_9$ ,  $e_{10}$  as they are all manipulation of object  $O_1$ .

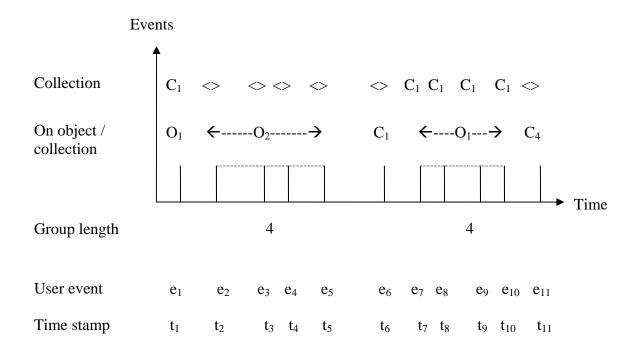


Figure 6.1: Grouping events on single element

Figure 6.2 shows the application of the second rule. Object  $O_1$  has 3 events applied on it, then object  $O_2$  has 2 events, and then object  $O_1$  has 3 more events. After a manipulation of the Collection  $C_1$ , there are edits to Objects  $O_4$ ,  $O_5$ , and  $O_6$  in Collection  $C_2$ . The first rule will group together the events on a single object as previously described. Events  $e_1$  through  $e_8$  are applied on different objects contained in the collection  $C_1$ , and so the three groups of events generated by the first rule will be grouped together creating a two-level hierarchic grouping of the events. In this example,  $e_9$ , which is an event on  $C_1$  is left out of any groups and then the groups and individual edits in  $e_{10}$  to  $e_{17}$  are grouped as they all occur in collection  $C_2$ .

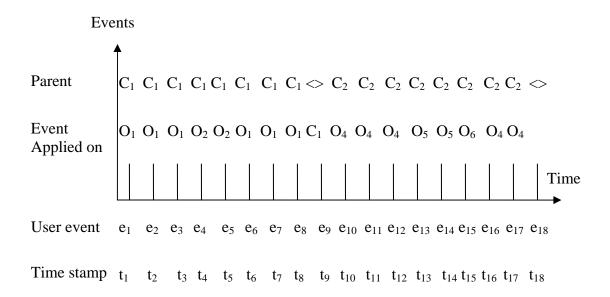


Figure 6.2: Grouping events in collection

While not part of the implementation in this thesis, additional layers of grouping could be added based on whether consecutive edits were to a particular spatial structure recognized by the VKB spatial parser. As the spatial parser is meant to recognize the hierarchy of perceptual structures created by users to express relationships about the information in the workspace, automatic grouping based on this structure would provide further levels of granularity in the edit history.

The primary weakness of this approach is the limited forms of groups recognized. Unlike the pattern-matching approach, there is no impact on the type of edits being performed on an object or within a collection. As long as two edits are consecutive and are to an individual object or within a particular collection, they will be grouped. Similar to the pattern-matching approach, time is also not included in this particular instantiation although it would be easy to add a cutoff to the rules such that edits with a certain gap in-between would not be grouped.

### 6.3 HIERARCHICAL AGGLOMERATIVE CLUSTERING (HAC)

The last approach for grouping history explored in this thesis uses hierarchical agglomerative clustering (HAC). HAC groups elements based on a similarity function. In this implementation, event dissimilarity is calculated based on a linear function of the time and space (position) of the VKB history. This is somewhat like Chiu and Wilcox's use of *time* and *space* for hierarchical agglomerative clustering in dynamically grouping user strokes in a pen-based and audio system [Chiu 1998]. Hierarchical agglomerative clustering (HAC) methods have also been used in [Yeung 1998], [Gatica-Perez 2001], and [Zhao 2001] in video analysis. Work in [Zhong 1996], [Yeung 1998], [Rui 2000] also proposes *visually-based* and *time-constrained* clustering.

The dissimilarity function is based on the time and space differences between history events. Events in the VKB history include an absolute timestamp. For the HAC analysis, a relative time of appearance for each event is derived from the actual timestamps. For each event there is one an associated workspace element (e.g. object or collection). These workspace elements have a spatial location/position within. Spatial distance between two events is calculated based on the distance between the workspace elements manipulated in the two events.

To be specific, consider the following example where  $e_I$  and  $e_2$  are events in VKB. Event  $e_I$  appears at time  $t_I$  and  $e_2$  appears at time  $t_2$ . Thus  $\Delta T = t_I - t_2$  (where  $t_I > t_2$ ). Event  $e_I$  was applied to symbol  $S_I$  and  $e_I$  was applied to symbol  $S_I$  and  $S_I$  and  $S_I$  respectively in the VKB space. The distance between symbols  $S_I$  and  $S_I$  is  $\Delta S_I$ , which is calculated as described in the next paragraph. The dissimilarity between event  $e_I$  and  $e_I$  is  $d = A * \Delta S_I + B * \Delta T_I$ , where A and B are coefficients.

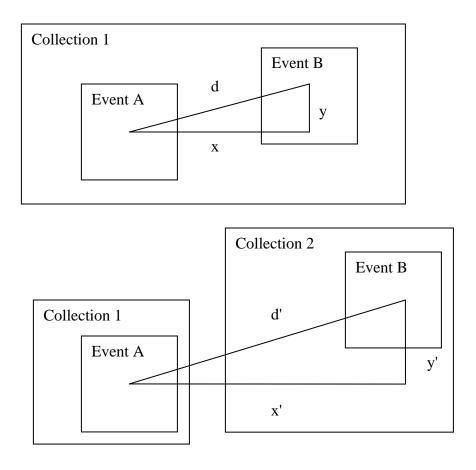


Figure 6.3: Calculation of spatial distance among nodes

For calculating spatial distance between two events, different strategies are applied based on whether the two events occur within the same collection. If the two events manipulate symbols within the same collection then their spatial distance is calculated to be the Euclidean distance between those symbols based on their x and y coordinates. If they belong to different collections, the spatial distance is calculated by adding 2000 to the Euclidean distance between the symbols. This value is chosen based on the maximum value of all spatial distances between two symbols in a single collection. In this current dataset that maximum distance is 1057. Hence the addition of 2000

guarantees that the events are treated as if they were further away than they would have been if they had been in the same collection. Figure 6.3 shows how spatial distance is calculated for two events in same and different collections. Here  $d = \sqrt{(x^2 + y^2)}$  and  $d'=2000+\sqrt{(x'^2+y'^2)}$ .

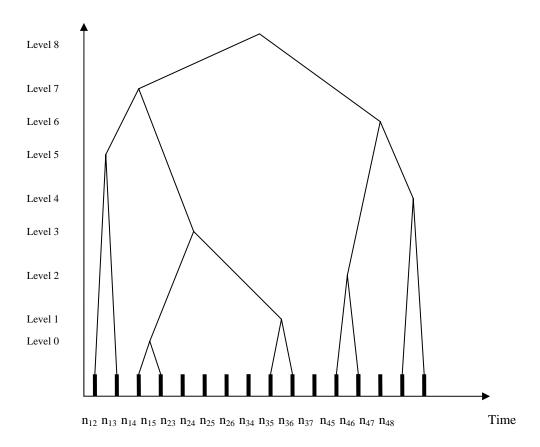


Figure 6.4: Non-threshold clustering process

Two different methods are taken in the implementation of the bottom-up clustering. In the first method, objects are clustered by comparing the nearest neighbors. The process begins in such a state that each item in the event set forms a cluster of one element. In each step, a search is made to find the best clusters to merge (e.g. those that are most similar to one another) and combines them. The procedure gradually creates larger clusters with possibly increasing number of events in it. At the end of the process a single cluster with all the events in it is created – this is the root node of a tree with depth n-l for n original elements. In order to generate potentially meaningful groupings, once the clustering is complete, levels of similarity must be identified at which groups will be produced. Figure 6.4 shows a partial clustering tree with eight levels. A brute-force implementation of this approach is  $O(n^2)$  in time, where n is the number of events in the history.

In the second method as shown in Figure 6.5, clustering is done based on *threshold* values. As before, all events initially form a separate cluster of one element. At each stage, an indicative *threshold* value is chosen to form larger clusters at the next higher level in the hierarchy. By increasing the *threshold* values gradually, more events are included in different clusters and larger clusters are formed at each level. The last level of hierarchy includes all of the events. Figure 6.4 show this method. A simple implementation of this algorithm takes O(n\*m) time, where m is the number of thresholds considered.

In this thesis, the clustering method using *threshold values* has been used. The initial *threshold value* is obtained by considering the inter-distance among events at the lowest level. In the lowest level, after calculating inter-distance among all the pair-wise neighboring events, the minimum and maximum among them are found. The initial threshold value starts from this minimum and reaches up to the maximum value by increasing 10% at each step.

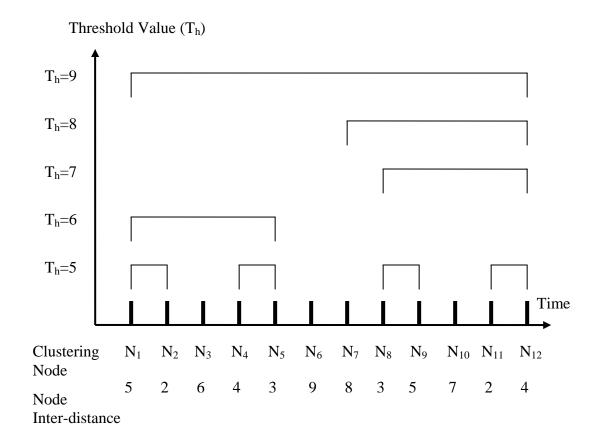


Figure 6.5: Clustering process using threshold method

### 7. COMPARISON OF CLUSTERING ANALYSIS

The objective of this thesis work is to group VKB edit history automatically in such a way that they will be similar to if the user had done the grouping manually. By implementing and comparing the three approaches, this thesis attempts to discern the strengths and weaknesses of the three approaches.

Hey-Chung Kum, et. al [Kum 2002] examine the problem of mining sequential patterns and propose a comprehensive evaluation method to assess the quality of the mined results. They propose four evaluation criteria. The methods are: (a) recoverability (b) the number of spurious patterns (c) the number of redundant patterns and (d) the degree of extraneous items in the patterns, to quantitatively assess the quality of the mined result from a wide variety of synthetic datasets with varying randomness and noise levels.

### 7.1 EXPERIMENTAL DATA

The different approaches described in the previous section to analyze VKB history were applied to a real-world dataset generated over a long period of time in the Center for the Study of the Digital Libraries (CSDL) at Texas A&M University. This file contained the event history captured during weekly meetings over a period of over four years. The following is a discussion of different observations about the CSDL VKB data file.

There are a total of 4138 events applied over 371 symbols (both objects and collections) in this VKB workspace. Out of 371 symbols, there are 21 collections and 350 objects in the file. Out of 7134 events, 433 events are applied on collections and 3699 events are applied on objects. Remaining events are applied on desktop or other entity in the VKB workspace.

Events in the history include a timestamp to indicate the actual time the event occurred. The value of the timestamp when the first event appeared is '941663618480' and that for last event is '1080768901707'. These values represent number of milliseconds elapsed after 12:00:00 PM January 1, 1900. For the ease of analysis, this real-time value was converted into a relative timestamp for computing the time gap between events. Table 7.1 shows the distribution of events during the multiple year (230 week) authoring process.

Table 7.1: Distribution of events across the multi-year authoring process

Serial number	Relative time of	Events sequence id	Number of events
	appearance range (in		appearing during
	weeks)		the time slot
1	0-50	1-1579	1579
2	51-100	1580-2848	1268
3	101-150	2849-3323	474
4	151-200	3324-3540	216
5	200-230	3541-4137	596

One aspect of this distribution is that there is almost no activity or event occurrence except at these weekly meetings. Most of the events occur on a specific day of the week and within a one or two hour period. Figure 7.1 shows the appearance of events over a period of 30 weeks. From this graph it is evident that events appear as a cluster once in a week. This graph shows some discontinuity due to meetings not occurring every week or meetings where the data file was not edited. Figure 7.2 shows the distribution of events for one meeting over a period of approximately one hour. It is clear that there are periods

of activity in the meeting involving edits to the data file and other periods of activity where no edits occur.

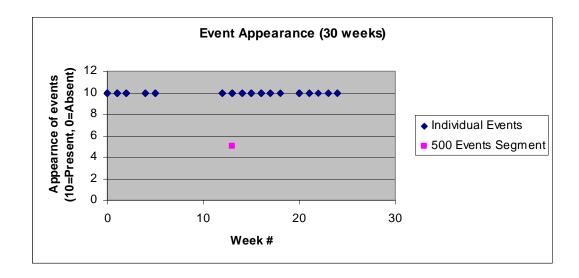


Figure 7.1: Event appearance -30 weeks

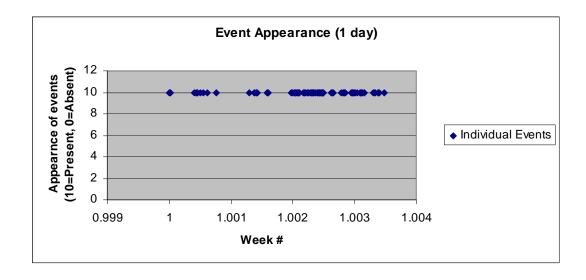


Figure 7.2: Event appearance during part of one day

For the ease of handling data and efficient implementation of pattern based analysis, entire event set has been grouped into 8 segments. Each segment contains 500 events in it except the last segment which contains 638 events. The segmentation was necessary for the pattern recognition based approach, as comparing and analyzing the entire event set is time consuming. The disadvantage of this segmentation of the original event set is that it can skip some event sequence (at most 8 chunks at 8 segment boundaries) due to this discontinuity.

Table 7.2: VKB operation summary

Serial Number	Operation Type	Operation code
1	Add Symbol	A
2	Change Border Color	В
3	Change Content of item	С
4	Delete Symbol	D
5	Change Font	F
6	Change Background Color	G
7	Change Color index	L
8	Move Symbol	M
9	Minimize	N
10	Change Border Pallet	P
11	Resize Symbol	R
12	Change Transparency	T
13	Change Attribute	U
14	Change Border Width	W
15	Maximize	X
16	Change Font Color	1
17	Change Background Pallet	p

The CSDL data file used in this thesis does not contain all the operations/activities defined/available in VKB. The history recorded in this data file contains 17 different operations applied over the VKB objects/collections. The operations are coded using alphabetic codes for ease of identification. Table 7.2 displays the operations included in this VKB history file and their associated codes.

## 7.2 RESULTS AND OBSERVATIONS FOR THE PATTERN-BASED APPROACH

One observation of event sequences is the repetition of a single event type. This common phenomenon is observed in almost all methods. Different repetition sequences with 20 length up to were found. An example repetitive sequence is "MMMMMMMMMMM". In this sequence the same operation M ("Move Symbol") is applied again and again. Most likely, these represent a period of reorganization on the part of the user, although this information alone cannot distinguish between activity within a single collection and activity that happens across multiple collections. The Move (M), Add (A), Create (C), and Change Attribute (U) events are found with highest sequence length. Repetition sequence for operations Change Transparency (T), and Change Background Pallet (p) are found with smaller sequence length.

 the entire sequence. Some of the sequences belonging to this category are MMMMACMMMMMM, MMCRMMMMMMM, and MMMMMMMCRMM.

Table 7.3: Token with maximum length from pattern based method

		Seg.								
Token	Length	1	2	3	4	5	6	7	8	Total
MMMMMMMMM										
MMMMMCMM	19	0	0	2	0	0	0	0	0	2
MMMMMMMMM										
MMMMMCRM	19	0	2	0	0	0	0	0	0	2
MMWMMMMMMMMMMM	15	0	0	2	0	0	0	0	0	2
AUUUUUUUUUU	13	2	0	0	0	0	0	0	0	2
MMMACRMMMMMMM	13	0	0	2	0	0	0	0	0	2
MMMMMMACRMMM	13	0	0	2	0	0	0	0	0	2
MMMMMMMMMMMMM	13	0	0	0	2	0	0	0	0	2
MMMMMMMMMM	13	0	2	0	0	0	0	0	0	2
MMMMACMMMMMM	12	0	0	0	0	2	0	0	0	2
MMMMMMMMM	12	0	0	0	0	2	0	0	0	2
MMMMACRMACR	11	0	0	0	0	0	0	0	2	2
MMMMACRMMMM	11	0	0	2	0	0	0	0	0	2
MMMMMMMMF	11	0	2	0	0	0	0	0	0	2
RMMMMMMMM	11	0	3	0	0	0	0	0	0	3
WMMMMMMMM	11	0	0	0	0	0	2	0	0	2
ACMMMMMMM	10	0	0	3	0	0	0	0	0	3
ACRACRACRM	10	0	0	0	0	0	0	0	2	2
CRMMMMMMM	10	0	0	0	2	0	2	0	0	4
MACRMMMMM	10	0	0	0	0	0	0	0	2	2
MCCCCCCCM	10	0	0	0	2	0	0	0	0	2
MMACMMMMM	10	0	0	0	0	0	0	0	2	2
MMMACRMMMM	10	0	0	3	0	0	0	0	2	5
MMMMACRMMM	10	0	0	3	0	0	0	0	0	3
MMMMMACRRG	10	0	0	0	0	0	2	0	0	2
MMMMMCMMMM	10	0	0	2	0	0	0	0	0	2

Table 7.4: Token with maximum frequency of appearance from pattern based method

Token	Length	Seg. 1	Seg. 2	Seg. 3	Seg. 4	Seg. 5	Seg. 6	Seg. 7	Seg. 8	Total
ACRM	4	0	5	0	5	3	0	0	54	67
RMMM	4	2	18	8	9	0	6	9	8	60
MMAC	4	2	0	0	16	12	13	4	9	56
RMMMM	5	0	13	4	7	7	5	0	5	41
MACR	4	0	4	0	0	3	13	4	15	39
MMRM	4	2	15	2	8	0	0	9	0	36
CRMM	4	0	6	0	5	4	7	5	8	35
MRMM	4	0	12	2	7	4	0	6	0	31
MMMR	4	0	14	3	7	6	0	0	0	30
MMMMAC	6	0	0	6	6	6	0	0	6	24
CMMMM	5	0	0	8	7	5	0	4	0	24
MACM	4	3	2	3	6	9	0	0	0	23
ACAC	4	0	0	12	0	5	0	3	0	20
MACRM	5	2	2	0	3	0	0	0	12	19
MMMAC	5	0	2	9	0	0	0	0	8	19
CMMM	4	0	2	10	0	7	0	0	0	19
RMAC	4	0	5	0	2	0	0	0	12	19
ACMM	4	0	0	9	4	5	0	0	0	18
MMMRM	5	0	12	0	0	0	0	5	0	17
MMRMM	5	0	8	0	5	0	0	4	0	17

Different tokens found in the VKB file appear with different frequency in the entire event space. Token ACRM appears with a highest frequency, 67 times over the entire history. Table 7.4 contains the 20 tokens with the highest frequency of appearance.

Table 7.4 also shows the distribution of tokens among the eight segments of history data. It is interesting to note that 54 of the 67 appearances of ACRM are in the last segment of the history data. This indicates that this may be the result of some feature added to VKB towards the end of the four year period. As indicated, some of the patterns appear more frequently at the beginning of the event space while others appears more frequently at the end of event space. Figure 7.3 graphs the distribution of tokens among different segments those appears with highest frequency. The label *token\_freqa*, *token\_freqb*, ....., *token\_freqh* represents the number of occurrences in segments 1, 2, 3... 8 respectively.

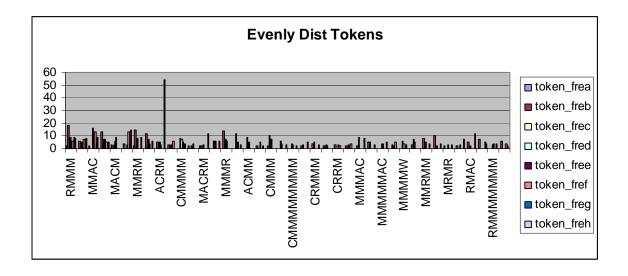


Figure 7.3: Distribution of tokens among different segments

# 7.3 RESULTS AND OBSERVATIONS FOR THE RULE-BASED APPROACH

The rule-based method produced a total of 174 tokens. The longest tokens were of length 10. Unlike the pattern-based approach, the rule-based approach allows tokens with length smaller than 4. Table 7.5 shows longest 25 tokens.

Table 7.5: Tokens of maximum length in rule based approach

Token string	Token length
ACRMMMMMMM	10
ACRMMCRCCRM	10
ARCRRGGMFR	9
ACRFMRTCM	8
MTTTTTTT	8
ACRMMBMWR	8
CCCCCCCC	8
ARCRGRMMM	8
FFFFIFFI	7
ACRMRCRM	7
WWMGGBWR	7
ACRMGTMM	7
CCCCCCC	7
CCCCCCC	7
ACRCRRMM	7
MMMMMMM	7
ARGRCRMM	7

Table 7.5 Continued

Token string	Token length
ACMCRCRR	7
MMFRMMMF	7
ACRRMMRW	7
ACRCRRCR	7
MMRCRCR	6
GGWBBBG	6
CRRCRCR	6
ACGWWGG	6

Tokens that had the highest frequency of appearance based on the rule-based approach are shown in Table 7.6. Notice that the frequencies are considerably smaller than those found by the pattern-matching approach.

Table 7.6: Token with maximum frequency of appearance from rule based method

Token String	Frequency
ACRM	23
ACRC	7
ACRMM	7
MMMM	7
ACRG	6
ARCR	6
ACRRM	5
ACRWM	3
CCCCCCC	3
CMCM	3
MMRM	3
ACGM	2
ACGR	2
ACMC	2
ACMR	2

Due to the rule-based method's grouping of activity on a single object or collection, the method identified a variety of different tokens applied to same symbol over the course of the event history. Table 7.7 shows different tokens applied to the same symbol.

Table 7.7: Events applied on same symbol

Symbol	Parent	Number of	
Id	ID	Tokens	Token String
17	0	3	ACGMX, MMRM, WMMM
			MMMM, RMMMM,
52	0	4	RRMMM
157	52	3	ACRG, MGBMRC, TTTT
689	52	3	ACGWWGG, MTTTTTTT, MMRM
			ACRC, ACRGW, CCCCCCCC,
788	52	5	CCCCCCC, CRRC
			RFIR, RRMMM, FIRRFR, BWRBG,
4535	17	5	RFMRM, FMRM

# 7.4 RESULTS AND OBSERVATIONS FOR THE HIERARCHICAL CLUSTERING APPROACH

The hierarchical-agglomerative clustering approach relies heavily on the computation of similarity, in this case a linear function of the time and space distances between events. The following analysis provides a sense for these distance values and their distribution.

There were a total of 3291 potential nodes (pairs of consecutive events) generated. The maximum time between two subsequent events found was 18044945643 milliseconds, or 208 days. Clearly, there was a large period of time when meetings did not occur or the data file was not used. (Indeed, the faculty member running the group was on sabbatical for a year and so weekly meetings were much less frequent and of a different character.) The minimum time between events was 10 milliseconds, potentially indicating events added by a single user edit.

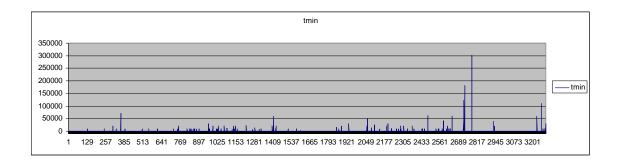


Figure 7.4: Time between events in the edit history

Figure 7.4 show the time between subsequent events in the history record. As can be seen, the vast majority of edits occur relatively few minutes apart. This is not surprising as a time gap of approximately 10000 minutes would be seen for weekly meetings. Figure 7.5 shows the distribution of the time between events.

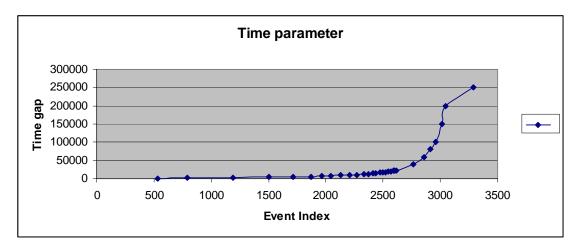


Figure 7.5: Distribution of time gap between subsequent edits

Of the 3291 pairs of consecutive events, 837 pairs (25%) were in different collections. For events within a single collection, the highest spatial distance was 1057.62. When

two operations were on the same object, the spatial distance is 0 – there were 1320 pairs (40%) where this was the case. Figure 7.6 shows the spatial distance between two consecutive events. Remember that 2000 was added to the computed distance when the events occurred in different collections.

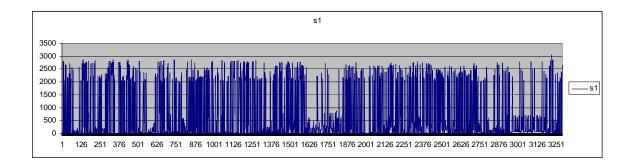


Figure 7.6: Spatial distance between events in the edit history

Figure 7.7 shows the distribution of spatial distances between events. It consists of two parabolic curves, one under 2000 for those event pairs that were within a single collection and one at or above 2000 for event pairs involving different collections.

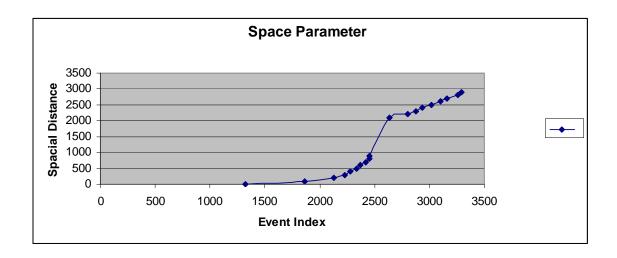


Figure 7.7: Distribution of spatial distances between subsequent events

The overall similarity function is calculated based on the linear function d=s+t where both the coefficients of the linear function have been assumed to be 1. For clustering purposes, a threshold value of up to 30010 was considered. Out of 3291 edit events, 2628 events (79%) are covered within this threshold value, indicating their membership in a group. Thus, this approach generated lots of groups that included the majority of the edit events in the recorded history.

## 7.5 COMPARING RESULTS FROM THE THREE METHODS

The complete set of tokens generated from pattern-based method, rule-based method and hierarchical clustering method are shown in Appendix 1, Appendix 2 and Appendix 3. Some of the groups were generated from more than one approach. Table 7.8 shows the 20 patterns found by all three clustering methods.

Table 7.8: Common tokens obtained from all three methods

Token #	Token
1	ACMM
2	ACMR
3	ACRG
4	ACRM
5	ACRMM
6	ACRRM
7	CMCM
8	CMMM
9	CRCR
10	CRMM
11	CRMR
12	CRRC
13	FMRM
14	MMMM
15	MMMMM
16	MMRM
17	MRCR
18	RCRR
19	TTTT
20	WMMM

# 8. RESULTS AND DISCUSSION

The strategies developed for automatic clustering in this thesis work were applied on a real data set obtained from a research group's use of VKB. To better assess the three clustering approaches, the same data set is manually grouped by two subjects using VKB. From the outputs obtained from the two subjects a single representative output was generated. The output of this manual clustering of VKB events is shown in Table 8.1.

Table 8.1: List of groups obtained from manual grouping

Time stamp	Description of objects on which events were	Token
	applied	
Wed Nov. 03 15:44:31 CST 1999	Evaluation	ACRM
Same as above	System feature	ACRCR
Same as above	History undo	ACMGB
Same as above	Visual Mapping	ACW
Same as above	Done	ARCRRGB
Same as above	WWW 2000	ACGBRM
Same as above	DIS 2000	ACRMRMRCR
Same as above	WWW 2000	MRCRM
Same as above	NRHM Journal	ACRRM
Same as above	tempest	ACRMMMMMMM
Wed Nov. 10 15:48:44 CST 1999	Necessary Feature	ACRGB
Same as above	Types for objects	ACMRMM
Same as above	Bringing up the web	CRRCRCR
Wed Nov 17 16:02:07 CST 1999	WWW 2000	AGBCM
Same as above	Object 160	WWMGBGBWWR
Same as above	Collection 1	NX
Wed Dec 01 15:48:50 CST 1999	Object 248	ARMMGB
Wed Dec 08 15:31:40 CST 1999	Object 248	BBBBBBBBBBBBB
Wed Jan 26 17:20:09 CST 2000	Object 248	MRCRTFIRM
Wed Feb 02 17:43:11 CST 2000	XML Output	GBGBGBGMG
Same as above	HT 2001	ACCR

Table 8.1 Continued

Same as above	Time stamp	Description of objects on which events were	Token
Wed Feb 09 17:45:45 CST 2000         Type Management         AXCGB           Same as above         Apply to existing         ACR           Same as above         Propagating visual changes         GBCRCRR           Same as above         Visual mapping         ACRT           Wed Mar 22 17:29:14 CST 2000         Smart Exploding         MRCR           Same as above         Linking Navigation         GBGBWBBGBGB           Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	•		
Same as above         Apply to existing         ACR           Same as above         Propagating visual changes         GBCRCRR           Same as above         Visual mapping         ACRT           Wed Mar 22 17:29:14 CST 2000         Smart Exploding         MRCR           Same as above         Linking Navigation         GBGBWBBGBGB           Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Same as above	Visual Knowledge builder	ACRFIMRTCM
Same as above         Propagating visual changes         GBCRCRR           Same as above         Visual mapping         ACRT           Wed Mar 22 17:29:14 CST 2000         Smart Exploding         MRCR           Same as above         Linking Navigation         GBGBWBBGBGB           Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MIMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Wed Feb 09 17:45:45 CST 2000	Type Management	AXCGB
Same as above         Visual mapping         ACRT           Wed Mar 22 17:29:14 CST 2000         Smart Exploding         MRCR           Same as above         Linking Navigation         GBGBWBBGBGB           Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Same as above	Apply to existing	ACR
Wed Mar 22 17:29:14 CST 2000         Smart Exploding         MRCR           Same as above         Linking Navigation         GBGBWBBGBGB           Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Same as above	Propagating visual changes	GBCRCRR
Same as above         Linking Navigation         GBGBWBBGBGB           Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Same as above	Visual mapping	ACRT
Wed Mar 29 17:33:26 CST 2000         Linking to history         CMMM           Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Wed Mar 22 17:29:14 CST 2000	Smart Exploding	MRCR
Wed Apr 26 17:39:04 CST 2000         ADL         MRM           Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Same as above	Linking Navigation	GBGBWBBGBGB
Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Wed Mar 29 17:33:26 CST 2000	Linking to history	CMMM
Wed May 17 18:06:26 CST 2000         Session level         ACRMMGBW           Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Wed Apr 26 17:39:04 CST 2000		MRM
Wed Jul 12 17:44:15 CST 2000         Misc. Objects         MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	=	Session level	ACRMMGBW
Wed Aug 09 18:23:39CST 2000         System features         MMMM           Wed Aug 23 18:12:01 CST 2000         Palette         ACGC           Thu Aug 31 18:23:27 CST 2000         Link manager         ACCGBWRM           Same as above         Palette editing         GWBM           Tue Oct 17 17:37:50 CST 2000         Different objects         MMMMMMMMM           Tue Nov 07 17:44:41 CST 2000         Object 2130         CMM           Tue Nov 16 17:36:38 CST 2000         Object 2261         ACMCM           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT		Misc. Objects	MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
Wed Aug 09 18:23:39CST 2000         System features         MMMM           Wed Aug 23 18:12:01 CST 2000         Palette         ACGC           Thu Aug 31 18:23:27 CST 2000         Link manager         ACCGBWRM           Same as above         Palette editing         GWBM           Tue Oct 17 17:37:50 CST 2000         Different objects         MMMMMMMMM           Tue Nov 07 17:44:41 CST 2000         Object 2130         CMM           Tue Nov 16 17:36:38 CST 2000         Object 2261         ACMCM           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Wed Aug 02 18:15:22 CST 2000	Suggestion	ACGBRMTTTTT
Wed Aug 23 18:12:01 CST 2000         Palette         ACGC           Thu Aug 31 18:23:27 CST 2000         Link manager         ACCGBWRM           Same as above         Palette editing         GWBM           Tue Oct 17 17:37:50 CST 2000         Different objects         MMMMMMMM           Tue Nov 07 17:44:41 CST 2000         Object 2130         CMM           Tue Nov 16 17:36:38 CST 2000         Object 2105         CMR           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT			MMMM
Thu Aug 31 18:23:27 CST 2000		•	ACGC
Same as above         Palette editing         GWBM           Tue Oct 17 17:37:50 CST 2000         Different objects         MMMMMMMM           Tue Nov 07 17:44:41 CST 2000         Object 2130         CMM           Tue Nov 16 17:36:38 CST 2000         Object 2105         CMR           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	· ·	Link manager	ACCGBWRM
Tue Nov 07 17:44:41 CST 2000         Object 2130         CMM           Tue Nov 16 17:36:38 CST 2000         Object 2105         CMR           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	•		GWBM
Tue Nov 07 17:44:41 CST 2000         Object 2130         CMM           Tue Nov 16 17:36:38 CST 2000         Object 2105         CMR           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Tue Oct 17 17:37:50 CST 2000	e e	MMMMMMMM
Tue Nov 16 17:36:38 CST 2000         Object 2105         CMR           Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Tue Nov 07 17:44:41 CST 2000		CMM
Tue Nov 21 17:50:42 CST 2000         Object 2261         ACMCM           Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Tue Nov 16 17:36:38 CST 2000	· ·	CMR
Tue Nov 28 17:48:59 CST 2000         Collection 2340         MCMM           Tue Jan 23 17:38:44 CST 2001         DL 2001         CMCM           Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Tue Nov 21 17:50:42 CST 2000	· ·	ACMCM
Tue Mar 06 17:59:19 CST 2001         Collection 2340         RMMMM           Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Tue Nov 28 17:48:59 CST 2000	· ·	MCMM
Tue Mar 08 20:20:54 CST 2001         Collection 2437         MMR           Same as above         Object 2339         MGBMRCMMM           Same as above         XML Output         MMRCRCR           Same as above         Collection 2403         MBGM           Tue May 01 18:01:58 CDT 2001         Object 788         CCCCCCCC           Same as above         Object 2339         TTTT	Tue Jan 23 17:38:44 CST 2001	DL 2001	CMCM
Same as above Object 2339 MGBMRCMMM  Same as above XML Output MMRCRCR  Same as above Collection 2403 MBGM  Tue May 01 18:01:58 CDT 2001 Object 788 CCCCCCC  Same as above Object 2339 TTTT	Tue Mar 06 17:59:19 CST 2001	Collection 2340	RMMMM
Same as above XML Output MMRCRCR Same as above Collection 2403 MBGM Tue May 01 18:01:58 CDT 2001 Object 788 CCCCCCC Same as above Object 2339 TTTT	Tue Mar 08 20:20:54 CST 2001	Collection 2437	MMR
Same as above XML Output MMRCRCR Same as above Collection 2403 MBGM Tue May 01 18:01:58 CDT 2001 Object 788 CCCCCCC Same as above Object 2339 TTTT	Same as above	Object 2339	MGBMRCMMM
Same as above Collection 2403 MBGM  Tue May 01 18:01:58 CDT 2001 Object 788 CCCCCCC  Same as above Object 2339 TTTT	Same as above		MMRCRCR
Same as above Object 2339 TTTT	Same as above		MBGM
Same as above Object 2339 TTTT	Tue May 01 18:01:58 CDT 2001	Object 788	CCCCCCC
			TTTT
Tue Jul 1/ 15:55:48 CDT 2001   Old Task that might   ACGBMR	Tue Jul 17 15:53:48 CDT 2001	Old Task that might	ACGBMR
Same as above Encrypted Password ACRCGBM			
Tue Aug 28 15:41:28 CDT 2001 User id in history ACRWBMRM			
Same as above Overview Window ACRBGM			
Wed Sep 05 16:07:35 CDT 2001 Grouping history ACRRMMRW			
Thu Feb 14 16:52:34 CST 2002 Link data base ACMRRMM			
Wed Jun 19 16:36:22 CDT 2002 XML data file format ACMMRM			
Thu Feb 13 16:54:54 CST 2003 Magnetic poetry study MCRMRGBW			

Table 8.1 Continued

Time stamp	Description of objects on which events were	Token
	applied	
Wed Sep 10 15:16:34 CDT 2003	Attribute analysis in type	ACRCM
Same as above	Relation suggestion	CRCR
Same as above	Logarithmic distribution	MCRR
Same as above	Encrypted password	CRMM
Wed Oct 22 16:26:09 CDT 2003	Do we base it	ACRRWGB
Same as above	Symbol Scenarios	ACRCRRCR
Same as above	VITE journal paper	FIRRFIR
Same as above	VITE journal paper	RFIMRM

The edit sequences obtained from manual grouping were compared with those identified by the three automatic methods. There were a total of 70 manual groups. Of these, 8 groups were detected by all three strategies. Another 8 groups were detected by 2 strategies. 24 groups were detected by only one strategy and 30 groups were not detected by any strategy at all.

Out of the 70 manual groups generated, the pattern-based approach detected 14 groups, the rule-based approach detected 28 groups, and the HAC approach detected 22 groups. Table 8.2 lists all the manual groups and which group was detected by which strategies.

Table 8.2: Detection of manual groups by different strategies

			Detected by	Total detection
	Detected by	Detected by Rule	Hierarchical	By different
Token	Pattern Based?	Based?	Clustering?	strategies
ACRRM	YES	YES	YES	3
MRCR	YES	YES	YES	3
CMMM	YES	YES	YES	3
MMMM	YES	YES	YES	3
CMCM	YES	YES	YES	3

Table 8.2 Continued

			Detected by	Total detection
	Detected by	Detected by Rule	Hierarchical	By different
Token	Pattern Based?	Based?	Clustering?	strategies
TTTT	YES	YES	YES	3
CRCR	YES	YES	YES	3
CRMM	YES	YES	YES	3
ACRCR	YES	YES	NO	2
ACGBRM	NO	YES	YES	2
MMMMMM	YES	NO	YES	2
GWBM	NO	YES	YES	2
MMMMMMMM	YES	NO	YES	2
MCMM	YES	NO	YES	2
RMMMM	YES	YES	NO	2
ACRBGM	NO	YES	YES	2
ACW	NO	NO	YES	1
MRCRM	NO	YES	NO	1
ACRMMMMMMM	NO	YES	NO	1
ACMRMM	YES	NO	NO	1
CRRCRCR	NO	YES	NO	1
AAAAAA	NO	NO	YES	1
ACR	NO	NO	YES	1
ACRT	NO	YES	NO	1
MRM	NO	NO	YES	1
MMMMMMMMMMMMMMM	NO	NO	YES	1
ACGC	NO	YES	NO	1
CMM	NO	NO	YES	1
CMR	NO	NO	YES	1
MMR	NO	NO	YES	1
MMRCRCR	NO	YES	NO	1
MBGM	NO	YES	NO	1
CCCCCCC	NO	YES	NO	1
ACRRMMRW	NO	YES	NO	1
ACMRRMM	NO	YES	NO	1
ACMMRM	NO	YES	NO	1
ACRCM	NO	YES	NO	1
MCRR	NO	YES	NO	1
ACRCRRCR	NO	YES	NO	1
FIRRFIR	NO	YES	NO	1
ACMGB	NO	NO	NO	0

Table 8.2 Continued

			Detected by	Total detection
	Detected by	Detected by Rule	Hierarchical	By different
Token	Pattern Based?	Based?	Clustering?	strategies
ARCRRGB	NO	NO	NO	0
ACRMRMRCR	NO	NO	NO	0
ACRGB	NO	NO	NO	0
GBGBGBGB	NO	NO	NO	0
AGBCM	NO	NO	NO	0
GGGGGBBBBBB	NO	NO	NO	0
GBGBGBGBGB	NO	NO	NO	0
WWMGBGBWWR	NO	NO	NO	0
NX	NO	NO	NO	0
ARMMGB	NO	NO	NO	0
BBBBBBBBBBBBB	NO	NO	NO	0
MRCRTFIRM	NO	NO	NO	0
GBGBGBGMG	NO	NO	NO	0
ACCR	NO	NO	NO	0
ACRFIMRTCM	NO	NO	NO	0
AXCGB	NO	NO	NO	0
GBCRCRR	NO	NO	NO	0
GBGBWBBGBGB	NO	NO	NO	0
ACRMMGBW	NO	NO	NO	0
ACGBRMTTTTT	NO	NO	NO	0
ACCGBWRM	NO	NO	NO	0
ACMCM	NO	NO	NO	0
MGBMRCMMM	NO	NO	NO	0
ACGBMR	NO	NO	NO	0
ACRCGBM	NO	NO	NO	0
ACRWBMRM	NO	NO	NO	0
MCRMRGBW	NO	NO	NO	0
ACRRWGB	NO	NO	NO	0
RFIMRM	NO	NO	NO	0

As a final comparison, Table 8.3 shows the number of groups generated by each of the three methods and how many of the manually-constructed groups were identified by each approach. The rule-based method not only detected the highest number of manual

groups but it also generated the fewest groups. This could indicate that it generates the fewest number of spurious groups, having the highest precision and recall of the three methods.

Table 8.3: Statistics of detected groups by automatic strategies

Strategies	Number of
	groups
Event groups detected by Pattern-based method	403
Event groups detected by Rule-based method	130
Event groups detected by HAC based method	613
Manual groups detected by Pattern-based method	14
Manual groups detected by Rule-based method	28
Manual groups detected by HAC based method	22

While this indicates the potential value of a few simple rules for clustering edit history, the advantages of the other approaches should also be acknowledged. The pattern-based approach does more than just grouping edit events, it uncovers repeated patterns of actions that could be used to generate macros to better support VKB users. This would require tuning the algorithm to be more selective and would benefit from the inclusion of wildcards and regular expression matching to the general approach. The HAC approach similarly needs to be tuned to be much more selective in grouping edit events. Of all the approaches, it is the one that could potentially recognize a single activity involving structures in multiple collections of a VKB workspace. Finally, the success of the rule-based method indicates that the addition of rules for additional levels of grouping based on the spatial parser should be investigated.

### 9. CONCLUSION

History mechanisms available in hypertext systems allow access to past user interactions with the system. This availability allows users to evaluate past work and to learn from past activity. It also allows systems to identify usage patterns and potentially predict behaviors with the system. Thus, recording history is useful to both the system and the user.

The Visual Knowledge Builder (VKB) is a *spatial hypertext* – a visual workspace for collecting, organizing, and sharing information. It stores a detailed history of all user edit interactions during previous authoring sessions. Various tools and techniques have been developed to group and annotate VKB history. Such grouping may be valuable for a number of applications: accessing desired segments of long edit histories, identifying portions of edit history with special or similar attributes, and predicting future interaction during VKB authoring sessions. But the problem with these tools is that the grouping operation or annotation is currently performed manually. For a large VKB history that has been growing over a long period of time, creating groups using such tools is difficult and time consuming. This thesis examines methods to analyze VKB history in order to create groups/clusters from history events automatically.

Three approaches to automatic grouping are compared in this thesis. The first approach is a pattern-matching approach that identifies repeated patterns of edit events in the history. The second approach is a rule-based approach that uses simple rules, such as "group all consecutive events on a single object". The third approach uses hierarchical agglomerative clustering (HAC) where edits are grouped based on a function of edit time and edit location. Each approach has its own theoretical strengths and weaknesses. By implementing and evaluating the three approaches, this thesis examines their practical strengths and weaknesses as well.

The results showed that the pattern-matching approach generated many potential groupings but few matched those that were generated by people. Tuning of the algorithm to be much more selective, while also extending it to include wildcards and regular expressions, would likely be required before this approach would be usable.

The rule-based approach performed best in that it best matched human-defined groups and generated the fewest number of groups. Extensions to this approach include additional levels of grouping based on the spatial structures recognized by a spatial parser and the tuning of the rules to include time, position, and event type considerations.

The hierarchic agglomerative clustering approach was in between the other two approaches with regards to identifying human-defined groups. This algorithm relies on a similarity measure that has the potential to be much better defined based on the results of this thesis. The combination of such tuning with better rules for selecting clustering levels could rival or surpass the effectiveness of the rule-based approach. This is a case where the simplest approach and implementation performed the best. This could be because the rules best match what people do when they are forced to group edit events or it could be because the complexities of the other methods require significant tuning to generate reasonably good results.

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## APPENDIX 1

## TOKENS GENERATED FROM PATTERN BASED ANALYSIS

Table A-1: Token generated from pattern based method

Token #	Token generated
1	AAAAG
2	AAAG
3	AAAGAA
4	AAGAA
5	AAGGA
6	ACAC
7	ACACAC
8	ACACC
9	ACACRRMM
10	ACCAC
11	ACCC
12	ACCM
13	ACGM
14	ACMAC
15	ACMACM
16	ACMC
17	ACMM
18	ACMMM
19	ACMMMM
20	ACMMMMM
21	ACMMMMM
22	ACMMMMMM
23	ACMMMMMMM
24	ACMR
25	ACMRM
26	ACMRMM
27	ACRA
28	ACRAC
29	ACRACR
30	ACRACRACRM

Table A-1 Continued

Token #	Token generated
31	ACRCR
32	ACRCRR
33	ACRG
34	ACRGACR
35	ACRM
36	ACRMAC
37	ACRMACR
38	ACRMACRM
39	ACRMM
40	ACRMMM
41	ACRMMMM
42	ACRR
43	ACRRM
44	ACRRMACR
45	ACRW
46	ACWA
47	ACWG
48	AGAA
49	AGAAAG
50	ARCRAC
51	AUUUUUUUUUU
52	BACW
53	BBBB
54	BBBWBB
55	BBGGG
56	BBWW
57	BBWWGGBB
58	BMBM
59	BMMMM
60	BWWGG
61	BWWGGB
62	CACC
63	CACMM
64	CACR
65	CCACC
66	ССССССССМ
67	CCCCM
68	CCCCMC

Table A-1 Continued

Token #	Token generated
69	CCMCMCM
70	CCMCMCMCM
71	CCMM
72	CCRMM
73	CGACR
74	CMAC
75	CMCC
76	CMCM
77	CMCMC
78	CMCMCM
79	CMCMCMCM
80	CMMAC
81	CMMACM
82	CMMACMAC
83	CMMCM
84	CMMCMMAC
85	CMMM
86	CMMMM
87	CMMMMM
88	CMMMMAC
89	СМММММ
90	СММММММ
91	СМММММММ
92	CMMR
93	CMWC
94	CRAC
95	CRACGBM
96	CRACR
97	CRACRACR
98	CRCR
99	CRMM
100	CRMMM
101	CRMMMAC
102	CRMMMM
103	CRMMMMMM
104	CRMR
105	CRRAC
106	CRRC

Table A-1 Continued

107   CRRM   108   CRRMM   109   FMRM   110   FRMMM   111   FACR   112   FRM   113   GAAAG   114   GAAAGG   115   GAAAGGA   116   GBBWGG   117   GBWGG   118   GBWWGGAAA   120   GCMM   121   GGAAA   122   GGAAAG   122   GGAAAG   123   GGBB   124   GGGG   125   GGGG   126   GGGM   127   GGMM   128   GMAC   129   GMMAC   131   GMMACR   131   GMMACR   131   GMMACR   131   GMMMACR   132   GMMM   133   GMMMACR   134   GMMMMMM   135   GRMAC   136   GMMMMMMM   137   GRMAC   138   GMMMACR   139   GMMACR   130   GMMACR   131   GMMMACR   131   GMMMACR   132   GMMM   133   GMMMACR   134   GMMMMMMM   135   GRMAC   136   MACAC   137   MACACM   138   MACCMCMCMCM   139   MACG   140   MACM   141   MACMM   141   MACMM   142   MACR   143   MACRG   144   MACRM   144   MACRM   144   MACRM   144   MACRM   144   MACRM   144   MACRG   144   MACRM   144	Token #	Token generated
109 FMRM	107	CRRM
110 FRMM  111 FACR  112 FIRM  113 GAAA  114 GAAAG  115 GAAAGGA  116 GBBWGG  117 GBMGG  118 GBWWGG  119 GBWWGGAAA  120 GCMM  121 GGAAA  122 GGAAAG  123 GGBB  124 GGGG  125 GGGGG  126 GGGM  127 GGMM  128 GMAC  129 GMMA  130 GMMAC  131 GMMACR  131 GMMACR  131 GMMMMMM  135 GRMMC  136 MACC  137 MACACM  138 MACCMCMCM  141 MACM  141 MACM  142 MACR  142 MACR  143 MACR  144 MACR  144 MACR  144 MACR  144 MACR  144 MACR  144 MACR	108	CRRMM
111 FIACR 112 FIRM 113 GAAA 114 GAAAG 115 GAAAGGA 116 GBBWGG 117 GBMGG 118 GBWWGG 119 GBWWGGAAA 120 GCMM 121 GGAAA 122 GGAAA 122 GGAAA 122 GGAAA 122 GGAM 123 GGBB 124 GGG 125 GGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMACR 131 GMMACR 132 GMMM 133 GMMMMMMMM 133 GMMMMMMMMM 135 GRAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 141 MACMM 142 MACR	109	FMRM
112 FIRM 113 GAAA 114 GAAAG 115 GAAAGGA 116 GBBWGG 117 GBMGG 118 GBWWGGAAA 120 GCMM 121 GGAAA 122 GGAAAG 123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMACR 131 GMMACR 133 GMMMMM 133 GMMMACR 133 GMMMMMM 133 GMMACR 134 GMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	110	FRMMM
113 GAAA 114 GAAAG 115 GAAAGGA 116 GBBWGG 117 GBMGG 118 GBWWGG 119 GBWWGGAAA 120 GCMM 121 GGAAA 122 GGAAA 122 GGAAAG 123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMACR 131 GMMACR 132 GMMM 133 GMMACR 133 GMMMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 137 MACACM 138 MACCMCMCM 140 MACM 141 MACM 141 MACM 142 MACR	111	FIACR
114 GAAAG 115 GAAAGGA 116 GBBWGG 117 GBMGG 118 GBWWGG 119 GBWWGGAAA 120 GCMM 121 GGAAAG 122 GGAAAG 123 GGBB 124 GGGG 125 GGGGG 126 GGMM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMAC 131 GMMAC 131 GMMACR 131 GMMMMMM 133 GMMMACR 134 GMMMMMMM 135 GRAAC 135 GRACC 136 MACACC 137 MACACM 138 MACCMCMCM 139 MACM 140 MACM 141 MACMM 141 MACMM 142 MACR	112	FIRM
115 GAAAGGA 116 GBBWGG 117 GBMGG 118 GBWWGG 119 GBWWGGAAA 120 GCMM 121 GGAAA 122 GGAAA 122 GGAAA 123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMACR 131 GMMACR 132 GMMM 133 GMMACR 134 GMMMMMM 135 GRAC 137 MACACM 138 MACACM 139 MACG 140 MACM 141 MACMM 141 MACMM 141 MACMM	113	GAAA
116   GBBWGG   117   GBMGG   118   GBWWGG   119   GBWWGGAAA   120   GCMM   121   GGAAA   122   GGAAAG   123   GGBB   124   GGGG   125   GGGGG   126   GGGM   127   GGMM   128   GMAC   129   GMMA   130   GMMAC   131   GMMACR   131   GMMACR   131   GMMMACR   132   GMMM   133   GMMMMMMM   133   GMMMMMMM   135   GMMMMMMM   136   GMMMMMMMM   137   GMMC   138   MACACC   137   MACACM   138   MACCMCMCM   139   MACG   140   MACM   141   MACM   142   MACR   143   MACRG   144   MACRG   145   MACRG   145   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG   148   MACRG   149   MACRG   140   MACRG   140   MACRG   141   MACRG   142   MACRG   143   MACRG   144   MACRG   145   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG   148   MACRG   149   MACRG   140   MACRG   140   MACRG   140   MACRG   141   MACRG   142   MACRG   143   MACRG   143   MACRG   144   MACRG   145   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG	114	GAAAG
117 GBMGG 118 GBWWGG 119 GBWWGGAAA 120 GCMM 121 GGAAA 122 GGAAAG 123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMACR 131 GMMACR 132 GMMM 133 GMMMCR 133 GMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	115	GAAAGGA
118   GBWWGG   119   GBWWGGAAA   120   GCMM   121   GGAAA   122   GGAAA   122   GGAAAG   123   GGBB   124   GGGG   125   GGGGG   126   GGMM   127   GGMM   128   GMAC   129   GMMA   130   GMMAC   131   GMMACR   131   GMMACR   131   GMMACR   132   GMMM   133   GMMMACR   134   GMMMMMM   135   GRMAC   136   GRMAC   137   MACACM   138   MACCMCMCM   139   MACG   140   MACM   141   MACM   141   MACM   142   MACR   143   MACRG   144   MACR   144   MACR   144   MACR   144   MACR   145   MACR   146   MACR   147   MACR   148   MACR   149   MACR   140   MACR   141   MACR   142   MACR   143   MACRG   144   MACR   144   MACR   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG   149   MACRG   140   MACRG   140   MACRG   140   MACRG   140   MACRG   140   MACRG   141   MACRG   142   MACRG   143   MACRG   143   MACRG   144   MACRG   144   MACRG   145   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   147   MACRG   148   MAC	116	GBBWGG
119   GBWWGGAAA   120   GCMM   121   GGAAA   122   GGAAAG   123   GGBB   124   GGGG   125   GGGGG   126   GGGM   127   GGMM   128   GMAC   129   GMMA   130   GMMAC   131   GMMACR   131   GMMACR   132   GMMM   133   GMMACR   134   GMMMMMM   135   GRMAC   137   MACACM   138   MACCMCMCM   139   MACG   140   MACM   141   MACM   141   MACM   142   MACR   143   MACRG   144   MACR   144   MACR   144   MACR   145   MACR   145   MACR   146   MACR   147   MACR   148   MACR   149   MACR   140   MACR   140   MACR   141   MACR   142   MACR   143   MACRG   144   MACR   144   MACR   145   MACR   145   MACR   145   MACR   146   MACR   147   MACR   148   MACR   148   MACR   148   MACR   149   MACR   140   MACR   140   MACR   141   MACR   142   MACR   143   MACRG   140   MACR   144   MACR   144   MACR   145   MACR   145   MACR   145   MACRG   146   MACR   147   MACR   148   MACRG   149   MACR   149   MACR   149   MACR   149   MACR   149   MACR   149   MACR   141   MACRG   140   MACR   141   MACRG   140   MACR   141   MACRG   140   MACR   141   MACRG	117	GBMGG
120   GCMM   121   GGAAA   122   GGAAAG   123   GGBB   124   GGGG   125   GGGGG   126   GGGM   127   GGMM   128   GMAC   129   GMMA   130   GMMAC   131   GMMACR   131   GMMACR   132   GMMM   133   GMMMACR   134   GMMMMMM   135   GRMAC   136   MACAC   137   MACACM   138   MACCMCMCM   139   MACG   140   MACM   141   MACMM   142   MACR   143   MACRG   143   MACRG   144   MACR   144   MACR   144   MACR   144   MACR   144   MACR   144   MACR   145   MACR   145   MACR   145   MACR   146   MACR   147   MACR   148   MACR   148   MACR   148   MACR   149   MACR   140   MACR   141   MACR   143   MACRG   140   MACR   143   MACRG   144   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG   148   MACRG   148   MACRG   149   MACRG   140   MACRG   141   MACRG   143   MACRG   144   MACRG   145   MACRG   145   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   147   MACRG   148   MACRG   148	118	GBWWGG
121 GGAAA 122 GGAAAG 123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 141 MACMM 142 MACR	119	GBWWGGAAA
122 GGAAAG 123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMMMM 133 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 137 MACACM 138 MACCMCMCM 140 MACM 141 MACMM 141 MACMM 142 MACR 143 MACRG	120	GCMM
123 GGBB 124 GGGG 125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 131 GMMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 141 MACMM 142 MACR	121	GGAAA
124   GGGG   125   GGGGG   126   GGGM   127   GGMM   128   GMAC   129   GMMA   130   GMMAC   131   GMMACR   132   GMMM   133   GMMMACR   134   GMMMMMM   135   GRMAC   136   MACAC   137   MACACM   138   MACCMCMCM   139   MACG   140   MACM   141   MACMM   142   MACR   143   MACRG   143   MACRG   144   MACR   145   MACR   145   MACRG   145   MACRG   146   MACR   147   MACRG   148   MACRG   148   MACRG   148   MACRG   148   MACRG   149   MACRG   140   MACRG   140   MACRG   140   MACRG   141   MACRG   142   MACRG   143   MACRG   143   MACRG   144   MACRG   144   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG	122	GGAAAG
125 GGGGG 126 GGGM 127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM	123	GGBB
126   GGGM   127   GGMM   128   GMAC   129   GMMA   130   GMMAC   131   GMMAC   131   GMMACR   132   GMMM   133   GMMMACR   134   GMMMMMM   135   GRMAC   136   MACAC   137   MACACM   138   MACCMCMCM   138   MACCMCMCM   139   MACG   140   MACM   141   MACMM   142   MACR   143   MACRG   140   MACR   143   MACRG   140   MACR   144   MACR   143   MACRG   140   MACR   144   MACR   144   MACRG   145   MACRG   140   MACR   141   MACRG   142   MACR   143   MACRG   144   MACRG   145   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   148   MACRG   149   MACRG   140   MACRG   140   MACRG   140   MACRG   141   MACRG   142   MACRG   143   MACRG   143   MACRG   144   MACRG   145   MACRG   145   MACRG   146   MACRG   147   MACRG   147   MACRG   148   MACRG   1	124	GGGG
127 GGMM 128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 142 MACR	125	GGGGG
128 GMAC 129 GMMA 130 GMMAC 131 GMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 142 MACR 143 MACRG	126	GGGM
129 GMMAC 130 GMMACR 131 GMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 142 MACR	127	GGMM
130 GMMAC   131 GMMACR   132 GMMM   133 GMMMACR   134 GMMMMMM   135 GRMAC   136 MACAC   137 MACACM   138 MACCMCMCM   139 MACG   140 MACM   141 MACMM   142 MACR   143 MACRG   144 MACRG   145 MACRG   145 MACRG   145 MACRG   146 MACRG   147 MACRG   148 MACRG   148 MACRG   148 MACRG   148 MACRG   149 MACRG   140 MACRG	128	GMAC
131 GMMACR 132 GMMM 133 GMMMACR 134 GMMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 141 MACMM	129	GMMA
132 GMMM 133 GMMMACR 134 GMMMMM 135 GRMAC 136 MACAC 137 MACACM 138 MACCMCMCM 139 MACG 140 MACM 141 MACMM 142 MACR	130	GMMAC
133 GMMMACR  134 GMMMMMM  135 GRMAC  136 MACAC  137 MACACM  138 MACCMCMCM  139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	131	GMMACR
134 GMMMMM  135 GRMAC  136 MACAC  137 MACACM  138 MACCMCMCM  139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	132	GMMM
135 GRMAC  136 MACAC  137 MACACM  138 MACCMCMCM  139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	133	GMMMACR
136 MACAC  137 MACACM  138 MACCMCMCM  139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	134	GMMMMM
137 MACACM  138 MACCMCMCM  139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	135	GRMAC
138 MACCMCMCM  139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	136	MACAC
139 MACG  140 MACM  141 MACMM  142 MACR  143 MACRG	137	MACACM
140 MACM  141 MACMM  142 MACR  143 MACRG	138	MACCMCMCM
141 MACMM  142 MACR  143 MACRG	139	MACG
142 MACR 143 MACRG	140	MACM
143 MACRG	141	MACMM
	142	MACR
144 MACRM	143	MACRG
	144	MACRM

Table A-1 Continued

145   MACRMMG	Token #	Token generated
147       MACRMMM         148       MACRMMMM         149       MACRMMMMM         150       MARC         151       MARCR         152       MBWM         153       MCAC         154       MCCCCCCCC         155       MCCCCCCCCM         156       MCCM         157       MCCMR         158       MCCR         159       MCMC         160       MCMCCM         161       MCMCM         162       MCMM         163       MCMMMMM         164       MCMMMMMM         165       MCRM         166       MCRM         167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACMAC         172       MMACMACMAC         173       MMACMMMMM         174       MMACRMACR         175       MMACR         177       MMACRM         180       MMACR         181       MMACR	145	MACRMM
148       MACRMMMM         149       MACRMMMMM         150       MARC         151       MARCR         152       MBWM         153       MCAC         154       MCCCCCCCCC         155       MCCCCCCCCCM         156       MCCM         157       MCCMR         158       MCCR         159       MCMC         160       MCMCCM         161       MCMM         162       MCMM         163       MCMMMM         164       MCMMMMM         165       MCRM         166       MCRM         167       MGAC         168       MGMM         169       MGMMM         169       MGMMM         170       MMAC         171       MMACMAC         172       MMACMMMMM         173       MMACMMMMM         174       MMACRMMMMM         175       MMACR         179       MMACRM         180       MMACR         181       MMACR	146	MACRMMG
149 MACRMMMMM  150 MARC  151 MARCR  152 MBWM  153 MCAC  154 MCCCCCCC  155 MCCCCCCCM  156 MCCM  157 MCCMR  158 MCCR  159 MCMC  160 MCMCCM  161 MCMCM  162 MCMM  163 MCMMMMMM  164 MCMMMMM  165 MCRM  166 MCRMM  167 MGAC  168 MGMM  169 MGMC  171 MMACC  171 MMACM  172 MMACMACM  173 MMACMMMMM  174 MMACMMMMM  175 MMACR  176 MMACR  177 MMACR  177 MMACR  177 MMACRM  178 MMACRM  179 MMACR  170 MMACR  171 MMACRM  171 MMACRM  171 MMACRM  172 MMACRMMMMM  173 MMACRMMMMM  174 MMACRMMMMMM  175 MMACRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	147	MACRMMM
150 MARC  151 MARCR  152 MBWM  153 MCAC  154 MCCCCCCC  155 MCCCCCCCM  155 MCCM  157 MCCMR  158 MCCR  159 MCMC  160 MCMCM  161 MCMCM  162 MCMM  163 MCMM  164 MCMMMMMM  165 MCRM  166 MCRMM  170 MGAC  171 MMACM  172 MMACMAC  171 MMACM  172 MMACMMMMM  174 MMACMMMMM  175 MMACR  176 MMACR  177 MMACRC  177 MMACRC  178 MMACRC  178 MMACRM  179 MMACRC  171 MMACRC  177 MMACRC  178 MMACRM  179 MMACRC  177 MMACRC  178 MMACRM  179 MMACRM  170 MMACRC  177 MMACRC  178 MMACRM  179 MMACRM  179 MMACRM  170 MMACRC  177 MMACRM  177 MMACRM  178 MMACRM  179 MMACRM  179 MMACRM	148	MACRMMMM
151 MARCR 152 MBWM 153 MCAC 154 MCCCCCCCC 155 MCCCCCCCM 156 MCCCCCCCM 157 MCCMR 158 MCCR 159 MCMC 160 MCMCM 161 MCMCM 162 MCMM 163 MCMMMM 164 MCMMMMM 165 MCRM 166 MCRMM 167 MGAC 168 MGMM 169 MGMMM 170 MMAC 171 MMACM 172 MMACMMMMM 174 MMACMMMMMM 175 MMACR 176 MMACR 177 MMACRM 178 MMACRM 179 MMACRM 179 MMACRM 179 MMACRM 179 MMACRM 180 MMACR 171 MMACRM 180 MMACRM 180 MMACRR	149	MACRMMMMM
152 MBWM 153 MCAC 154 MCCCCCCCC 155 MCCCCCCCM 156 MCCM 157 MCCMR 158 MCCR 159 MCMC 160 MCMCM 161 MCMCM 162 MCMM 163 MCMMCM 164 MCMMMMM 165 MCRM 166 MCRMM 167 MGAC 168 MGMM 169 MGMMM 169 MGMMM 170 MMAC 171 MMACM 172 MMACMMMMM 175 MMACR 176 MMACR 177 MMACRC 177 MMACRC 178 MMACR 179 MMACR 179 MMACR 170 MMACR 171 MMACR 171 MMACR 172 MMACR 173 MMACRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	150	MARC
153 MCAC  154 MCCCCCCCC  155 MCCCCCCCM  156 MCCM  157 MCCMR  158 MCCR  159 MCMC  160 MCMCM  161 MCMCM  162 MCMM  163 MCMMCM  164 MCMMMMM  165 MCRM  166 MCRMM  167 MGAC  168 MGMM  169 MGMMM  170 MMAC  171 MMACM  172 MMACMACM  173 MMACMMMMM  174 MMACMMMMMM  175 MMACR  176 MMACR  177 MMACR  177 MMACR  178 MMACRM  179 MMACR  179 MMACR  171 MMACR  171 MMACR  172 MMACRC  173 MMACRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	151	MARCR
154   MCCCCCCC   155   MCCCCCCCM   156   MCCM   157   MCCMR   158   MCCR   159   MCMC   160   MCMCM   161   MCMCM   162   MCMM   162   MCMM   163   MCMMMM   164   MCMMMMM   165   MCRM   166   MCRMM   167   MGAC   168   MGMM   169   MGMMM   170   MMAC   MMACM   MMACM	152	MBWM
155         MCCCCCCCCM           156         MCCM           157         MCCMR           158         MCCR           159         MCMC           160         MCMCM           161         MCMCM           162         MCMM           163         MCMMCM           164         MCMMMM           165         MCRM           166         MCRM           167         MGAC           168         MGMM           169         MGMMM           170         MMAC           171         MMACM           172         MMACMAC           173         MMACMMMMM           174         MMACMMMMMM           175         MMACRM           176         MMACR           177         MMACR           178         MMACRM           180         MMACR           181         MMACR	153	MCAC
156   MCCM   157   MCCMR   158   MCCR   159   MCMC   160   MCMCCM   161   MCMCM   162   MCMM   163   MCMMCM   164   MCMMMM   165   MCRM   166   MCRM   166   MCRM   167   MGAC   168   MGMM   169   MGMMM   169   MGMMM   170   MMAC   171   MMACM   171   MMACM   172   MMACMACM   173   MMACMMMMM   174   MMACMMMMMM   175   MMACMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	154	MCCCCCCCC
157   MCCMR   158   MCCR   159   MCMC   160   MCMCCM   161   MCMCM   162   MCMM   162   MCMMMM   163   MCMMMM   165   MCRM   166   MCRMM   167   MGAC   168   MGMM   169   MGMMM   170   MMAC   171   MMACM   171   MMACM   172   MMACMMMMM   173   MMACMMMMM   174   MMACMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	155	MCCCCCCCM
158   MCCR   159   MCMC   160   MCMCCM   161   MCMCM   162   MCMM   163   MCMMCM   164   MCMMMM   165   MCRM   166   MCRM   166   MCRMM   167   MGAC   168   MGMM   169   MGMMM   170   MMAC   171   MMACM   172   MMACMAC   173   MMACMACM   174   MMACMMMMM   175   MMACMAC   175   MMACMAC   176   MMACMAC   177   MMACMAC   177   MMACMAC   178   MMACMAC   179   MMACMAC   170   MMACC   170   MMACC   171   MMACMACMAC   171   MMACMACMAC   172   MMACMACMAC   173   MMACMACMAC   174   MMACMACMAC   175   MMACCC   176   MMACCC   177   MMACCC   178   MMACCC   178   MMACCC   178   MMACCC   179   MMACCCC   178   MMACCCC   178   MMACCCC   178   MMACCCC   178   MMACCCC   178   MMACCCC   179   MMACCCC   179   MMACCCC   179   MMACCCC   179   MMACCCC   179   MMACCCCC   179   MMACCCCC   179   MMACCCCC   179   MMACCCCC   179   MMACCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC	156	MCCM
159 MCMC 160 MCMCCM 161 MCMCM 162 MCMM 163 MCMMCM 164 MCMMMMM 165 MCRM 166 MCRMM 167 MGAC 168 MGMM 169 MGMMM 170 MMAC 171 MMACM 172 MMACMAC 173 MMACMMMMM 174 MMACMMMMM 175 MMACC 176 MMACC 177 MMACC 177 MMACC 178 MMACC 177 MMACCR 178 MMACRC 178 MMACRC 179 MMACRC 179 MMACRC 178 MMACRC 179 MMACRMMMM 179 MMACRC 179 MMACRC 178 MMACRM 179 MMACRMMMM 180 MMACRC 180 MMACRC 180 MMACRC 180 MMACRC 181 MMACRMMMMM 180 MMACRC 180 MMACRC	157	MCCMR
160 MCMCCM 161 MCMCM 162 MCMM 163 MCMMCM 164 MCMMMMM 165 MCRM 166 MCRMM 167 MGAC 168 MGMM 169 MGMMM 170 MMAC 171 MMACM 171 MMACM 172 MMACMAC 173 MMACMAMMMM 174 MMACMAMMMM 175 MMACC 176 MMACR 177 MMACR 177 MMACR 178 MMACR 179 MMACRC 178 MMACRC 178 MMACRC 178 MMACRM 179 MMACRMMMM 179 MMACRC 178 MMACRM 179 MMACRMMMM 180 MMACRC 181 MMACR	158	MCCR
161 MCMCM 162 MCMM 163 MCMMCM 164 MCMMMMM 165 MCRM 166 MCRMM 167 MGAC 168 MGMM 169 MGMMM 170 MMAC 171 MMACM 171 MMACM 172 MMACMAC 173 MMACMMMMM 174 MMACMMMMM 175 MMACC 175 MMACR 176 MMACR 177 MMACR 177 MMACR 178 MMACR 179 MMACR 179 MMACR 179 MMACRM 180 MMACR 180 MMACR 181 MMACR	159	MCMC
162       MCMM         163       MCMMCM         164       MCMMMMM         165       MCRM         166       MCRMM         167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACR         181       MMACR	160	MCMCCM
163       MCMMCM         164       MCMMMMM         165       MCRM         166       MCRMM         167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACR         181       MMAR	161	MCMCM
164       MCMMMMM         165       MCRM         166       MCRMM         167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	162	MCMM
165       MCRM         166       MCRMM         167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	163	MCMMCM
166       MCRMM         167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	164	MCMMMMM
167       MGAC         168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	165	MCRM
168       MGMM         169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	166	MCRMM
169       MGMMM         170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMM         174       MMACMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	167	MGAC
170       MMAC         171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	168	MGMM
171       MMACM         172       MMACMAC         173       MMACMMMMM         174       MMACMMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	169	MGMMM
172       MMACMAC         173       MMACMMMMM         174       MMACMMMMMM         175       MMACMR         176       MMACR         177       MMACRC         178       MMACRM         179       MMACRMM         180       MMACRR         181       MMAR	170	MMAC
173 MMACMMMMM 174 MMACMMMMMM 175 MMACMR 176 MMACR 177 MMACRC 178 MMACRM 179 MMACRMM 180 MMACRM	171	MMACM
174 MMACMMMMMM  175 MMACMR  176 MMACR  177 MMACRC  178 MMACRM  179 MMACRMM  180 MMACRR  181 MMAR	172	MMACMAC
175 MMACMR  176 MMACR  177 MMACRC  178 MMACRM  179 MMACRMM  180 MMACRR  181 MMAR	173	MMACMMMM
176 MMACR 177 MMACRC 178 MMACRM 179 MMACRMM 180 MMACRR 181 MMAR	174	MMACMMMMM
177 MMACRC  178 MMACRM  179 MMACRMM  180 MMACRR  181 MMAR	175	MMACMR
178 MMACRM 179 MMACRMM 180 MMACRR 181 MMAR	176	MMACR
179 MMACRMM  180 MMACRR  181 MMAR	177	MMACRC
180 MMACRR 181 MMAR	178	MMACRM
181 MMAR	179	MMACRMM
	180	MMACRR
182 MMARC	181	MMAR
	182	MMARC

Table A-1 Continued

Token #	Token generated
183	MMBW
184	MMCM
185	MMCMC
186	MMCMM
187	MMCMMMMM
188	MMCR
189	MMCRR
190	MMFR
191	MMGG
192	MMGW
193	MMMA
194	MMMAC
195	MMMACM
196	MMMACR
197	MMMACRM
198	MMMACRMMM
199	MMMACRMMMM
200	MMMACRMMMMMM
201	MMMAR
202	MMMC
203	MMMCMM
204	MMMCR
205	MMMF
206	MMMG
207	MMMM
208	MMMMA
209	MMMMAC
210	MMMMACAC
211	MMMMACM
212	MMMMACMMMMM
213	MMMMACRM
214	MMMMACRMACR
215	MMMMACRMMM
216	MMMMACRMMMM
217	MMMMC
218	MMMMCMM
219	MMMMCMMM
220	MMMMCR
L	

Table A-1 Continued

Token #	Token generated
221	MMMMCRM
222	MMMMM
223	MMMMMA
224	MMMMMAC
225	MMMMMACAC
226	MMMMMACM
227	MMMMMACMC
228	MMMMMACR
229	MMMMMACRRG
230	MMMMMC
231	MMMMMCMM
232	MMMMMCMMMM
233	MMMMFRMM
234	MMMMM
235	MMMMMA
236	MMMMMAC
237	MMMMMACR
238	MMMMMMC
239	MMMMMM
240	MMMMMMA
241	MMMMMMAC
242	MMMMMMACM
243	MMMMMMACR
244	MMMMMMACRMMM
245	MMMMMMC
246	MMMMMMMA
247	MMMMMMMAC
248	MMMMMMMM
249	MMMMMMMMF
250	MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
251	MMMMMMMMMMMMMMCRM
252	MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
253	MMMMMMMMR
254	MMMMMMMW
255	MMMMMMMR
256	MMMMMMMMM
257	MMMMMMR
258	MMMMMMRM

Table A-1 Continued

259   MMMMMR   260   MMMMMW   261   MMMMMW   262   MMMMR   263   MMMMRM   263   MMMMRM   264   MMMMRM   265   MMMMW   266   MMMMWW   266   MMMMWW   267   MMMM   268   MMMMR   269   MMMMR   269   MMMRM   270   MMMRMM   271   MMMRMMM   271   MMMRMMMMM   272   MMMRMMMMMMM   273   MMMRMMMMMMM   274   MMMWW   275   MMMWW   275   MMMWW   276   MMMWW   277   MMMM   278   MMMMMM   279   MMMR   279   MMMR   280   MMMRF   280   MMMRF   281   MMMRM   282   MMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
261       MMMMMMW         262       MMMMMR         263       MMMMMRM         264       MMMMRM         265       MMMMW         266       MMMMWWW         267       MMMMN         268       MMMR         269       MMMRMM         270       MMMRMMM         271       MMMRMMMM         272       MMMRMMMMMM         273       MMMRMMMMMMMM         274       MMMW         275       MMMWW         276       MMMWW         277       MMM         278       MMMNMM         279       MMR         280       MMRF         281       MMRMM         282       MMMRMM         283       MMMRMMM
262       MMMMMR         263       MMMMMRM         264       MMMMMW         265       MMMMWW         266       MMMMWWW         267       MMMMN         268       MMMR         269       MMMRM         270       MMMRMM         271       MMMRMMMM         272       MMMRMMMMM         273       MMMRMMMMMMM         274       MMMW         275       MMMWW         276       MMMWW         277       MMM         278       MMMNMM         279       MMR         280       MMRF         281       MMRM         282       MMMRMM         283       MMRRMMM         284       MMMRMMMM
263       MMMMMRM         264       MMMMMW         265       MMMMW         266       MMMMWW         267       MMMN         268       MMMR         269       MMMRMM         270       MMMRMMM         271       MMMRMMMM         272       MMMRMMMMMM         273       MMMRMMMMMMM         274       MMMW         275       MMMWW         276       MMMWW         277       MMMN         278       MMMNMM         279       MMR         280       MMRF         281       MMRM         282       MMRMM         283       MMRMMM         284       MMMRMMMM
264       MMMMMRMM         265       MMMMWW         266       MMMMWWW         267       MMMMN         268       MMMR         269       MMMRM         270       MMMRMM         271       MMMRMMMM         272       MMMRMMMMMM         273       MMMRMMMMMMM         274       MMMW         275       MMMWW         276       MMMWW         277       MMM         278       MMMNMM         279       MMR         280       MMRF         281       MMMRM         282       MMMRMM         283       MMMRMMM         284       MMMRMMMM
265 MMMMWW 266 MMMMWWW 267 MMMMR 268 MMMMR 269 MMMMRM 270 MMMMRMM 271 MMMRMMMMMMMMM 271 MMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
266       MMMMWWW         267       MMMMN         268       MMMMR         269       MMMMRM         270       MMMMRMM         271       MMMRMMMM         272       MMMRMMMMMM         273       MMMMMMMMMM         274       MMMW         275       MMMWW         276       MMMWW         277       MMM         278       MMMNMM         279       MMR         280       MMMR         281       MMMRM         282       MMMRMM         283       MMMRMMM         284       MMMRMMMM
267       MMMMN         268       MMMMR         269       MMMMRM         270       MMMMRMM         271       MMMRMMM         272       MMMMRMMMMM         273       MMMMMMMMMM         274       MMMW         275       MMMWMM         276       MMMWW         277       MMN         278       MMMNMM         279       MMR         280       MMMRF         281       MMMRMM         282       MMMRMM         283       MMMRMMM         284       MMMRMMM
268       MMMMR         269       MMMMRM         270       MMMMRMM         271       MMMMRMMM         272       MMMRMMMMMM         273       MMMRMMMMMMM         274       MMMW         275       MMMWMM         276       MMMWW         277       MMMN         278       MMMNMMM         279       MMR         280       MMMRF         281       MMMRMM         282       MMMRMMM         283       MMMRMMM         284       MMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
269       MMMMRM         270       MMMMRMM         271       MMMRMMMM         272       MMMRMMMMMM         273       MMMRMMMMMMM         274       MMMW         275       MMMWW         276       MMMWW         277       MMMN         278       MMMNMMM         279       MMR         280       MMMRF         281       MMMRM         282       MMMRMM         283       MMMRMMM         284       MMMRMMMMM
270       MMMMRMM         271       MMMMRMMM         272       MMMMRMMMMMM         273       MMMMRMMMMMMM         274       MMMW         275       MMMWMM         276       MMMWW         277       MMMN         278       MMMNMMM         279       MMR         280       MMMR         281       MMMRM         282       MMMRMM         283       MMMRMMM         284       MMMRMMMM
271       MMMMRMMM         272       MMMMRMMMMMM         273       MMMMMMMMMMMMMM         274       MMMW         275       MMMWMM         276       MMMWW         277       MMMN         278       MMMNMMM         279       MMR         280       MMMF         281       MMMRM         282       MMMRMM         283       MMMRMMM         284       MMMRMMMM
272       MMMMRMMMMMM         273       MMMMRMMMMMMM         274       MMMW         275       MMMWMM         276       MMMWW         277       MMMN         278       MMMNMMM         279       MMR         280       MMMRF         281       MMMRM         282       MMMRMM         283       MMMRMMM         284       MMMRMMMM
273 MMMMRMMMMMM  274 MMMW  275 MMMWWM  276 MMMWW  277 MMMN  278 MMMNMMM  279 MMMR  280 MMMRF  281 MMMRMM  282 MMMRMM  283 MMMRMMM  284 MMMRMMMM
274 MMMWW 275 MMMMWW 276 MMMWW 277 MMMN 278 MMMNMMM 279 MMMR 280 MMMRF 281 MMMRM 282 MMMRMM 283 MMMRMMM 284 MMMRMMMM
275 MMMWWM 276 MMMWW 277 MMMN 278 MMMNMMM 279 MMMR 280 MMMRF 281 MMMRM 282 MMMRMM 283 MMMRMMM 284 MMMRMMM
276 MMMWW  277 MMMN  278 MMMNMMM  279 MMMR  280 MMMRF  281 MMMRM  282 MMMRMM  283 MMMRMMM  284 MMMRMMM
277 MMMN 278 MMMNMMM 279 MMMR 280 MMMRF 281 MMMRM 282 MMMRMM 283 MMMRMMM 284 MMMRMMM
278 MMMNMMM 279 MMMR 280 MMMRF 281 MMMRM 282 MMMRMM 283 MMMRMMM 284 MMMRMMM
279 MMMR 280 MMMRF 281 MMMRM 282 MMMRMM 283 MMMRMMM 284 MMMRMMM
280 MMMRF  281 MMMRM  282 MMMRMM  283 MMMRMMM  284 MMMRMMMM
281 MMMRM 282 MMMRMM 283 MMMRMMM 284 MMMRMMMM
282 MMMRMM 283 MMMRMMM 284 MMMRMMMM
283 MMMRMMM 284 MMMRMMMM
284 MMMRMMM
285 MMMRMR
286 MMMRRM
287 MMMW
288 MMMWM
289 MMMWMM
290 MMMWMMM
291 MMMWW
292 MMNM
293 MMNMM
294 MMRM
295 MMRMC
296 MMRMM

Table A-1 Continued

Token #	Token generated
297	MMRMMM
298	MMRMMMM
299	MMRMMMMMM
300	MMRMMMRM
301	MMRMMMRMM
302	MMRMMRM
303	MMRMRM
304	MMRR
305	MMWM
306	MMWMM
307	MMWMMMMMMMMM
308	MMWMMWM
309	MMWW
310	MMWWB
311	MMWWW
312	MRAC
313	MRACM
314	MRCM
315	MRCR
316	MRCRMMMMM
317	MRCRMMR
318	MRMAC
319	MRMACR
320	MRMC
321	MRMM
322	MRMMM
323	MRMMMM
324	MRMMMM
325	MRMMMMM
326	MRMMMMMM
327	MRMMMRM
328	MRMMRM
329	MRMR
330	MRMRM
331	MRRM
332	MRRRR
333	MWAC
334	MWMMMMM

Table A-1 Continued

Token #	Token generated
335	MWWMMM
336	RACCCC
337	RACGM
338	RACMMM
339	RACR
340	RACRR
341	RCRA
342	RCRR
343	RMAC
344	RMACR
345	RMACRM
346	RMFI
347	RMMM
348	RMMMACRM
349	RMMMC
350	RMMMM
351	RMMMA
352	RMMMM
353	RMMMMM
354	RMMMMMM
355	RMMMMMMM
356	RMMMMMMM
357	RMMMMMMMM
358	RMMMR
359	RMMMRM
360	RMMMRMM
361	RMMMRMMM
362	RMMR
363	RMMRMM
364	RMMWW
365	RMRF
366	RMRM
367	RMRMMM
368	RMRMR
369	RMRR
370	RRMA
371	RRMM
372	RRMMMM
L	

Table A-1 Continued

Token #	Token generated
373	RRRR
374	RRRRM
375	RRRRR
376	TTTT
377	TTTTT
378	TTTTTT
379	WACR
380	WACRMM
381	WBMM
382	WGGB
383	WGGBB
384	WGGBBWW
385	WMAC
386	WMMM
387	WMMMM
388	WMMMMM
389	WMMMMM
390	WMMMMMMMM
391	WMMMRMAC
392	WMMW
393	WWBM
394	WWGG
395	WWGGB
396	WWGGBB
397	WWGGBBWWW
398	WWMM
399	WWMMMM
400	WWWG
401	WWWGG
402	WWWMM
403	рррр

## **APPENDIX 2**

## GROUPS GENERATED FROM RULE BASED ANALYSIS

Table A-2: Group generated from rule based method

	Group generated
1	ACBWRM
2	ACCMMRR
3	ACGBRM
4	ACGC
5	ACGGRM
6	ACGM
7	ACGMR
8	ACGMX
9	ACGR
10	ACGRM
11	ACGWB
12	ACGWWGG
13	ACMC
14	ACMCC
15	ACMCRCRR
16	ACMG
17	ACMM
18	ACMMRM
19	ACMR
20	ACMRM
21	ACMRRMM
22	ACRBGM
23	ACRC
24	ACRCGM
25	ACRCM
26	ACRCR
27	ACRCRRCR
28	ACRCRRM
29	ACRCRRMM
30	ACRFMRTCM

Table A-2 Continued

Group #	Group generated
31	ACRG
32	ACRGG
33	ACRGW
34	ACRM
35	ACRMFIM
36	ACRMG
37	ACRMGTMM
38	ACRMM
39	ACRMMBMWR
40	ACRMMCRCCRM
41	ACRMMGW
42	ACRMMMMMMM
43	ACRMRCRM
44	ACRMW
45	ACRRG
46	ACRRM
47	ACRRMG
48	ACRRMMRW
49	ACRRWBG
50	ACRT
51	ACRW
52	ACRWBMM
53	ACRWM
54	ACRWR
55	ACWBRM
56	ACWGM
57	ACWR
58	AGCM
59	AGMM
60	ARBC
61	ARCMC
62	ARCR
63	ARCRGRMMM
64	ARCRR
65	ARCRRGGMFR
66	ARGCRM
67	ARGRCRMM
68	ARMC
L	

Table A-2 Continued

Group #	Group generated
69	ARMMG
70	AXCG
71	BWRBG
72	CCCC
73	CCCCCCCC
74	CCCCCCCCC
75	CCMC
76	СМСМ
77	CMMM
78	CRCR
79	CRMM
80	CRMR
81	CRMRCMC
82	CRRC
83	CRRCRCR
84	FFFFIFFI
85	FMRM
86	FIRRFR
87	FIRRFIR
88	GBBGW
89	GBCR
90	GBGGBG
91	GBGWMB
92	GCRCRR
93	GGGGGG
94	GGWBBBG
95	GWBM
96	MBGM
97	MBWC
98	MBWM
99	MCRMRGW
100	MCRR
101	MFFI
102	MGBMRC
103	MGFIRC
104	MMFR
105	MMFRMMMF
106	MMMM

Table A-2 Continued

Group #	Group generated
107	MMMMM
108	MMMMMMM
109	MMMRCR
110	MMRCRCR
111	MMRM
112	MMTT
113	MRCR
114	MRCRM
115	MTTTTTT
116	RCCCCC
117	RCRM
118	RCRR
119	RFMRM
120	RFIR
121	RMMMM
122	RMMRRM
123	RRCR
124	RRMMM
125	RRMR
126	TTTT
127	WBGBGM
128	WBGG
129	WMMM
130	WWMGGBWR

## **APPENDIX 3**

# GROUPS GENERATED FROM HAC BASED ANALYSIS

Table A-3: Groups generated from HAC method

Group #	Group Generated
1	AAA
2	AAAA
3	AAAAA
4	AAAAAA
5	AAAAAA
6	AAAAAAAA
7	AAAAAAAA
8	AAAAAAAAA
9	AAAAAAAAAAAAAA
10	AAAAAAAAAAAAAAAA
	AAAAAAAAAAAAAAAAAAAAAAAAAAAGBBWGGBBWGGB
11	AAAGAAUUUUUUUUUUU
	AAAAAAAAAAAAAAAAAAAAAAAAAAGBBWGGBBWGGBWWGGAAAGG
12	AAAGAAUUUUUUUUUUUUUCRMRAAAAAAAAAAAAAAAAAAAAA
	AAAAAAAAAAAAAAAAAAAAAAAAAGWGGBBWWGGBBWWWWGBWWGGAAA
13	AGAAAGGAUUUUUUUUUUUUUAAAAAAAAAAAAAAAAAA
14	AAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAA
15	AAAAAAAAAAAAAAAAAAAAAAAAAGWGGBBWWGGBBWWWWGBWWGGA
16	AAAAAAAAAAAAAAAAAAAAAAWWWGGBBWWWGGBBBWWGGBBA
17	AAAAAAAAAACM
18	AAAAAAAAAACMGMMM
19	AAAAAAAWWWGGBBWWWGGBBBWWGGBBA
20	AAAAAGBBWGGBBW
21	AAAAAGWGGBBWWG
22	AAAAAGWGGBBWWGGBBWWWWGBWWGGA
23	AAAAAWWWGGBBWW
24	AAAAAWWWGGBBWWWGGBBBWWGGBBA
25	AAAGAAAGGA
26	AAGGAAAGAA
27	ACA

Table A-3 Continued

Group #	Group generated
28	ACAC
29	ACACMACACMGGMMMM
30	ACACMRMMRMMRMC
31	ACACRRMM
32	ACACRRMMRW
33	ACBWRM
34	ACBWRMMMG
35	ACC
36	ACCGMGWW
37	ACCM
38	ACCMCMC
39	ACGBRM
40	ACGMRA
41	ACGMRACRCGMMM
42	ACGRA
43	ACM
44	ACMACMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
45	ACMACRRMGA
46	ACMACRRMGACACACCMMACMACGACMACMMACM
47	ACMCRCR
48	ACMM
49	ACMMMM
50	ACMMMMA
51	ACMMMMACRM
52	ACMMMRACMCMCRM
53	ACMR
54	ACMRACM
55	ACMRRM
56	ACR
57	ACRA
58	ACRAAMMMMMMMMMMMMMMMCRMRGWACRMMRCCACRRMRMMMMRMFI
59	ACRACR
60	ACRACRMM
61	ACRBGM
62	ACRCMMMMMMMMMMM
63	ACRCRRMMMMM
64	ACRCRRMMMMMMMMMM
65	ACRG

Table A-3 Continued

Group #	Group generated
66	ACRGA
67	ACRGACRACRACRMMMACRMGACMRMMMACRMMMM
68	ACRM
69	ACRMACR
70	ACRMACRM
71	ACRMACRMCRCRCRACR
72	ACRMFIMMM
73	ACRMGTMM
74	ACRMM
75	ACRMMBMWR
76	ACRMMGWACRWACRMMMWM
77	ACRMMM
78	ACRMMMM
79	ACRMMMMMMRM
80	ACRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
81	ACRMRMACRMACGRACAC
82	ACRMW
83	ACRMWACM
84	ACRR
85	ACRRG
86	ACRRM
87	ACRRMGMM
88	ACRRMMM
89	ACRRMWWMMWW
90	ACRTACMMMM
91	ACRWBMMMM
92	ACRWM
93	ACRWMACRM
94	ACW
95	ACWA
96	ACWBRM
97	AGAAGGAGAAAG
98	AGCM
99	AGMMM
100	AGMMMM
101	AMMMMMMMMMMMMMM
102	ARB
103	ARG
	•

Table A-3 Continued

Group #	Group generated
104	ARGR
105	ARM
106	ARMM
107	AXCGACRACRAR
108	AXCGACRACCAGG
109	BBB
110	BBBWBBBBWBB
111	BBBWBBBBWBBTT
112	BBG
113	BGGG
114	BGM
115	BGW
116	ВМВ
117	BMGMBW
118	BMGMBWMWW
119	BWM
120	CAC
121	CACC
122	CACCC
123	CACCM
124	CACCMMACMACGA
125	CACM
126	CACMMRMRM
127	CACMRMMR
128	CACRM
129	CACRRMRM
130	CARB
131	CARBCMMRMACMMARCRR
132	CBWRM
133	CCAC
134	CCACCC
135	CCC
136	CCCACCAC
137	CCCC
138	CCCCC
139	CCCCCC
140	CCCCCCC
141	cccccccc

Table A-3 Continued

Group #	Group generated
142	CCCCCCCMCCCCCCC
143	CCCCCCCMCCCCCCMW
144	CCCCCMCCCCCCC
145	CCCCMM
146	CCM
147	CCMC
148	CCMM
149	CCMRCRMM
150	CCRRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
151	CGA
152	CGACRC
153	CGB
154	CGBMGGBMG
155	CGBMGGBMGGA
156	CGBMMR
157	CGBR
158	CGBRM
159	CGC
160	CGCC
161	CGCCCCCCCCCCCCCCCCC
162	CGCCCCCCCCCCCCCCCCCCCC
163	CGCCCCCCCCCCCCCCCCCMBGGGACMRMMM
164	CGGB
165	CGGBMMMMM
166	CGGBMMMMMARGR
167	CGGG
168	CGGRMA
169	CGM
170	CGMG
171	CGMM
172	CGMRA
173	CGMXA
174	CGR
175	CGRMA
176	CGRMACRMRCRMMR
177	CGW
178	CGWBA
179	CGWWGG

Table A-3 Continued

Group #	Group generated
180	CMA
181	CMACMMACM
182	CMC
183	CMCARM
184	CMCCCCMM
185	CMCM
186	CMCMCMCMCMCMCM
187	CMCMCMCMCMCM
188	CMCMMCMM
189	CMCMR
190	CMG
191	CMGA
192	CMGACGWBA
193	CMGACGWBACWGMACWACWGACBACWA
194	CMGGG
195	CMGGM
196	CMGGMMMM
197	CMM
198	CMMAR
199	CMMC
200	CMMCM
201	CMMFFI
202	CMMM
203	CMMMM
204	CMMMMMA
205	СМММММММММММММММММ
206	CMMMMMR
207	CMMMMMRRM
208	CMMMR
209	CMMMRACMCMCR
210	CMMRM
211	CMMRMA
212	CMMRMRM
213	CMMRR
214	CMR
215	CMRM
216	CMRMM
217	CMRMMMMMMMMAR

Table A-3 Continued

Group #	Group generated
218	CMRRM
219	CMWCMCM
220	CMXN
221	CNCMM
222	CNMXMMXMMMM
223	CRA
224	CRAC
225	CRACCCCACCACCRMMRRMM
226	CRACGBMGGBMGGACRACACACCCMGGG
227	CRACGBMGGBMGGACRACACACCCMGGGMMM
228	CRACR
229	CRACRACCC
230	CRACRMM
231	CRACRMMMA
232	CRACRRCAC
233	CRAR
234	CRB
235	CRBG
236	CRC
237	CRCCRMMMMM
238	CRCGMMM
239	CRCMMMMMMMMMMM
240	CRCR
241	CRCRACWWBBMMMMMMM
242	CRCRM
243	CRCRRAMMMNMM
244	CRCRRCR
245	CRFMRT
246	CRFMRTCMMFFI
247	CRG
248	CRGG
249	CRGRM
250	CRGW
251	CRM
252	CRMA
253	CRMACR
254	CRMACRMMM
255	CRMACRMMMMMMMMMMMMM

Table A-3 Continued

256   CRMACRIWACRWR   257   CRMDMMR   258   CRMF   259   CRMG   260   CRMGACMRMMACRMMMM   261   CRMGTMM   262   CRMM   263   CRMMA   264   CRMMBWW   265   CRMMGWACRWACRMMMWM   266   CRMMGWACRWACRMMMWM   267   CRMMGWACRWACRMMMWM   268   CRMMGWACRWACRMMMWM   270   CRMMMMM   271   CRMMRMMM   271   CRMMRMMM   272   CRMMR   273   CRMMR   274   CRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	Group #	Group generated
258         CRMFI           259         CRMG           260         CRMGACMRMMMACRMMMM           261         CRMGTMM           262         CRMM           263         CRMMA           264         CRMBWW           265         CRMGWA           266         CRMMGWACRWACRMMMWM           269         CRMMM           269         CRMMM           260         CRMMMM           270         CRMMMMM           271         CRMMRMMMM           272         CRMMR           273         CRMMR           274         CRMMRMMMMMM           275         CRMIRA           276         CRMR           277         CRMROWACRMMRCMAMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	256	CRMACRMWACRWR
259         CRMG           260         CRMGACMRMMMACRMMMM           261         CRMGTMM           262         CRMM           263         CRMMA           264         CRMMBWW           265         CRMGW           266         CRMMGWA           267         CRMMGWA           268         CRMMM           269         CRMMM           269         CRMMM           270         CRMMMM           271         CRMMMMM           272         CRMMR           273         CRMMRM           274         CRMMRM           275         CRMMR           276         CRMIR           277         CRMRMAMMMMMMMMRMR           277         CRMRGWACRMMRCCACRRMRMMMM           277         CRMRGWACRMMRCCACRRMRMMMM           279         CRMRMM           280         CRRMMM           281         CRW           282         CRRW           283         CRR           284         CRC           285         CRRCA           286         CRRCACRCRRMM           287         CREA	257	CRMDMMR
260         CRMGACMRMMMACRMMMM           261         CRMGTMM           262         CRMM           263         CRMMA           264         CRMMBWW           265         CRMMGWA           266         CRMMGWA           267         CRMMGWACRWACRMMMWM           268         CRMMM           269         CRMMMM           270         CRMMRMMMM           271         CRMMRMMMM           272         CRMMR           273         CRMMR           274         CRMMR           275         CRMIRA           274         CRMIRA           275         CRMIRA           276         CRMR           277         CRMGWACRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	258	CRMFI
261         CRMMM           262         CRMM           263         CRMMA           264         CRMMBMW           265         CRMMGWA           266         CRMMGWA           267         CRMMGWACRWACRMMMWM           268         CRMMM           269         CRMMMM           270         CRMMRMMM           271         CRMMRMMMM           272         CRMMR           273         CRMMR           274         CRMIR           273         CRMIRA           274         CRMIRA           275         CRMIRA           276         CRMR           277         CRMIRMMINIMMINIMMINIMMINIMMINIMMINIMMINI	259	CRMG
262         CRMMA           263         CRMMA           264         CRMMBWW           265         CRMMGW           266         CRMMGWA           267         CRMMGWA           268         CRMMM           269         CRMMM           270         CRMMMMM           271         CRMMRMMMM           272         CRMR           273         CRMRA           274         CRMRMRMM           275         CRMRMMRM           276         CRMR           277         CRMROWACRMMCCACRIMINAMINAMINAMINAMINAMINAMINAMINAMINAMIN	260	CRMGACMRMMMACRMMMM
263         CRMMA           264         CRMMBMW           265         CRMMGW           266         CRMMGWA           267         CRMMGWACRWACRMMMWM           268         CRMMM           269         CRMMMM           270         CRMMRMMM           271         CRMMRMMMMR           272         CRMR           273         CRMRA           274         CRMRMRMM           275         CRMRMMRMM           276         CRMR           277         CRMRGWACRMRCCACRRMRMMMRM           278         CRMRMA           279         CRMRMM           280         CRMRMMM           281         CRMW           282         CRMWM           283         CRR           284         CRC           285         CRRCA           286         CRRCACCRRMMM           287         CRRCA           288         CRRC           289         CRRM           290         CRRMA           291         CRRMACRM	261	CRMGTMM
264         CRMMGW           265         CRMMGWA           266         CRMMGWA           267         CRMMGWACRWACRMMMWM           268         CRMMM           269         CRMMMM           270         CRMMMMMM           271         CRMMRMMMM           272         CRMMR           273         CRMMRA           274         CRMMRMMRMM           275         CRMRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	262	CRMM
265         CRMMGW           266         CRMMGWA           267         CRMMGWACRWACRMMMWM           268         CRMM           269         CRMMM           270         CRMMMM           271         CRMMRMMM           272         CRMMR           273         CRMMRA           274         CRMMRMRMM           275         CRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	263	CRMMA
266         CRMMGWA           267         CRMMGWACRWACRMMMWM           268         CRMM           269         CRMMM           270         CRMMMM           271         CRMMRMMMM           272         CRMMR           273         CRMMRA           274         CRMMRMMMM           275         CRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	264	CRMMBMW
267         CRMMGWACRWACRMMMWM           268         CRMMM           269         CRMMMM           270         CRMMMMM           271         CRMMRMMMMR           272         CRMMR           273         CRMMRA           274         CRMMRMMMM           CRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	265	CRMMGW
268         CRMMM           269         CRMMMM           270         CRMMMMM           271         CRMMRMMMR           272         CRMMR           273         CRMMRA           274         CRMMRMMRMM           CRMIRMINIMINIMINIMINIMINIMINIMINIMINIMINI	266	CRMMGWA
269         CRMMMM           270         CRMMMMMM           271         CRMMRMMMMR           272         CRMMR           273         CRMMRA           274         CRMMRMMMMM           275         CRMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	267	CRMMGWACRWACRMMMWM
270   CRMMMMMMR   271   CRMMRMMMMR   272   CRMMR   273   CRMMR   274   CRMMRMMMMM   274   CRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	268	CRMMM
271         CRMMRMMMR           272         CRMMR           273         CRMMRA           274         CRMMRMMMMM           275         CRMRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	269	CRMMMM
272         CRMMR           273         CRMMRA           274         CRMMRMMRMM           275         CRMRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	270	CRMMMMM
273         CRMMRA           274         CRMMRMMRMM           CRMMRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	271	CRMMRMMMR
274         CRMMRMMRMM           CRMMRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	272	CRMMR
CRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	273	CRMMRA
275       MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM	274	CRMMRMMRMM
276       CRMR         277       CRMRGWACRMMRCCACRRMRMMMRM         278       CRMRMA         279       CRMRMM         280       CRMRMMM         281       CRMW         282       CRMWM         283       CRR         284       CRRC         285       CRRCA         286       CRRCACRCRRMMM         287       CRRCR         288       CRRG         289       CRRM         290       CRRMACRM         291       CRRMG		CRMMRMMRMMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM
277         CRMRGWACRMMRCCACRRMRMMMMRM           278         CRMRMA           279         CRMRMM           280         CRMRMMM           281         CRMW           282         CRMWM           283         CRR           284         CRC           285         CRRCA           286         CRRCACRCRRMMM           287         CRRCR           288         CRRG           289         CRRM           290         CRRMACRM           291         CRRMG	275	MMMMMMMMMMMMMMMRMRMR
278         CRMRMA           279         CRMRMM           280         CRMRMMMM           281         CRMW           282         CRMWM           283         CRR           284         CRRC           285         CRRCA           286         CRRCACRCRRMMM           287         CRRCR           288         CRRG           289         CRRM           290         CRRMACRM           291         CRRMG	276	CRMR
279       CRMRMM         280       CRMRMMMM         281       CRMW         282       CRMWM         283       CRR         284       CRRC         285       CRRCA         286       CRRCACRCRRMMM         287       CRRCR         288       CRRG         289       CRRM         290       CRRMACRM         291       CRRMG	277	CRMRGWACRMMRCCACRRMRMMMRM
280       CRMRMMMM         281       CRMW         282       CRMWM         283       CRR         284       CRRC         285       CRRCA         286       CRRCACRCRRMMM         287       CRRCR         288       CRRG         289       CRRM         290       CRRMACRM         291       CRRMG	278	CRMRMA
281 CRMW 282 CRMWM 283 CRR 284 CRRC 285 CRRCA 286 CRRCACRCRMMM 287 CRRCR 288 CRRG 290 CRRM 290 CRRMACRM 291 CRRMG	279	CRMRMM
282       CRMWM         283       CRR         284       CRRC         285       CRRCA         286       CRRCACRCRRMMM         287       CRRCR         288       CRRG         289       CRRM         290       CRRMACRM         291       CRRMG	280	CRMRMMM
283 CRR 284 CRRC  285 CRRCA  286 CRRCACRCRMMM  287 CRRCR  288 CRRG  290 CRRM  290 CRRMACRM  291 CRRMG	281	CRMW
284       CRRC         285       CRRCA         286       CRRCACRCRRMMM         287       CRRCR         288       CRRG         289       CRRM         290       CRRMACRM         291       CRRMG	282	CRMWM
285 CRRCA 286 CRRCACRCRMMM  287 CRRCR  288 CRRG  289 CRRM  290 CRRMACRM  291 CRRMG	283	CRR
286 CRRCACRCRRMMM  287 CRRCR  288 CRRG  289 CRRM  290 CRRMACRM  291 CRRMG	284	CRRC
287 CRRCR 288 CRRG 289 CRRM 290 CRRMACRM 291 CRRMG	285	CRRCA
288 CRRG 289 CRRM 290 CRRMACRM 291 CRRMG	286	CRRCACRCRRMMM
289 CRRM 290 CRRMACRM 291 CRRMG	287	CRRCR
290 CRRMACRM 291 CRRMG	288	CRRG
291 CRRMG	289	CRRM
	290	CRRMACRM
292 CRRMGA	291	CRRMG
	292	CRRMGA

Table A-3 Continued

293 294	CRRMM
294	ODDIA 4.6
	CRRMMM
295	CRRMMMM
296	CRRMMRW
297	CRRMR
298	CRRWBG
299	CRT
300	CRTA
301	CRTACMMMM
302	CRW
303	CRWB
304	CRWBMMMM
305	CRWM
306	CRWMA
307	CRWR
308	CWA
309	CWBRM
310	CWGM
311	CWGMACWACW
312	CWRM
313	CWRMMM
314	FFFFIFFI
	FFI
	FFIFFI
	FMR
	FMRM
319	FMRT
320	FRA
	FRM
322	FRMMM
323	FIR
324	FIRR
325	FIRRFRMBWR
326	FIRRFRMBWRB
327	FIRRFRMBWRBGM
328	FIRRFI
329	GACB
330	GBBGGG

Table A-3 Continued

Group #	Group generated
331	GBBGW
332	GBBW
333	GBBWGGBBW
334	GBBWWWW
335	GBBWWWWGB
336	GBG
337	GBGGBG
338	GBGW
339	GBM
340	GBMG
341	GBW
342	GBWR
343	GFB
344	GGB
345	GGBB
346	GGBBA
347	GGBBW
348	GGBBWW
349	GGBWW
350	GGBWWGGB
351	GGG
352	GGGBBBWW
353	GGGG
354	GGM
355	GGMFRACGMXACGGRMA
356	GGMFRACGMXACGGRMACGRMACRMRCRMMR
357	GGW
358	GGWB
359	GGWBBBG
360	GMG
361	GMMM
362	GWB
363	GWBM
364	GWGGBBWWG
365	MACACMM
366	MACGACRCMACRGW
367	MACM
368	MACMMM

Table A-3 Continued

Group #	Group generated
369	MACRGG
370	MACRM
371	MACRMMA
372	MACRMMACGWWGG
373	MAM
374	MAR
375	MARCRACGBMMR
376	MARMMGR
377	MAXCACRGACRRM
378	MBG
379	MBM
380	MBMBMMW
381	MBMW
382	MBW
383	MCACM
384	MCCC
385	MCM
386	MCMM
387	MCMMM
388	MCRMMCRR
389	MFC
390	MFRM
391	MFRMMM
392	MFRMMMF
393	MFIR
394	MGB
395	MGBMRCMMMMMR
396	MGFIR
397	MGG
398	MGGBWR
399	MGGG
400	MGGM
401	MGMM
402	MGR
403	MMA
404	MMACA
405	MMACGC
406	MMACMRCCCCC

Table A-3 Continued

Group #	Group generated
407	MMACMRCCCCCC
408	MMACMRM
409	MMACRMMMMM
410	MMACRMWMM
411	MMARM
412	MMCM
413	MMCMM
414	MMCMMMMM
415	MMCMMMMMRRM
416	MMFRM
417	MMGWBM
418	MMGWBMM
419	MMM
420	MMMACRM
421	MMMACRMACRM
422	MMMACRMMMMMMMM
423	MMMCMMWM
424	MMMCR
425	MMMG
426	MMMM
427	MMMMA
428	MMMMACWRMMMM
429	MMMMM
430	MMMMMA
431	MMMMMACM
432	MMMMMACMMMMMMGBGWMBMMMM
433	MMMMMGBGW
434	MMMMMGBGWMBMMMM
435	MMMMMM
436	MMMMMMACACCRRMMRMMMMMMMMMMMMMMMMMMMMMMM
437	MMMMMM
438	MMMMMMACMCACRM
439	MMMMMMCCCCMMM
440	MMMMMMM
441	MMMMMMMM
442	MMMMMMMMACACRRMM
443	MMMMMMMFRM
444	MMMMMMMM

Table A-3 Continued

Group #	Group generated
445	MMMMMMMMM
446	MMMMMMMMMMM
447	MMMMMMMMMMMMM
448	MMMMMMMMMMMMM
449	MMMMMMMMMMMMMMM
450	ММММММММММММММММ
451	МММММММММММММММММ
452	МММММММММММММММММММММММММММММММММММММММ
453	MMMMMMMMMAR
454	MMMMMMRMCRMMCRRACRMMMM
455	MMMMMMMMMMMMM
456	MMMMMW
457	MMMMN
458	MMMMNMM
459	MMMMRC
460	MMMMRM
461	MMMMRMRMR
462	MMMMW
463	MMMN
464	MMMR
465	MMMRFRMMMC
466	MMMRFIRM
467	MMMRM
468	MMMRMCRMMCRRA
469	MMMRMM
470	MMMRMMRMRCRMMMMMMMMMMMMMMMMMMMMMMMMMMMM
471	MMMRMMWWBM
472	MMMW
473	MMMWM
474	MMMWMMM
475	MMMWMMMMMM
476	MMN
477	MMR
478	MMRFRMMM
479	MMRFIRM
480	MMRM
481	MMRMMCMMMMMRRMBGM
482	MMRMMM
L	L

Table A-3 Continued

Group #	Group generated
483	MMRMMMMMMM
484	MMRMMMRM
485	MMRMMMRMMMRM
486	MMRRMRMR
487	MMRRMRMCACACMRMMRMMRMCMMMMM
488	MMW
489	MMWBGGMMM
490	MMWBGGMMMACRMACACMMRMRMACR
491	MMWM
492	MMWW
493	MMWWW
494	MMWWWWW
495	MMWWWWWM
496	MMX
497	MMXMGFIRCMM
498	MMXMGFIRCMMACM
499	MMXMGFIRCMMACMMMMMM
500	MMXMMMNM
501	MRC
502	MRCR
503	MRCRTFRM
504	MRCRTFRMC
505	MRM
506	MRMACRWMMMRMACMCCRMRMMMM
507	MRMMM
508	MRMMMR
509	MRMMMRM
510	MRMMMRMMM
511	MRMMMW
512	MRMMMRM
513	MRMMR
514	MRMMRA
515	MRMMRACAR
516	MRMMRMR
517	MRMRMR
518	MRRC
519	MRRCRRC
520	MRT

Table A-3 Continued

Group #	Group generated
521	MRW
522	MTT
523	MWA
524	MWACMMMM
525	MWACRMACRMMMMMMMMMMMMMMACRM
526	MWB
527	MWM
528	MWMMMM
529	MWR
530	MWW
531	MWWB
532	MWWBB
533	MWWBBMMMMM
534	MWWM
535	MXDNN
536	NCCMXN
537	NMX
538	NMXMMX
	NMXMMXMMMM
540	NXAAAAAGBM
541	NXAAAAAAGBMWW
542	NXCMMMMMACGACRMRMACRMACGRACACN
543	NXMXNX
544	RACC
545	RACMM
546	RACMMM
547	RCA
548	RCRM
549	RCRR
550	RFMRM
551	RFI
552	RGW
553	RMACMC
554	RMG
555	RMM
556	RMMM
557	RMMMR
558	RMMR

Table A-3 Continued

Group #	Group generated
559	RMMRMR
560	RMMRMRMR
561	RMR
562	RRCR
563	RRCRCRA
564	RRM
565	RRMRR
566	RRRR
567	RRRRR
568	TTT
569	TTTT
570	UUU
571	บบบบ
572	บบบบบ
573	บบบบบบ
574	บบบบบบบ
575	บบบบบบบบบบบ
576	บบบบบบบบบบบ
577	WBG
578	WBGB
579	WBGBGM
580	WBGG
581	WBGGMMM
582	WBMGR
583	WBR
584	WBRMM
585	WGGGBBBWW
586	WMMM
587	WMRRCRRCCCCCCC
588	WWB
589	WWBB
590	WWBBMMMMMM
591	WWBM
592	WWGG
593	WWGGA
594	WWW
595	WWWGGBBWW
596	WWWMMMMGBMRCMMMMMR

Table A-3 Continued

Group #	Group generated
597	www
598	XACGMMMNM
599	XAR
600	XCA
601	XCACRGACRRM
602	XCG
603	XCGA
604	XCMCM
605	XMM
606	XMMNMXGWBN
607	XWN
608	XXA
609	XXACRG
610	pGGG
611	ppPP
612	ррр
613	ррррр

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1994